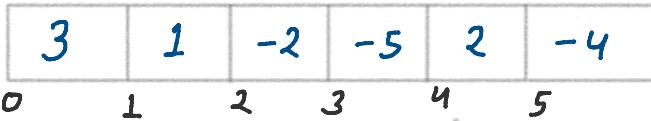
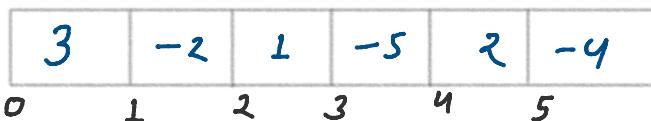


HW CLASS: 10 14/9/2023

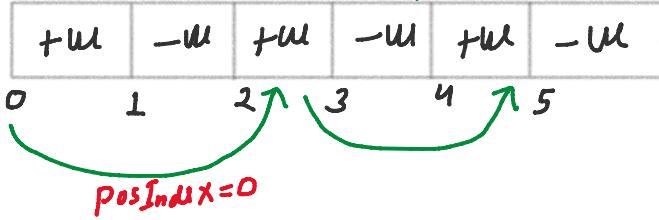
<https://www.linkedin.com/in/manojofficialmj/>

1. Re-arrange array elements (Leetcode-2149)

<i>Input</i>	<i>nums</i>		<i>size = 6</i>
--------------	-------------	--	-----------------

<i>Output</i>	
---------------	--

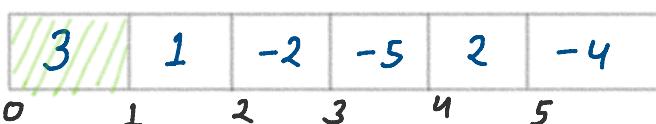
Observation

<i>ANS</i>	
------------	---

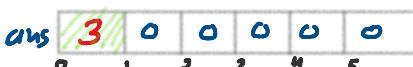
Note

- ① Array's size always even
- ② Negative no's == positive nos
- ③ pairs of numbers always start from positive no.

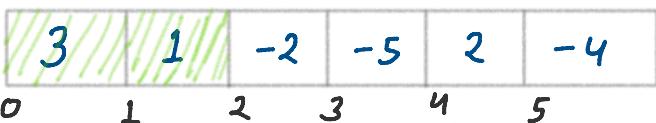
*DryRun*iteration: 0

<i>nums</i>	
-------------	--

 i^{th} index = 0 $posIndex = 0$ $negIndex = 1$ ① $nums[i^{th}] > 0$ $3 > 0$
 $ans[posIndex] = nums[i^{th}]$ $ans[0] = 3$ $posIndex = posIndex + 2$ $= 0 + 2$ $= 2$ \curvearrowright

<i>ans</i>	
------------	---

iteration: 1

<i>nums</i>	
-------------	--

$\text{index} = 1$
 $\text{posIndex} = 2$
 $\text{negIndex} = 1$

① $\text{nums}[\text{index}] > 0$
 $1 > 0$
 $\text{ans}[\text{posIndex}] = \text{nums}[\text{index}];$
 $\text{ans}[2] = 1$
 $\text{posIndex} = \text{posIndex} + 2;$
 $= 2 + 2$
 $= 4$

ans	3	0	1	0	0	0
0	1	2	3	4	5	

Iteration: 2

nums	3	1	-2	-5	2	-4
0	1	2	3	4	5	

$\text{index} = 2$
 $\text{posIndex} = 4$
 $\text{negIndex} = 1$

① $\text{nums}[\text{index}] < 0$
 $-2 < 0$
 $\text{ans}[\text{negIndex}] = \text{nums}[\text{index}];$
 $\text{ans}[1] = -2$
 $\text{negIndex} = \text{negIndex} + 2;$
 $= 1 + 2$
 $= 3$

ans	3	-2	1	0	0	0
0	1	2	3	4	5	

Iteration: 3

nums	3	1	-2	-5	2	-4
0	1	2	3	4	5	

$\text{index} = 3$
 $\text{posIndex} = 4$
 $\text{negIndex} = 3$

① $\text{nums}[\text{index}] < 0$
 $-5 < 0$
 $\text{ans}[\text{negIndex}] = \text{nums}[\text{index}];$
 $\text{ans}[3] = -5$
 $\text{negIndex} = \text{negIndex} + 2;$
 $= 3 + 2$
 $= 5$

ans	3	-2	1	-5	0	0
0	1	2	3	4	5	

Iteration: 4

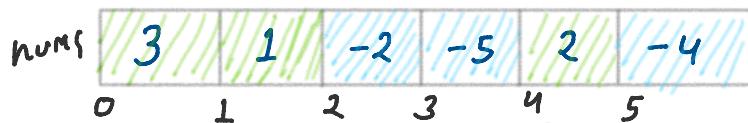
nums	3	1	-2	-5	2	-4
0	1	2	3	4	5	

$\text{index} = 4$
 $\text{posIndex} = 4$
 $\text{negIndex} = 5$

① $\text{nums}[\text{index}] > 0$
 $2 > 0$
 $\text{ans}[\text{posIndex}] = \text{nums}[\text{index}];$
 $\text{ans}[4] = 2$
 $\text{posIndex} = \text{posIndex} + 2;$
 $= 4 + 2$
 $= 6$

ans	3	-2	1	-5	2	0
0	1	2	3	4	5	

Iteration: 5



index = 5

posIndex = 6

negIndex = 5

① $\text{nums}[\text{index}] < 0$

$$-4 < 0$$

$\text{ans}[\text{negIndex}] = \text{nums}[\text{index}]$;

$$\text{ans}[5] = -4$$

$\text{negIndex} = \text{negIndex} + 2$;

$$= 5 + 2$$

$$= 7$$



Iteration: 6

$(\text{index} < \text{size})$
→ **6 < 6** X END

Final Output

```

● ● ●
// HW 00: Re-arrange array elements (Leetcode-2149)

class Solution {
public:
    vector<int> rearrangeArray(vector<int>& nums) {
        // Size of nums
        int size=nums.size();

        // Create new vector array
        vector<int> ans(size,0);

        // Create positive index and negative index
        int posIndex=0;
        int negIndex=1;

        // Iterate the entire array
        for(int index=0;index<size;index++){
            // When element is positive then use even index in ans
            if(nums[index]>0){
                ans[posIndex]=nums[index];
                posIndex+=2;
            }
            // When element is negative then use odd index in ans
            else{
                ans[negIndex]=nums[index];
                negIndex+=2;
            }
        }

        // Return new array
        return ans;
    }
};

```

$T.C. \Rightarrow O(N)$

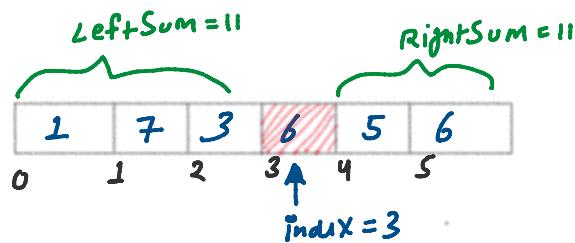
2. Find pivot element (Leetcode-724)

Example 1:
 Input: $\text{nums} = [1, 7, 3, 6, 5, 6]$
 Output: 3
 Explanation:
 The pivot index is 3.
 $\text{Left sum} = \text{nums}[0] + \text{nums}[1] + \text{nums}[2] = 1 + 7 + 3 = 11$
 $\text{Right sum} = \text{nums}[4] + \text{nums}[5] = 5 + 6 = 11$

Example 2:
 Input: $\text{nums} = [1, 2, 3]$
 Output: -1
 Explanation:
 There is no index that satisfies the conditions in the problem statement.

DRY RUN

Example 1:



APPROACH PSEUDO CODE:

- Step 01: find total sum of array as right sum
- Step 02: subtract element one by one from right sum until left sum is equal to right sum
- Step 03: return the index which terminate the loop

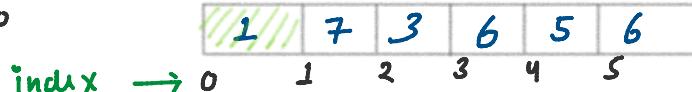
①

$$\text{TotalSum} = 1 + 7 + 3 + 6 + 5 + 6$$

$$\text{RightSum} = 28$$

②

iteration: 0



$$\text{RightSum} = 28$$

$$\text{LeftSum} = 0$$

$$\text{index} = 0$$

$$\hookrightarrow \text{RightSum} = \text{RightSum} - \text{nums}[\text{index}]$$

$$= 28 - 1$$

$$= 27$$

$$\hookrightarrow (\text{RightSum} == \text{LeftSum})$$

$$27 == 0 \quad \text{X fail}$$

$$\hookrightarrow \text{LeftSum} = \text{LeftSum} + \text{nums}[\text{index}]$$

$$= 0 + 1$$

= 1

Iteration: 1

index → 0	1	7	3	6	5	6
	1	2	3	4	5	6

$$\text{RightSum} = 27$$

$$\text{LeftSum} = 1$$

$$\text{Index} = 1$$

$$\begin{aligned}
 \hookrightarrow \text{RightSum} &= \text{RightSum} - \text{nums}[index] \\
 &= 27 - 7 \\
 &= 20 \\
 \hookrightarrow (\text{RightSum} &== \text{LeftSum}) \\
 20 &== 1 \quad \times \text{FAIL}
 \end{aligned}$$

$$\begin{aligned}
 \hookrightarrow \text{LeftSum} &= \text{LeftSum} + \text{nums}[index] \\
 &= 1 + 7 \\
 &= 8
 \end{aligned}$$

Iteration: 2

index → 0	1	7	3	6	5	6
	1	2	3	4	5	6

$$\text{RightSum} = 20$$

$$\text{LeftSum} = 8$$

$$\text{Index} = 2$$

$$\begin{aligned}
 \hookrightarrow \text{RightSum} &= \text{RightSum} - \text{nums}[index] \\
 &= 20 - 3 \\
 &= 17 \\
 \hookrightarrow (\text{RightSum} &== \text{LeftSum}) \\
 17 &== 8 \quad \times \text{FAIL}
 \end{aligned}$$

$$\begin{aligned}
 \hookrightarrow \text{LeftSum} &= \text{LeftSum} + \text{nums}[index] \\
 &= 8 + 3 \\
 &= 11
 \end{aligned}$$

Iteration: 3

index → 0	1	7	3	6	5	6
	1	2	3	4	5	6

$$\text{RightSum} = 17$$

$$\text{LeftSum} = 11$$

$$\text{Index} = 3$$

$$\begin{aligned}
 \hookrightarrow \text{RightSum} &= \text{RightSum} - \text{nums}[index] \\
 &= 17 - 6 \\
 &= 11 \\
 \hookrightarrow (\text{RightSum} &== \text{LeftSum}) \\
 11 &== 11 \quad \checkmark \text{ TRUE}
 \end{aligned}$$

→ return index

Output: 3

1	7	3	6	5	6
0	1	2	3	4	5
11	11	11	Loop END	11	11

```

// HW 01: Find pivot element (Leetcode-724)
class Solution {
public:
    int pivotIndex(vector<int>& nums) {
        int n=nums.size();
        int rightSum=0;
        int leftSum=0;

        // Step 01: total sum as right sum
        for(int i=0;i<n;i++){
            rightSum+=nums[i];
        }

        for(int i=0;i<n;i++){
            rightSum-=nums[i]; // Subtract element one by one from right sum until left sum equal to right sum
            if(rightSum==leftSum){
                return i; // when leftsum and rgt sum are equal then return index to break the loop
            }
            leftSum+=nums[i]; // left sum is increment by nums[i] element
        }
        return -1; // when there is no index that satisfies the conditions in the problem statement, then return -1
    }
}

