

FuseIC3

An Algorithm for Checking Large Design Spaces

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October 5, 2017

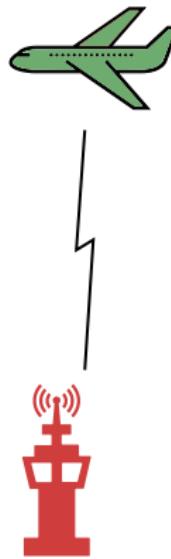
What is a Design Space?

Airspace Allocation

Design of allocation policies to ensure all airborne agents are safely separated.

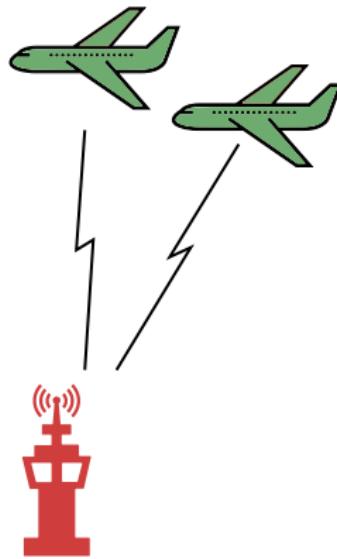
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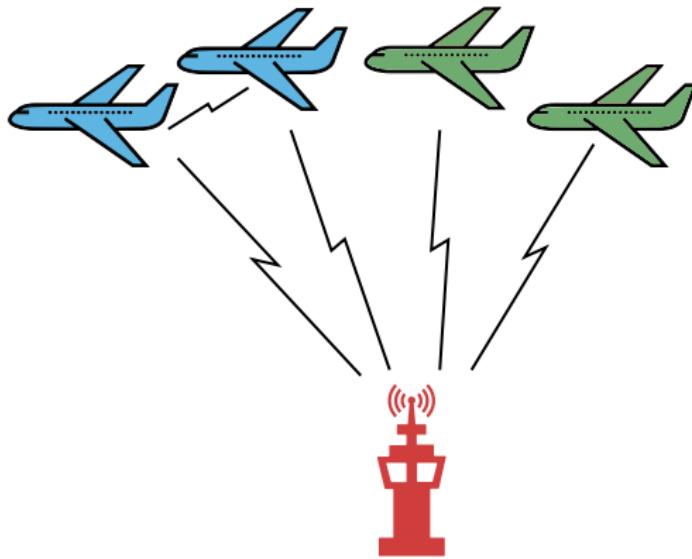
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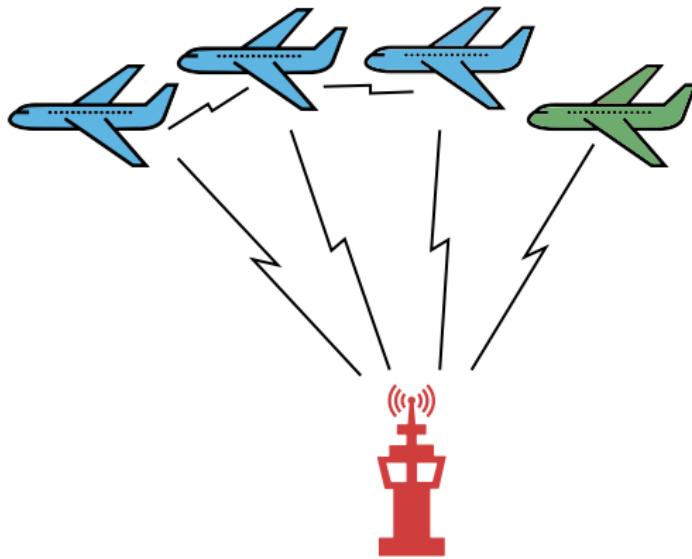
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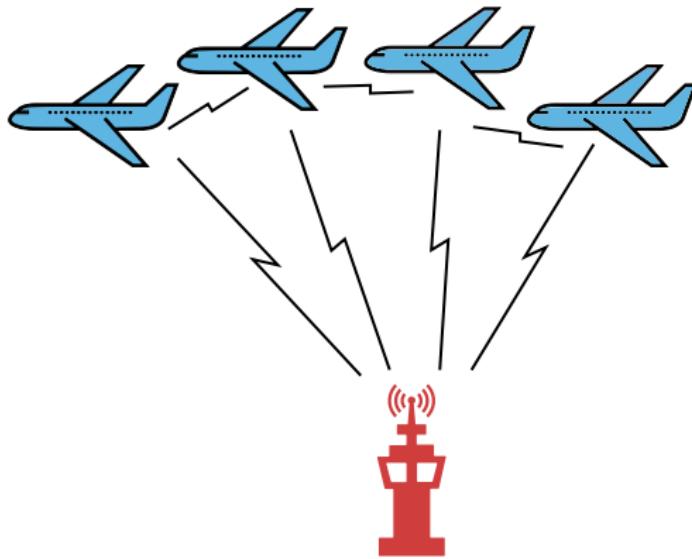
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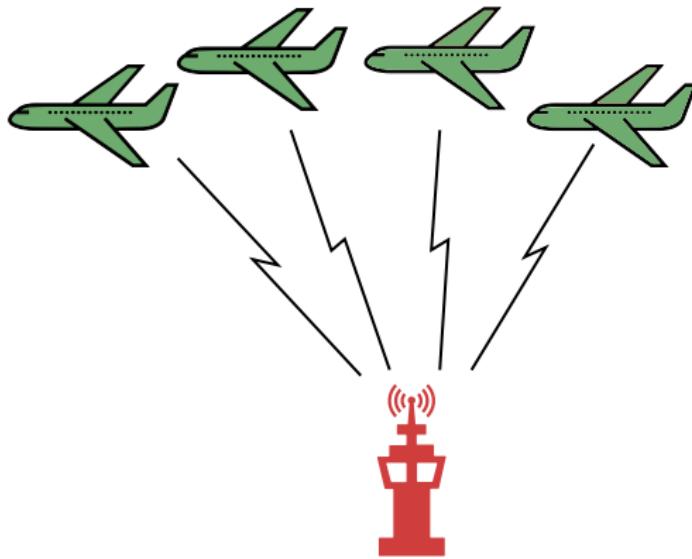
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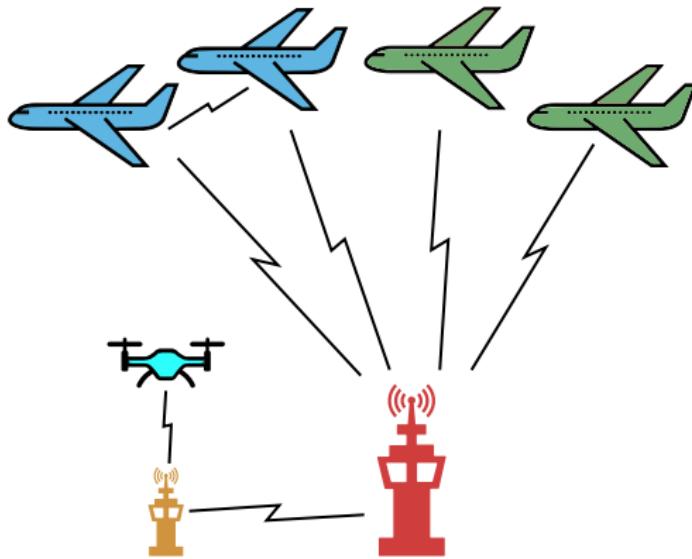
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Design of allocation policies to ensure all airborne agents are safely separated.



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Design of allocation policies to ensure all airborne agents are safely separated.

Lots of design choices!

What is a Design Space?

What is a Design Space?

Set of Design Choices for a System.

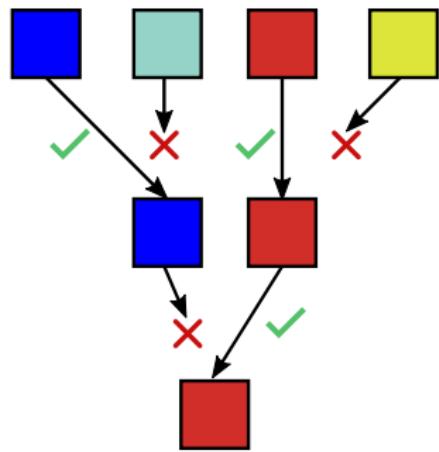
Design Problem

Design Problem

Complex systems are often modeled as **design spaces**.

Design Problem

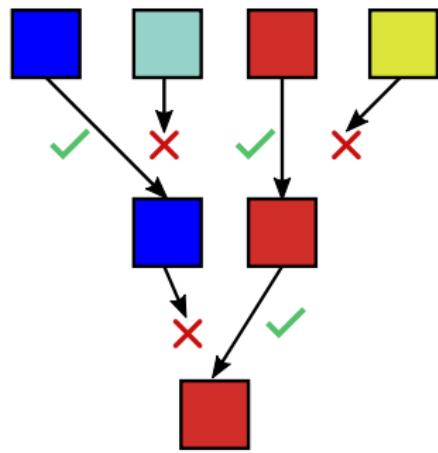
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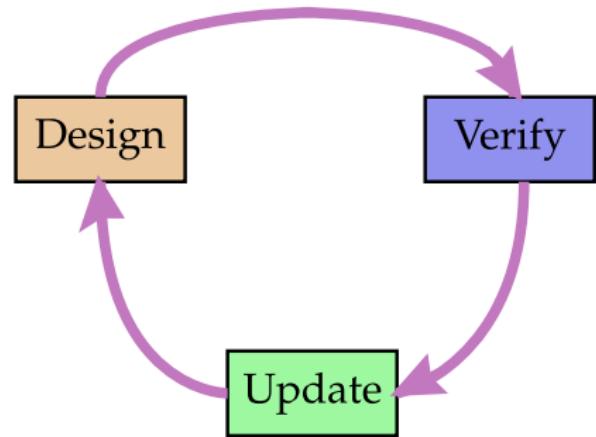
Alternative Comparison

Design Problem

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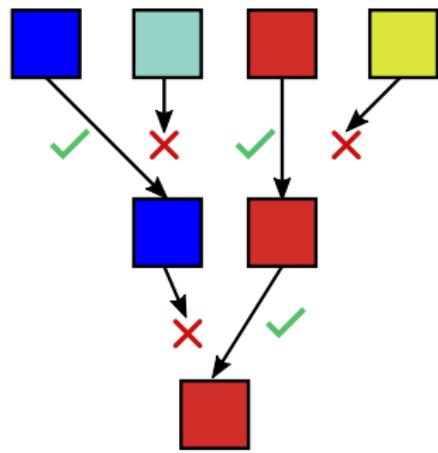
Alternative Comparison



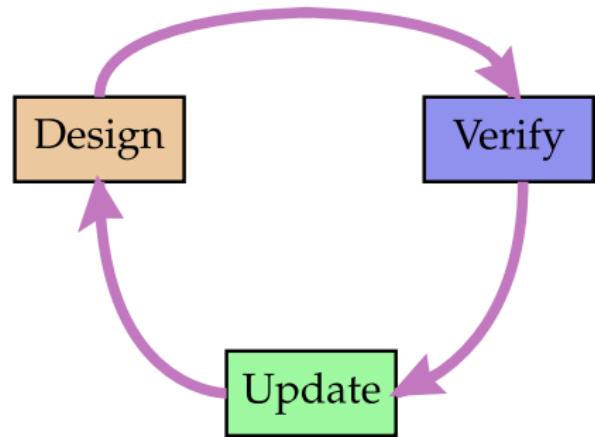
Incremental Development

Design Problem

Complex systems are often modeled as **design spaces**.



Alternative Comparison

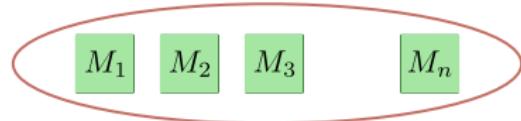


Incremental Development

Model checking!

