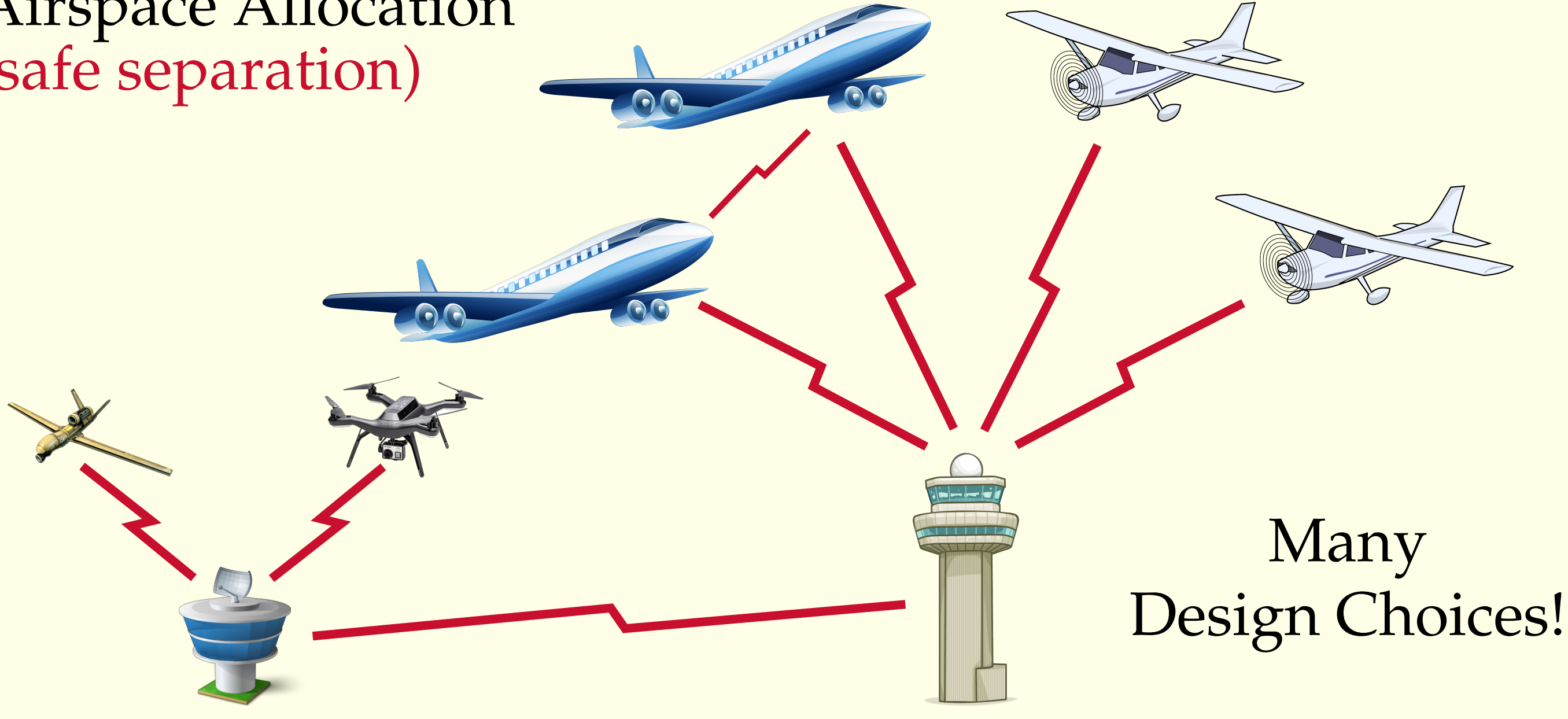


## 1. Motivation

Airspace Allocation  
(safe separation)



- The design of complex systems often requires analyzing several variants of the system under development for:
  - narrowing in on the final system design, and
  - check capabilities of system with varying features.
- The **design choices** constitute the system's **design space**.