```

$T.C \Rightarrow O(n)$ } $T.C \Rightarrow O(n)$ } Time complexity
 $= O(n) + O(n)$
 $= O(n)$

3. Find Duplicate Number (Leetcode-287)

Example 1:
Input: nums = [1,3,4,2,2]
Output: 2

Example 2:
Input: nums = [3,1,3,4,2]
Output: 3

Example 3:
Input: nums = [2,2,2,2,2]
Output: 2

Example 4:
Input: nums = [1,2,3,4]
Output: -1

APPROACH:

- Method 01: Sorting approach
- Method 02: Negative marking approach
- Method 03: Position and swapping approach

Method 01: Sorting approach

nums	1	3	4	2	2
	0	1	2	3	4

① $\text{nums}[i] \in [1, N]$
② $\text{size} = N+1$

Output: 2

DRY RUN

Step 01: Sort the array

1	2	2	3	4
0	1	2	3	4

Step 02: Iterate the sorted array

Iteration 0

1	2	2	3	4
0	1	2	3	4

index = 0

$(\text{nums}[\text{index}] \neq \text{nums}[\text{index} + 1])$
1 \neq 2 True
 $\text{index}++;$

Iteration 1

1	2	2	3	4
0	1	2	3	4

index = 1

$(\text{nums}[\text{index}] \neq \text{nums}[\text{index} + 1])$
2 \neq 2 False
 $\text{return } \text{nums}[\text{index}];$

Duplicate = 2 at index 1

```
● ● ●  
// Solution 01: Sorting method  
class Solution {  
public:  
    int findDuplicate(vector<int>& nums) {  
        // Step 01: Sort nums  
        sort(nums.begin(), nums.end());  $\rightarrow \text{T.C.} = O(N \log N)$   
        // Step 02: Iterate sorted array  
        int duplicate=-1;  
        for(int i=0;i<nums.size()-1;i++){  
            // Check duplicate number  
            if(nums[i]==nums[i+1]){  
                duplicate = nums[i];  
                break;  
            }  
        }  
        return duplicate;  
    }  
    // T.C. = O(N log N)  
    // S.C. = O(N)
```

$\rightarrow \text{T.C.} = O(N-1)$

$$\Rightarrow O(N \log N) + O(N-1)$$
$$\Rightarrow O(N \log N)$$

Method 02: Negative marking approach

nums	1	3	4	2	2
0	1	2	3	4	

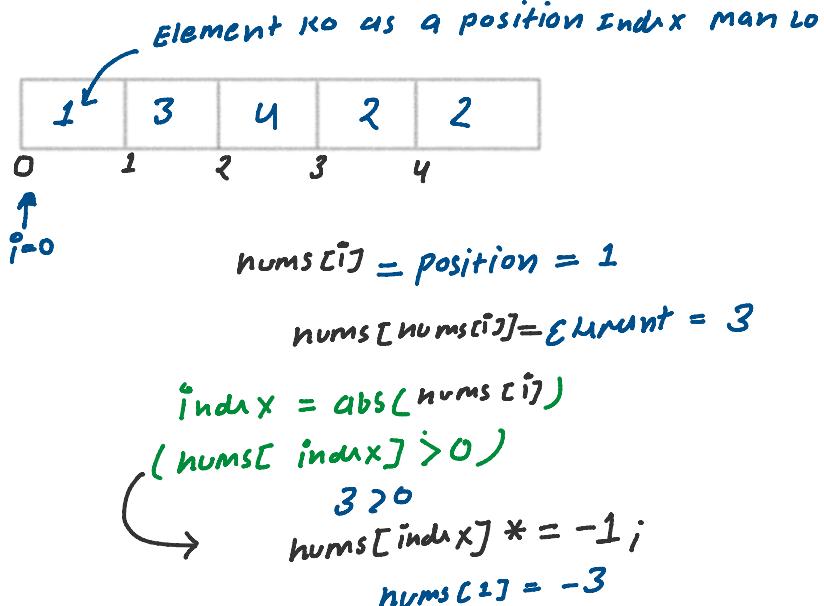
- ① $\text{nums}[i] \in [1, N]$
 ② $\text{size} = N+1$

Output: 2

Step 01: Iterate the array
 Step 02: Mark visited
 Step 03: Already visited position then return duplicate

DRY RUN

Iteration 0



Index = 1

Iteration 1

Index = 2

1	-3	4	2	2
0	1	2	3	4

$\text{index} = \text{abs}(\text{nums}[i])$
 $(\text{nums}[\text{index}] > 0)$
 $4 > 0$
 $\text{nums}[\text{index}] * = -1;$
 $\text{nums}[2] = -4$

Iteration 2

Index = 4

1	-3	-4	2	2
0	1	2	3	4

$\text{index} = \text{abs}(\text{nums}[i])$
 $(\text{nums}[\text{index}] > 0)$
 $2 > 0$

index = 4

(nums[index] > 0)
2 > 0
 $\text{nums}[index] * = -1;$
 $\text{nums}[4] = -2$

Iteration 3

1	-3	-4	2	-2
0	1	2	3	4

i=3

index = 2

index = abs(nums[i])
(nums[index] > 0)
 $-4 > 0$ *False*

Return Duplicated

return INDEX = 2

```
// Solution 02: Negative marking method
class Solution {
public:
    int findDuplicate(vector<int>& nums) {
        int duplicate=-1;
        for(int i=0;i<nums.size();i++){
            // Store absolute position temporary
            int index=abs(nums[i]);
            // Not visited position
            if(nums[index]>0){
                nums[index]*=-1;
            }
            // Already visited position
            else{
                duplicate=index;
                return duplicate;
            }
        }
        return duplicate;
    }
};

// T.C. = O(N)
// S.C. = O(1)
```

Method 03: Position and swapping approach (Position index==Element)

<i>nums</i>	1	3	4	2	2
	0	1	2	3	4

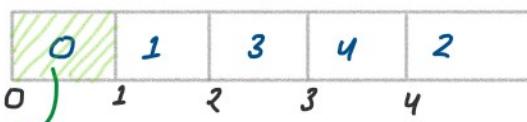
① $\text{nums}[i] \in [1, N]$
 ② $\text{size} = N+1$



(B) $O(2x - INT)$

Output: 2

NORMAL



size = 5

Agar 0th index par zero ke alawa koi or element dobara se aata hai to iska matlb wo ek duplicate number hona chahiye

DRY RUN

num	1	3	4	2	2
	0	1	2	3	4

while ($num[0] \neq num[num[0]]$)

$$1 \neq 3$$

it=0

swap(1,3)

num	3	1	4	2	2
	0	1	2	3	4

it=1

$$2 \neq 2$$

swap(3,2)

num	2	1	4	3	2
	0	1	2	3	4

it=2

$$2 \neq 4$$

swap(2,4)

num	4	1	2	3	2
	0	1	2	3	4

it=3

$$4 \neq 2$$

swap(4,2)

num	2	1	2	3	4
	0	1	2	3	4

it=4

$$2 \neq 2 \text{ FALSE}$$

return num[0] 2 is duplicate

```

// Solution 03: Position and swaping marking method
class Solution {
public:
    int findDuplicate(vector<int>& nums) {
        while(nums[0] != nums[nums[0]]){ → T.C. => O(N)
            swap(nums[0],nums[nums[0]]);
        }
        return nums[0];
    }
};

// T.C. = O(N)
// S.C. = O(1)

```

4. Missing Element From An Array With Duplicates (GFG)

Problem: Given an array $arr[]$ of size N having integers in the range $[1, N]$ with some of the elements missing. The task is to find the missing elements.

Note: There can be duplicates in the array.

EXAMPLE 01:
Input: $arr[] = \{1, 3, 5, 3, 4\}$, $N = 5$
Output: 2

EXAMPLE 02:
Input: $arr[] = \{1, 3, 3, 3, 5\}$, $N = 5$
Output: 2 4

EXAMPLE 03:
Input: $arr[] = \{1, 2, 3, 4, 4, 7, 7\}$, $N = 7$
Output: 5 6

Approach:

- Negative marking approach
- Sorting approach

1. Negative marking approach

$arr[]$	1	3	5	3	3	4
0	1	2	3	4		

observation
 $\hookrightarrow N = 5$
 $\bullet arr[i] \in [1, 5]$

Step 01: Apply Visited Method
-1 3 -5 -3 -4

Step 02: All positive index are missing
 \hookrightarrow output: 2

DRY RUN

Iteration: 0	Step 01: Apply Visited Method
	1 3 5 3 4

$i = 0$
 $index = abs(arr[i]) - 1$
 $if (arr[index - 1] > 0) {$
 $arr[index - 1] = 0$

$i = 1$
 $\text{if } (\text{arr}[i-1] > 0) \{$
 $1 > 0$
 $\text{arr}[i-1] *= -1;$
 $\}$
 $\text{arr}[0] = -1$

Iteration:1

-1	3	5	3	3	4
0	1	2	3	4	

$i = 1$
 $i = 3$
 $\text{index} = \text{abs}(\text{arr}[i]) 3$
 $\text{if } (\text{arr}[i-1] > 0) \{$
 $5 > 0$
 $\text{arr}[i-1] *= -1;$
 $\}$
 $\text{arr}[2] = -5$

Iteration:2

-1	3	-5	3	3	4
0	1	2	3	4	

$i = 2$
 $i = 5$
 $\text{index} = \text{abs}(\text{arr}[i]) 5$
 $\text{if } (\text{arr}[i-1] > 0) \{$
 $4 > 0$
 $\text{arr}[i-1] *= -1;$
 $\}$
 $\text{arr}[4] = -4$

Iteration:3

-1	3	-5	3	-4	
0	1	2	3	4	

$i = 3$
 $i = 3$
 $\text{index} = \text{abs}(\text{arr}[i]) 3$
 $\text{if } (\text{arr}[i-1] > 0) \{$
 $-5 > 0 \rightarrow \text{False}$
 $\text{arr}[i-1] *= -1;$
 $\}$
 i++;

Iteration:4

-1	3	-5	3	-4	
0	1	2	3	4	

$i = 4$
 $i = 4$
 $\text{index} = \text{abs}(\text{arr}[i]) 4$
 $\text{if } (\text{arr}[i-1] > 0) \{$
 $3 > 0$
 $\text{arr}[i-1] *= -1;$

```

        if( arr[i] > 0 ) {
            arr[i-1] *= -1;
            arr[3] = -3
}

```

Iteration: 5

-1	3	-5	-3	-4
0	1	2	3	4

$i^{\circ} = 5, N = 5 \Rightarrow i^{\circ} < N \times \text{END}$

Step 02: All positive index are missing

-1	3	-5	-3	-4
0	1	2	3	4

$\text{arr}[i] > 0$

Iteration: 0

X

Iteration: 1

X

→ point $\rightarrow (i+1) = 2$

↑
Output

Iteration: 2

X

Iteration: 3

X

Iteration: 5

X



```

// Solution 01: Negative marking method
void findMissing(vector<int> arr){
    int n = arr.size();

    // Step 01: Apply Visited Method
    for(int i=0;i<n;i++){
        int index=abs(arr[i]);
        if(arr[index-1]>0){
            arr[index-1]*=-1;
        }
    }

    // Step 02: All positive index are missing
    for(int i=0;i<n;i++){
        if(arr[i]>0){
            cout<<i+1<<" ";
        }
    }
}

T.C. = O(N) + O(N) = O(N)

