Untitled

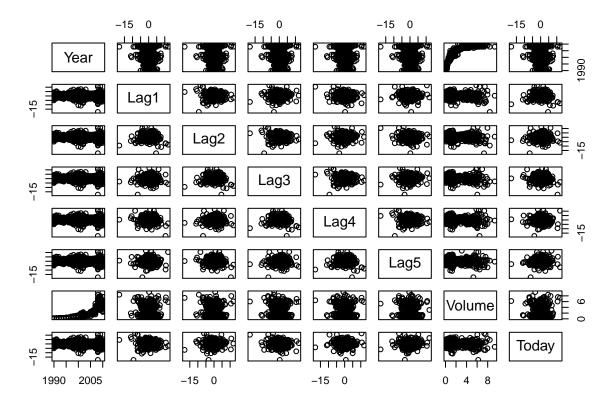
Rohitashwa Chakraborty

30/07/2021

EXERCISE 4.10:

4.10.a

```
##
         Year
                                            Lag2
                                                                Lag3
                        Lag1
                                                                  :-18.1950
##
    Min.
           :1990
                   Min.
                           :-18.1950
                                       Min.
                                              :-18.1950
                                                           Min.
##
    1st Qu.:1995
                   1st Qu.: -1.1540
                                       1st Qu.: -1.1540
                                                           1st Qu.: -1.1580
    Median:2000
                   Median: 0.2410
                                       Median: 0.2410
                                                           Median: 0.2410
           :2000
##
    Mean
                   Mean
                             0.1506
                                       Mean
                                                0.1511
                                                           Mean
                                                                  : 0.1472
##
    3rd Qu.:2005
                   3rd Qu.:
                            1.4050
                                       3rd Qu.: 1.4090
                                                           3rd Qu.: 1.4090
##
    Max.
           :2010
                           : 12.0260
                                              : 12.0260
                                                                  : 12.0260
                   Max.
                                       Max.
                                                           Max.
##
         Lag4
                             Lag5
                                               Volume
                                                                  Today
           :-18.1950
                                                                     :-18.1950
##
                               :-18.1950
                                                   :0.08747
    Min.
                       Min.
                                           Min.
                                                              Min.
##
    1st Qu.: -1.1580
                        1st Qu.: -1.1660
                                           1st Qu.:0.33202
                                                              1st Qu.: -1.1540
##
    Median : 0.2380
                       Median: 0.2340
                                           Median :1.00268
                                                              Median: 0.2410
          : 0.1458
                               : 0.1399
                                                   :1.57462
    Mean
                       Mean
                                           Mean
                                                              Mean
                                                                     : 0.1499
    3rd Qu.:
                                                              3rd Qu.:
##
             1.4090
                        3rd Qu.:
                                 1.4050
                                           3rd Qu.:2.05373
                                                                        1.4050
##
    Max.
           : 12.0260
                       Max.
                               : 12.0260
                                           Max.
                                                   :9.32821
                                                              Max.
                                                                     : 12.0260
    Direction
##
    Down:484
##
##
    Up :605
##
##
##
##
```



Positive Correlation between Year and Volume observed.

4.10.b

```
##
## Call:
## glm(formula = Direction ~ ., family = binomial, data = Weekly[,
##
       c(2:7, 9)])
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                           Max
                      0.9913
## -1.6949 -1.2565
                              1.0849
                                        1.4579
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
                           0.08593
                                     3.106
                                             0.0019 **
## (Intercept) 0.26686
## Lag1
              -0.04127
                           0.02641 - 1.563
                                             0.1181
## Lag2
               0.05844
                           0.02686
                                    2.175
                                             0.0296 *
## Lag3
              -0.01606
                           0.02666 -0.602
                                             0.5469
                           0.02646 -1.050
## Lag4
              -0.02779
                                             0.2937
## Lag5
              -0.01447
                           0.02638 -0.549
                                             0.5833
              -0.02274
                           0.03690 -0.616
## Volume
                                            0.5377
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
```

```
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 1496.2 on 1088 degrees of freedom
## Residual deviance: 1486.4 on 1082 degrees of freedom
## AIC: 1500.4
##
## Number of Fisher Scoring iterations: 4
```

To check if a parameter is significant or not, we must check for its P-Vaue.

From the Summary, only Lag2 has a P-Value < 0.05. Thus, only Lag2 is statistically significant.

4.10.c

```
## Reference
## Prediction Down Up
## Down 54 48
## Up 430 557
```

Accuracy : 56.11 %

Recall/Sensitivity : 92.07 %

Precision : 56.43 %

Specificity : 11.16 %

Up Prediction Rate : 56.43 %

Down Prediction Rate: 52.94 %

48 "Up" were mistaken for "Down". 430 "Down" were mistaken for "Up". 54 "Down" + 557 "Up" were predicted accurately . Model is has higher accuracy when the prediction is "Up"

These results were obtained from the same set of observations the model was trained upon. Therefore, it is highly likely that the results would prove to be *overly optimistic* when tested on a new set of data.