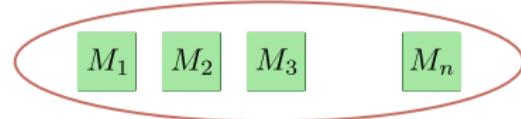
Classical Model Checking of a Design Space

Set of Models \mathcal{M}

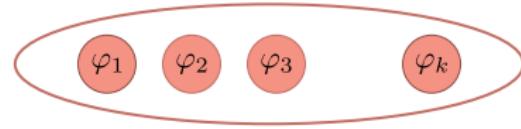


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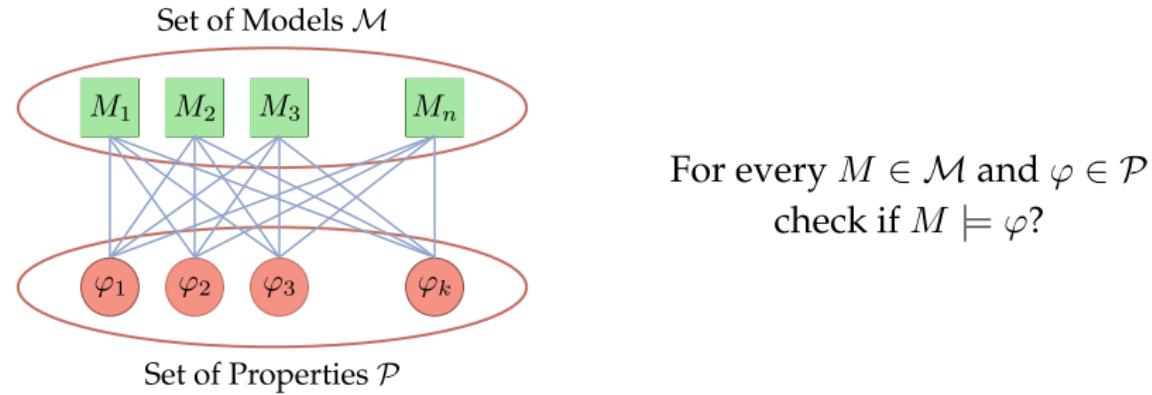
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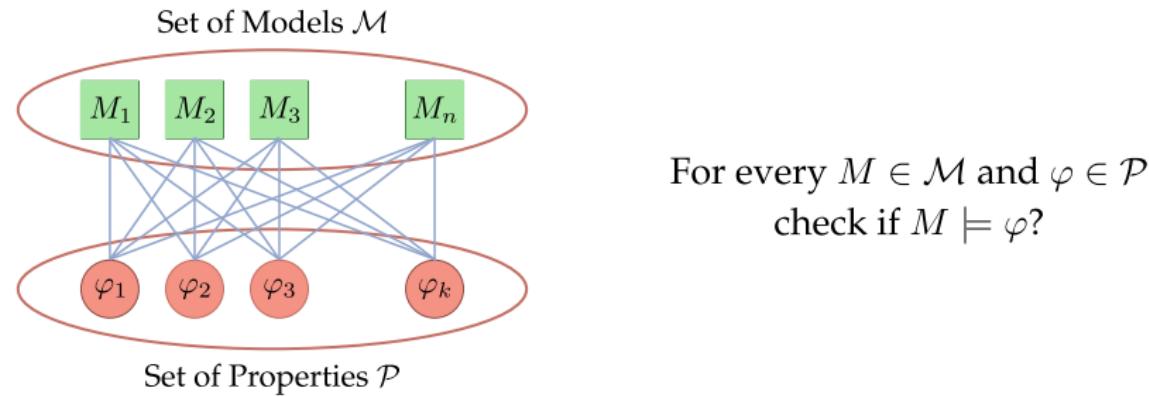
Set of Properties \mathcal{P}



Classical Model Checking of a Design Space

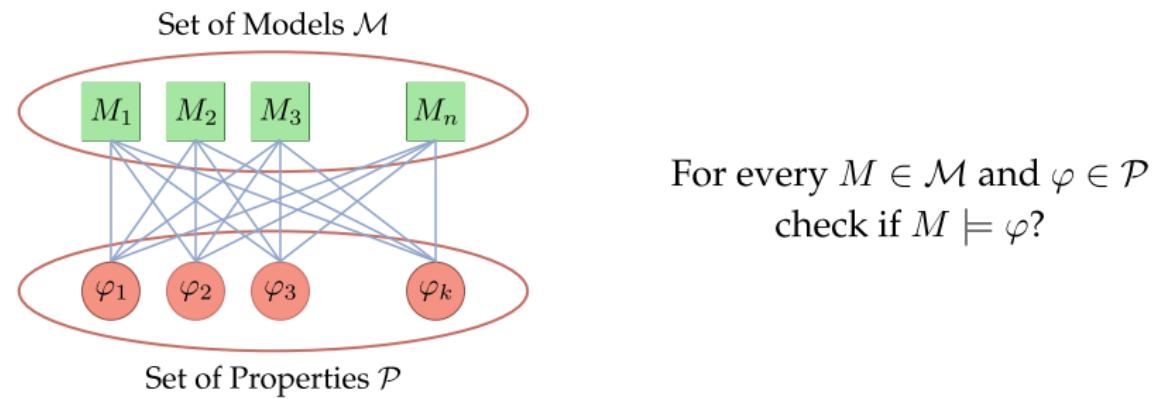


Classical Model Checking of a Design Space



- Inefficient for large design spaces
 - ▶ may not scale to handle combinatorial size of the design space.

Classical Model Checking of a Design Space



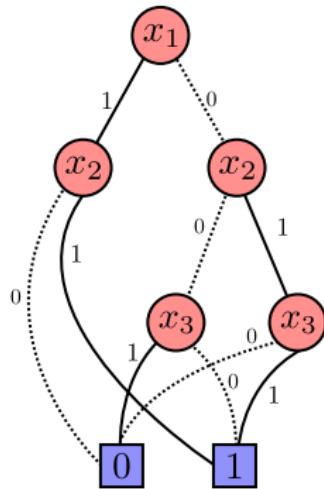
- Inefficient for large design spaces
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Can we do better?

Related Work

① Reusing BDD variable orderings

$$x_1 < x_2 < x_3$$

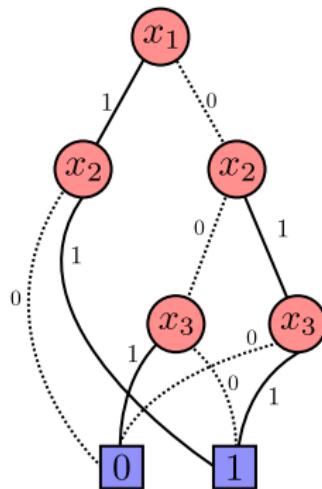


(Beer et al., 1996; Yang et al., 1998)

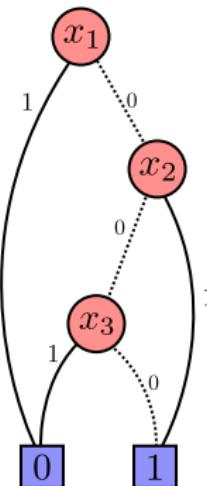
Related Work

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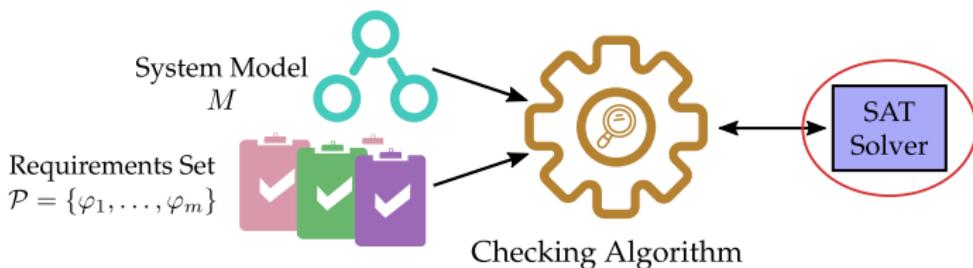


FuseIC3 is SAT-based

(Beer et al., 1996; Yang et al., 1998)

Related Work

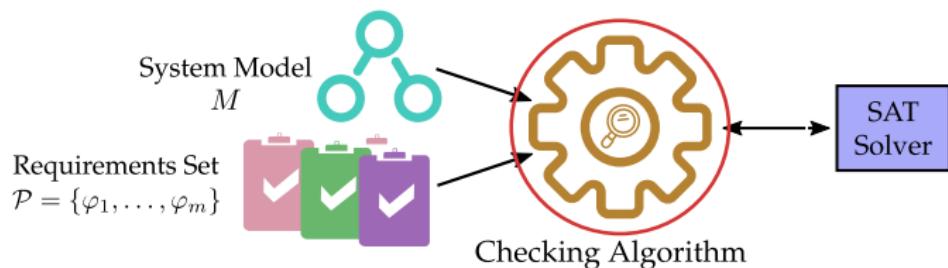
② SAT solver optimizations and clause reuse



(Marques-Silva, 2007; Schrammel et al., 2016; Chockler et al., 2011; Khasidashvili et al., 2006; Khasidashvili & Nadel, 2012)

Related Work

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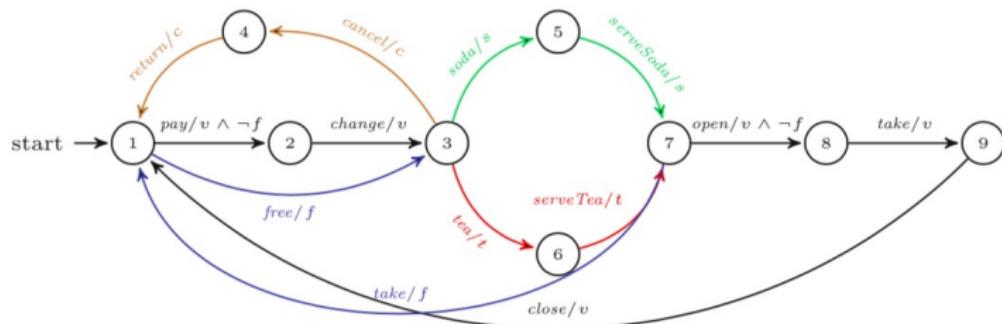


FuseIC3 reuses model checking artifacts

(Marques-Silva, 2007; Schrammel et al., 2016; Chockler et al., 2011; Khasidashvili et al., 2006; Khasidashvili & Nadel, 2012)

Related Work

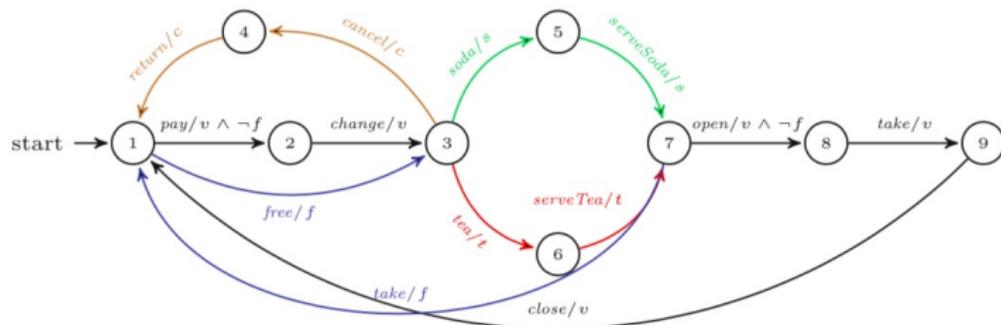
③ Software product line verification



(Ben-David et al., 2015; Classen et al., 2012, 2011, 2010; Dimovski et al., 2015)

Related Work

③ Software product line verification



FuseIC3 does not require custom modeling

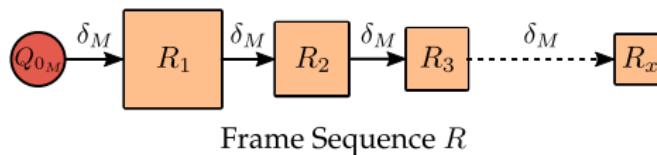
(Ben-David et al., 2015; Classen et al., 2012, 2011, 2010; Dimovski et al., 2015)

High-level View of IC3/PDR

Model $M = (\Sigma, Q_M, Q_{0_M}, \delta_M)$ and Safety property φ

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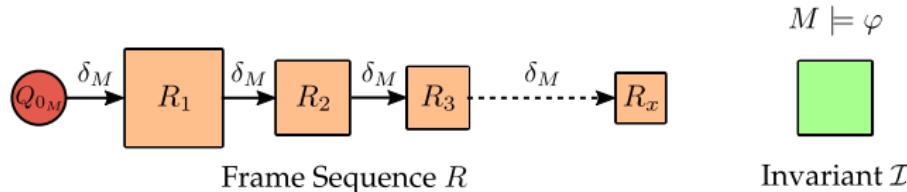


Frame Invariants

1. for $i > 0$, R_i is CNF, over-approximated states reachable in up to i steps
2. $R_{i+1} \subseteq R_i$ (monotonic)
3. $R_i \wedge \delta_M \models R'_{i+1}$
4. for $i < x$, $R_i \models \varphi$

High-level View of IC3/PDR

Model $M = (\Sigma, Q_M, Q_{0_M}, \delta_M)$ and Safety property φ

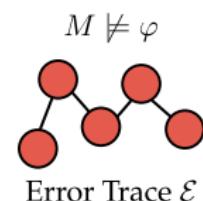
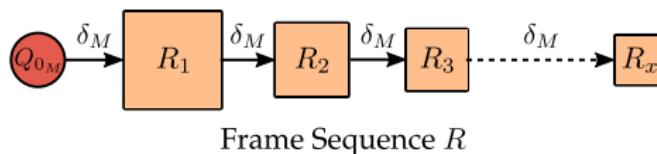