```

2. Sorting approach

<i>arr</i>	1	3	5	3	4
	0	1	2	3	4

Step 01: Sorting array

1	3	3	4	5
0	1	2	3	4

Step 02: Printing missing element

$$(arr[i] \neq i+1)$$

Iteration: 0
 $i=0$

$$1 \neq 1 \quad \text{False}$$

Iteration: 1
 $i=1$

$$3 \neq 2 \quad \text{True} \rightarrow \text{Print } (i+1) = 2$$

Iteration: 2
 $i=2$

$$3 \neq 3 \quad \text{False}$$

Iteration: 3
 $i=3$

$$4 \neq 4 \quad \text{False}$$

Iteration: 4
 $i=4$

$$5 \neq 5 \quad \text{False}$$

Output

```

● ● ●

// Solution 02: Sorting method
void findMissing(vector<int> arr){
    int n = arr.size();
    // Step 01: Sorting array → T.C. → O(N log N)
    sort(arr.begin(), arr.end());

    // Step 02: Printing missing element
    for(int i=0; i<n; i++){
        if(arr[i] != i+1){ → T.C. → O(N)
            cout << i+1 << " ";
        }
    }
} → T.C. → O(N log N) + O(N) ⇒ O(N log N)

```

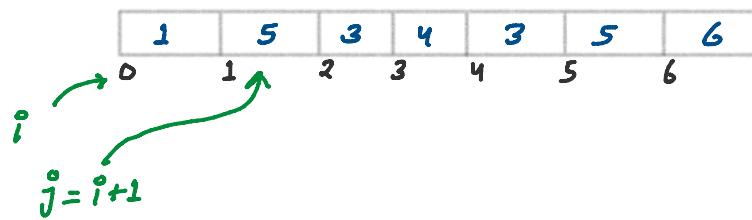
5. Find First Repeating Element (GFG)

EXAMPLE 01:
INPUT: arr{1, 5, 3, 4, 3, 5, 6} and N=7
OUTPUT: 2
Explanation: Value 5 is at index 2

EXAMPLE 02:
INPUT: arr{1, 2, 3, 4, 5, 6, 7} and N=7
OUTPUT: -1
Explanation: No repeated value

Note: Position return should be according to 1-based indexing

Brute force approach



i	$j = i+1$	$\text{arr}[i] == \text{arr}[j]$
0	1	$1 == 5 X$
	2	$1 == 3 X$
	3	$1 == 4 X$
	4	$1 == 5 X$
	5	$1 == 6 X$
	6	
1	2	$5 == 3 X$
	3	$5 == 4 X$
	4	$5 == 3 X$
	5	$5 == 5 L$

$\rightarrow \text{return } (i+1);$

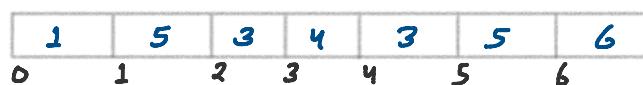
```

// BRUTE FORCE APPROACH
int bruteForceSol(int *arr, int n) {
    for(int i=0; i<n; i++){ → T.C. = O(N)
        for(int j=i+1; j<n; j++){ → T.C. = O(N)
            if(arr[i]==arr[j]){
                return i+1;
            }
        }
        return -1;
    }
    // TIME COMPLEXITY: O(N^2)
    // SPACE COMPLEXITY: O(1)

```

$\Rightarrow O(N \times N)$
 $\Rightarrow O(N^2)$
 $T.C. \Rightarrow O(N^2)$

Optimal approach with hashing technique



Step 01: Traverse array and store it's element as hashing

KEY	VALUE
1	1
5	2
3	2
4	1
6	1

arr[5]

occurrences

Step 02: Traverse array to check each element if it has occurrence in future

1	5	3	3	4	3	5	5	6
0	1	2	3	4	5	6	7	8

arr[i] > 1	KEY	VALUE
$i=0$	1 > 2 X	1
$p=1$	5 > 2 ✓	2
	3	2
	4	1
	6	1

Return $i+1$

Hashing: We can use unordered map to store array's element in pair of key and value

Declaration of unordered map

Unordered_map<int, int> hash
 ↗ Name
 ↗ keyType
 ↗ valueType

Read more from this resource: https://www.geeksforgeeks.org/unordered_map-in-cpp-stl

```
// OPTIMAL SOLUTION WITH HASHING APPROACH
int optimalSol(int arr[], int n){
    // Declared unordered_map
    unordered_map<int, int> hash;

    // Step 01: Traverse array and store it's element as hashing
    for(int i=0; i<n; i++){
        hash[arr[i]]++; T.C = O(N)
    }

    // Step 02: Traverse array to check each element if it has occurrence in future
    for(int i=0; i<n; i++){
        if(hash[arr[i]] > 1){ T.C = O(N)
            return i+1;
        }
    }
    return -1;
}
// TIME COMPLEXITY: O(N)
// SPACE COMPLEXITY: O(N)
```

$T.C \Rightarrow O(N) + O(N)$
 $\Rightarrow O(N)$

6. Common Element in 3 Sorted Array (GFG)

Example 01:

Input:

```
n1 = 6; A = {1, 5, 10, 20, 40, 80}
n2 = 5; B = {6, 7, 20, 80, 100}
n3 = 8; C = {3, 4, 15, 20, 30, 70, 80, 120}
Output: 20 80
```

Example 02:

Input:

```
n1 = 3; A = {3, 3, 3}
n2 = 3; B = {3, 3, 3}
n3 = 3; C = {3, 3, 3}
Output: 3
```

Optimal Approach:

Step 01: remove duplicates from sorted array

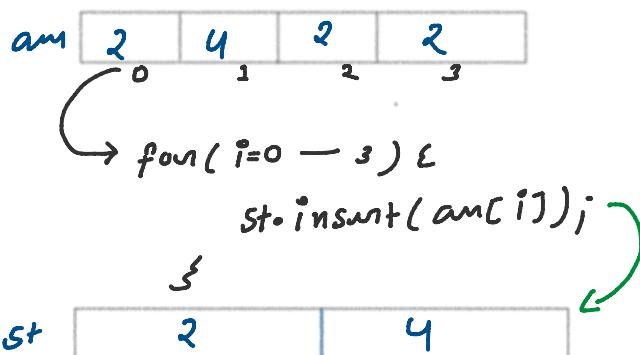
Step 02: store common value of all three arrays in new array

Step 01: store unique element in new array with the help of C++ STL Data Structure is `set(dataType)`

Declaration of set

`set<int> st;`
 ↓
 Data Type NAME

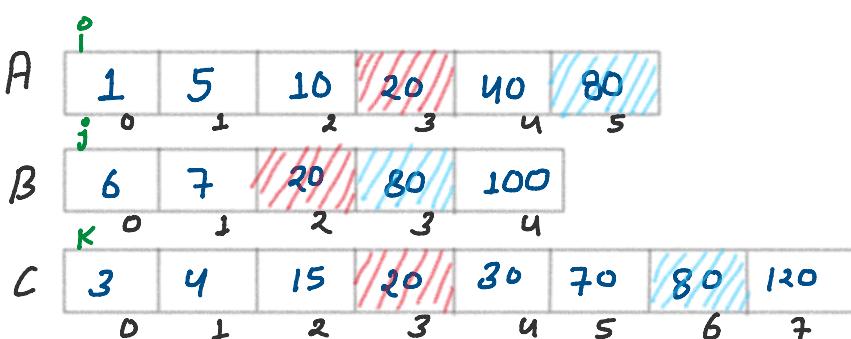
EXAMPLE



Read more from this resource: <https://www.geeksforgeeks.org/set-in-cpp-stl/>

DRY RUN

Step 02: store common value of all three arrays in new array



if (A[i] == B[j] && B[k] == C[l] && C[m] == A[i])
 {
 st.insert(A[i]);
 i++, j++, k++, l++, m++;
 }
 ... until B[k] != C[l]

i++, j++, k++

}
 Else if ($A[i] < B[j]$)
 {
 i++
 }
 Else if ($B[j] < C[k]$)
 {
 j++
 }
 Else
 {
 k++
 }

Terminating Condition

($i < n_1 \&& j < n_2 \&& k < n_3$)

```

● ● ●
// Common Element in 3 Sorted Array (GFG)
class Solution
{
public:
    vector<int> commonElements ( int A[], int B[], int C[], int n1, int n2, int n3 )
    {
        vector<int> ans;
        set<int> st;
        int i=0, j=0, k=0;

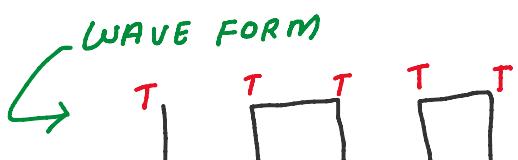
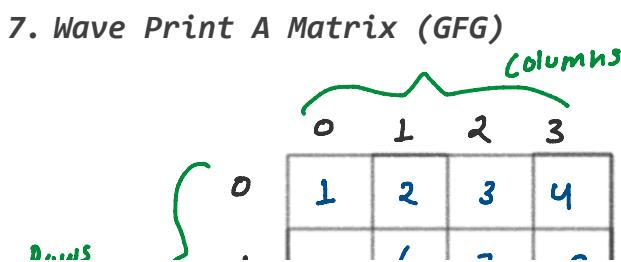
        while(i<n1 && j<n2 && k<n3)
        {
            if(A[i]==B[j] && B[j]==C[k] && C[k]==A[i])
            {
                st.insert(A[i]);
                i++, j++, k++;
            }
            else if(A[i]<B[j])
            {
                i++;
            }
            else if(B[j]<C[k])
            {
                j++;
            }
            else
            {
                k++;
            }
        }

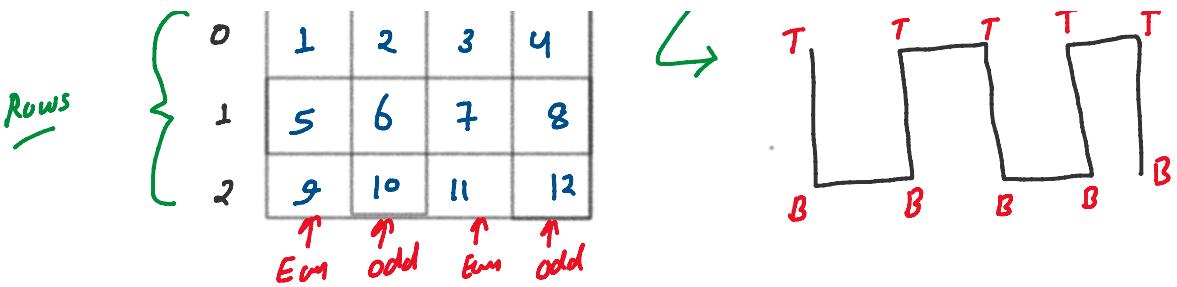
        for(auto i: st)
        {
            ans.push_back(i);
        }

        return ans;
    }
};

// TIME COMPLEXITY: O(N1+N2+N3)
// SPACE COMPLEXITY: O(N1+N2+N3)

```





Approach:

- When number of column is even then print row top to bottom
- When number of column is odd then print row bottom to top

```

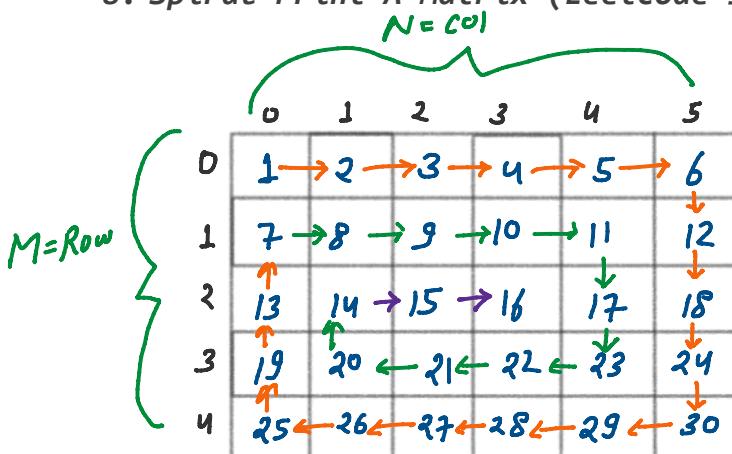
// Print wave matrix
void printWaveMatrix(vector<vector<int>> matrix){
    int row = matrix.size();
    int col = matrix[0].size();

    // Iterate array column wise
    for(int startCol=0; startCol<col; startCol++){

        // when startCol==even then print row top to bottom
        if((startCol & 1)==0){
            for(int i=0;i<row;i++){
                cout<<matrix[i][startCol]<< " ";
            }
        }
        // when startCol==odd then print row bottom to top
        else{
            for(int i=row-1;i>=0;i--){
                cout<<matrix[i][startCol]<< " ";
            }
        }
    }
}
    
```

$T \cdot C \Rightarrow O(M \times N)$

8. Spiral Print A Matrix (Leetcode-54)



Output:

1 2 3 4 5 6 12 18 24 30 29 28 27 26 25
19 13 7 8 9 10 11 17 23 22 21 14 15 16

<code>startingRow = 0</code>
<code>endingCol = 5</code>
<code>endingRow = 4</code>
<code>startingCol = 0</code>

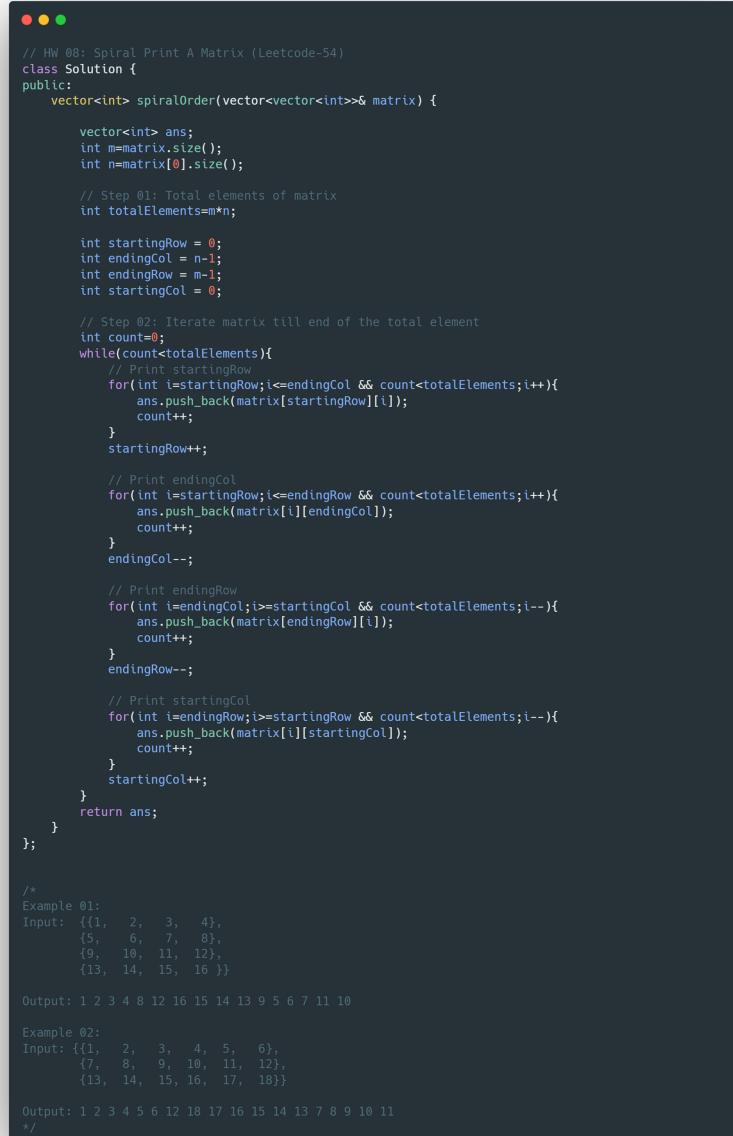
<code>startingRow = 1</code>
<code>endingCol = 4</code>
<code>endingRow = 3</code>
<code>startingCol = 1</code>

<code>startingRow = 2</code>
<code>endingCol = 3</code>
<code>endingRow = 2</code>
<code>startingCol = 2</code>

Optimal Approach:

- Step 01: find total elements
 Step 02: iterate matrix till end of the total element and print
- Print startingRow
 - Print endingCol
 - Print endingRow

- Print startingCol



```
// HW 08: Spiral Print A Matrix (Leetcode-54)
class Solution {
public:
    vector<int> spiralOrder(vector<vector<int>>& matrix) {
        vector<int> ans;
        int m=matrix.size();
        int n=matrix[0].size();

        // Step 01: Total elements of matrix
        int totalElements=m*n;

        int startingRow = 0;
        int endingCol = n-1;
        int endingRow = m-1;
        int startingCol = 0;

        // Step 02: Iterate matrix till end of the total element
        int count=0;
        while(count<totalElements){
            // Print startingRow
            for(int i=startingRow;i<=endingCol && count<totalElements;i++){
                ans.push_back(matrix[startingRow][i]);
                count++;
            }
            startingRow++;

            // Print endingCol
            for(int i=startingRow;i<=endingRow && count<totalElements;i++){
                ans.push_back(matrix[i][endingCol]);
                count++;
            }
            endingCol--;

            // Print endingRow
            for(int i=endingCol;i>=startingCol && count<totalElements;i--){
                ans.push_back(matrix[endingRow][i]);
                count++;
            }
            endingRow--;

            // Print startingCol
            for(int i=endingRow;i>=startingRow && count<totalElements;i--){
                ans.push_back(matrix[i][startingCol]);
                count++;
            }
            startingCol++;
        }
        return ans;
    }

    /*
    Example 01:
    Input: {{1, 2, 3, 4},
             {5, 6, 7, 8},
             {9, 10, 11, 12},
             {13, 14, 15, 16}}
    Output: 1 2 3 4 8 12 16 15 14 13 9 5 6 7 11 10

    Example 02:
    Input: {{1, 2, 3, 4, 5, 6},
             {7, 8, 9, 10, 11, 12},
             {13, 14, 15, 16, 17, 18}}
    Output: 1 2 3 4 5 6 12 18 17 16 15 14 13 7 8 9 10 11
    */
}
```

15. Add two numbers represented by two array (GFG)

Example 01:
Input : A[] = {1, 2}, B[] = {2, 1}
Output : 33

Example 02:
Input : A[] = {9, 5, 4, 9}, B[] = {2, 1, 4}
Output : 9763

Example 03:
Input : A[] = {2, 1, 4}, B[] = {9, 5, 4, 9}
Output : 9763

Example 04:
Input : A[] = {9, 1, 4}, B[] = {8, 1, 4}
Output : 1728

Example 05:
Input : A[] = {0, 0, 2, 1, 4}, B[] = {0, 0, 2, 1, 4}
Output : 428

TRY RUN

DRY RUN

Example 02:

A	<table border="1"> <tr> <td>9</td><td>5</td><td>4</td><td>9</td></tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td></tr> </table>	9	5	4	9	0	1	2	3
9	5	4	9						
0	1	2	3						

B	<table border="1"> <tr> <td>2</td><td>1</td><td>4</td></tr> <tr> <td>0</td><td>1</td><td>2</td></tr> </table>	2	1	4	0	1	2
2	1	4					
0	1	2					

$$N = 4$$

Output: 9763

$$M = 3$$

Iteration 0

A	<table border="1"> <tr> <td>9</td><td>5</td><td>4</td><td>9</td></tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td></tr> </table>	9	5	4	9	0	1	2	3	1	0	→ carry
9	5	4	9									
0	1	2	3									
				→ i = 3								
B	<table border="1"> <tr> <td>2</td><td>1</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td> </tr> </table>	2	1	4	0	1	2			→ j = 2		
2	1	4										
0	1	2										
			3	→ digit								

$$(i >= 0 \ \& \ \& \ j >= 0)$$

$$\text{carry} = 0$$

$$\begin{aligned} x &= A[i] + B[j] + \text{carry} \\ &= 9 + 4 + 0 \\ &= 13 \end{aligned}$$

$$\begin{aligned} \text{digit} &= x \% 10^i \\ &= 3 \end{aligned}$$

$$\begin{aligned} \text{carry} &= x / 10^i \\ &= 1 \end{aligned}$$

Iteration 1

A	<table border="1"> <tr> <td>9</td><td>5</td><td>4</td><td>9</td></tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td></tr> </table>	9	5	4	9	0	1	2	3	0	1	0	→ carry
9	5	4	9										
0	1	2	3										
				→ i = 2									
B	<table border="1"> <tr> <td>2</td><td>1</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td> </tr> </table>	2	1	4	0	1	2			→ j = 1			
2	1	4											
0	1	2											
		6	3	→ digit									

$$(i >= 0 \ \& \ \& \ j >= 0)$$

$$\text{carry} = 1$$

$$\begin{aligned} x &= A[i] + B[j] + \text{carry} \\ &= 4 + 1 + 1 \\ &= 6 \end{aligned}$$

$$\begin{aligned} \text{digit} &= x \% 10^i \\ &= 6 \end{aligned}$$

$$\begin{aligned} \text{carry} &= x / 10^i \\ &= 0 \end{aligned}$$

Iteration 2

A	<table border="1"> <tr> <td>9</td><td>5</td><td>4</td><td>9</td></tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td></tr> </table>	9	5	4	9	0	1	2	3	0	0	1	0	→ carry
9	5	4	9											
0	1	2	3											
					→ i = 1									
B	<table border="1"> <tr> <td>2</td><td>1</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td> </tr> </table>	2	1	4	0	1	2				→ j = 0			
2	1	4												
0	1	2												
		7	6	3	→ digit									

$$(i >= 0 \ \& \ \& \ j >= 0)$$

$$\text{carry} = 0$$

$$\begin{aligned} x &= A[i] + B[j] + \text{carry} \\ &= 5 + 2 + 0 \\ &= 7 \end{aligned}$$

$$\begin{aligned} \text{digit} &= x \% 10^i \\ &= 7 \end{aligned}$$

$$\begin{aligned} \text{carry} &= x / 10^i \\ &= 0 \end{aligned}$$

Iteration 3

A	0	0	1	0	→ carry
	9	5	4	9	
	0	1	2	3	→ i = 0
B	0	2	1	4	→ j = -1
	9	7	6	3	→ digit

$$(j >= 0)$$

$$\hookrightarrow \text{carry} = 0$$

$$x = A[i] + 0 + \text{carry}$$

$$= 9 + 0 + 0$$

$$= 9$$

$$\text{digit} = x \% 10^i$$

$$= 9$$

$$\text{carry} = x / 10^i$$

$$= 0$$

Iteration 4

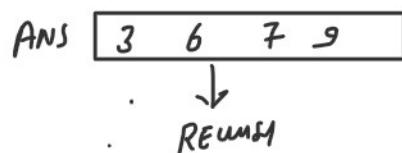
A	0	0	1	0	→ carry
	9	5	4	9	
	0	1	2	3	→ i = -1
B	0	2	1	4	→ j = -1
	9	7	6	3	→ digit

