

Stack

Q what is Stack?

→ Stack is a data structure which follow last in first out rule, it store memory in homogeneous form.

Stack Question

- 1) Nearest greater element to left
- 2) Nearest greater element to right
- 3) Nearest smaller element to left.
- 4) Nearest smaller element to right
- 5) Stack span problem
- 6) Maximum area of Histogram
- 7) Max area of rectangle in binary search
- 8) Rain trapping
- 9) Implementing a min stack
- 10) Implementing stack using heap
- 11) The celebrity problem
- 12) Longest valid Parenthesis
- 13) Interactive Tati (# Tower of Hanoi)

How to identify stack question?

I) Array / Heap → Most probability stack question

II) Brute force → n^2

Note

if there are two loops present in the array and the second loop is dependent on i so in that condition we can use stack

$j \rightarrow 0 \text{ to } i$
 $j \rightarrow i \text{ to } n$
 $j \rightarrow i \text{ to } n$
 $j \rightarrow n \text{ to } i$

} in this scenario we can use stack.

Question 1

Nearest greater element to right \Rightarrow Next largest elem

input \rightarrow [1, 3, 2, 5, 4]
↓
[3 5 5 -1 -1]

input \rightarrow 1 3 0 0 1 4

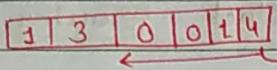
[3 4 2 1 4 -1] \rightarrow op

Borut force

```
int ans[] = new int[n]
for (int i=0; i<n; i++)
    flag = true;
    for (int j=j+1; j<n; j++)
        if (arr[i] < arr[j])
            ans[i] = arr[j];
            flag = false;
    }
    if (flag)
        ans[i] = -1;
```

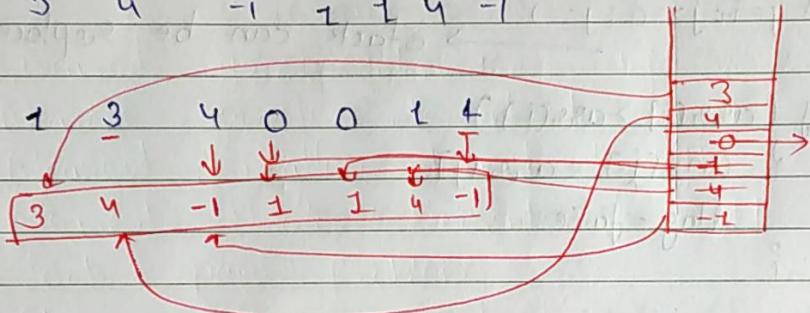
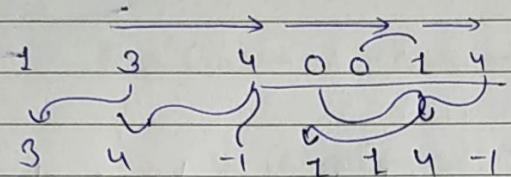
} this can be changed into stack

Note → if our dependent loop is in i to $n-1$ and at that time we will travel in $n-1$ to i



Brute force

stack approach direction



int next_greater_to_right (int arr[])

{

stack <Integer> st = new stack <Integer>();

int [] ans = new int [arr.length];

for (int i = arr.length - 1; i >= 0; i--)

{ if (st.isEmpty())

{ ans[i] = -1; }

if (st.isEmpty() || st.peek() > arr[i])

{

ans[i] = st.peek();

}

else if (!st.isEmpty() && st.peek() <= arr[i])