**Model checking aids system development via a thorough comparison of all design choices**

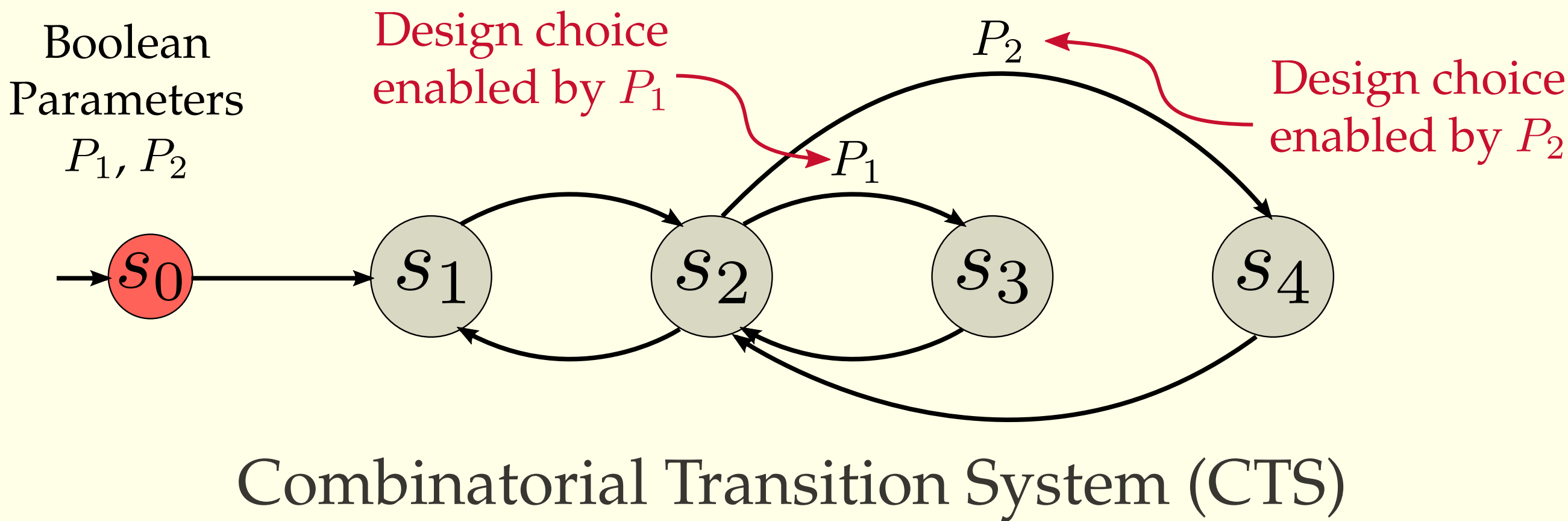
## 2. Modeling Design Spaces



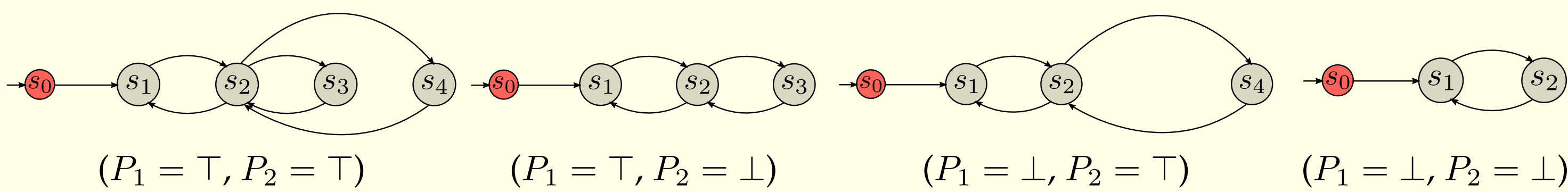
**Classical Method** – Every design choice is a model.  
very hard to cross-validate as design-space grows