4.10.d

```
## Reference
## Prediction Down Up
## Down 9 5
## Up 34 56
```

[Logistic Regression] Overall Fraction of Correct Predictions (Accuracy): 0.62

4.10.g

```
## Reference
## Prediction Down Up
## Down 21 30
## Up 22 31
## [KNN (k = 1)] Overall Fraction of Correct Predictions (Accuracy): 0.5
```

4.10.h

Considering **only Accuracy** as our metric, we can conclude that *Logistic Regression* outperforms KNN (with k=1)

4.10.i

Experimenting with different KNN models:

```
## Predictors: Lag2
## [KNN (k = 30)] Accuracy: 0.53
## [KNN (k = 130)] Accuracy: 0.57
## [KNN (k = 230)] Accuracy: 0.59
## [KNN (k = 330)] Accuracy: 0.59
## Predictors: Lag2, Lag1
## [KNN (k = 30)] Accuracy: 0.54
## [KNN (k = 130)] Accuracy: 0.57
## [KNN (k = 230)] Accuracy: 0.59
## [KNN (k = 330)] Accuracy: 0.59
##
## Predictors: Lag2^2
## [KNN (k = 30)] Accuracy: 0.62
## [KNN (k = 130)] Accuracy : 0.62
## [KNN (k = 230)] Accuracy: 0.59
## [KNN (k = 330)] Accuracy: 0.59
##
## Predictors: Lag2*Lag1
## [KNN (k = 30)] Accuracy: 0.55
## [KNN (k = 130)] Accuracy: 0.57
## [KNN (k = 230)] Accuracy: 0.57
## [KNN (k = 330)] Accuracy: 0.59
##
## Predictors: All
## [KNN (k = 30)] Accuracy: 0.89
## [KNN (k = 130)] Accuracy: 0.86
## [KNN (k = 230)] Accuracy: 0.79
## [KNN (k = 330)] Accuracy: 0.75
```

Considering only **Accuracy**, we can conclude that the following models perform the best:

K= 30, Predictors: All Predictors

Experimenting with different Logistic Regression Models:

Logistic Regression

```
##
## [Predictors: Lag2 ] Accuracy : 0.62
## [Predictors: Lag2*Lag1 ] Accuracy : 0.58
## [Predictors: Lag2*Lag1 ] Accuracy : 0.58
## [Predictors: I(Lag2^2) ] Accuracy : 0.59
## [Predictors: All] Accuracy : 1
```

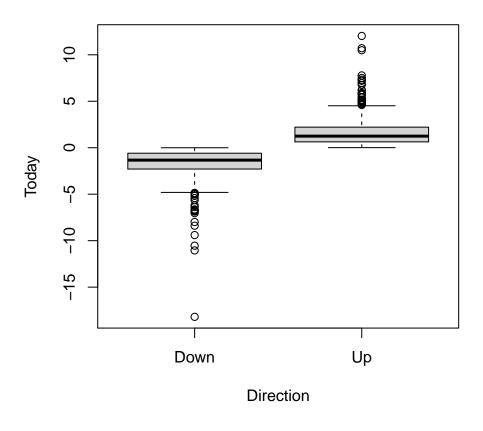
Considering Accuracy, It seems Using **All the Parameters** gives by far the most accurate model with a **100%** Accuracy.

Confusion Matrix for Linear Regression Model with All Predictors:

```
## Reference
## Prediction Down Up
## Down 43 0
## Up 0 61
```

NOTE: This is not surprising because one of the predictors the model trains upon is **Today**. This predictor seems to have a distinct linear boundary when plotted against **Direction**

Spread of Today v/s Direction



EXERCISE 6.9:

6.9.a

Creating a 80--20 split between Train and Test set

Length of College Dataset: 777

Length of Train Dataset : 622

Length of Test Dataset : 155

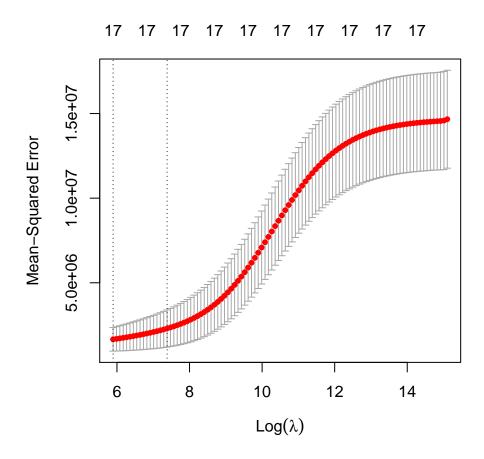
6.9.b

The test error on applying Linear Regression on a Model with All Parameters is:

1578073.167

6.9.c

Optimal Lambda, by 10-fold cross-validation is: 362.660783476255



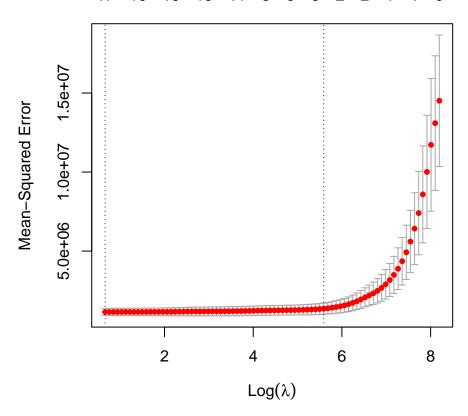
The test error on applying ${\bf Ridge\text{-}Regression}$ on a Model with All Parameters is:

1447148.005

6.9.d

 $\mbox{\tt \#\#}$ Optimal Lambda, by 10-fold cross-validation is: 1.93541152134794

17 16 16 13 11 5 3 3 2 2 1 1 0



The test error on applying Lasso-Regression on a Model with All Parameters is:

1565219.591

Coefficients of Predictors using the Lasso-Regression method are:

```
PrivateYes
                                     Enroll
                                               Top10perc
                                                             Top25perc
                                                                         F.Undergrad
##
                       Accept
    -381.594455
                  4108.880244 -1025.359690
                                              864.928922
                                                           -247.672551
                                                                          333.295597
##
    P.Undergrad
                     Outstate
                                 Room.Board
                                                              Personal
                                                                                  PhD
##
                                                    Books
##
      98.397947
                  -293.010691
                                 153.190780
                                               32.808299
                                                             10.803342
                                                                         -157.271619
##
       Terminal
                    S.F.Ratio
                               perc.alumni
                                                   Expend
                                                             Grad.Rate
##
      -3.363536
                    68.276135
                                   7.318633
                                              297.806071
                                                             96.507224
```

Thus, Non-Zero Coefficient Estimate Predictors are:

```
"PrivateYes"
                       "Accept"
                                      "Enroll"
                                                     "Top10perc"
                                                                    "Top25perc"
##
                       "P.Undergrad"
       "F.Undergrad"
                                      "Outstate"
                                                     "Room.Board"
                                                                    "Books"
                       "PhD"
## [11] "Personal"
                                      "Terminal"
                                                     "S.F.Ratio"
                                                                    "perc.alumni"
## [16] "Expend"
                       "Grad.Rate"
```

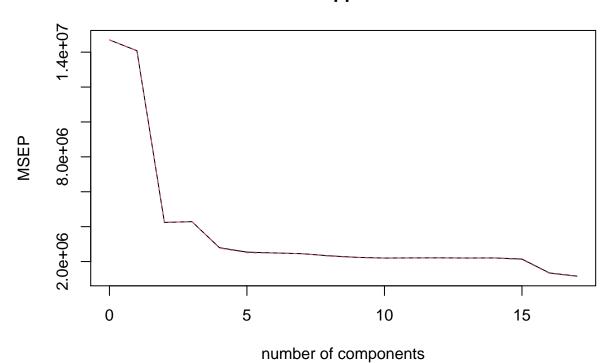
Apps

85.40

85.75

85.75

Apps



```
## Data:
            X dimension: 622 17
  Y dimension: 622 1
## Fit method: svdpc
## Number of components considered: 17
##
## VALIDATION: RMSEP
## Cross-validated using 10 random segments.
          (Intercept) 1 comps
                                 2 comps
                                         3 comps
                                                   4 comps
                                                             5 comps
                                                                      6 comps
## CV
                 3834
                           3753
                                    2060
                                             2071
                                                       1672
                                                                1594
                                                                         1579
                                                                1583
## adjCV
                 3834
                           3754
                                    2057
                                             2072
                                                       1665
                                                                         1576
##
          7 comps 8 comps
                            9 comps
                                     10 comps
                                               11 comps
                                                           12 comps
                                                                     13 comps
## CV
             1566
                       1526
                                1497
                                          1483
                                                     1486
                                                               1488
                                                                         1484
             1565
                                                     1484
## adjCV
                       1519
                                1494
                                          1481
                                                               1485
                                                                         1481
##
          14 comps
                    15 comps
                               16 comps
                                         17 comps
## CV
              1486
                         1464
                                   1160
                                             1079
              1483
                                             1073
## adjCV
                         1454
                                   1150
## TRAINING: % variance explained
##
         1 comps 2 comps 3 comps 4 comps 5 comps 6 comps
                                                                 7 comps
## X
          32.019
                    57.05
                              64.13
                                       70.01
                                                75.36
                                                          80.38
                                                                   84.09
                                                                             87.44
## Apps
           4.315
                    72.01
                              72.02
                                       81.89
                                                83.65
                                                          83.73
                                                                   83.98
                                                                             85.12
                            11 comps
##
                  10 comps
                                       12 comps
                                                13 comps 14 comps
         9 comps
                                                                      15 comps
## X
           90.48
                     92.84
                                94.92
                                          96.78
                                                     97.86
                                                               98.72
                                                                         99.36
                                                     85.88
```