(MUJHE ANS ME 0 NAHI CHAIYE)

if(carry > 0) FALSE

push kando Ans me agar TRUE HAI

Yeh Ans actual me kis tarike se save hai ans ke andar



Final
Ans

9	7	6	3
---	---	---	---

DRY RUN

Example 05:

Input : $A[] = \{0, 0, 2, 1, 4\}$, $B[] = \{0, 0, 2, 1, 4\}$
Output : 428

Iteration 0

A	0	0	2	1	4	0	0	→ carry
	0	1	2	3	4			→ i = 4
B	0	0	2	1	4			→ j = 4
	0	1	2	3	4			

($i >= 0$ & $j >= 0$)

$$\text{carry} = 0$$

$$x = A[i] + B[j] + \text{carry}$$

$$= 4 + 4 + 0 = 8$$

$$\text{digit} = x \% 10$$

$$= 8$$

$$\text{carry} = x / 10$$

$$= 0$$

Iteration 1

A	<table border="1"> <tr><td>0</td><td>0</td><td>2</td><td>1</td><td>4</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	2	1	4	0	1	2	3	4	$i = 3$
0	0	2	1	4								
0	1	2	3	4								
B	<table border="1"> <tr><td>0</td><td>0</td><td>2</td><td>1</td><td>4</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	2	1	4	0	1	2	3	4	$j = 3$
0	0	2	1	4								
0	1	2	3	4								
	<table border="1"> <tr><td>2</td><td>8</td></tr> </table>	2	8	$\rightarrow \text{Digit}$								
2	8											

$$(i=0 \text{ & } j=0)$$

$$\text{carry} = 0$$

$$x = A[i] + B[j] + \text{carry}$$

$$= 1 + 1 + 0 = 2$$

$$\text{digit} = x \% 10$$

$$= 2$$

$$\text{carry} = x / 10$$

$$= 0$$

Iteration 2

A	<table border="1"> <tr><td>0</td><td>0</td><td>2</td><td>1</td><td>4</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	2	1	4	0	1	2	3	4	$i = 2$
0	0	2	1	4								
0	1	2	3	4								
B	<table border="1"> <tr><td>0</td><td>0</td><td>2</td><td>1</td><td>4</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	2	1	4	0	1	2	3	4	$j = 2$
0	0	2	1	4								
0	1	2	3	4								
	<table border="1"> <tr><td>4</td><td>2</td><td>8</td></tr> </table>	4	2	8	$\rightarrow \text{Digit}$							
4	2	8										

$$(i=0 \text{ & } j=0)$$

$$\text{carry} = 0$$

$$x = A[i] + B[j] + \text{carry}$$

$$= 2 + 2 + 0 = 4$$

$$\text{digit} = x \% 10$$

$$= 4$$

$$\text{carry} = x / 10$$

$$= 0$$

Iteration 3

A	<table border="1"> <tr><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	0	0	0	0	1	2	3	4	$i = 1$
0	0	0	0	0								
0	1	2	3	4								
B	<table border="1"> <tr><td>0</td><td>0</td><td>2</td><td>1</td><td>4</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	2	1	4	0	1	2	3	4	$j = 1$
0	0	2	1	4								
0	1	2	3	4								
	<table border="1"> <tr><td>0</td><td>4</td><td>2</td><td>8</td></tr> </table>	0	4	2	8	$\rightarrow \text{Digit}$						
0	4	2	8									

$$(i=0 \text{ & } j=0)$$

$$\text{carry} = 0$$

$$x = A[i] + B[j] + \text{carry}$$

$$= 0 + 0 + 0 = 0$$

$$\text{digit} = x \% 10$$

$$= 0$$

$$\text{carry} = x / 10$$

$$= 0$$

Iteration 4

A	<table border="1"> <tr><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	0	0	0	0	1	2	3	4	$i = 0$
0	0	0	0	0								
0	1	2	3	4								
B	<table border="1"> <tr><td>0</td><td>0</td><td>2</td><td>1</td><td>4</td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> </table>	0	0	2	1	4	0	1	2	3	4	$j = 0$
0	0	2	1	4								
0	1	2	3	4								

$$(i=0 \text{ & } j=0)$$

$$\text{carry} = 0$$

$$x = A[i] + B[j] + \text{carry}$$

$$= 0 + 0 + 0 = 0$$

A	<table border="1"> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td> </tr> </table>	0	1	2	3	4	0	1	2	3	4	$i = 0$
0	1	2	3	4								
0	1	2	3	4								
B	<table border="1"> <tr> <td>0</td><td>0</td><td>2</td><td>1</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td> </tr> </table>	0	0	2	1	4	0	1	2	3	4	$j = 0$
0	0	2	1	4								
0	1	2	3	4								
	<table border="1"> <tr> <td>0</td><td>0</td><td>4</td><td>2</td><td>8</td> </tr> <tr> <td></td><td></td><td></td><td></td><td></td> </tr> </table>	0	0	4	2	8						$\rightarrow \text{digit}$
0	0	4	2	8								

$$\begin{aligned}
 X &= A[i] + B[j] + \text{carry} \\
 &= 0 + 0 + 0 = 0 \\
 \text{digit} &= X \% 10 \\
 &= 0 \\
 \text{carry} &= X / 10 \\
 &= 0
 \end{aligned}$$

Iteration 5

A	<table border="1"> <tr> <td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td> </tr> </table>	0	0	0	0	0	0	0	1	2	3	4	$\rightarrow \text{carry}$
0	0	0	0	0	0								
0	1	2	3	4									
B	<table border="1"> <tr> <td>0</td><td>0</td><td>2</td><td>1</td><td>4</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td> </tr> </table>	0	0	2	1	4	0	1	2	3	4	$\rightarrow j = -1$	
0	0	2	1	4									
0	1	2	3	4									
	<table border="1"> <tr> <td>0</td><td>0</td><td>4</td><td>2</td><td>8</td> </tr> <tr> <td></td><td></td><td></td><td></td><td></td> </tr> </table>	0	0	4	2	8						$\rightarrow \text{digit}$	
0	0	4	2	8									

\leftarrow if(carry > 0) fail
 \leftarrow push kardo ANS ME AGAR TRUE
 Hai
 Yeh Ans actual me kis tarike se save hai ans ke andar

ANS

8	2	4	0	0
---	---	---	---	---

\downarrow
REVERSE

Final
ANS

0	0	4	2	8
---	---	---	---	---

WRONG ANS

Solution

ANS	<table border="1"> <tr> <td>8</td><td>2</td><td>4</td><td>0</td><td>0</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td><td>4</td> </tr> </table>	8	2	4	0	0	0	1	2	3	4
8	2	4	0	0							
0	1	2	3	4							
	while (ans.size() - 1 == 10)										
\leftarrow	ans.pop(); Delete last element										
①	$\text{size} = 5 \quad \text{ans}[4] = 0$										
	<table border="1"> <tr> <td>8</td><td>2</td><td>4</td><td>0</td> </tr> <tr> <td>0</td><td>1</td><td>2</td><td>3</td> </tr> </table>	8	2	4	0	0	1	2	3		
8	2	4	0								
0	1	2	3								
②	$\text{size} = 4 \quad \text{ans}[3] = 0$										
	<table border="1"> <tr> <td>8</td><td>2</td><td>4</td> </tr> </table>	8	2	4							
8	2	4									
	\downarrow REVERSE										
	<table border="1"> <tr> <td>4</td><td>2</td><td>8</td> </tr> </table>	4	2	8							
4	2	8									

FIR Right ANS Kaisi
AYEGA

RUK jao

CORRECT
ANS

```

  ● ● ●

// HW 15: Add two numbers represented by two array (GFG)
#include<iostream>
#include<vector>
#include <bits/stdc++.h>
using namespace std;

// Add two numbers represented by two array

```

```

// HW 15: Add two numbers represented by two array (GFG)
#include<iostream>
#include<vector>
#include <bits/stdc++.h>
using namespace std;

// Add two numbers represented by two array
vector<int> calc_Sum(int a[], int n, int b[], int m){
    int i=n-1;
    int j=m-1;
    vector<int> ans;
    int carry = 0;

    // Case: 01 Jab i and j both are greater than or equal to 0 hoga
    while(i>=0 && j>=0){
        int x = a[i] + b[j] + carry;
        int digit = x % 10;
        // Push digit in ans
        ans.push_back(digit);
        carry = x / 10;
        i--;
        j--;
    }
    // Case 02: Jab i greater than or equal to 0 hoga
    while(i>=0){
        int x = a[i] + 0 + carry;
        int digit = x % 10;
        // Push digit in ans
        ans.push_back(digit);
        carry = x / 10;
        i--;
    }
    // Case 03: Jab j greater than or equal to 0 hoga
    while(j>=0){
        int x = 0 + b[j] + carry;
        int digit = x % 10;
        // Push digit in ans
        ans.push_back(digit);
        carry = x / 10;
        j--;
    }
    // Case 04: Jab Carry greater than 0 hoga
    if(carry > 0){
        ans.push_back(carry);
    }
    // Case 05: Jab actual ans ke last position par zero ho tab tak use delete karte rahenge
    while(ans[ans.size()-1] == 0){
        ans.pop_back();
    }
    // Actual ans ko reverse krdo correct ans ke liye
    reverse(ans.begin(), ans.end());
    return ans;
}

int main(){
    int a[]={9, 5, 4, 9};
    int b[]={2, 1, 4};
    int n = sizeof(a)/sizeof(a[0]);
    int m = sizeof(b)/sizeof(b[0]);

    vector<int> correctAns = calc_Sum(a, n, b, m);
    for (auto i : correctAns) {
        cout<<i;
    }

    return 0;
}

/*
Time Complexity: O(N + M)
Space Complexity: O(N + M)

Where N and M are size of array of a and b respectively
*/

```

9. Factorial of A Large Number (GFG)

Example 01:
Enter number: 5
120

Example 02:
Enter number: 100
93326215443944152681699238856266700490715968264381621
468592963895217599992299156089414639761565182862536

Example 01:
Enter number: 5
120

```
Example 02:  
Enter number: 100  
93326215443944152681699238856266700490715968264381621  
468592963895217599932299156089414639761565182862536  
97920827223758251185210916864000000000000000000000000000000
```

DRY RUN

$$N = 5! \Rightarrow 1 * 2 * 3 * 4 * 5 = 120$$

$$\begin{aligned} \text{Carry} &= 0 \\ x &= \text{ans}[j] * i + \text{carry} \\ \text{ans}[j] &= x \% 10 \\ \text{carry} &= x / 10 \end{aligned}$$

ans initially 1 element stored
Karega

Iteration: 01

$$Canary = 0 \quad i = 2 \quad \hat{j} = 0 \quad size = 1$$

Ans $\frac{1}{0} \rightarrow j$
 $1 - \sin 2\theta$

$$\begin{aligned} x &= \text{ans}[j] * i + \text{carry} \\ &= 1 * 2 + 0 \\ &= 2 \end{aligned}$$

$$c_{avg} = x / 10$$

Interaction: 02

$$Canary = 0 \quad i = 3 \quad j = 0 \quad size = 1$$

$$\text{Ans} \quad \boxed{2} \quad \begin{matrix} \rightarrow \\ 0 \\ 1 \end{matrix} = \text{size}$$

$$\begin{aligned} x &= \text{ans}[j] * i + \text{carry} \\ &= 2 * 3 + 0 \\ &= 6 \end{aligned}$$

$$\text{am}[j] = X \% 10 \\ = 6$$

$$c_{avg} = x / 10$$
$$= P$$

Iterations: 03

$$\text{Carry} = 0 \quad i = 4 \quad j = 0 \quad \text{sum} = 1$$

Ans 6 $0 \rightarrow i$

$$\text{carry} = 0 \quad i = 4 \quad j$$

$$x = \text{ans}[j] * 10 + \text{carry}$$

$$= 6 * 10 + 0$$

$$= 24$$

$$\text{ans}[j] = X \% 10$$

$$= 4$$

$$\text{carry} = X / 10$$

$$= 2$$

Ans

6

 $\stackrel{i}{\rightarrow}$
0
1 — size

$$\Rightarrow \text{carry} = 2 \quad i = 4 \quad j = 1 \quad \text{size} = 1$$

while ($\text{carry} > 0$)