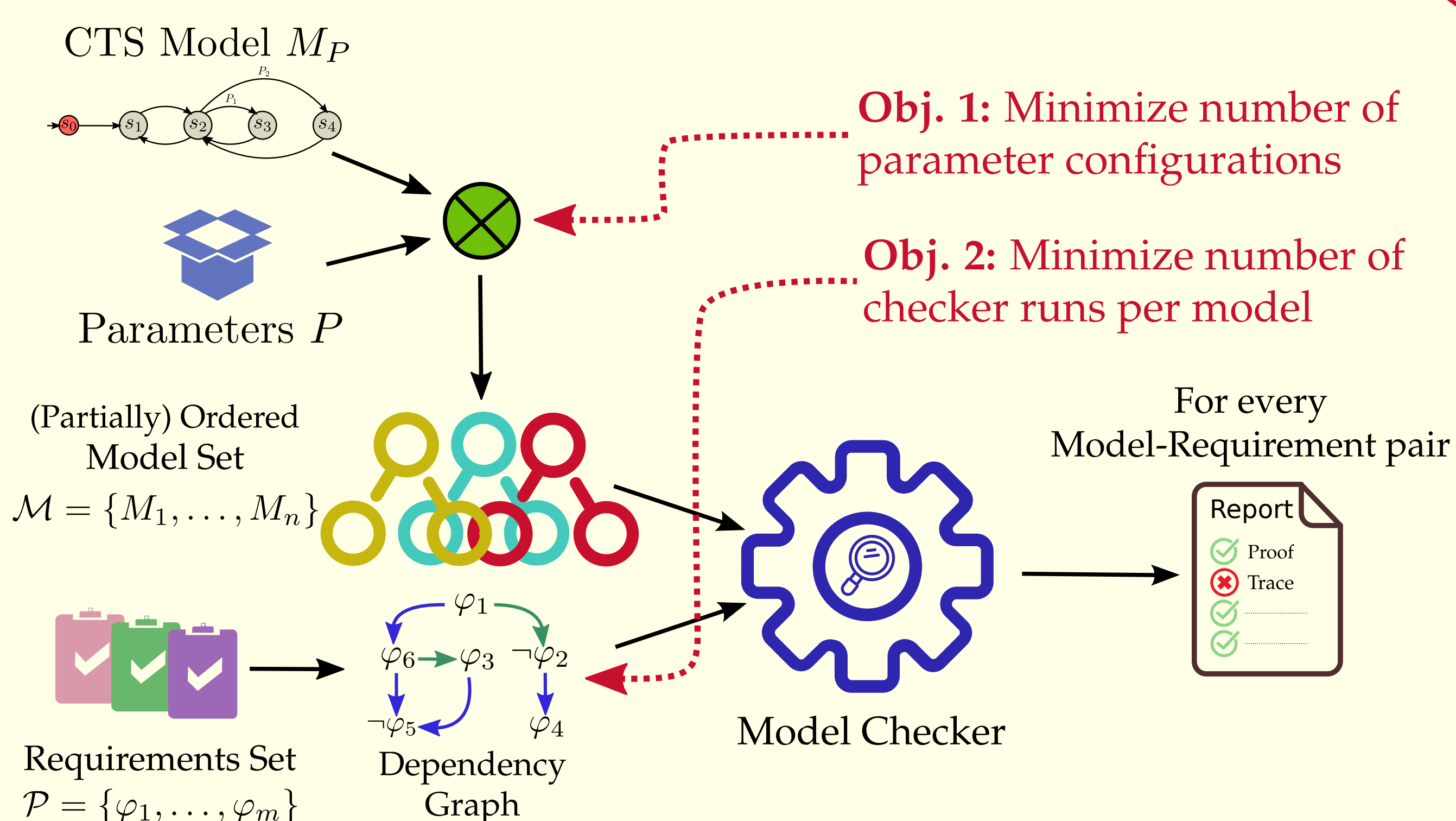
**Scalable Method** – Every design choice is a parameter.  
efficient, easier to maintain as design evolves