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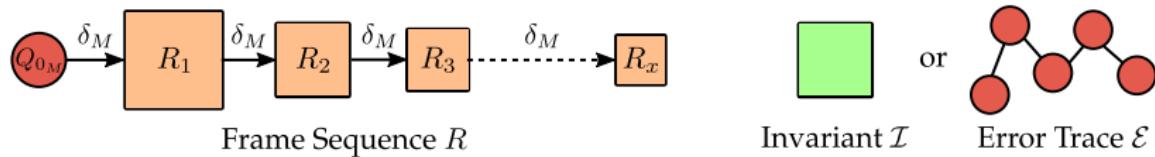


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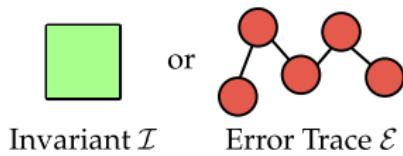
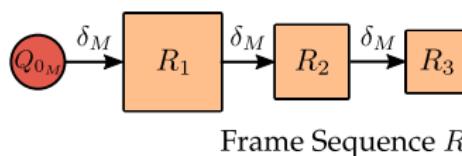


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Overview of FuseIC3

Model $M = (\Sigma, Q_M, Q_{0_M}, \delta_M)$ and Safety property φ

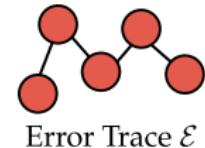
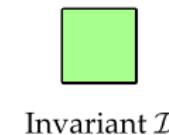
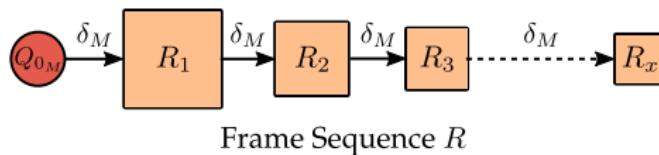


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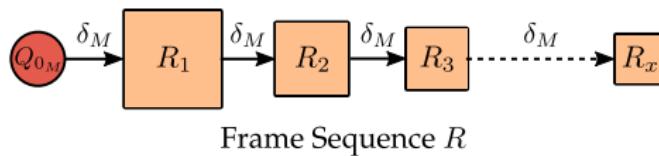
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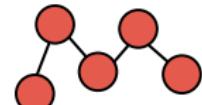
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Frame Sequence R



Invariant \mathcal{I}

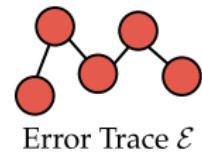
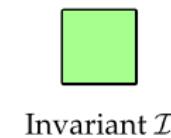
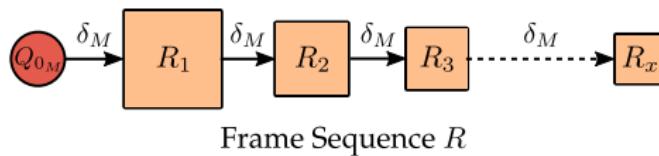


Error Trace \mathcal{E}

Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ

Overview of FuseIC3

Model $M = (\Sigma, Q_M, Q_{0_M}, \delta_M)$ and Safety property φ

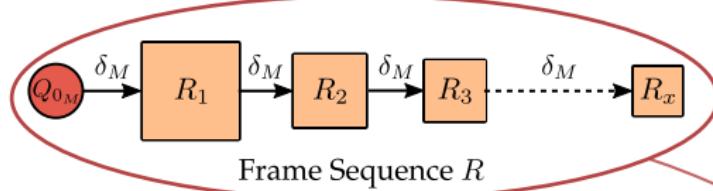


Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ

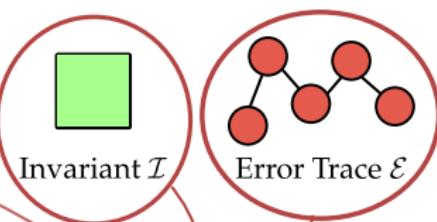
Goal: Compute frame sequence S for model N

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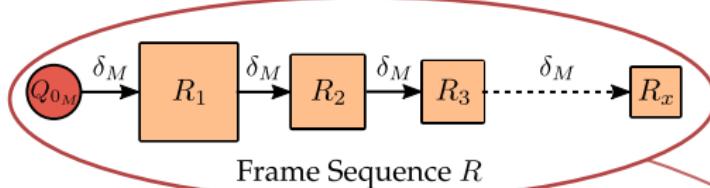


Information
Reuse

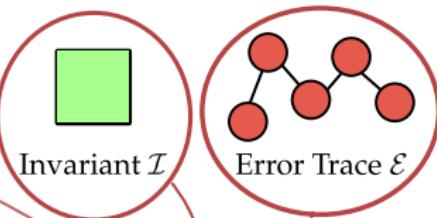
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Goal: Compute frame sequence S for model N

Information
Reuse
after
Repair

Assumptions and Intuition

Assumption 1

The different models in the design space are **related**, i.e., have overlapping reachable states.

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Assumption 2

The models in the design space are checked **sequentially**.

Assumptions and Intuition

Intuition

Set of related models $\{M_1, M_2, M_3, M_4\}$

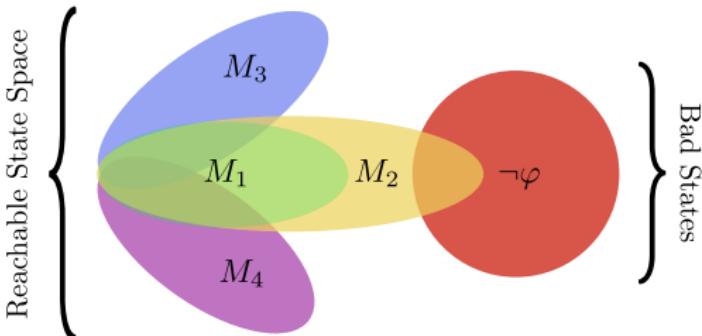
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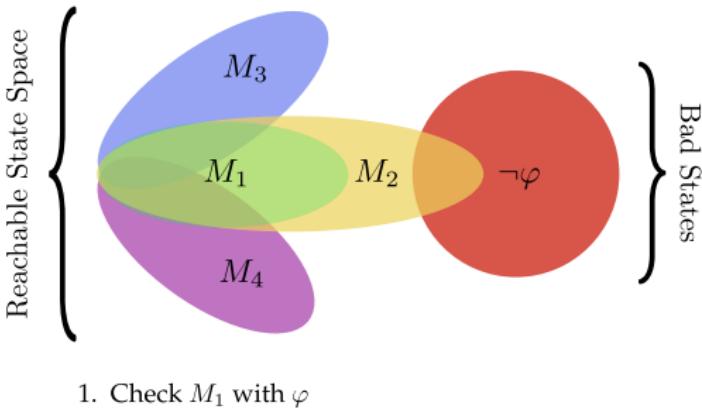
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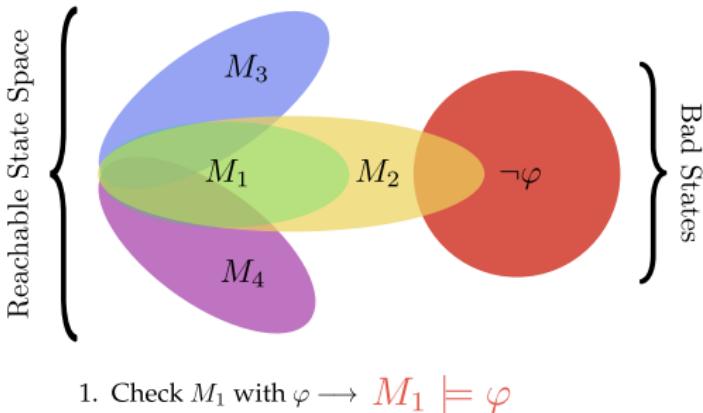


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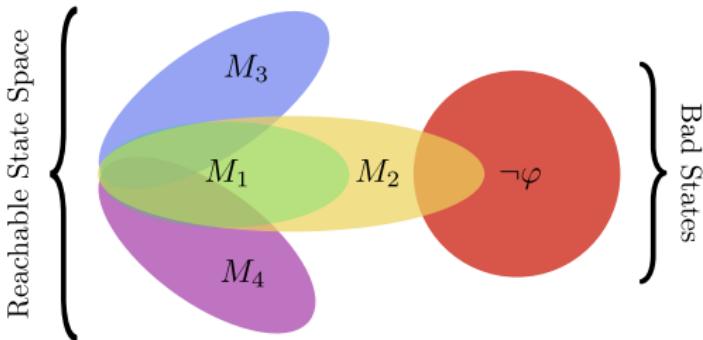
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The models in the design space are checked **sequentially**.

1. Check M_1 with $\varphi \rightarrow M_1 \models \varphi$
2. Check M_2 with $\varphi \rightarrow$

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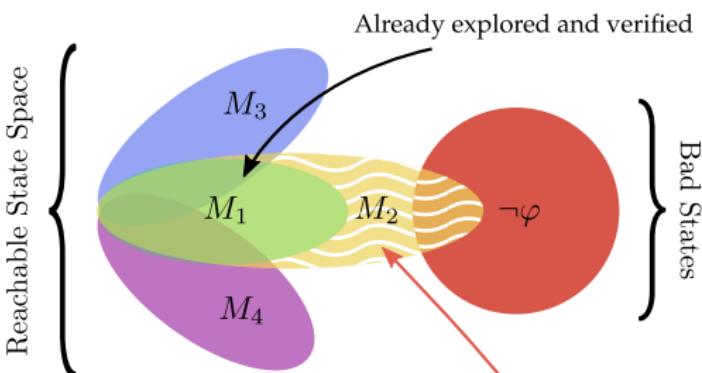
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Intuition

Set of related models $\{M_1, M_2, M_3, M_4\}$

Safety property φ



1. Check M_1 with $\varphi \rightarrow M_1 \models \varphi$
2. Check M_2 with $\varphi \rightarrow$

When checking M_2 , FuseIC3 reuses the already explored and verified state space of M_1 and only checks

Assumptions and Intuition

Intuition

Set of related models $\{M_1, M_2, M_3, M_4\}$

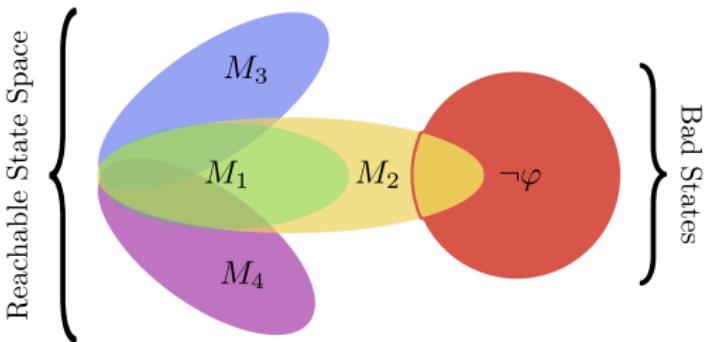
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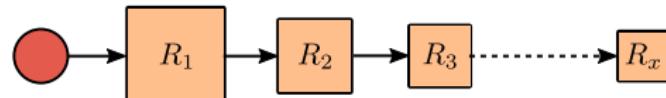


1. Check M_1 with $\varphi \rightarrow M_1 \models \varphi$
2. Check M_2 with $\varphi \rightarrow M_2 \not\models \varphi$

Internal State

Internal State

(last known)



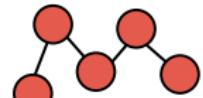
Frame Sequence R

(last known)



Invariant \mathcal{I}

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Error Trace \mathcal{E}

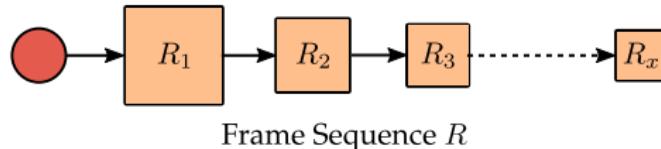
Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ

Internal state
maintained
by FuseIC3

Basic Checks

Internal State

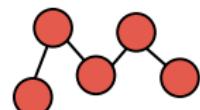
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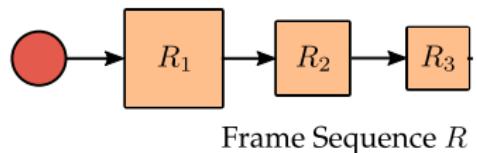
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Goal: Compute frame sequence S for mode N

Basic Checks

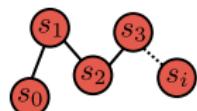
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Invariant \mathcal{I}

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Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N