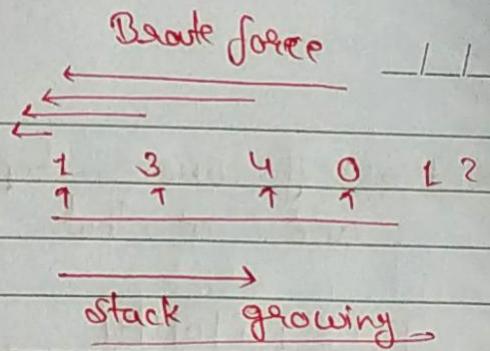
{

st.pop();

if (st.isEmpty()) { ans[i] = -1; }

else { ans[i] = st.peek(); }

} st.push(arr[i]); DOMS



Next greater to left

$\boxed{1 \ 3 \ 4 \ 0 \ 1 \ 2}$

$\rightarrow [-1 \ -1 \ -1 \ 4 \ 4 \ 4]$

Brute force

$ans[0] = -1;$

for (int i=0; i<n; i++)

 for (int j=i+1; j>=0; j--)

 → stack can be replaced

 if ($arr[j] > arr[i]$)

$ans[j] = arr[j]$

 flag = false;

 ?

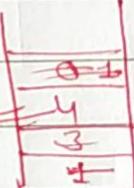
?

 if (flag) $\{ ans[i] = -1; \}$

?

This Problem is similar to Next greater element but the loop flow will be opposite

1 3 4 0 1 2
 ↓ ↓ ↓ ↓ ↓ ↓
 -1 -1 -1 4 4 4



↑

Next - greater element to left

void int [] nextGreaterLeft (int [] arr) {

int [] ans = new int [arr.length];

Stack <Integer> st = new Stack <Integer>();

for (int i=0; i<arr.length; i++)

{

if (st.isEmpty())

{ ans[i] = -1; }

else if (!st.isEmpty() && st.peek() > arr[i])

{

ans[i] = st.peek();

}

else if (!st.isEmpty() && st.peek() <= arr[i])

{

while (!st.isEmpty() && st.peek() <= arr[i])

{ st.pop(); }

if (!st.isEmpty())

{ ans[i] = -1; }

else

{ ans[i] = st.peek(); }

}

st.push(arr[i]); // Pushing the current element

{

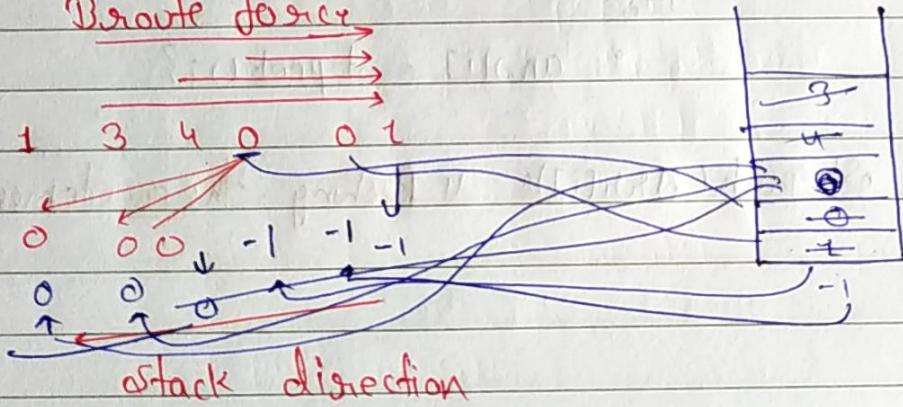
Next smaller element to Right

input \rightarrow 1, 3, 4, 0, 0, 1

Brute force

```
for (int i=0; i<arr.length; i++)  
{ flag = true;  
    for (int j = i+1; j<arr.length; j++)  
        if (arr[j] < arr[i])  
            { ans[i] = arr[j];  
                flag = false;  
            }  
        if (flag)  
            ans[i] = -1;  
}
```

Brute force



final code for next smaller to right

```
int [] arr & nextSmaller (int [] arr)
{
    int [] ans = new int [arr.length];
    stack<Integer> st = new stack<Integer>();
    for (int i = n-1; i >= 0; i++)
    {
        if (st.isEmpty())
            ans[i] = -1;
        else if (!st.isEmpty() && st.peek() < arr[i])
            ans[i] = st.peek();
        else if (!st.isEmpty() && st.peek() >= arr[i])
        {
            while (!st.isEmpty() && st.peek() >= arr[i])
                st.pop();
            if (st.isEmpty())
                ans[i] = -1;
            else
                ans[i] = st.peek();
        }
        st.push(arr[i]);
    }
    return ans;
}
```