- Parameters are added as preprocessor directives.
  - works with off-the-shelf checkers, like NUXMV
  - every **parameter configuration** is a valid model



## 3. Problem Statement

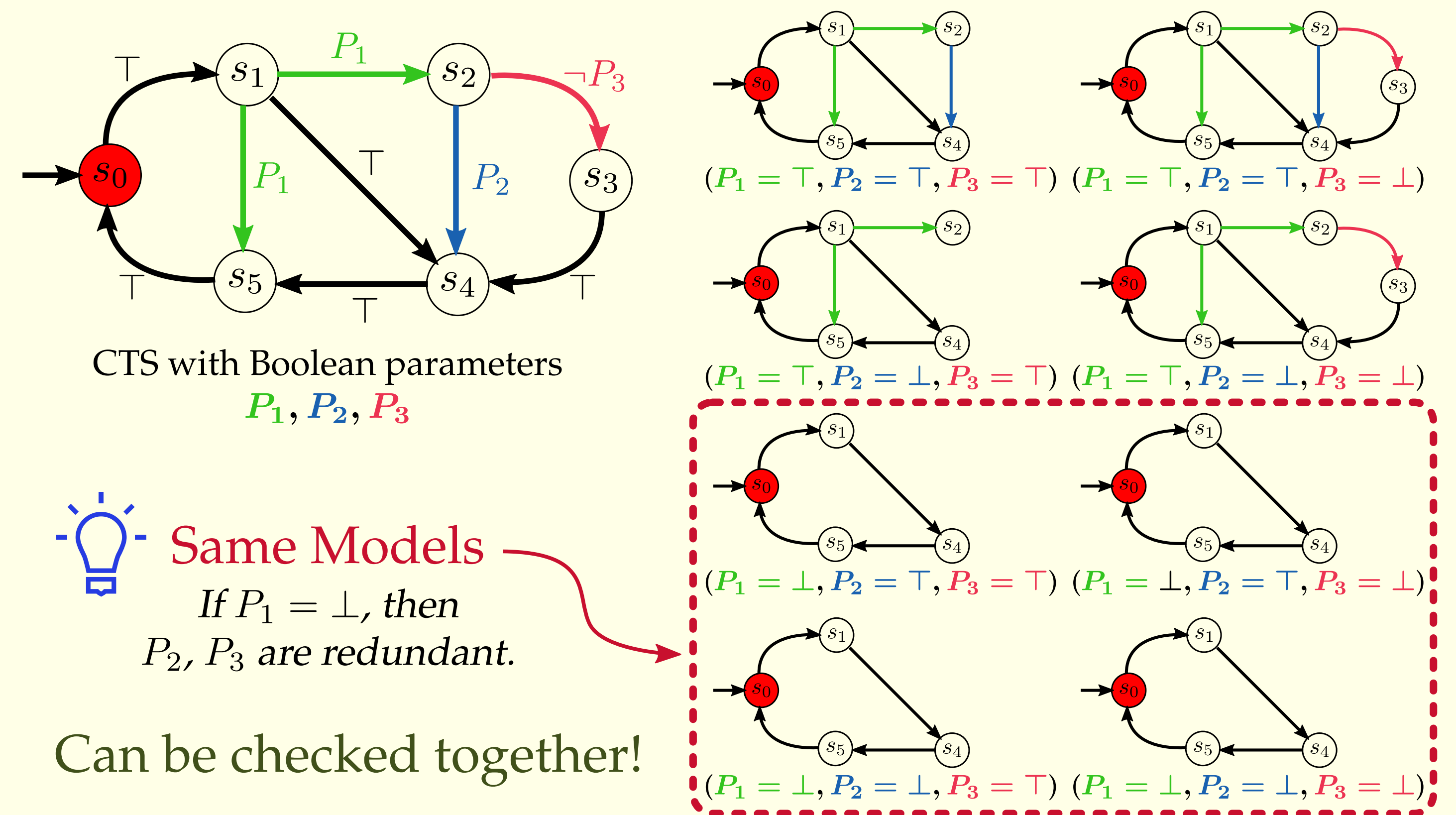


## 4. Our Solution

Discover Design-Space Dependencies, or  $D^3$

- Reduces design space by finding dependencies between:
  - parameters** (number of models to check)
  - properties** (number of model-checking runs)
- Is fully automatic, works with off-the-shelf checkers

i) Minimize number of parameter configurations (GENPC)



- Finds dependencies between parameter settings via reduction to a reachability problem.

ii) Minimize number of model-checking runs (CHECKRP)

$$\varphi_1 = \Box p \quad \varphi_2 = \Box(p \wedge q) \quad \varphi_3 = \Box(p \vee q)$$

$M \models \varphi_2$  then  $M \models \varphi_1$   
 $\varphi_1$  and  $\varphi_2$  are dependent

$M \models \varphi_2$  then  $M \models \varphi_3$   
 $\varphi_2$  and  $\varphi_3$  are dependent

- Finds dependencies between properties via fast LTL satisfiability checking.

keys	dependencies	result
$\varphi_1$	$T$ $\varphi_2$ $T$ $\varphi_3$ $T$ $\varphi_5$ $T$	$\varphi_1$ $F$ ✓
	$F$ $\varphi_3$ $F$	$\varphi_2$ $F$ ✓
$\varphi_2$	$T$ $\varphi_3$ $T$ $\varphi_4$ $T$	$\varphi_3$ $F$ ✓
	$F$ $\varphi_1$ $F$	$\varphi_4$ $T$ ✓
$\varphi_3$	$T$ $\varphi_1$ $T$ $\varphi_4$ $T$	$\varphi_5$ $T$ ✓
	$F$ $\varphi_2$ $F$ $\varphi_6$ $T$	$\varphi_6$ $T$ ✓
	...	...