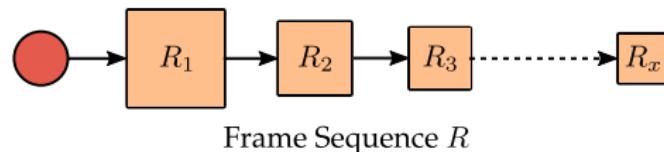
CHECKINVARIANT

\mathcal{I} is inductive invariant
w.r.t model N

Basic Checks

Internal State

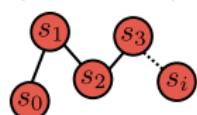
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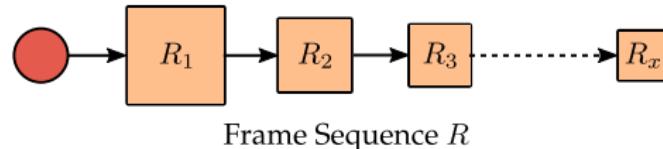


$N \models \varphi$

Basic Checks

Internal State

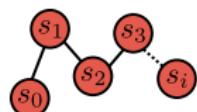
(last known)

Frame Sequence R

(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N

CHECKINVARIANT

\mathcal{I} is inductive invariant
w.r.t model N

 $N \models \varphi$

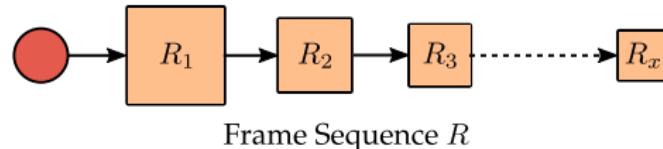
SIMULATECEX

\mathcal{E} is valid trace
w.r.t to model N

Basic Checks

Internal State

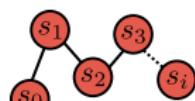
(last known)



(last known)

Invariant \mathcal{I}

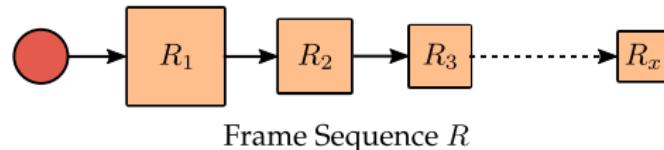
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N CHECKINVARIANT \mathcal{I} is inductive invariant
w.r.t model N  $N \models \varphi$ SIMULATECEX \mathcal{E} is valid trace
w.r.t to model N  $N \not\models \varphi$

Basic Checks

Internal State

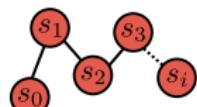
(last known)



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N

CHECKINVARIANT

\mathcal{I} is inductive invariant
w.r.t model N

 $N \models \varphi$

SIMULATECEX

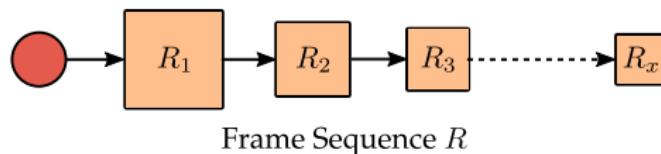
\mathcal{E} is valid trace
w.r.t to model N

 $N \not\models \varphi$

Instant Verification

Frame Reuse

Internal State



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E}

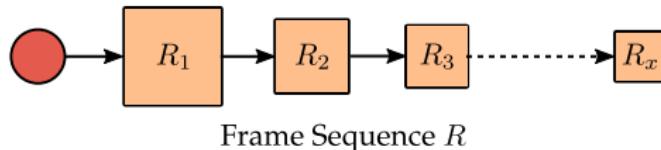
Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ

Goal: Compute frame sequence S for mode N

Frame Reuse

Internal State

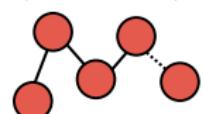
(last known)



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E}

Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ

Goal: Compute frame sequence S for mode N

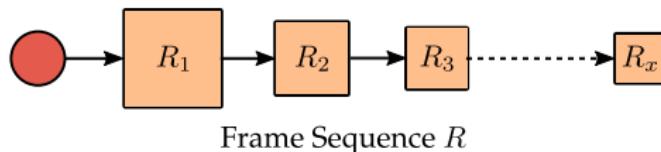


Frame Sequence S

Frame Reuse

Internal State

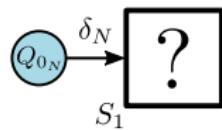
(last known)



(last known)

Invariant \mathcal{I}

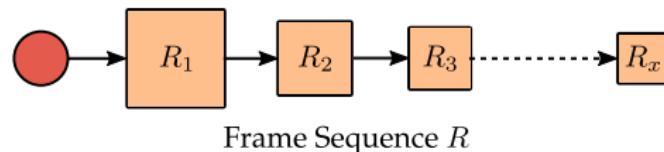
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S

Frame Reuse

Internal State

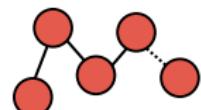
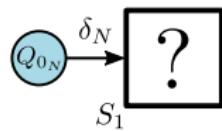
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(last known)

Invariant \mathcal{I}

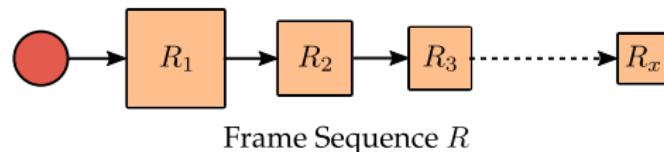
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N We want to compute S_1 using known information

Frame Reuse

Internal State

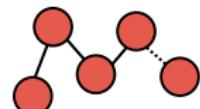
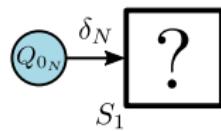
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(last known)

Invariant \mathcal{I}

(last known)

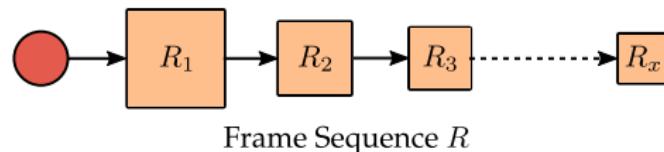
Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S We want to compute S_1 using known information

$$S_0 \wedge \delta_N \rightarrow R'_1 ?$$

Frame Reuse

Internal State

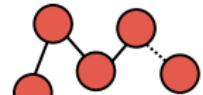
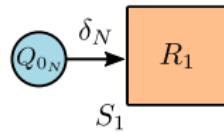
(last known)



(last known)

Invariant \mathcal{I}

(last known)

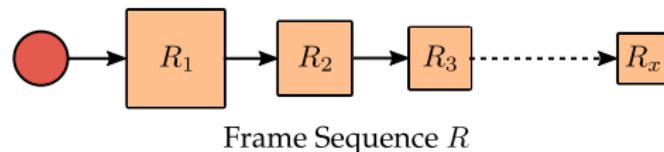
Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S We want to compute S_1 using known information

$$S_0 \wedge \delta_N \rightarrow R'_1? \quad \checkmark$$

Frame Reuse

Internal State

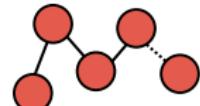
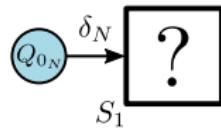
(last known)

Frame Sequence R

(last known)

Invariant \mathcal{I}

(last known)

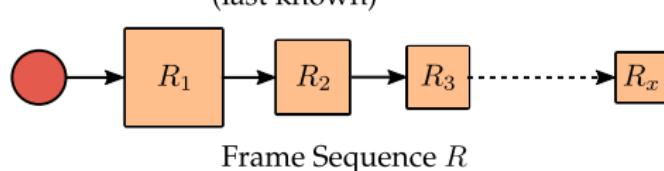
Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S We want to compute S_1 using known information

$$S_0 \wedge \delta_N \rightarrow R'_1?$$



Frame Reuse

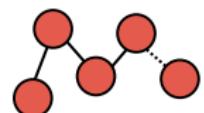
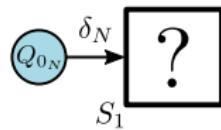
Internal State

Frame Sequence R

(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S We want to compute S_1 using known information

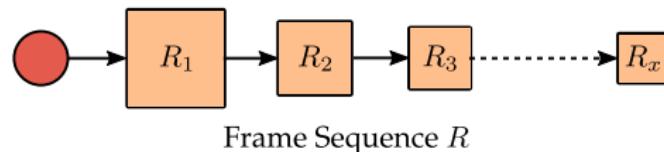
$$S_0 \wedge \delta_N \rightarrow R'_1? \quad \text{X}$$

Repair R_1

Frame Repair

Internal State

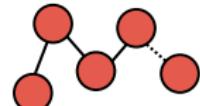
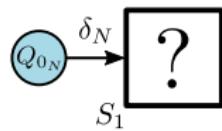
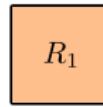
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Frame Sequence R

(last known)

Invariant \mathcal{I}

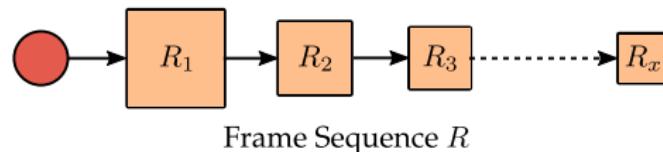
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

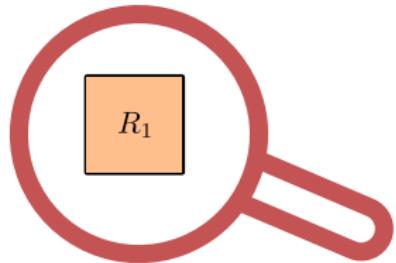
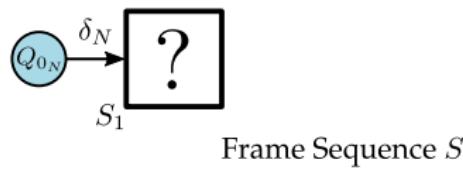
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(last known)

Invariant \mathcal{I}

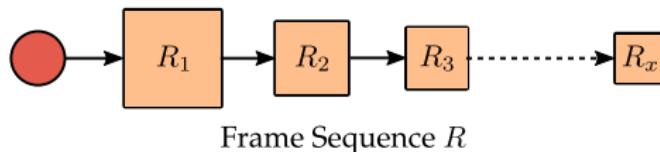
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

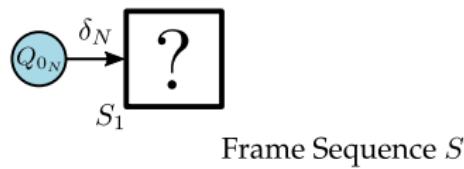
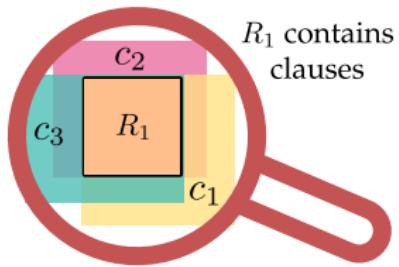
(last known)

Frame Sequence R

(last known)

Invariant \mathcal{I}

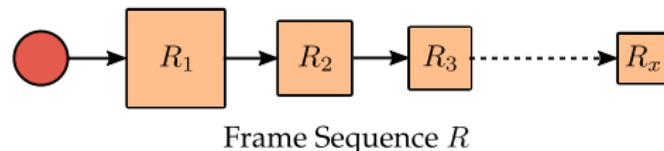
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

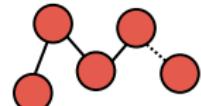
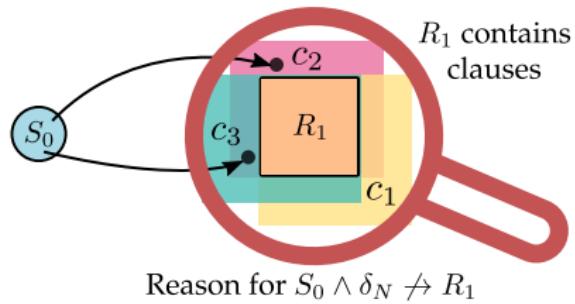
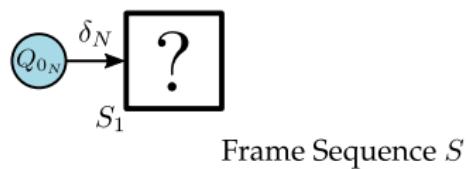
(last known)

Frame Sequence R

(last known)

Invariant \mathcal{I}

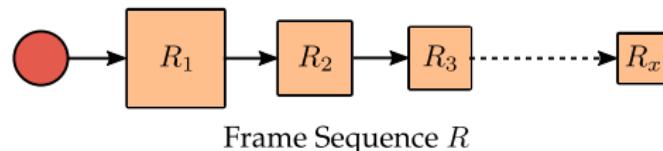
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Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