85.76

85.94

89.94

```
## X 99.83 100.00
## Apps 92.88 93.47
```

Minimum CV at

Minimum CV at $\mathbf{M} = 17$. Thus, using $predict(\dots, ncomp=17,\dots)$

The test error on applying **Principal Component Regression** on a Model with All Parameters is:

1578073.167

6.9.f

Apps WSE b 1.46+00 0.50-0-06 0.50-0-06 1.46+00 1.46

```
## Data:
            X dimension: 622 17
   Y dimension: 622 1
## Fit method: kernelpls
## Number of components considered: 17
##
## VALIDATION: RMSEP
## Cross-validated using 10 random segments.
##
          (Intercept)
                        1 comps
                                 2 comps
                                          3 comps
                                                    4 comps
                                                             5 comps
                                                                      6 comps
                           1880
## CV
                 3834
                                    1630
                                              1445
                                                       1391
                                                                1243
                                                                          1165
## adjCV
                 3834
                           1876
                                    1630
                                              1440
                                                       1374
                                                                1221
                                                                          1153
```

```
##
          7 comps 8 comps 9 comps 10 comps 11 comps
                                                           12 comps
                                                                      13 comps
## CV
             1143
                                1124
                       1130
                                           1121
                                                     1122
                                                                1118
                                                                          1116
## adjCV
             1133
                       1121
                                1116
                                           1112
                                                     1113
                                                                1109
                                                                          1108
##
          14 comps
                    15 comps
                               16 comps
                                          17 comps
## CV
              1116
                         1116
                                   1116
                                              1116
## adjCV
              1108
                         1108
                                   1108
                                              1108
##
## TRAINING: % variance explained
##
         1 comps
                  2 comps 3 comps
                                     4 comps
                                               5 comps
                                                        6 comps
                                                                 7 comps
                                                                           8 comps
                                        65.06
## X
           25.52
                     45.30
                              62.57
                                                 67.50
                                                          72.05
                                                                    76.04
                                                                             80.49
                                                                    93.24
## Apps
           77.30
                     83.58
                              87.50
                                        90.88
                                                 92.89
                                                          93.15
                                                                             93.31
##
         9 comps
                  10 comps
                             11 comps
                                       12 comps
                                                 13 comps
                                                            14 comps
                                                                       15 comps
## X
           82.50
                      85.41
                                87.76
                                           91.08
                                                     92.72
                                                                95.12
                                                                          96.97
                      93.42
                                                                93.47
           93.39
                                93.45
                                           93.46
                                                     93.46
                                                                          93.47
## Apps
##
         16 comps
                   17 comps
            97.98
## X
                      100.00
## Apps
            93.47
                       93.47
```

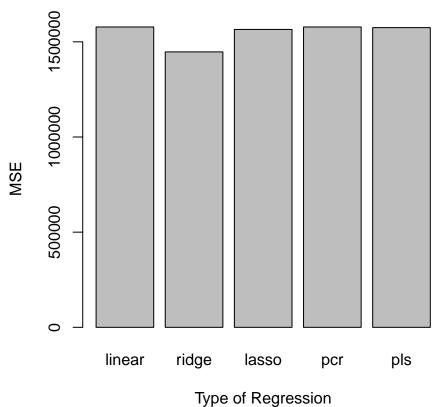
Minimum CV at $\mathbf{M} = 13$. Thus, using $predict(\dots, ncomp = 13, \dots)$

The test error on applying Partial Least Squares Regression on a Model with All Parameters is:

1574745.803

6.9.g

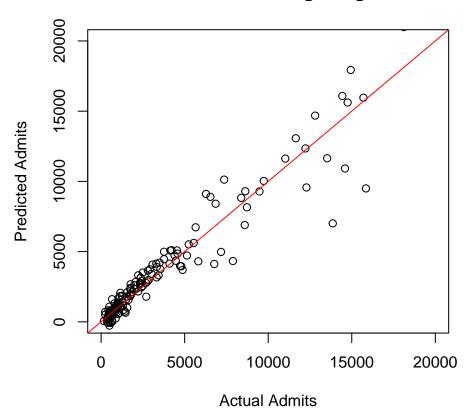




Most of the regression methods ("Linear", "Ridge", "Lasso", "PCR", "PLS") have approximately the same amount of error.