Property Table

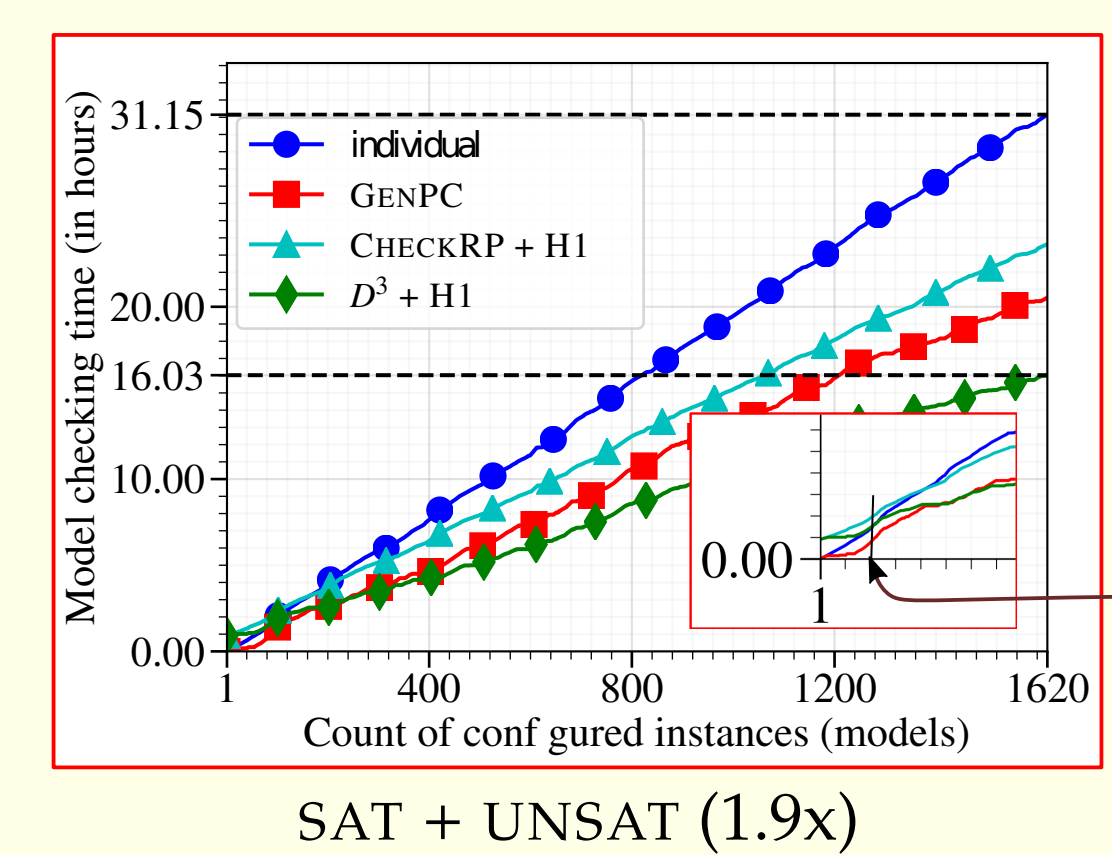