Jab tak mera carry equal to zero nahi ho jayega tab tak me ek new element add karta rahunga

{

$$\text{ans.push_back}(\text{carry} \% 10); \Rightarrow 2$$

$$\text{carry} = \text{carry} / 10; \Rightarrow 0$$

}

2	4
---	---

 $\stackrel{i}{\rightarrow}$

1 0

Iteration: 04

$$\text{carry} = 0 \quad i = 5 \quad j = 0 \quad \text{size} = 2$$

Ans

2	4
---	---

 $\stackrel{i}{\rightarrow}$
1 0

size = 2

$$x = \text{ans}[j] * 10 + \text{carry}$$

$$= 4 * 5 + 0$$

$$= 20$$

$$\text{ans}[j] = X \% 10$$

$$= 0$$

$$\text{carry} = X / 10$$

$$= 2$$

1

2	0
---	---

 $\stackrel{i}{\rightarrow}$

1 0

$$\text{carry} = 2 \quad i = 5 \quad j = 1 \quad \text{size} = 2$$

Ans

2	0
---	---

 $\stackrel{i}{\rightarrow}$
1 0

size = 2

$$x = \text{ans}[j] * 10 + \text{carry}$$

$$= 2 * 5 + 2$$

$$= 12$$

$$\text{ans}[j] = X \% 10$$

$$= 2$$

$$\text{carry} = X / 10$$

$$= 1$$

2	0
---	---

 $\stackrel{i}{\rightarrow}$

1 0

$$\text{cang} = \frac{x}{10}$$

= 1

$$\Rightarrow \text{cang} = 1 \quad i=5 \quad j=3 \quad size=2$$

while ($cang > 0$)

{

ans.push_back($cang \% 10$) ; $\Rightarrow 1$

$cang = cang / 10$; $i \Rightarrow 0$

}

1	2	0
2	1	0

↑

Actual

$i=6$ } $N=5$ } $\text{RUK jaao... } (i < N)$

0	2	1
0	1	2

REVERSE

1	2	0
---	---	---

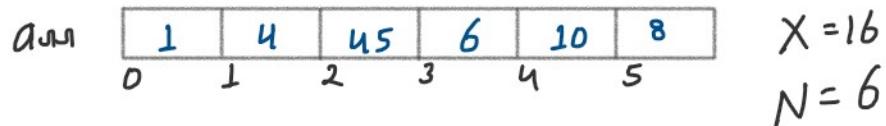


$$\underline{T \in O(N)}$$

10. Key Pair/Two Sum (GFG and Leetcode-1)

<p>Example 01:</p> <p>Input: $N = 6, X = 16$ $\text{Arr}[] = \{1, 4, 45, 6, 10, 8\}$ Output: Yes Explanation: $\text{Arr}[3] + \text{Arr}[4] = 6 + 10 = 16$</p>	<p>Example 02:</p> <p>Input: $N = 5, X = 10$ $\text{Arr}[] = \{1, 2, 4, 3, 6\}$ Output: Yes Explanation: $\text{Arr}[2] + \text{Arr}[4] = 4 + 6 = 10$</p>
--	--

Example: 01



Total Pairs

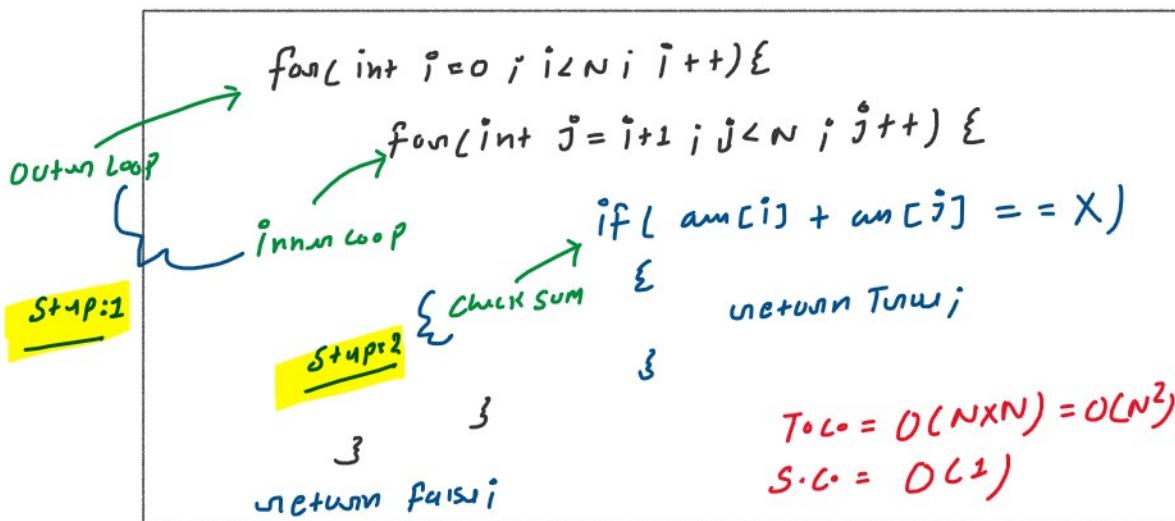
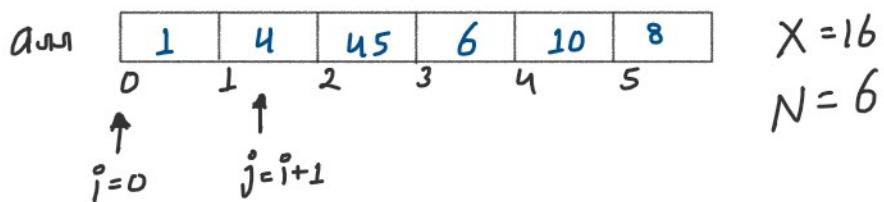
(1, 4)	(4, 45)	(45, 6)	(6, 10)	(10, 8)
(1, 45)	(4, 6)	(45, 10)	(6, 8)	
(1, 6)	(4, 10)	(45, 8)		
(1, 10)	(4, 8)			
(1, 8)				

$$\left. \begin{array}{l} \text{sum} = 16 \\ \text{target} = 16 \end{array} \right\} \rightarrow \text{YES}$$

Brute Force Approach:

Step 01: find all pairs

Step 02: check all pair's sum



Two Pointers Approach:

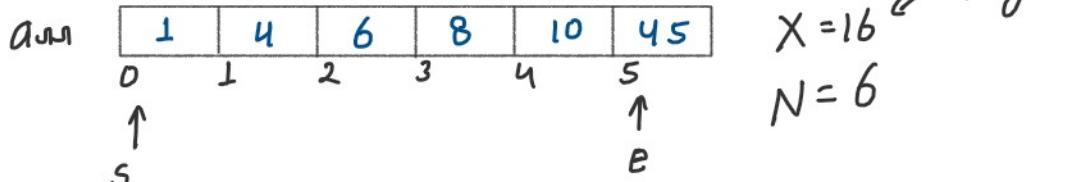
Step 01: Sort the array

Step 02: agar arr[s]+arr[e]==target hai to return YES kardo

Step 03: agar arr[s]+arr[e]<target to mujhe nearly answer s++
karne par jaldi mil skta hai

Step 04: agar arr[s]+arr[e]>target to mujhe nearly answer e--
karne par jaldi mil skta hai