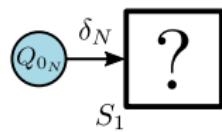
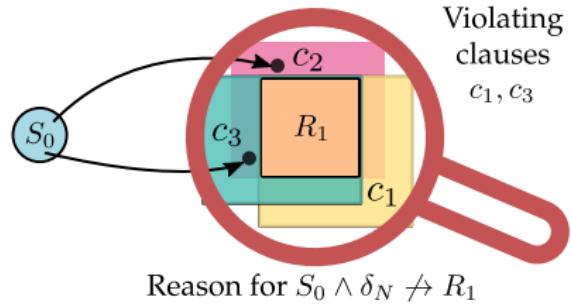
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Frame Sequence R

(last known)

Invariant \mathcal{I}

(last known)

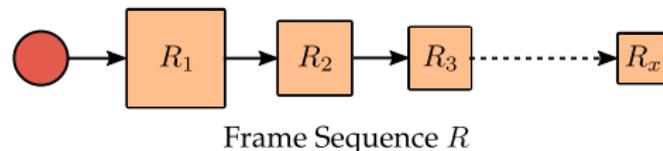
Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

FINDCLAUSES

Frame Repair

Internal State

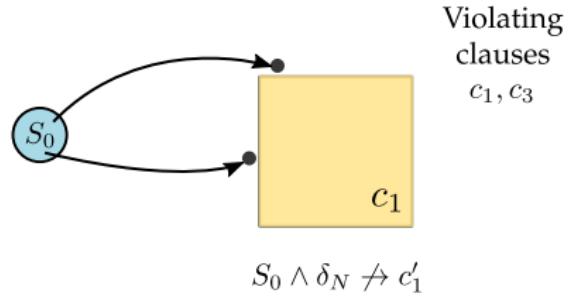
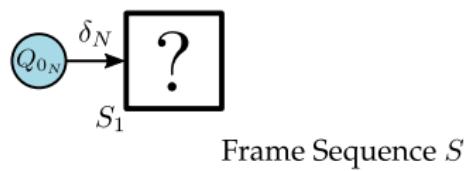
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(last known)

Invariant \mathcal{I}

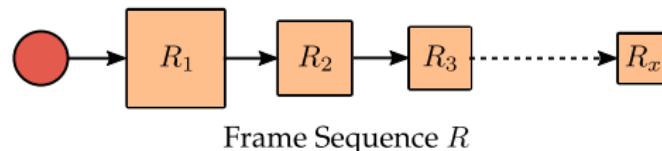
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

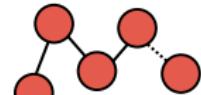
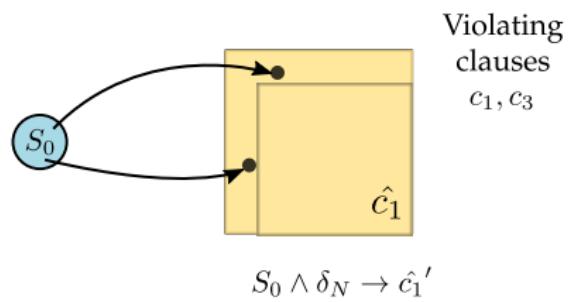
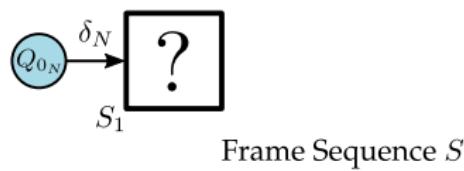
(last known)



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N 

$$S_0 \wedge \delta_N \rightarrow \hat{c}_1'$$

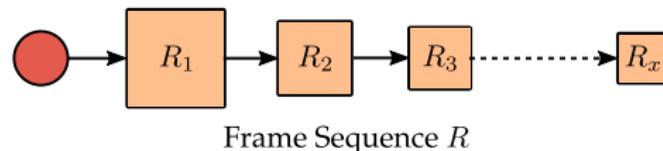
Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

EXPANDCLAUSE

Frame Repair

Internal State

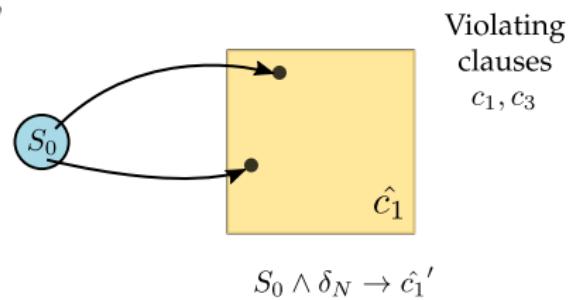
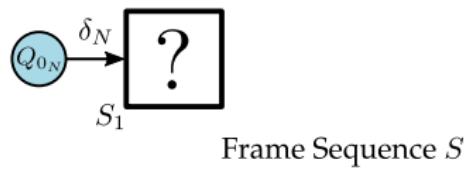
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(last known)

Invariant \mathcal{I}

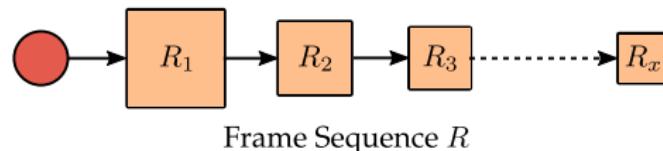
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

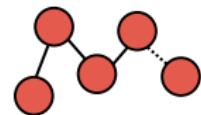
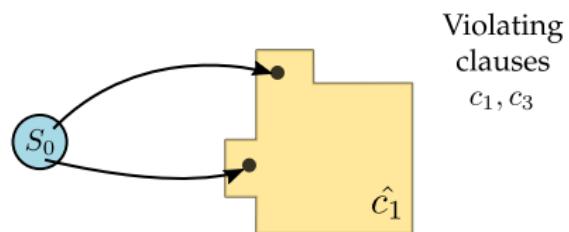
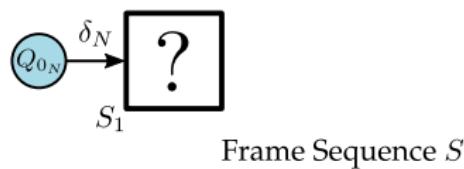
(last known)



(last known)

Invariant I

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N 

$$S_0 \wedge \delta_N \rightarrow \hat{c}_1'$$

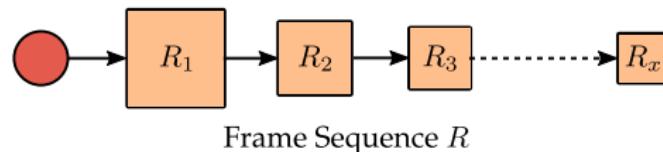
Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

SHRINKCLAUSE

Frame Repair

Internal State

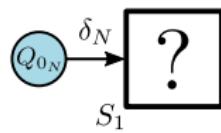
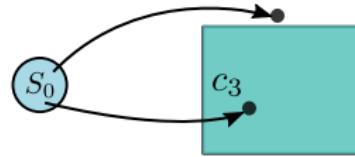
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Frame Sequence R

(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S 

Violating clauses
 c_1, c_3

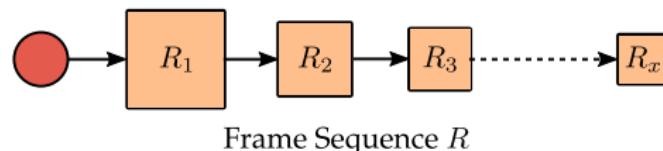
$$S_0 \wedge \delta_N \not\rightarrow c'_3$$

Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

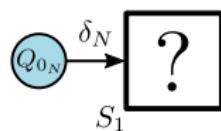
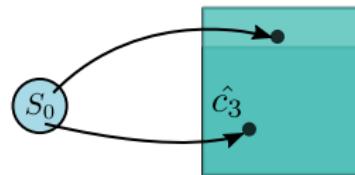
(last known)



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S 

$$S_0 \wedge \delta_N \rightarrow \hat{c}_3'$$

Violating clauses
 c_1, c_3

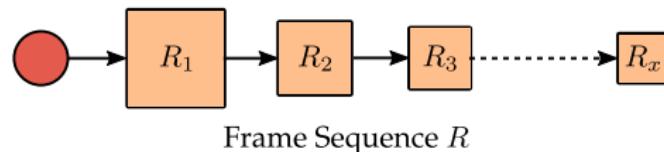
Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

EXPANDCLAUSE

Frame Repair

Internal State

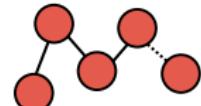
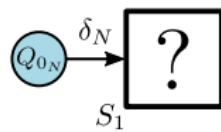
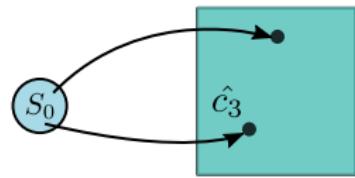
(last known)



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0_N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N Frame Sequence S 

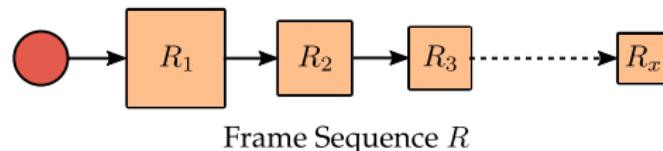
$$S_0 \wedge \delta_N \rightarrow \hat{c}_3'$$

Repair R_1 to \hat{R}_1 s.t. $S_0 \wedge \delta_N \rightarrow \hat{R}_1'$ is valid

Frame Repair

Internal State

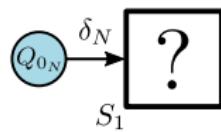
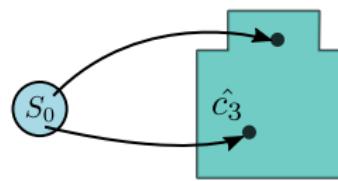
(last known)



(last known)

Invariant I

(last known)

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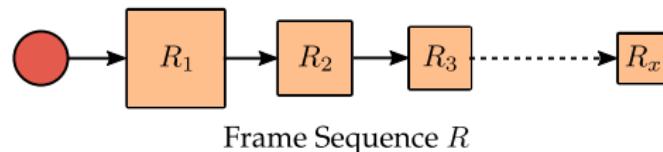
Violating clauses
 c_1, c_3

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Frame Repair

Internal State

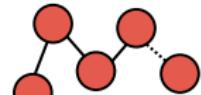
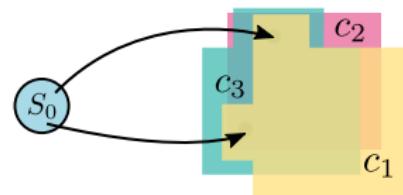
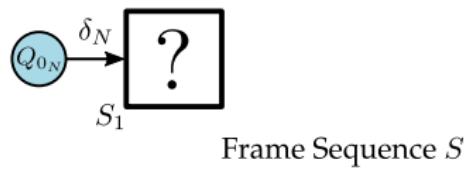
(last known)



(last known)

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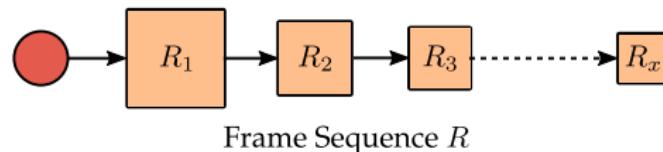
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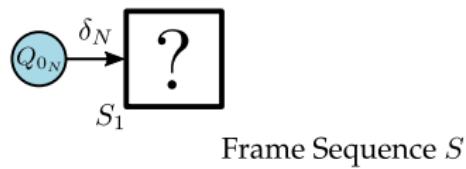
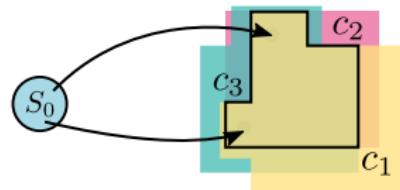
(last known)

Frame Sequence R

(last known)

Invariant \mathcal{I}

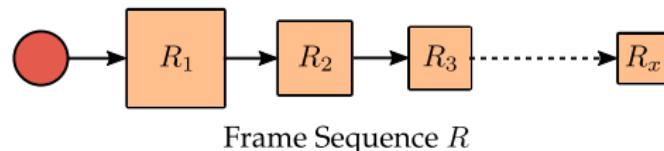
(last known)