The **Ridge Regression** outperforms others by a slight margin. Its **Test MSE** is: 1447148.005 (standard deviation = 5319499)

Prediction Error in Ridge Regression



EXERCISE 6.11:

6.11.a

Creating a 80-20 split between Train and Test set

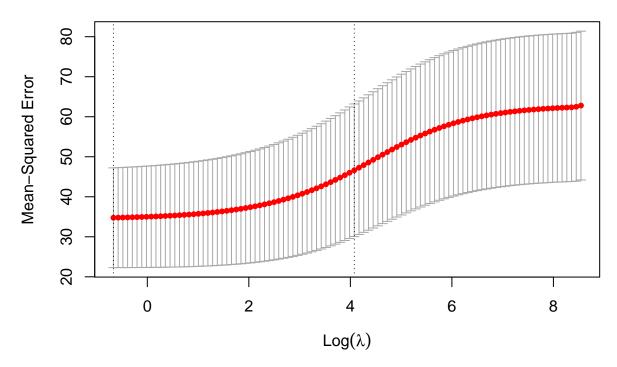
Length of Boston Dataset: 506

Length of Train Dataset : 405

Length of Test Dataset : 101

Ridge Regression

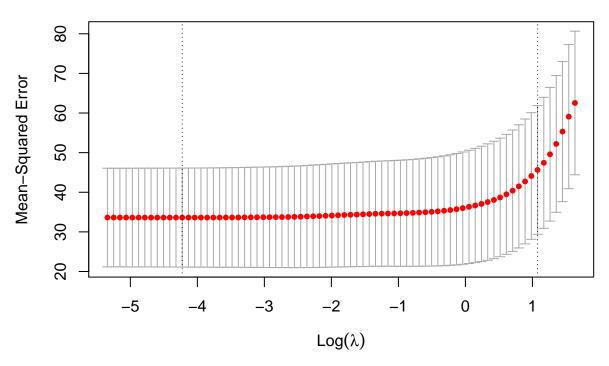




- ## Optimal Lambda, by 10-fold cross-validation is: 0.51
- ##
- ## Test Error of Ridge Regression: 79.45

Lasso Regression

13 13 13 13 13 11 11 11 8 6 4 4 3 3 3 1 1



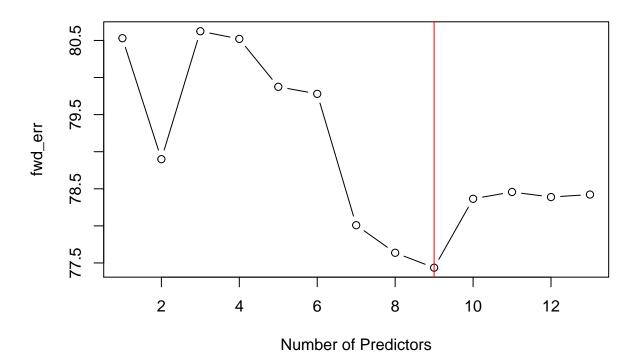
```
## Optimal Lambda, by 10-fold cross-validation is: 0.01
##
## Test Error of Lasso Regression: 78.45
```

Subset Selection (Forward Selection)

```
## Subset selection object
  Call: regsubsets.formula(crim ~ ., data = train, nvmax = ncol(Boston) -
##
       1)
## 13 Variables (and intercept)
##
           Forced in Forced out
## zn
               FALSE
                           FALSE
                          FALSE
## indus
               FALSE
                          FALSE
## chas
               FALSE
               FALSE
                          FALSE
## nox
## rm
               FALSE
                          FALSE
## age
               FALSE
                          FALSE
## dis
               FALSE
                          FALSE
## rad
               FALSE
                          FALSE
## tax
               FALSE
                          FALSE
## ptratio
               FALSE
                          FALSE
## black
                          FALSE
               FALSE
## lstat
               FALSE
                          FALSE
                          FALSE
## medv
               FALSE
```