Next smaller to left

Note → this question is exactly same as Next smaller to right only loop flow will be opposite

Final code for next smaller to left

```
int [] next_smaller_to_left (int [] arr)
```

```
{
```

```
int [] ans = new int [arr.length];
```

```
Stack<Integer> st = new Stack<Integer>();
```

```
for (int i=0; i<arr.length; i++)
```

```
if (st.isEmpty())
```

```
{ ans[i] = -1; }
```

```
else if (!st.isEmpty() && st.peek() < arr[i])
```

```
{ ans[i] = st.peek(); }
```

```
else if (!st.isEmpty() && st.peek() >= arr[i])
```

```
{ while (!st.isEmpty() && st.peek() >= arr[i])
    { st.pop(); }
```

```
if (st.isEmpty())
```

```
{ ans[i] = -1; }
```

```
else
```

```
{ ans[i] = st.peek(); }
```

```
?
```

```
st.push(arr[i]);
```

```
?
```

```
return ans;
```

```
?
```

Stock Span Problem

→ 100, 80, 60, 70, 60, 75, 85
 ↓ ↓ ↓ ↓ ↓ ↓
 1 2 3 4 5 6

next greater smaller left

60
80
100

- - - 80 70 80 100
 -1 100 80 80 -1 80 100

-1
 -1 -1

(4)

we need to store index of NGIL element so that we can find our ans

```

int ans[] = new int [length+1];
Stack<Integer> st = new Stack<Integer>();
for (int i=0; i<arr.length; i++) {
    if (st.isEmpty())
        ans[i] = -1;
    else if (!st.isEmpty() && arr[st.peek()] > arr[i])
        ans[i] = st.peek();
    else if (!st.isEmpty() && ans[st.peek()] <= arr[i])
        while (!st.isEmpty() && ans[st.peek()] <= arr[i])
            st.pop();
        if (st.isEmpty())
            ans[i] = -1;
        else
            ans[i] = st.peek();
    st.push(i);
}
  
```

when we have index of NGL after that we need a simple loop to small calculation

```
for (int i=0; kn; i++)  
    ans[i] = i - ans[i];?
```

↓
this will store our ans.

final code for stock span problem

```
int [] stockSpan (int []arr)  
{  
    //finding Nearest greater to left index  
  
    int [] ans = new int [arr.length];  
    Stack <Int> st = new Stack <Int>();  
  
    for (int i=0; i<arr.length; i++)  
    {  
        if (st.isEmpty())  
            ans[i] = -1;  
        else if (!st.isEmpty() && arr[st.peek()] < arr[i])  
            ans[i] = st.peek();  
        else if (!st.isEmpty() && arr[st.peek()] >= arr[i])  
            {  
                while (!st.isEmpty() && arr[st.peek()] <= arr[i])  
                    st.pop();  
                if (st.isEmpty())  
                    ans[i] = -1;  
                else  
                    ans[i] = st.peek();  
            }  
        st.push(i);  
    }
```

```

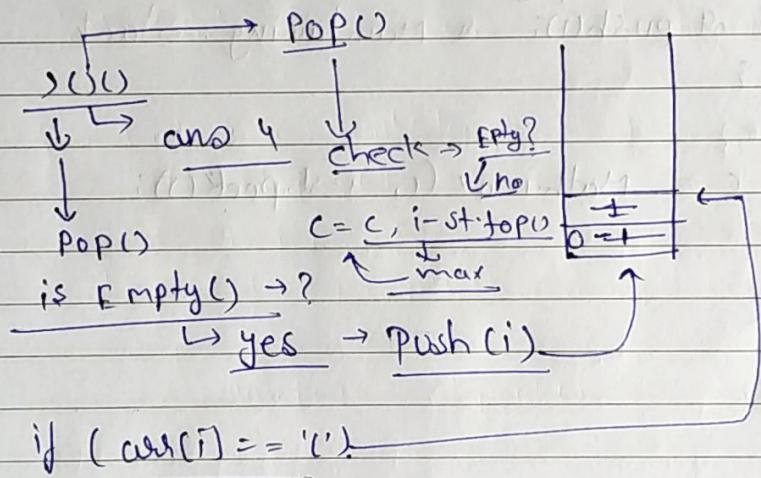
for (int i = 0; i < arr.length; i++) {
    if arr[i] == '('
        arr[i] = i - temp;
}