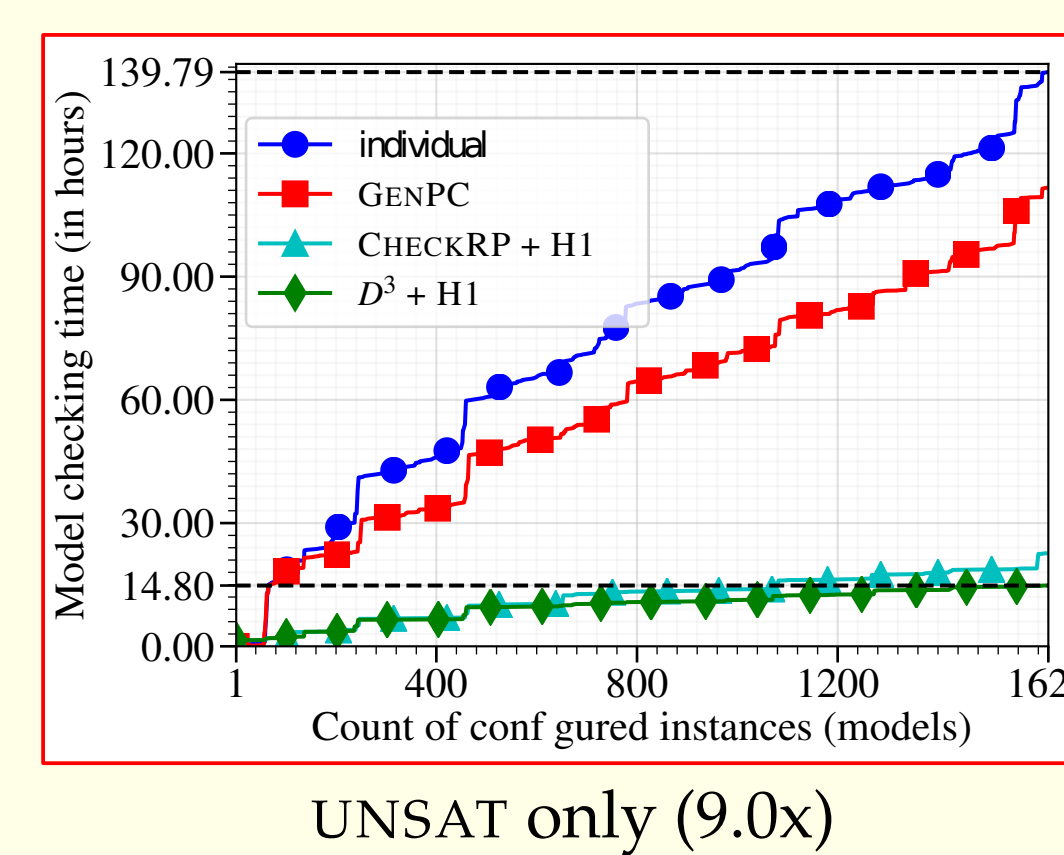
Result Array