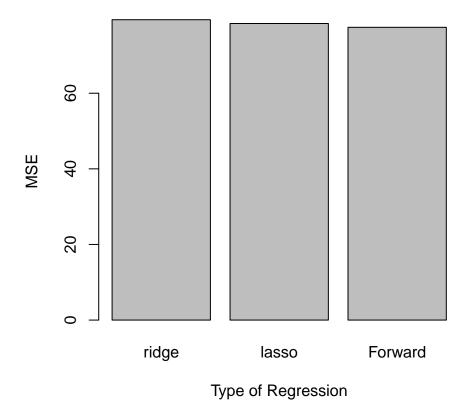
```
## 1 subsets of each size up to 13
## Selection Algorithm: exhaustive
                              age dis rad tax ptratio black lstat medv
           zn indus chas nox rm
## 1
    (1)
                        "*"
     (1)
##
     (1)
                                                    "*"
     (1
## 5
                                                    "*"
     (1
## 7
     (1)
                                                    "*"
                                                         "*"
     ( 1
                                                              "*"
## 10
                                                    "*"
                                                    "*"
                                                    "*"
## 12
## 13
      (1)
                                                    "*"
                                                              "*"
```

Test MSE for Forward Selection



Min. Test Error for Forward Selection is: 77.44

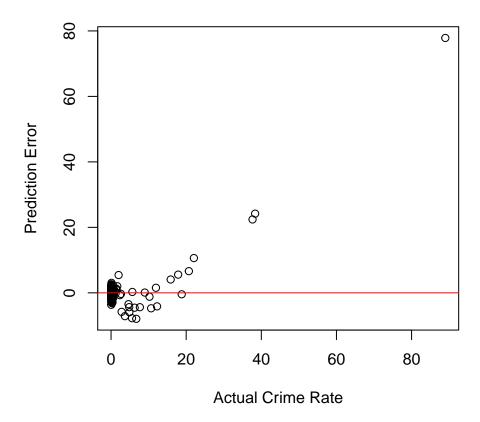
Comparison of Regression Fit



The regression methods ("Ridge", "Lasso", " $Forward\ Selection$ ") have approximately the same amount of error.

The Subset Selection (Forward Selection) Regression outperforms others by a slight margin. Its \mathbf{MSE} is: 69.55

Residuals



6.11.b

From the above Test Set Errors, we can reasonably conclude that the 11-parameter Forward selection model is the best fit to the Boston Dataset

6.11.c

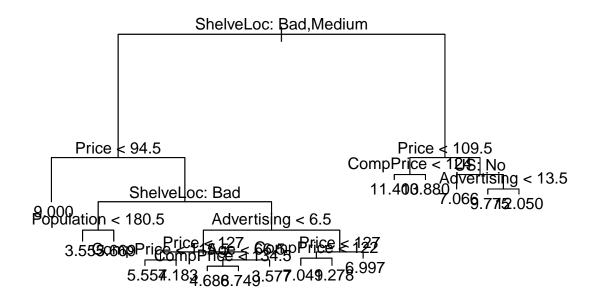
No because not all the predictors add much value to the model. Adding more predictors makes the model more complex and computationally expensive. Thus, If a predictor does not increase the amount of variance explained by the model significantly, we can drop it. In our case, We choose the Forward Selection model, which uses just 11 Predictors.

EXERCISE 8.8:

8.8.a

Length of Carseats Dataset: 400

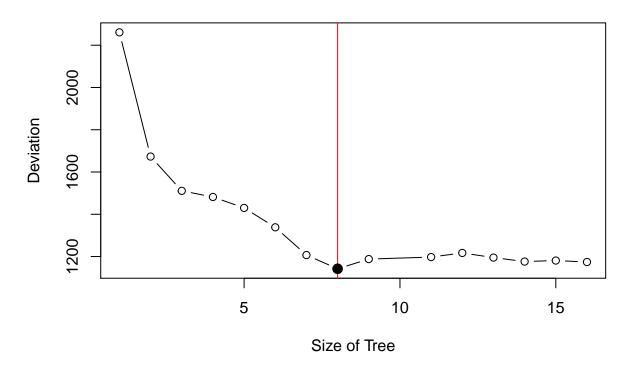
```
## Length of Train Dataset : 280
## Length of Test Dataset : 120
8.8.b
##
## Regression tree:
## tree(formula = Sales ~ ., data = carseats_train)
## Variables actually used in tree construction:
## [1] "ShelveLoc"
                    "Price"
                                  "Population" "Advertising" "CompPrice"
## [6] "Age"
## Number of terminal nodes: 16
## Residual mean deviance: 2.575 = 679.8 / 264
## Distribution of residuals:
     Min. 1st Qu. Median
                             Mean 3rd Qu.
## -3.5770 -1.0600 -0.2128 0.0000 1.0250 5.1330
```



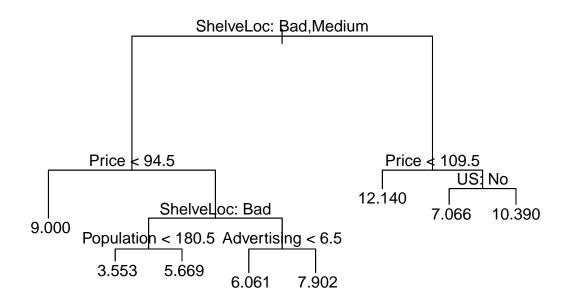
Test MSE for tree is: 4.27687725775323

8.8.c

Selecting Tree Size by Cross-Validation



Therefore, Cross-Validation suggests minimum Deviation at tree size of 8. Thus, Pruning the tree to size of 8



Test MSE for Pruned tree is: 5.08898603003723

We observe that Test MSE has increased to 5.09 after pruning.