```

between and;

Longest Valid Parenthesis

in this question we will maintain a stack of containing index of opening bracket and the last index || Bottom position of stack will contain a invalid index, or -1 ↳ which is not valid



Note

- stack k bottom ko ek invalid index se maintain krega
- initially → -1
- is kisi condition m stack empty ho jata hai which means ki vo ek valid parenthesis hai, that's why stack maintaining kene k rkiye
- PUSH(i)

Final code for Longest Parenthesis :-

```
int longestPara (int strng str)
{
    Stack<Integer> st = new Stack<Integer>();
    int c=0;
    for (int i=0; i<str.length(); i++)
    {
        if (str.charAt(i) == '(')
            st.push(i); // maintaining stack
        else
            st.pop(); // removing opening bracket
        if (st.isEmpty())
            st.push(i); // maintaining stack
        else
            c = Math.max(c, i-st.peek()); // calculating max
    }
    return c;
}
```

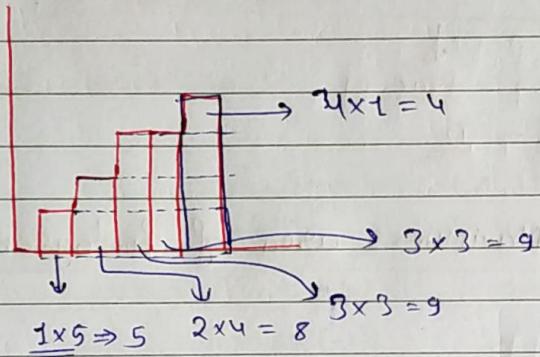
Maximum Area Histogram

input → n number of building and array height[] which represent the height of each building

op: → Maximum area of rectangle.

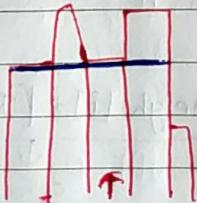
$n \Rightarrow 5$

height → 1, 2, 3, 3, 4



Maximum area of histogram
→ 9 And

Note → A building can be extended when the height of the other building is \geq current build



Here we need to find of out nearest smaller to left, nearest smaller to right [# indexed]

	0	1	2	3	4	5	6
arr →	6	2	5	4	5	1	6

Right [NSR index] 1 5 3 5 5 +7 +7

left [NSL index] -1 -1 1 1 3 -1 5
 $\frac{(-1)-(-1)}{(1-(-1)-1)} \frac{(5+1-1)}{(5+1-1)} \frac{3-1-1}{5-3-1} \frac{5-3-1}{7-5-1}$
 $\frac{-1+1}{7-5+1}$
 $\frac{7-5+1}{7-5-1}$

$b \Rightarrow R[i+1] \Rightarrow$ 1 5 1 3 1 7 1
 $\times 6 \quad \times 2 \quad \times 5 \quad \times 4 \quad \times 5 \quad \times 1 \quad \times 6$

$$\text{ans} = 12$$

steps for solving Maximum area of histogram ↗

1) Find of Nearest smaller to Right index

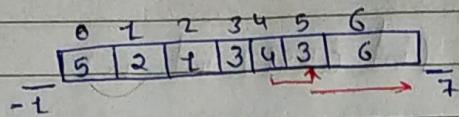
2) find of the nearest smaller to left index

3) iterate loop 0 to n.