$M \not\models \varphi_1$   
 $M \not\models \varphi_2$   $M \not\models \varphi_3$   $M \models \varphi_6$

One check  
Four results

## 5. Experimental Results

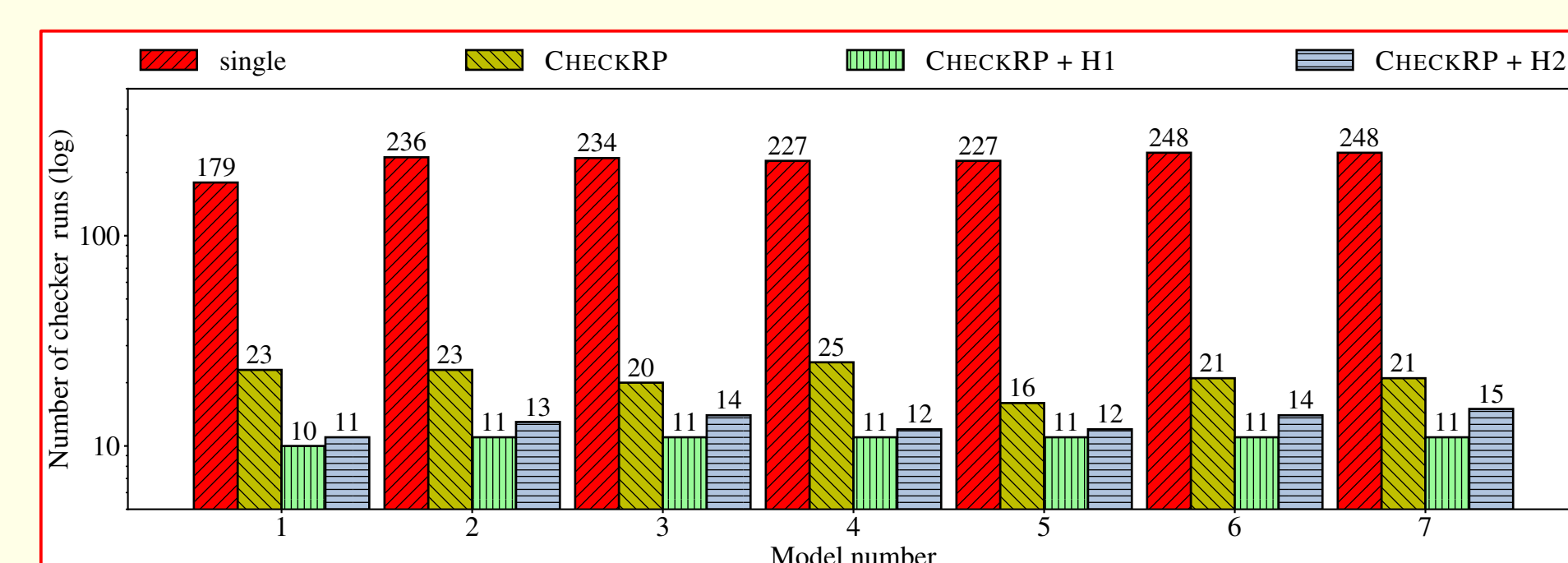
- NASA NextGen Air Traffic Control System



4.0x  
speedup

Crossover point  
(~ 120 models)

- BOEING Wheel Braking System



Heuristics  
H1: Maximum Dependence  
H2: Property Grouping

Fast  
multi-property  
verification