8.8.d

For Bagging, Implementing Random Forest with each tree considering all parameters (mtry = ncol(Carseats) - 1)

 ${m NOTE}:$ Subtracting 1 from ncol(Carseats) because one of the columns in the DataSet is the target column itself

Test MSE for Bagged Model is: 2.44628424130643

##		%IncMSE	IncNodePurity
##	ShelveLoc	78.6084580	748.557677
##	Price	62.4450684	591.976064
##	CompPrice	32.5703925	217.430548
##	Advertising	28.2289858	210.788050
##	Age	16.6401794	166.092738
##	Income	5.2444968	95.395989
##	Population	-0.1787145	82.961943
##	Education	3.3273281	63.948412
##	US	6.7573125	15.904009
##	Urban	-2.5443548	8.609084

From the above table, we see that **ShelveLoc** and **Price** are the most important predictors for Sales.

8.8.e

For Random Forest, each tree will consider a subset of parameters

$$m = \sqrt{(p)}$$

Thus: (mtry = floor(sqrt(ncol(Carseats) - 1)))

 ${m NOTE}:$ Subtracting 1 from ncol(Carseats) because one of the columns in the DataSet is the target column itself

Test MSE for Random Forest Model is: 2.90107946940021

We observe that reducing m from 10 (Bagging) to 3 (Random Forest) increases the Test MSE a little bit.

This increase in MSE can be explained by the fact that in Random Forest, unlike Bagging (wherein each tree is exposed to all the predictors), each tree is exposed to a subset of the predictors.

##		%IncMSE	IncNodePurity
##	ShelveLoc	48.4045567	549.59174
##	Price	40.2843961	508.51985
##	Age	16.7054144	232.84697
##	Advertising	19.8861191	211.35524
##	CompPrice	12.4875929	185.69329
##	Income	1.4748646	152.24336
##	Population	0.1294146	150.96879
##	Education	1.8102926	99.19403
##	US	4.4167507	27.62612
##	Urban	-1.7114750	17.57537

From the above table, we see that **ShelveLoc** and **Price** are the still most important predictors for Sales.

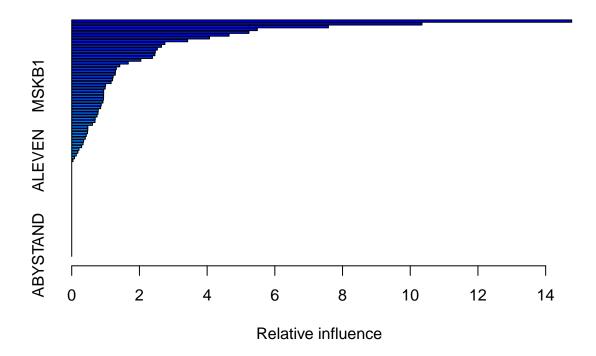
EXERCISE 8.11:

8.11.a

Length of Caravan Dataset: 5822

Length of Train Dataset : 1000

Length of Test Dataset : 4822



```
##
                          rel.inf
                  var
## PPERSAUT PPERSAUT 14.76897821
## MKOOPKLA MKOOPKLA 10.34608977
## MOPLHOOG MOPLHOOG
                      7.58276819
## MBERMIDD MBERMIDD
                       5.48219989
## PBRAND
              PBRAND
                       5.23496596
## ABRAND
              ABRAND
                       4.64846137
## MGODGE
              MGODGE
                       4.07035536
                       3.42388385
## MINK3045 MINK3045
## MAUT1
               MAUT1
                       2.75186778
## MGODPR
              {\tt MGODPR}
                       2.65078748
## MOSTYPE
             MOSTYPE
                       2.52899159
                       2.47005442
## MAUT2
               MAUT2
             PWAPART
                       2.45561187
## PWAPART
## MINKGEM
             MINKGEM
                       2.38496124
## MBERARBG MBERARBG
                       2.04151595
## MSKC
                MSKC
                       1.66946684
## MINK7512 MINK7512
                       1.41843892
## MRELGE
              MRELGE
                       1.31818732
## MSKA
                MSKA
                       1.29174003
## PBYSTAND PBYSTAND
                       1.28796768
## MFWEKIND MFWEKIND
                       1.22285160
## MBERHOOG MBERHOOG
                       1.20643199
## MGODOV
              MGODOV
                       1.16347453
```

```
## MSKB1
               MSKB1
                      1.00060171
                      0.98767774
## MHHUUR
              MHHUUR
## MBERBOER MBERBOER
                      0.94327732
## MFGEKIND MFGEKIND
                      0.94278746
## MAUTO
               MAUTO
                      0.94186003
## MGODRK
                      0.93716929
              MGODRK
                      0.92108809
## MINK4575 MINK4575
## MRELOV
              MRELOV
                      0.87214668
## MSKB2
               MSKB2
                      0.85468878
## MOPLMIDD MOPLMIDD
                      0.78499519
## MOSHOOFD MOSHOOFD
                      0.77643271
## APERSAUT APERSAUT
                      0.74746748
## MSKD
                MSKD
                      0.69351351
## MINKM30
             MINKM30
                      0.68778644
## PLEVEN
              PLEVEN
                      0.61251083
## MBERARBO MBERARBO
                      0.47629718
## PMOTSCO
             PMOTSCO
                      0.47452037
## MZPART
              MZPART
                      0.46517256
## MGEMLEEF MGEMLEEF
                      0.43011772
## MGEMOMV
             MGEMOMV
                      0.40006320
## MZFONDS
             MZFONDS
                      0.35216196
## MHKOOP
              MHKOOP
                      0.33449542
                      0.29175841
## MINK123M MINK123M
## MFALLEEN MFALLEEN
                      0.21368001
                      0.18161892
## MRELSA
              MRELSA
## MBERZELF MBERZELF
                      0.13498287
## MOPLLAAG MOPLLAAG
                      0.08308058
## ALEVEN
              ALEVEN
                      0.03799572
## MAANTHUI MAANTHUI
                      0.0000000
## PWABEDR
             PWABEDR
                      0.0000000
## PWALAND
             PWALAND
                      0.0000000
## PBESAUT
             PBESAUT
                      0.0000000
## PVRAAUT
             PVRAAUT
                      0.0000000
## PAANHANG PAANHANG
                      0.00000000
## PTRACTOR PTRACTOR
                      0.0000000
              PWERKT
                      0.00000000
## PWERKT
## PBROM
               PBROM
                      0.0000000
## PPERSONG PPERSONG
                      0.0000000
## PGEZONG
             PGEZONG
                      0.00000000
                      0.00000000
## PWAOREG
             PWAOREG
## PZEILPL
             PZEILPL
                      0.0000000
## PPLEZIER PPLEZIER
                      0.0000000
## PFIETS
              PFIETS
                      0.0000000
## PINBOED
             PINBOED
                      0.0000000
## AWAPART
             AWAPART
                      0.0000000
## AWABEDR
             AWABEDR
                      0.0000000
## AWALAND
             AWALAND
                      0.0000000
## ABESAUT
             ABESAUT
                      0.0000000
                      0.0000000
## AMOTSCO
             AMOTSCO
## AVRAAUT
             AVRAAUT
                      0.00000000
## AAANHANG AAANHANG
                      0.0000000
## ATRACTOR ATRACTOR
                      0.0000000
## AWERKT
              AWERKT
                      0.0000000
## ABROM
               ABROM
                      0.00000000
```

```
## APERSONG APERSONG 0.00000000
## AGEZONG 0.00000000
## AWAOREG AWAOREG 0.00000000
## AZEILPL AZEILPL 0.00000000
## APLEZIER APLEZIER 0.00000000
## AFIETS AFIETS 0.00000000
## AINBOED AINBOED 0.00000000
## ABYSTAND ABYSTAND 0.00000000
```

From the Table and Graph, we can conclude that the top **Most-Important Predictors** are: * PPERSAUT * MKOOPKLA * MOPLHOOG

8.11.c

Boosting

```
## Reference
## Prediction 0 1
## 0 4412 255
## 1 121 34
```

[Boosting] Fraction of the people predicted to make a purchase who in fact make one: 0.22

This value is also called the **Precision**

Logistic Regression

```
## Reference
## Prediction 0 1
## 0 4183 231
## 1 350 58
```

[Logistic Regression]Fraction of the people predicted to make a purchase who in fact make one: 0.14

KNN

```
## 2 102 202 302 402
## out_precision_knn 0.08362369 NA NA NA NA
```

Simply applying KNN does not work because the training data is highly skewed. The following is the Summary of **Purchase** in Training Set:

```
## 0 1
## 941 59
```

Thus, the model ends up predicting everything as class-0 or *Not Purchased* Whole this achieves a High accuracy, the precision is low.

In order to improve the model, we probably need to undersample the majority class in our training data.

Summary: Boosting outperforms Logistic Regression. ***