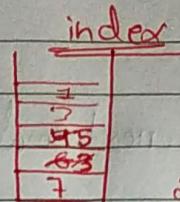
4) maximum value of $\frac{\text{height}[i] * [R[i] - L[i] - 1]}{\downarrow \text{area}}$

5) return max

NSR



1 2 7 7 3 7 7



st.push(n)

while ($i > 0$)

 | while ($st.peek() \neq n$)

 68 arr[st.pop()] =

NSL

-1 -1 -1 2 3 2 5

Final code

class Solution {

```

int[] next_smaller_left_idx (int []arr, int n)
{
    int left[] = new int[n];
    stack<Integer> st = new stack<Integer>();
    st.push(-1); // base condition

    int i=0;
    while (i < n)
    {
        while (st.peek() != -1 && arr[st.peek()] > arr[i])
            st.pop();

        left[i] = st.peek();
        st.push(i);
        i++;
    }
    return left;
}

```

}

```
int [] next_smaller_Right_index (int arr[], int n)
```

```
{
```

```
    int [] right = new int [n];
```

```
    Stack<Integer> st = new Stack<Integer>();
```

```
    st.push(n);
```

```
    int i = n-1;
```

```
    while (i >= 0)
```

```
        while (st.peek() != n && st.size(st.peek()) > arr[i])
```

```
            st.pop();
```

```
        right[i] = st.peek();
```

```
        st.push(i);
```

```
        i--;
```

```
}
```

```
    return right;
```

```
}
```

```
int Max_Area_Histogram (int []arr, int n) {
```

```
{
```

```
    int [] R = next_smaller_Right_index (arr, n);
```

```
    int [] L = next_smaller_left_index (arr, n);
```

```
    int max = Integer.MIN_VALUE;
```

```
    for (int i=0; i < n; i++)
```

```
        int h = arr[i];
```

```
        int b = R[i]-L[i]-1;
```

```
        max = Math.max (max, h*b);
```

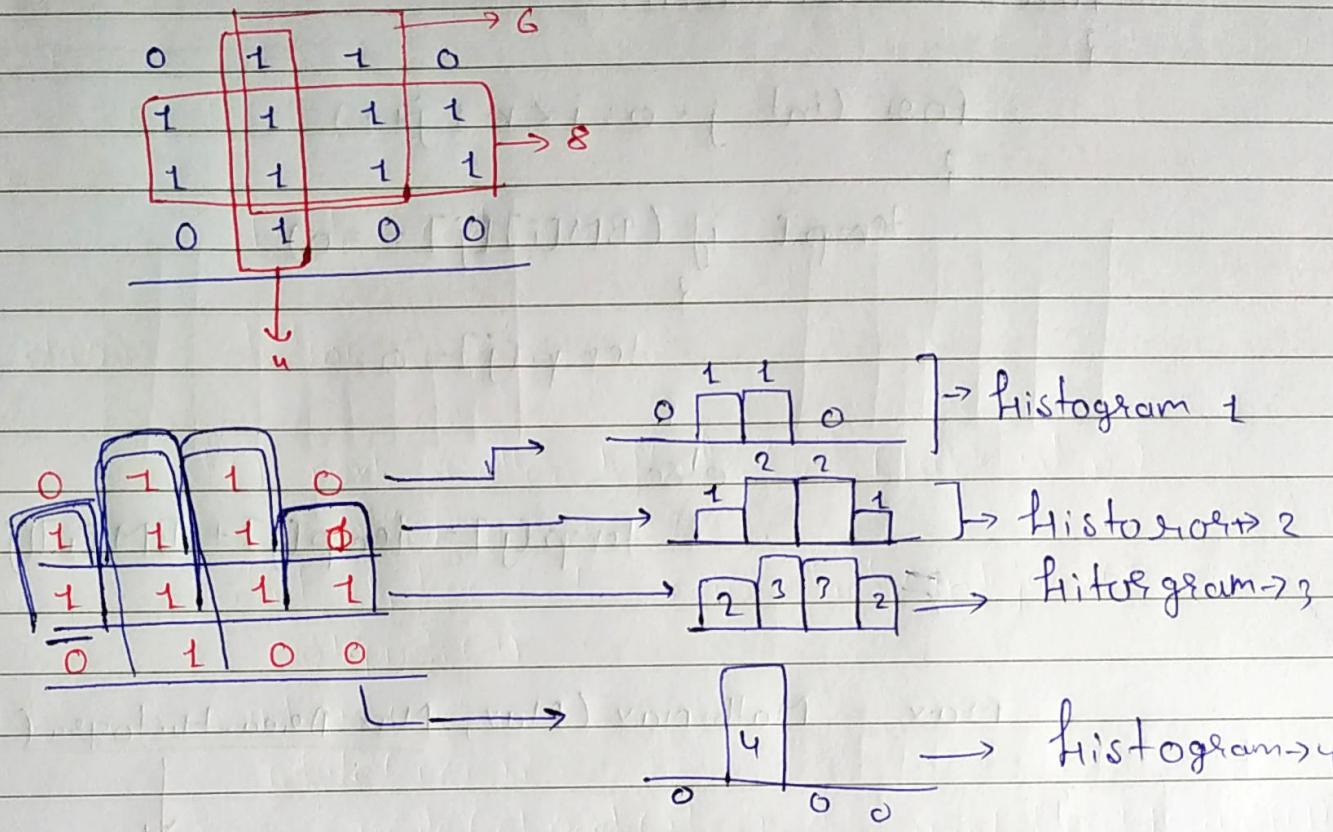
```
}
```

```
return max;
```

```
?
```