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Frame Repair

Internal State

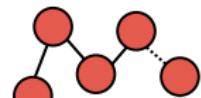
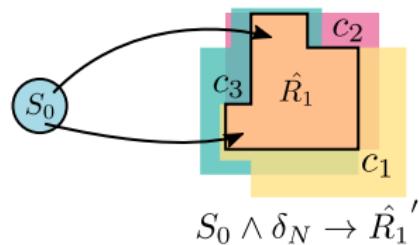
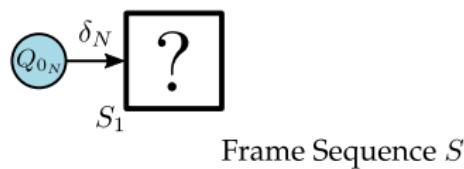
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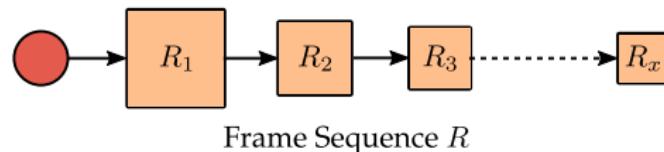
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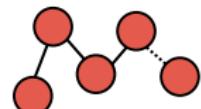
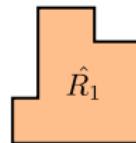
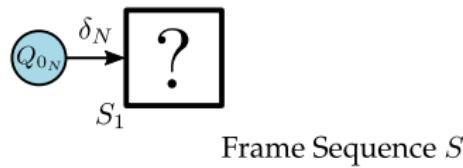
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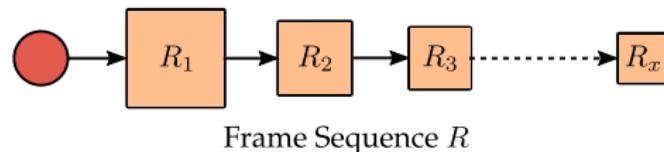
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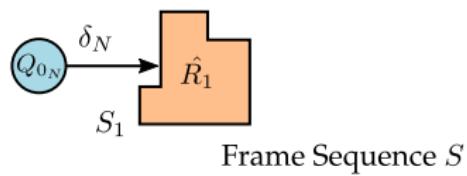
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(last known)

Invariant \mathcal{I}

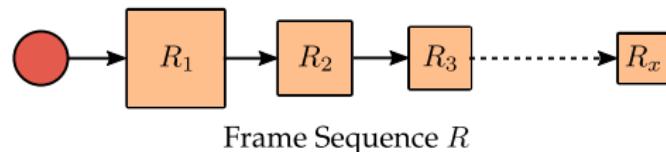
(last known)

Error Trace \mathcal{E} Model $N = (\Sigma, Q_N, Q_{0N}, \delta_N)$ and Safety property φ **Goal:** Compute frame sequence S for mode N 

Strengthen Frames

Internal State

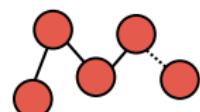
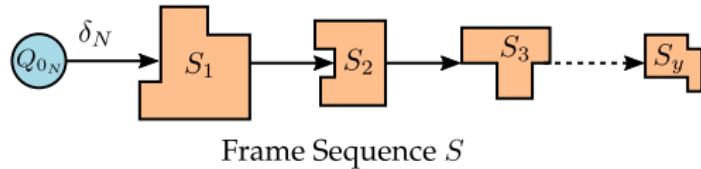
(last known)

Frame Sequence R

(last known)

Invariant \mathcal{I}

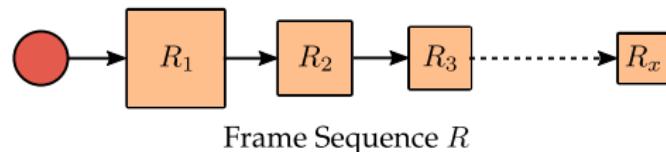
(last known)

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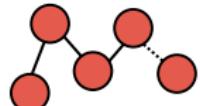
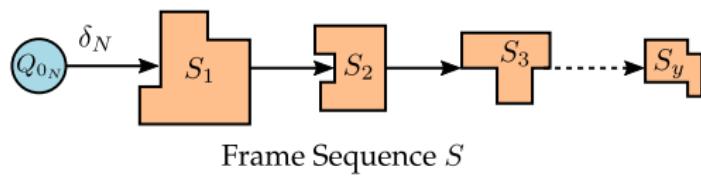
(last known)

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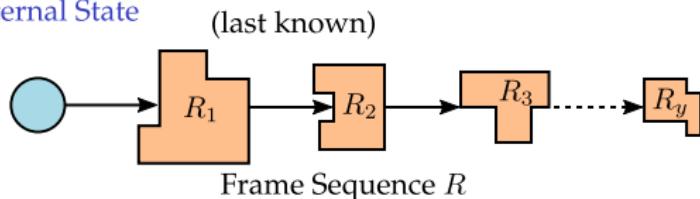
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$$N \models \varphi$$

Invariant: $S_{i+1} \equiv S_i$

Strengthen Frames

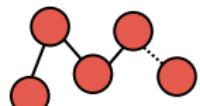
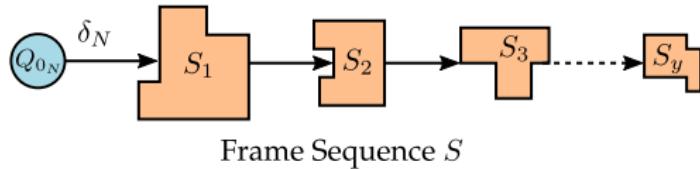
Internal State



(last known)

Invariant \mathcal{I}

(last known)

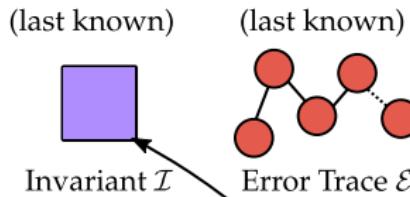
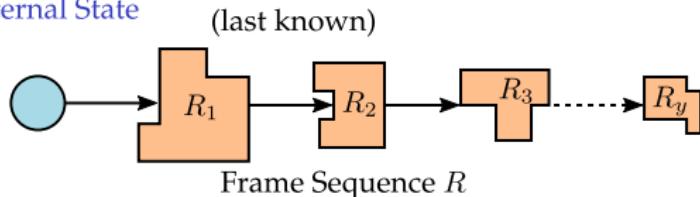
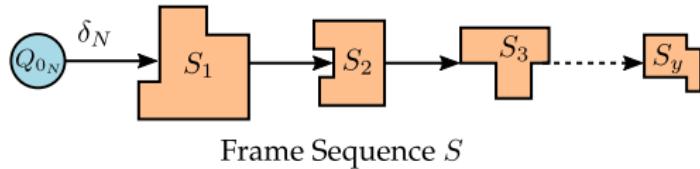
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Update last known

1. Frame Sequence

Strengthen Frames

Internal State

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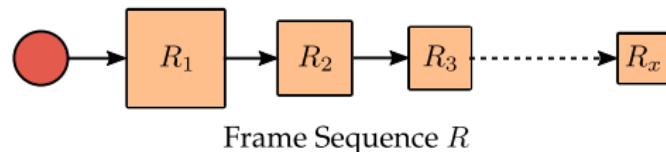
Update last known

1. Frame Sequence
2. Invariant

Strengthen Frames

Internal State

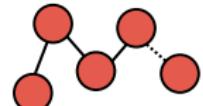
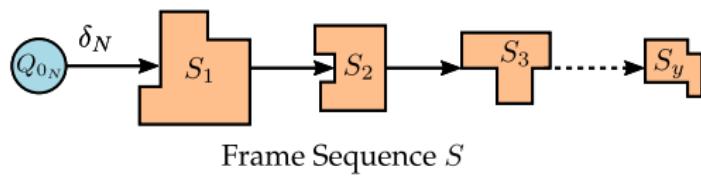
(last known)

Frame Sequence R

(last known)

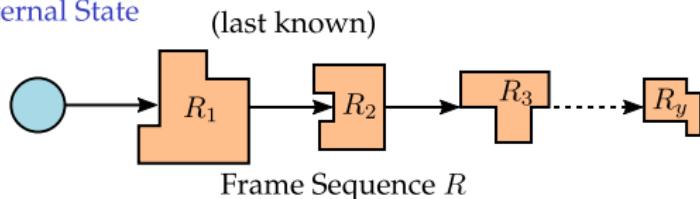
Invariant \mathcal{I}

(last known)

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Strengthen Frames

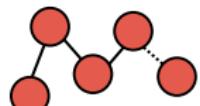
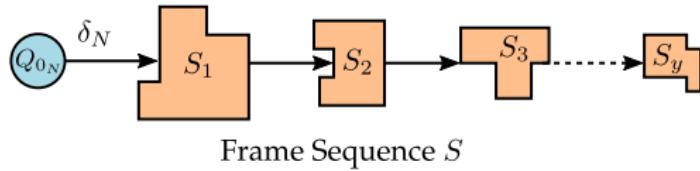
Internal State

Frame Sequence R

(last known)

Invariant \mathcal{I}

(last known)

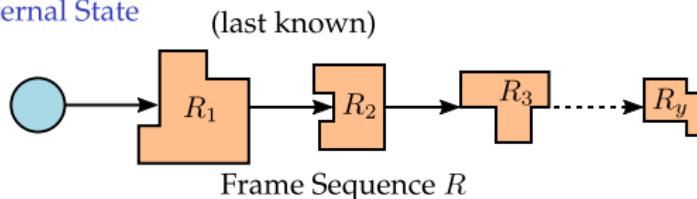
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Update last known

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Strengthen Frames

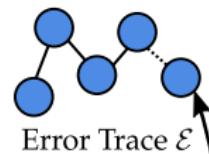
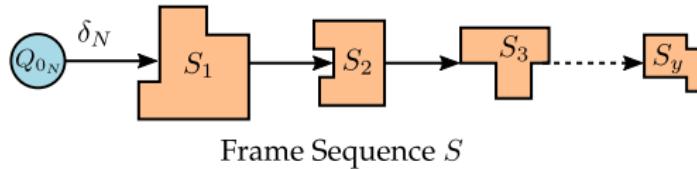
Internal State

Frame Sequence R

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Invariant \mathcal{I}

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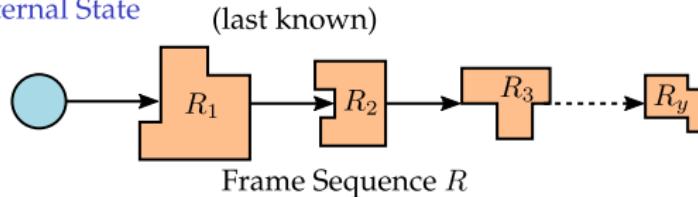
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Strengthen Frames

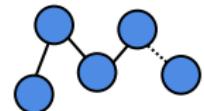
Internal State



(last known)

Invariant \mathcal{I}

(last known)

Error Trace \mathcal{E}

Ready for next model

Experiment Setup

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 - ③ Boeing AIR 6110 Wheel Braking System (WBS) (Bozzano et al., 2015)

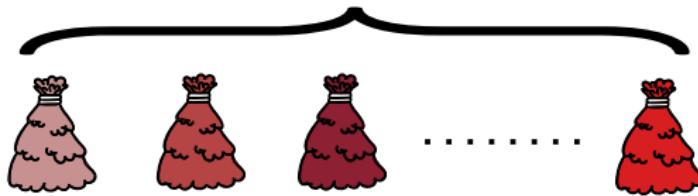
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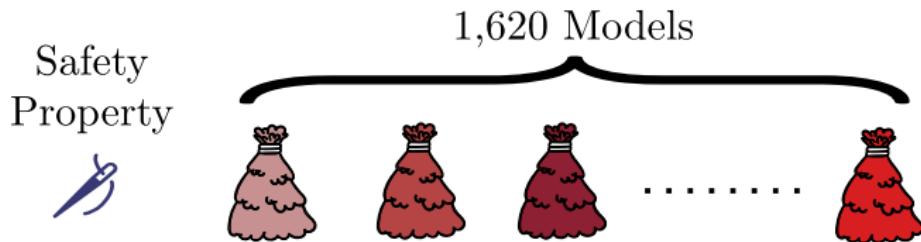
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NASA ATC Benchmark