Iteration: 01



$s=0$
 $e=5$
 $x=16$

$$(arr[s] + arr[e] > x)$$

$$1 + 45 > 16$$

$$e--$$

Iteration: 02

arr

1	4	6	8	10	45
0	1	2	3	4	5
\uparrow				\uparrow	e

$$X = 16 \leftarrow \text{target}$$

$$N = 6$$

$s=0$
 $e=4$
 $x=16$

$$(arr[s] + arr[e] < x)$$

$$1 + 10 < 16$$

$$s++$$

Iteration: 03

arr

1	4	6	8	10	45
0	1	2	3	4	5
\uparrow	\uparrow	s		\uparrow	e

$$X = 16 \leftarrow \text{target}$$

$$N = 6$$

$s=1$
 $e=4$
 $x=16$

$$(arr[s] + arr[e] < x)$$

$$4 + 10 < 16$$

$$s++$$

Iteration: 04

arr

1	4	6	8	10	45
0	1	2	3	4	5
	\uparrow			\uparrow	e

$$X = 16 \leftarrow \text{target}$$

$$N = 6$$

$s=2$
 $e=4$
 $x=16$

$$(arr[s] + arr[e] == x)$$

$$6 + 10 == 16$$

$$\text{return true}$$

OUTPUT: YES

```
// MM 10: Key Pair/Two Sum (GFG and Leetcode-1)
#include<iostream>
#include<vector>
#include <bits/stdc++.h>
using namespace std;

// TWO SUM
bool twoSum(vector<int> arr, int X){
    // Step 01: Sort the array
    sort(arr.begin(), arr.end());
    int N=arr.size();
    int s=0;
    int e=N-1;
```

```

// 11.10) Key Pair/Two Sum (GFG and Leetcode-1)
#include<iostream>
#include<vector>
#include<algorithm>
using namespace std;

// TWO SUM
bool twoSum(vector<int> arr, int X){
    // Step 01: Sort the array
    sort(arr.begin(), arr.end());

    int N=arr.size();
    int s=0;
    int e=N-1;

    while(s<e){
        // Step 02:
        if(arr[s]+arr[e]==X){
            return true;
        }
        // Step 03:
        // If pair sum is less than X, it means current pair is too small,
        // We have to move the starting index to right to consider larger pair.
        else if (arr[s]+arr[e]<X){
            {
                s++;
            }
        }
        // Step 04:
        // If pair sum is greater than X, it means current pair is too large,
        // We have to move the ending index to left to consider smaller pair.
        else{
            e--;
        }
    }
    return false;
}

int main(){
    vector<int> arr{1, 4, 45, 6, 10, 8};
    int X=10;

    bool ans = twoSum(arr,X);

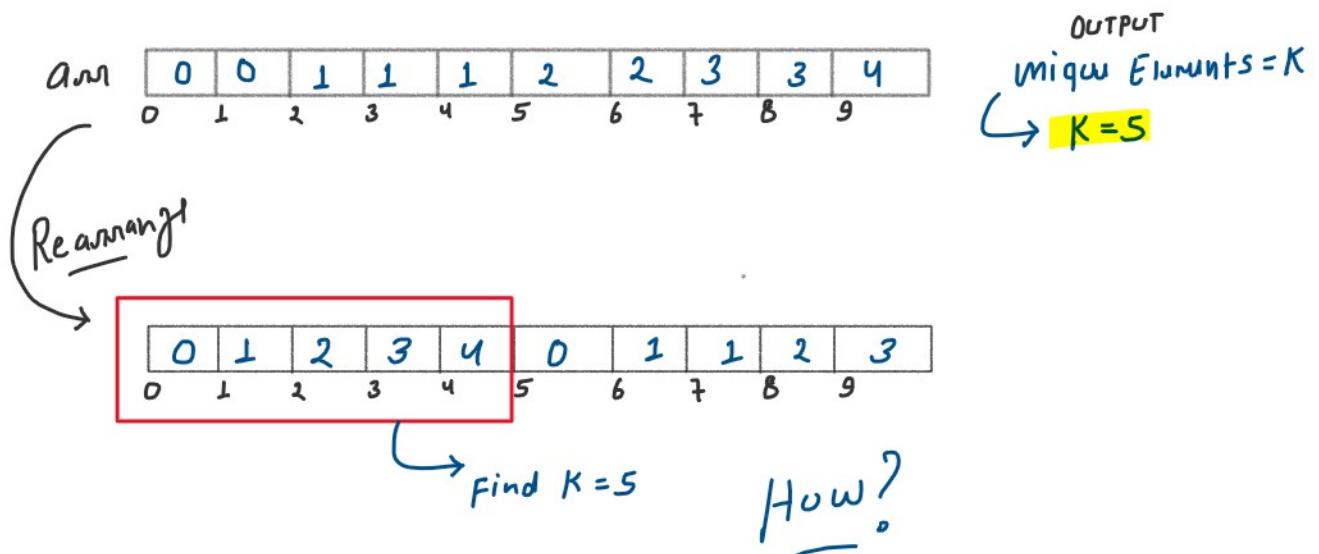
    if(ans){
        cout<<"YES"<<endl;
    }
    else{
        cout<<"NO"<<endl;
    }

    return 0;
}

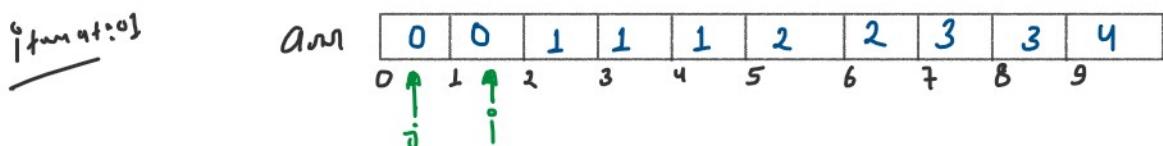
/*
Time Complexity: O(NlogN)+O(N)→O(NlogN), where N is size of array
Space complexity: O(1)
*/

```

11. Remove Duplicates From Sorted Array (Leetcode-26)



Two Pointers Approach:



$$arr[i] == arr[j]$$

$\rightarrow i++$

(where j is a position
of unique element)

$j=0$

$i=1$

$$arr[1] == arr[j]$$

$$0 == 0$$

↓
 $i++$

$i_{format}: 2$

arr

0	0	1	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9

j ↑ i ↑

$j=0$

$i=2$

$$arr[i] == arr[j]$$

$$1 == 0$$

↓
 $j++$

$$arr[j] = arr[i]$$

$i++$

$i_{format}: 3$

arr

0	1	1	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9

j ↑ i ↑

$j=1$

$i=3$

$$arr[i] == arr[j]$$

$$1 == 1$$

↓
 $i++$

$i_{format}: 4$

arr

0	1	1	1	1	1	2	2	3	3
0	1	2	3	4	5	6	7	8	9

j ↑ i ↑

$j=1$

$i=4$

$$arr[i] == arr[j]$$

$$1 == 1$$

↓
 $i++$

$i_{format}: 5$

arr

0	1	1	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9

j ↑ i ↑

$j=1$

$i=5$

$$arr[i] == arr[j]$$

$$2 == 1$$

$j = 1$
 $i = 5$

$\leftarrow \begin{matrix} arr[1] & 1 \\ 2 & 1 \end{matrix} = arr[1]$
 $j++$
 $arr[j] = arr[i]$
 $i++$

format: 6

arr

0	1	2	1	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9	

$\uparrow j$ $\downarrow i$

$j = 2$
 $i = 6$

$\leftarrow \begin{matrix} arr[6] & 2 \\ 2 & 2 \end{matrix} = arr[2]$
 $i++$

format: 7

arr

0	1	2	1	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9	

$\uparrow j$ $\uparrow i$

$j = 2$
 $i = 7$

$\leftarrow \begin{matrix} arr[7] & 3 \\ 3 & 2 \end{matrix} = arr[2]$
 $j++$
 $arr[2] = arr[i]$
 $i++$

format: 8

arr

0	1	2	3	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9	

$\uparrow j$ $\uparrow i$

$j = 3$
 $i = 8$

$\leftarrow \begin{matrix} arr[8] & 3 \\ 3 & 3 \end{matrix} = arr[3]$
 $i++$

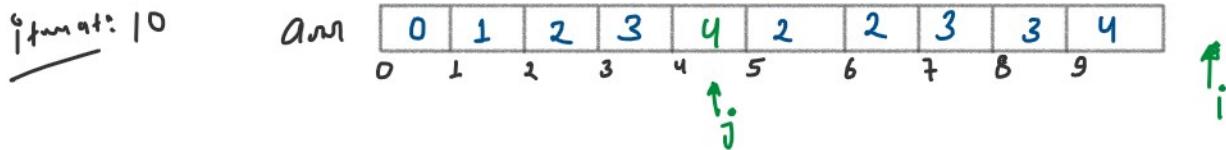
format: 9

arr

0	1	2	3	1	1	2	2	3	3	4
0	1	2	3	4	5	6	7	8	9	

$\uparrow j$ $\uparrow i$

$j = 3$
 $i = 9$
 $arr[i] = arr[j]$
 $4 = 3$
 $j++$
 $arr[j] = arr[i]$
 $3 = 3$
 $i++$



$j = 4$
 $i = 10$
 $N = 10$
 $i = 10$

$\left. \begin{array}{l} \\ \end{array} \right\} R \cup K \quad j_{900} \dots (i < N)$

return $(j+1)$
 $K = j+1$

```

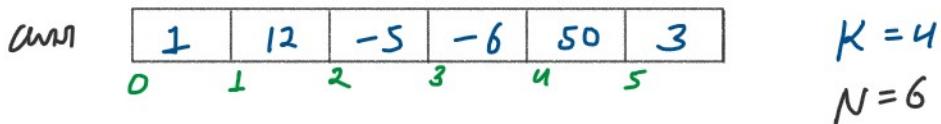
● ● ●
// HW 11: Remove Duplicates From Sorted Array (Leetcode-26)
class Solution {
public:
    int removeDuplicates(vector<int>& nums) {
        int N=nums.size();
        int j=0; // j is a unique element's position
        int i=1;
        while(i<N){
            if(nums[i]==nums[j]){
                i++;
            }else{
                nums[++j]=nums[i++];
            }
        }
        return j+1;
    }
};

Time Complexity: O(N), Where N is size of array
Space Complexity: O(1)
*/
/*
Example 1:
Input: nums = [1,1,1,2]
Output: 2, nums = [1,2,...]
Explanation: Your function should return k = 2, with the first two elements of nums being 1 and 2 respectively.
It does not matter what you leave beyond the returned k (hence they are underscores).

Example 2:
Input: nums = [0,0,1,1,1,2,2,3,3,4]
Output: 5, nums = [0,1,2,3,4,...]
Explanation: Your function should return k = 5, with the first five elements of nums being 0, 1, 2, 3, and 4 respectively.
It does not matter what you leave beyond the returned k (hence they are underscores).
*/

```

12. Maximum Average Subarray 1 (Leetcode-643)



METHOD: 1

Brute Force Approach:

- Step 01: find all sub arrays sum of Length K
- Step 02: find maximum average from sub arrays

Step:01

$i=0$	$j=3$	$\Rightarrow \text{maxSum} = 1 + 12 + (-5) + (-6)$
		$= 2$
$i=1$	$j=4$	$\Rightarrow \text{maxSum} = 12 + (-5) + (-6) + 50$
		$= 51$
$i=2$	$j=5$	$\Rightarrow \text{maxSum} = (-5) + (-6) + 50 + 3$
		$= 42$
$i=3$	$j=6$	$\text{RUK jaago... } (j < N) \text{ END}$

Step:02

$$\text{MaxAvg} = \frac{\text{MaxSum}}{K} = \frac{51}{4} \Rightarrow 12.75 \text{ output}$$

```

● ● ●

// Method 01: Brute force solution
class Solution {
public:
    double findMaxAverage(vector<int>& nums, int k) {
        int N = nums.size();
        int maxSum = INT_MIN;
        int i = 0, j=k-1;

        while(j < N){
            int sum = 0;
            for(int x=i;x<=j;x++){
                sum = sum + nums[x];
            }
            maxSum = max(maxSum, sum);
            j++, i++;
        }

        // Find maximum average of maximum sum
        double maxAvg = maxSum/(double)k;
        return maxAvg;
    }
};

/*
Time Complexity: O(N^2), Where N is size of array
Space Complexity: O(1)
*/

```

Arr

1	12	-5	-6	50	3
0	1	2	3	4	5

$K = 4$
 $N = 6$

METHOD: 1

Optimal Solution: Sliding Window Approach

Step 01: sum of first window

Step 02: first window ke first element ko subtract kardo and next new element ko add krdo with sum of first window me

Window: 1

window: 1					
1	12	-5	-6	50	3
0	1	2	3	4	5

$\text{sum} = 2$

window: 2					
1	12	-5	-6	50	3
0	1	2	3	4	5

$\text{sum} = 51$

window: 3					
1	12	-5	-6	50	3
0	1	2	3	4	5

$\text{sum} = 42$

$\text{sum} = \text{sum} - 12 + 3$
 $= 51 - 12 + 3$
 $= 42$

$\text{sum} = \text{sum} - 1 + 50$

$i=0$
 $j=K-1$

$j=k-1$

$$\begin{aligned}
 & \text{sum} = 2 \\
 & \text{sum} = 2 + 12 + (-5) + (-6) \\
 & = 2 + 12 + (-5) + (-6) \\
 & = 2
 \end{aligned}$$

$$\begin{aligned}
 & \text{sum} = \text{sum} - 1 + 50 \\
 & = 2 - 1 + 50 \\
 & = 51
 \end{aligned}$$

GENERAL FORMULA

Step- ① $\text{sum} = 2$

Step- ② $\text{sum} = \text{sum} - \text{arr}[i]$
 $i++$ and $j++$

$$\text{sum} = \text{sum} + \text{arr}[j]$$

```

● ● ●
// Optimal Solution: Sliding Window Approach
class Solution {
public:
    double findMaxAverage(vector<int>& nums, int k) {
        int N = nums.size();
        int i = 0, j=k-1;

        int sum = 0;
        // Step 01: Find sum of first window
        for(int x=i;x<=j;x++){
            sum = sum + nums[x];
        }

        int maxSum = sum;
        // Step 02: Find maxSum
        // Me pahle hi check kar loonga ki j out of bound to nahi ho raha hai
        j++; // pahle aap j ko use karlo uske baad increment by one kardo
        while(j<N){
            sum = sum - nums[i++];
            sum = sum + nums[j++];
            maxSum = max(maxSum, sum);
        }

        // Find maximum average of maximum sum
        double maxAvg = maxSum/(double)k;
        return maxAvg;
    }
};

/*
Time Complexity: O(N), Where N is size of array
Space Complexity: O(1)
*/
/*
Example 1:
Input: nums = [1,12,-5,-6,50,3], k = 4
Output: 12.75000 26.50000
Explanation: Maximum average is (12 + 5 + 6 + 50) / 4 = 51 / 4 = 12.75

Example 2:
Input: nums = [5], k = 1
Output: 5.00000

Example 3:
Input: nums = [1,12,-5,-6,50,3], k = 2
Output: 26.50000
*/

```

13. Find Pivot Index with prefix sum approach (Leetcode-724)

Example 1:

Input: $\text{nums} = [1, 7, 3, 6, 5, 6]$

Output: 3

Explanation:

The pivot index is 3.