Maximum area rectangle in binary Matrix

You are given an binary matrix you need to find out the maximum area rectangle which can be formed with 1.

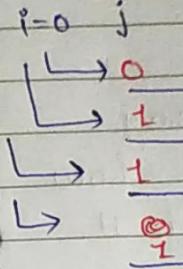


$$\text{ans} \Rightarrow \text{Max} \left(\begin{array}{c} \text{Max-Area Histogram}(1) \\ \text{--- --- --- (2)} \\ \text{--- --- - (3)} \\ \text{--- --- - (4)} \end{array} \right)$$

```

int max_area_of_BM (int BM [][], int n)
{
    int Max = Integer.MIN_VALUE;
    int temp [] = new int [n];
    for (int i = 0; i < n; i++)
    {
        for (int j = 0; j < n; j++)
        {
            if (BM[i][j] == 0)
                temp[j] = 0;
            else
                temp[j] = temp[j] + BM[i][j];
        }
        Max = Math.max (Max, Max_Area_Histogram (temp, n));
    }
}

```



function calling for
getting Max area
histogram
Solve in previous
question

Dry Run

i=0 j

\hookrightarrow	0	1	1	0
\hookrightarrow	1	1	1	1
\hookrightarrow	1	1	1	1
\hookrightarrow	0	0	0	0

temp \rightarrow [0 1 1 0] \rightarrow MAH(temp)

=> 2

temp \rightarrow [1, 2, 2, 1] \rightarrow MAH(temp)

=> 4

[2, 3, 3, 2] \rightarrow MAH(temp)

=> 8

[3, 4, 0, 0] \rightarrow MAH(temp)

=> 6

code

int MaxArea(int arr[][] arr, int n)

{ int ans = Integer.MIN_VALUE; int temp[] = new int[n];

for (int i=0; i<n; i++)

{

for (int j=0; j<n; j++)

{

if (arr[i][j] == 0)

 temp[j] = 0; ?

else

 temp[j] = temp[j] + arr[i][j]; ?