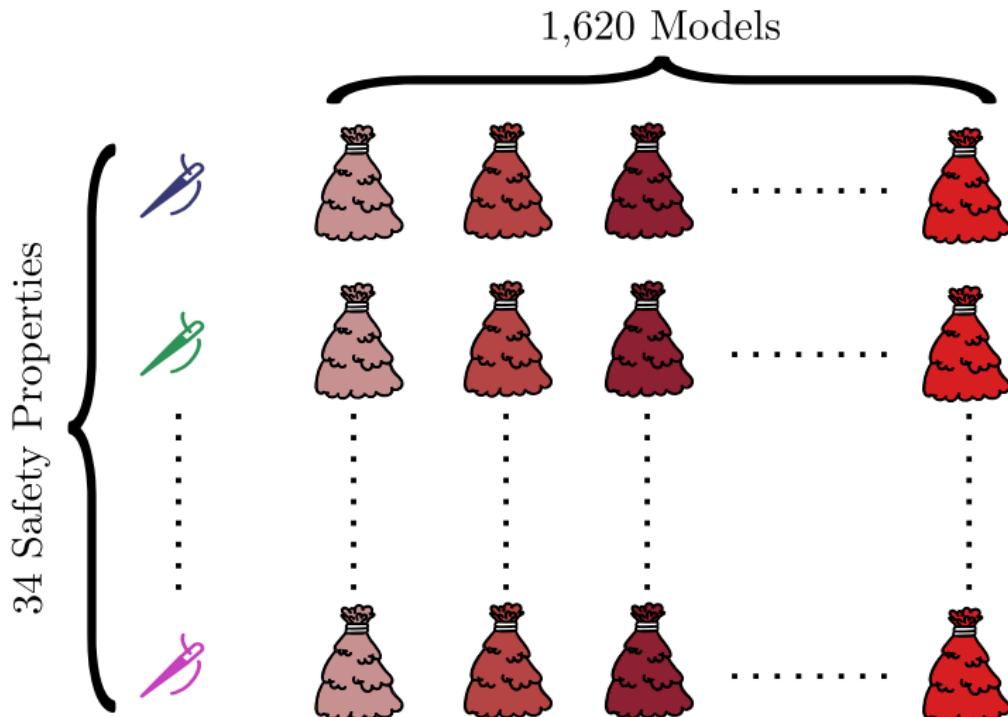
1,620 Models



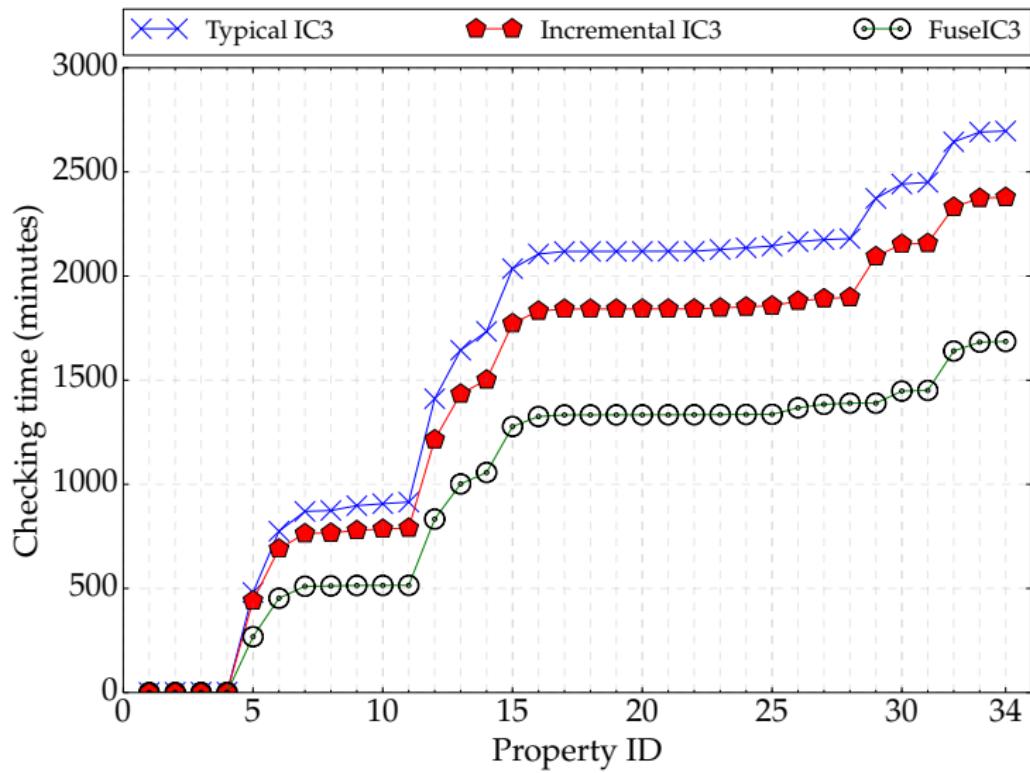
NASA ATC Benchmark



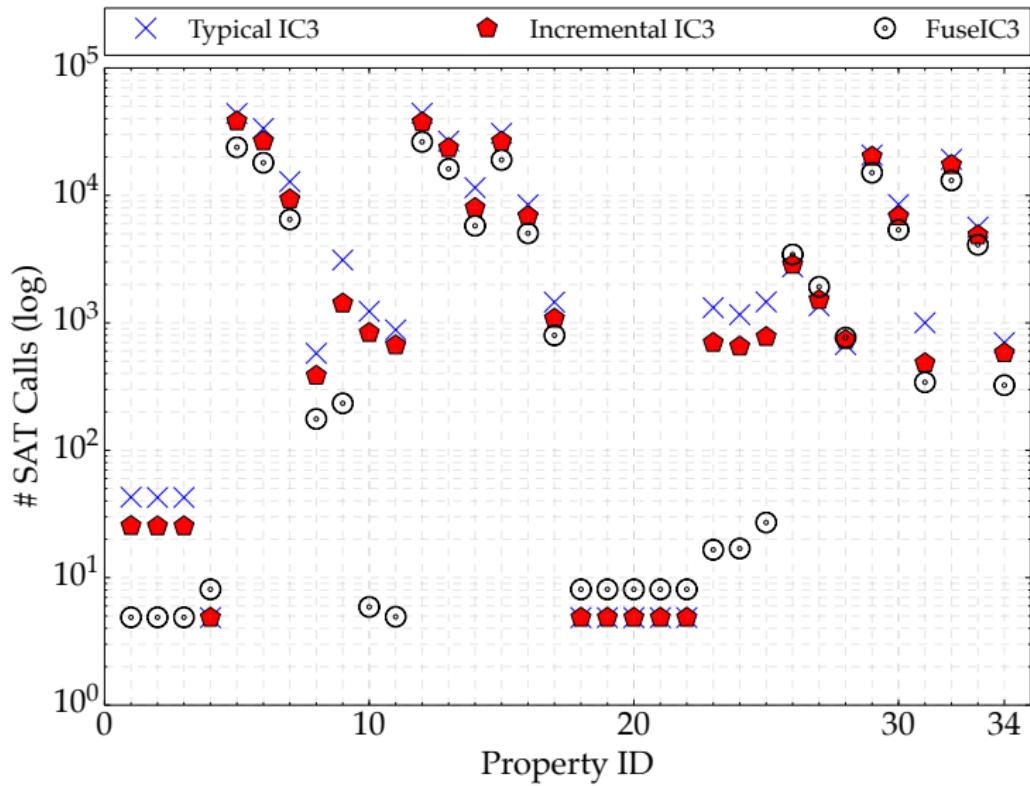
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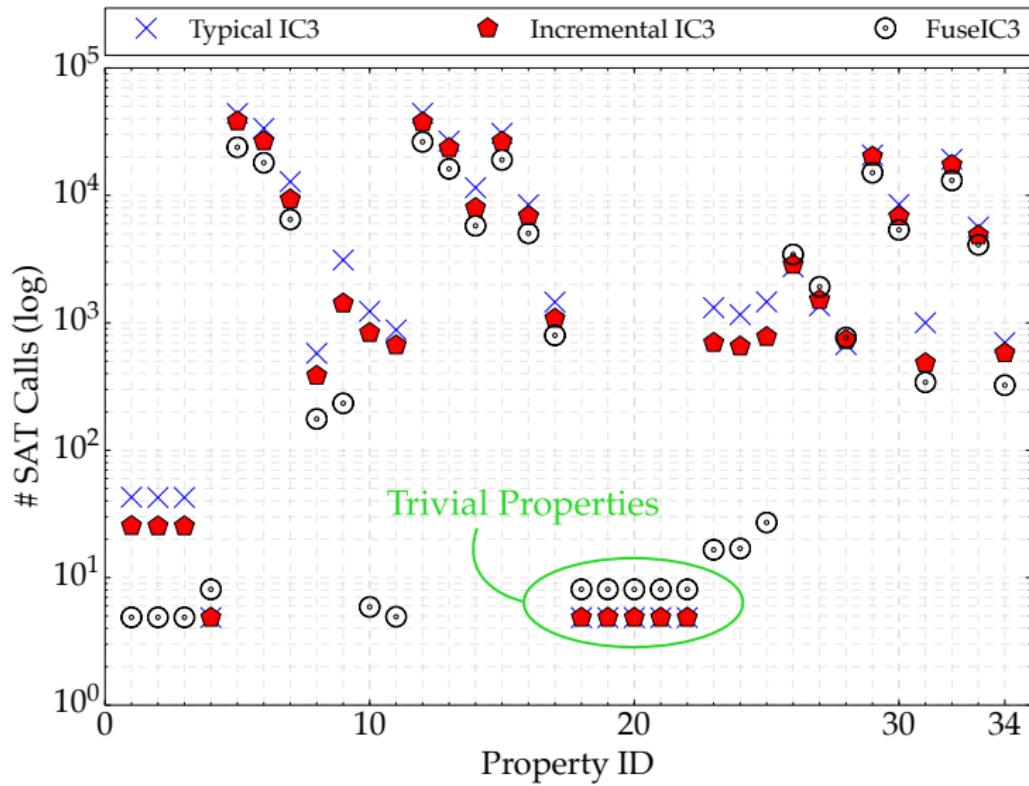
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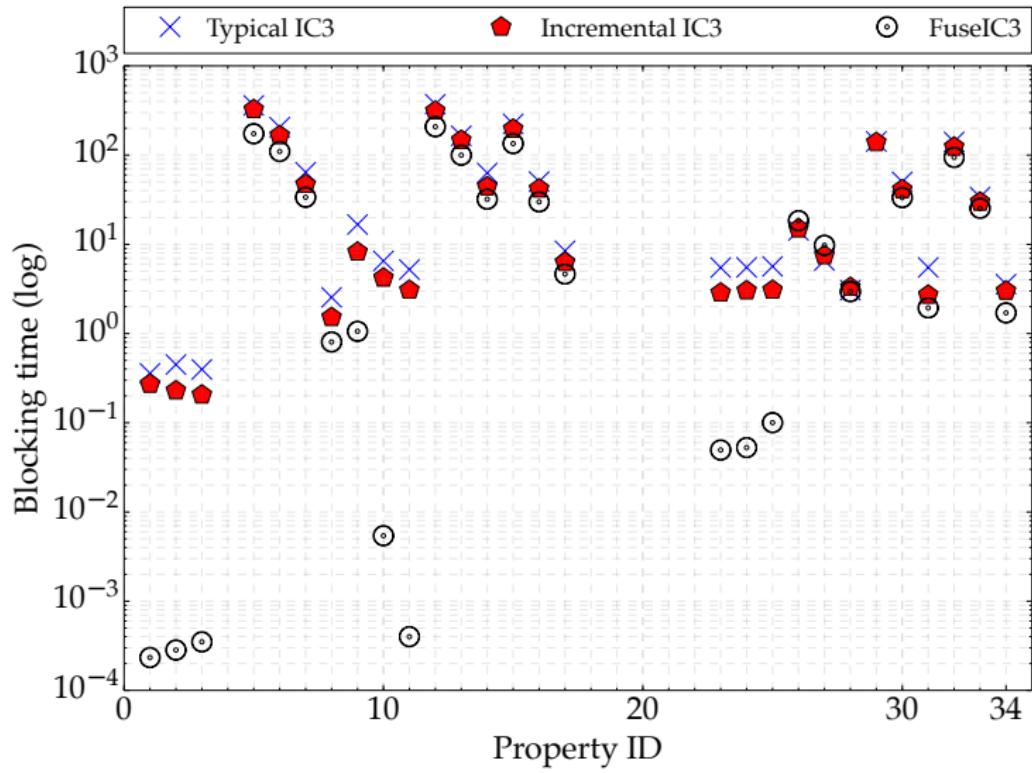
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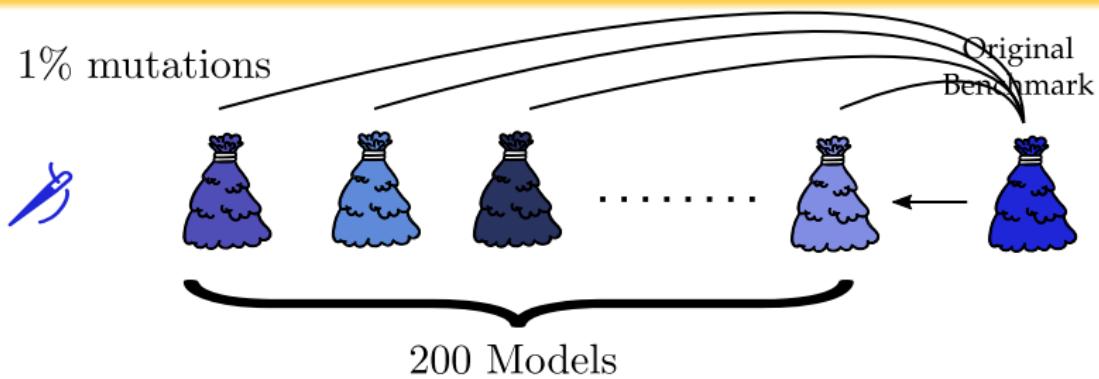