Left sum = $\text{nums}[0] + \text{nums}[1] + \text{nums}[2] = 1 + 7 + 3 = 11$

Right sum = $\text{nums}[4] + \text{nums}[5] = 5 + 6 = 11$

Example 2:

Input: $\text{nums} = [1, 2, 3]$

Output: -1

Explanation:

There is no index that satisfies the conditions in the problem statement.

Ex: 01

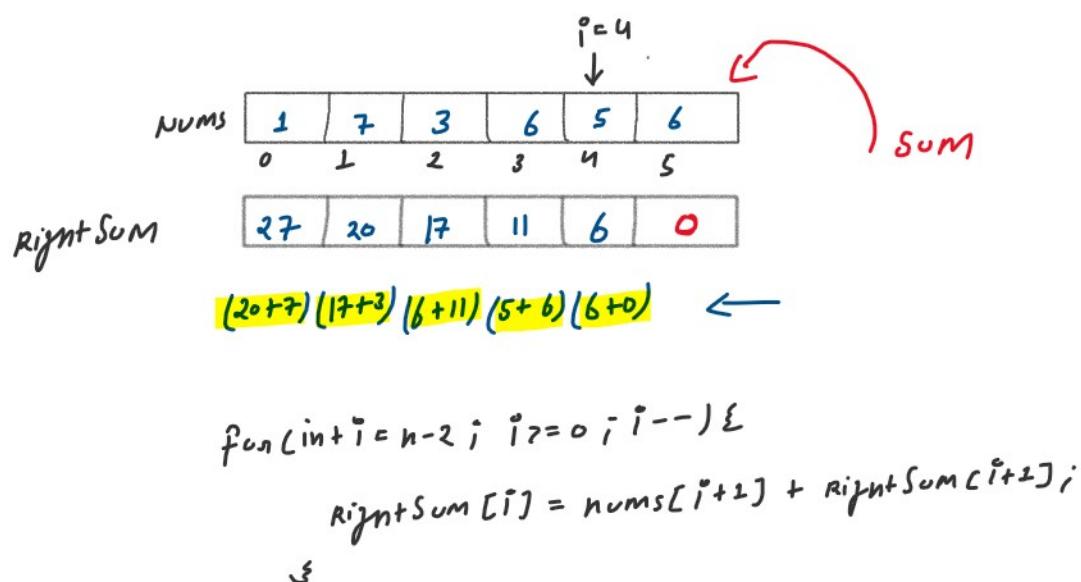
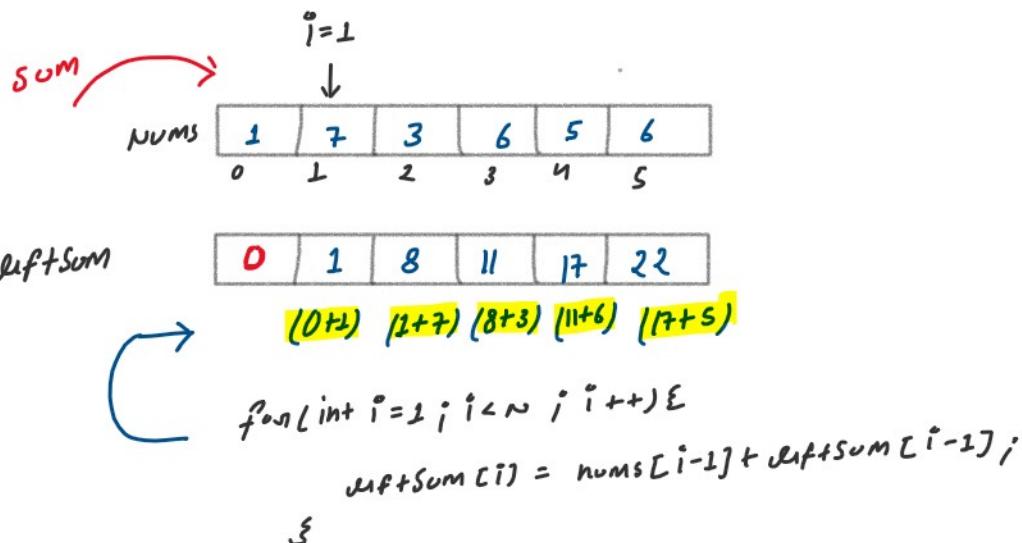
APPROACH PSEUDO CODE:

Ex: 01

APPROACH PSEUDO CODE:

- Step 01: create two vector rightSum and leftSum to prefix sum
- Step 02: iterate nums till rightSum[i]==leftSum[i]
- Step 03: return the index which terminate the loop

STEP 01



STEP 02

rightSum

27	20	17	11	6	0
0	1	2	3	4	5

leftSum

0	1	8	11	17	22
0	1	2	3	4	5

pivot Index at index 3
 ↗ return Index

Pivot Index

```

// Find Pivot Index with prefix sum approach (Leetcode-724)
class Solution {
public:
    int prefixSum(vector<int>& nums){
        int n=nums.size();
        vector<int> rightSum(n,0);
        vector<int> leftSum(n,0);

        // leftSum
        for(int i=1;i<n;i++){
            leftSum[i] = nums[i-1] + leftSum[i-1];
        }

        // rightSum
        for(int i=n-2;i>=0;i--){
            rightSum[i] = nums[i+1] + rightSum[i+1];
        }

        // Compare rightSum and leftSum to find pivot
        for(int i=0;i<n;i++){
            if(leftSum[i]==rightSum[i]){
                return i;
            }
        }
        return -1;
    }

    // Find Pivot Index
    int pivotIndex(vector<int>& nums) {
        int ans1 = prefixSum(nums);
        return ans1;
    }
};

/*
TIME COMPLEXITY: O(N), Where N is length of nums
SPACE COMPLEXITY: O(N), Where N is length of rightSum and leftSum
*/
/*
Example 1:
Input: nums = [1,7,3,6,5,6]
Output: 3
Explanation:
The pivot index is 3.
Left sum = nums[0] + nums[1] + nums[2] = 1 + 7 + 3 = 11
Right sum = nums[4] + nums[5] = 5 + 6 = 11

Example 2:
Input: nums = [1,2,3]
Output: -1
Explanation:
There is no index that satisfies the conditions in the problem statement.
*/

```

14. Missing Number (Leetcode-268)

Input	$\left\{ \begin{array}{c} \text{nums} \\ \hline 0 & 1 & 7 & 2 & 3 & 2 & 5 & 6 & 0 \end{array} \right.$ Given Range $[0, 7]$	$N = 7$
Output	$\left\{ \text{missing number} = 1 \right.$	

Approach: 1

Step:01 Sum of Num = 24
 Step:02 Sum of Range = $n * (\frac{n+1}{2}) = 28$

Approach: 1

Step:01 sum of nums = 24
 Step:02 sum of range = $n * (\frac{n+1}{2}) = 28$
 Step:03 missing no = step2 - step1 = $28 - 24 = 4$
O/P

```
/*
Approach 01:
Step 01: Sum of nums
Step 02: Sum of range [0,N]
Step 03: Find missingNum = Step2 - Step1

Time Complexity: O(N), where N is length of nums
Space Complexity: O(1), no extra space used
*/
int totalSum(vector<int>& nums){
    int n=nums.size();

    // Step 01: Sum of nums
    int sum = 0;
    for(int i=0;i<n;i++){
        sum+=nums[i];
    }

    // Step 02: Sum of range [0,N]
    int totalSum=(n*(n+1))/2;

    // Step 03: Find missingNum = Step2 - Step1
    int missingNum=totalSum-sum;

    return missingNum;
}
```

Approach: 02 XOR

Input { nums

0	1	7	2	3	3	4	5	6	0
---	---	---	---	---	---	---	---	---	---

 Given Range [0, 7] N=7

Output { missing number = 11

{ Approach 02:
 Step 01: XOR all nums[i] values
 Step 02: XOR all range items
 Step 03: return remaining range items }

$$\begin{aligned} A \wedge 0 &= A \\ A \wedge A &= 0 \end{aligned}$$

Rules.

Step:01 $A \wedge 0 \Rightarrow 0 \wedge 1 \wedge 7 \wedge 2 \wedge 3 \wedge 3 \wedge 4 \wedge 5 \wedge 6 \wedge 0$
Step:02 $A \wedge 1 \Rightarrow 0 \wedge 1 \wedge 2 \wedge 3 \wedge 4 \wedge 5 \wedge 6 \wedge 1$
 $\Rightarrow 0 \wedge 4$
 $\Rightarrow 4$ O/P

```
/*
Approach 02:
```

\Rightarrow **U** \rightarrow O/P

```

/*
Approach 02:
Step 01: XOR all nums[i] values
Step 02: XOR all range items
Step 03: return remaining range items

Time Complexity: O(N), where N is length of nums
Space Complexity: O(1), no extra space used
*/
int xorApproach(vector<int>& nums){
    int n=nums.size();
    int ans = 0;

    // Step 01: XOR all nums[i] values
    for(int i=0; i<n; i++){
        ans = ans ^ nums[i];
    }

    // Step 02: XOR all range items
    for(int i=0; i<=n; i++){
        ans = ans ^ i;
    }

    // Step 03: return remaining range items
    return ans;
}

```

Approach 03 **SORTING**

Input	{	nums	0 1 7 2 3 3 2 5 6 6 0	
		given Range	[0, 7]	$N=7$

Output { missing number = i

Approach 03:
 Step 01: Sorting nums
 Step 02: Compare nums[i] with indeces
 Step 03: Return not matched index or nums size

STEP:01

SORT

0	1	2	3	3	5	6	7
0	1	2	3	4	5	6	7

STEP:02

$i=0$

n

$num[i] == i$

$0 == 0$

Step-01 $i=0$ $\text{num}[i] == 1$

0	$0 == 0$
	$i++$

1 $1 == 1$

2	$2 == 2$
	$i++$

3 $3 == 3$

4	$5 == 4$
	Run loop \rightarrow Out

5 $i++$

Output = 4

Return 4 index

Ex: 2

nums

0	1
0	1

$N = 2$

Range $\in [0, 2]$

missing NO = 2

Step: 01

0	1
0	1

Step: 02

$i=0$ $\text{num}[i] == i$

0	$0 == 0$
	$i++$

1 $1 == 1$

2	i
	$i++$

outside of

loop

To Ans Kya Hoga?

Return $\text{nums.size}() = 2$

```
/*
Approach 03:
Step 01: Sorting nums
Step 02: Compare nums[i] with indeces
Step 03: Return not matched index or nums size in the case of example [0,1] missing num=2

Time Complexity: O(NlogN), where N is length of nums
Space Complexity: O(1), no extra space used
*/
int sortingApproach(vector<int>& nums){
    int n=nums.size();

    // Step 01: Sorting nums
    sort(nums.begin(), nums.end());

    // Step 02: Compare nums[i] with indeces
    for(int i=0;i<n;i++){
        if(nums[i]==i){
            continue;
        }
        else{
            // Step 03: Return not matched index
            return i;
        }
    }
}
```

```
        else
            // Step 03: Return not matched index
            return i;
    }
}

// Step 03: Return numsSize N when all index matched with nums[i]
return n;
```