Selected HWMCC Benchmarks

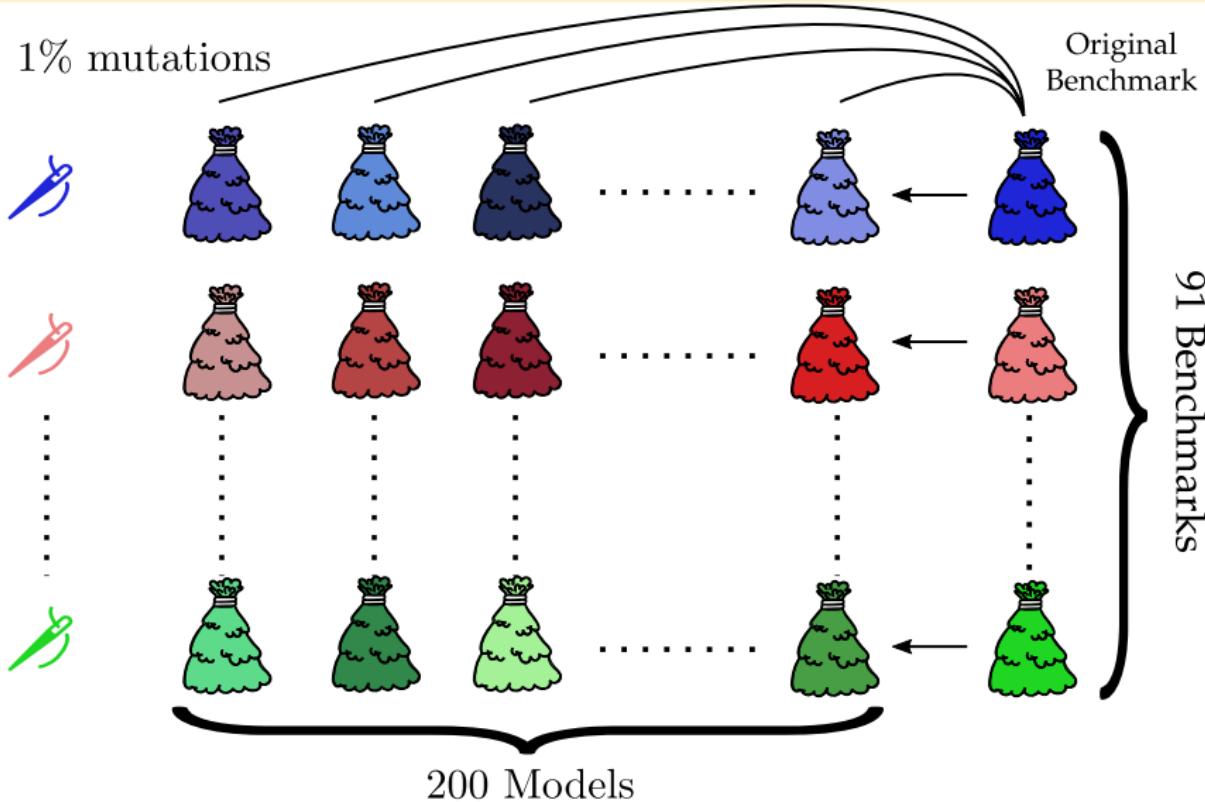
Original
Benchmark



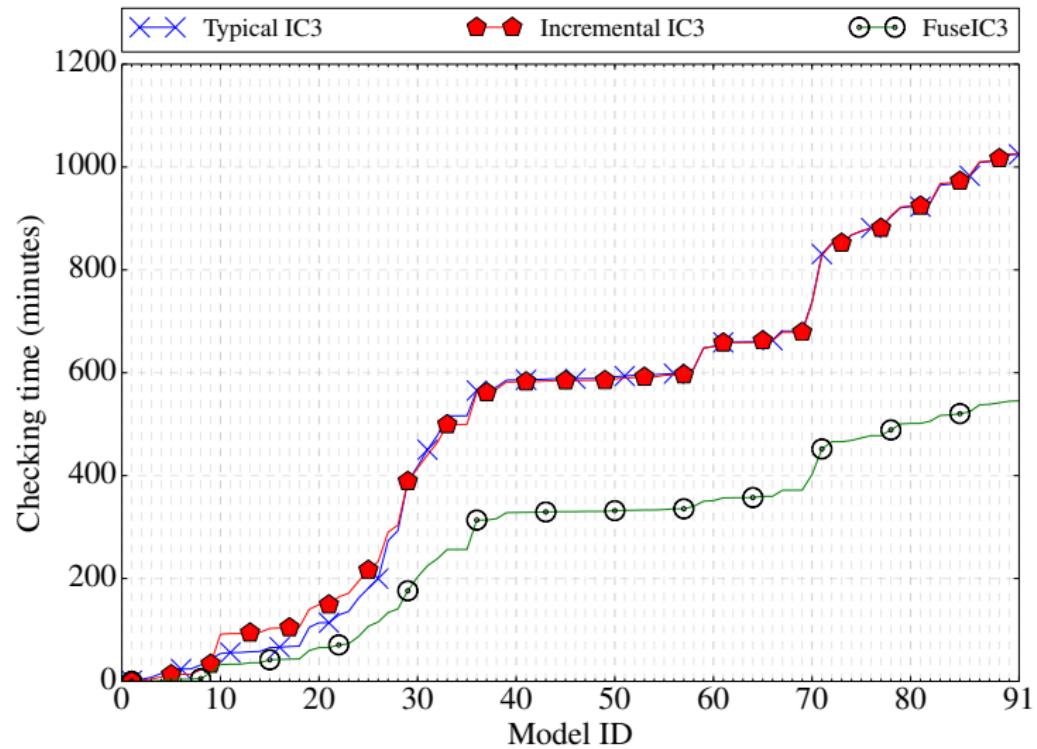
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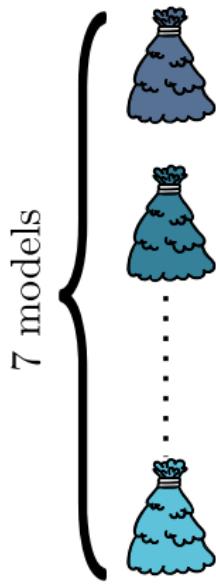
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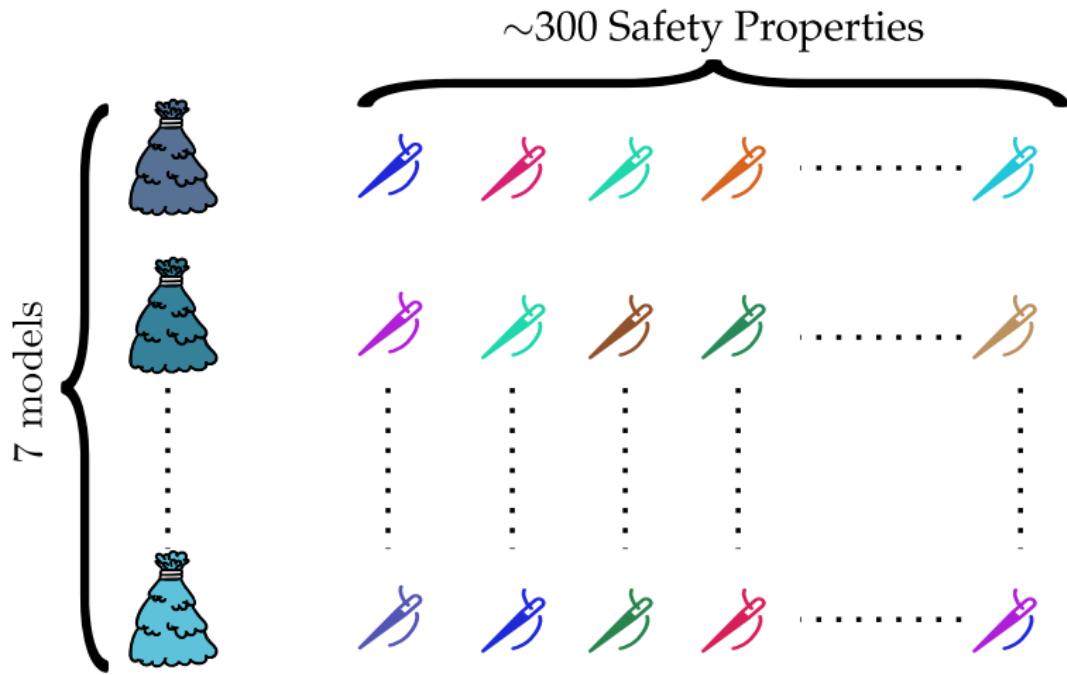
Boeing WBS Benchmark



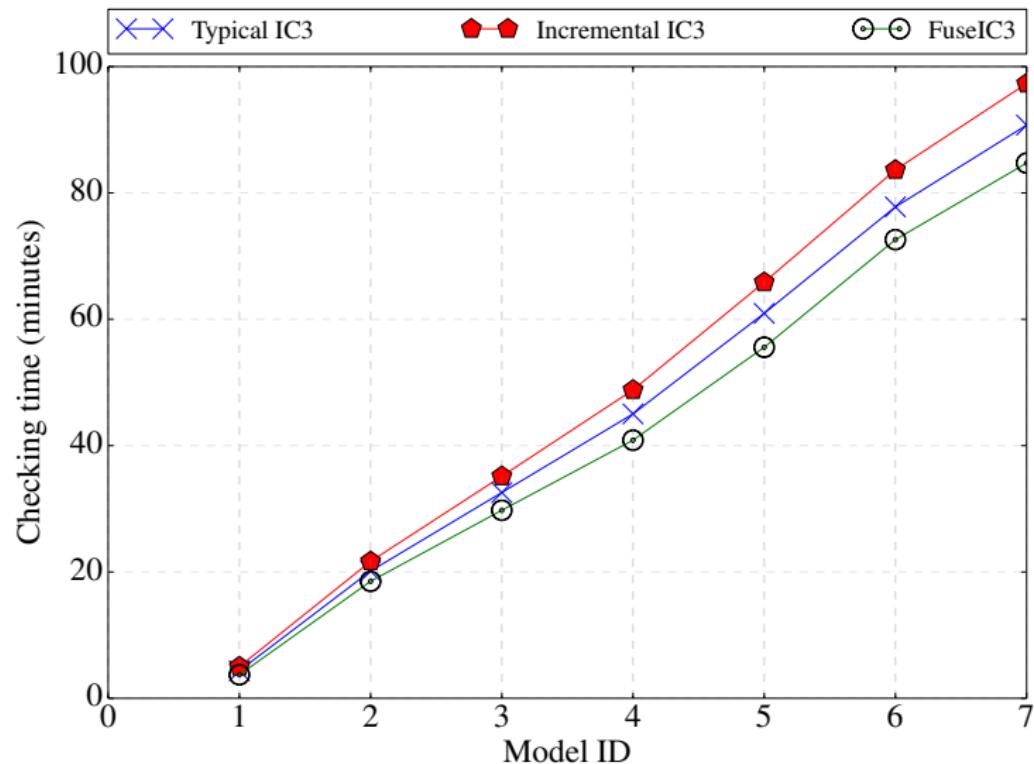
Boeing WBS Benchmark



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Thank You!

<http://temporallogic.org/research/FMCAD17>

- Beer, I., Ben-David, S., Eisner, C., & Landver, A. (1996). RuleBase: An industry-oriented formal verification tool. In *Dac*.
- Ben-David, S., Sterin, B., Atlee, J. M., & Beidu, S. (2015). Symbolic model checking of product-line requirements using SAT-based methods. In *Icse* (Vol. 1, pp. 189–199).
- Bozzano, M., Cimatti, A., Fernandes Pires, A., Jones, D., Kimberly, G., Petri, T., ... Tonetta, S. (2015). Formal design and safety analysis of AIR6110 wheel brake system. In *CAV*.
- Chockler, H., Ivrii, A., Matsliah, A., Moran, S., & Nevo, Z. (2011). Incremental Formal Verification of Hardware. In *Fmcad* (pp. 135–143).
- Classen, A., Cordy, M., Heymans, P., Legay, A., & Schobbens, P.-Y. (2012). Model checking software product lines with snip. (*STTT*), 1–24.
- Classen, A., Heymans, P., Schobbens, P.-Y., & Legay, A. (2011). Symbolic model checking of software product lines. In *Icse* (pp. 321–330).
- Classen, A., Heymans, P., Schobbens, P.-Y., Legay, A., & Raskin, J.-F. (2010). Model checking lots of systems: efficient verification of temporal properties in software product lines. In *Icse* (pp. 325–334).