?

ans = Math.max (max, MaxAreaHistogram (temp, n))

?
return ans;

?

maximum

↓

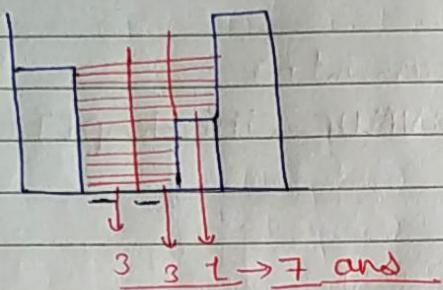
8 Ans

Steps

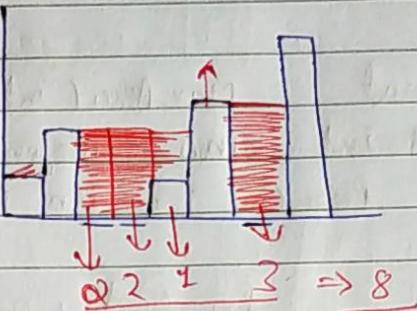
→ here each

In this Problem we are given an array which represent we need to find out how much water will going to be stored in it.

3, 0, 0, 2, 4



1 2 0 0 1 3 0 4



$$\begin{array}{r} 2 \\ \oplus \\ 3 \\ \hline 2 - 3 = -1 \end{array}$$

1	2	0	0	1	3	0	4
---	---	---	---	---	---	---	---

above water in this building

$$\text{temp} = \min(\underline{\text{MaxLeft}}, \underline{\text{MaxRight}}) - \text{height}[i]$$

if (temp < 0)

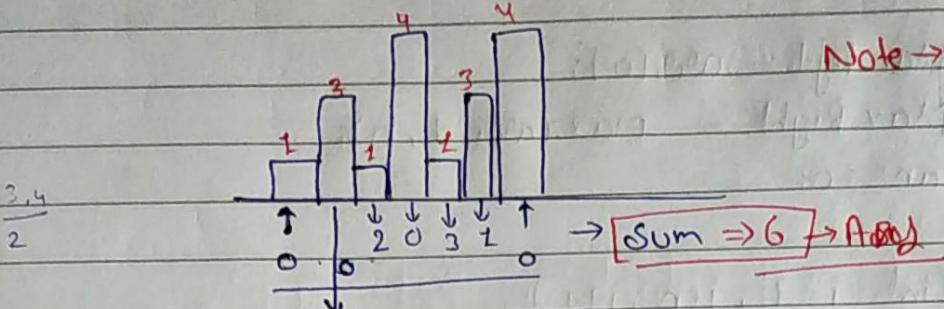
$$\text{temp} = 0$$

ans += temp;

Note

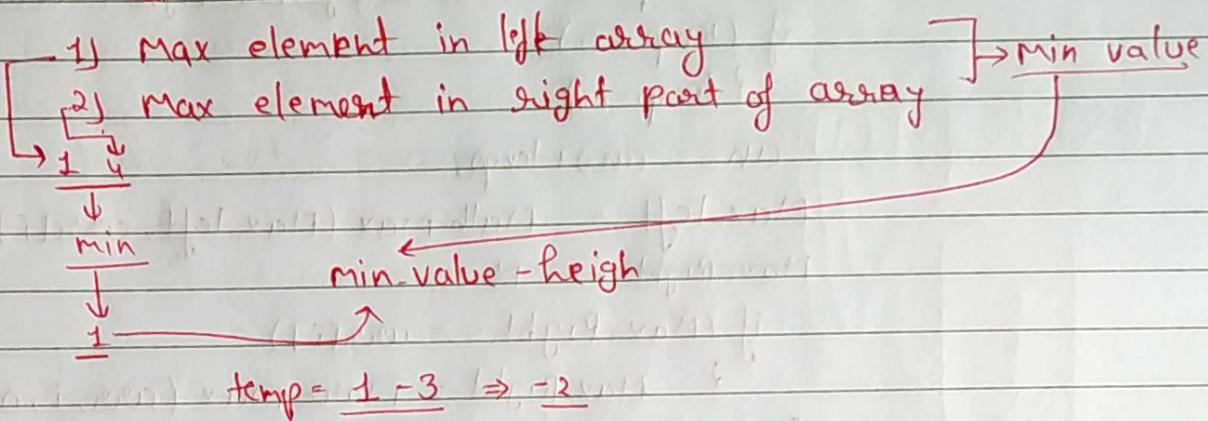
Steps

→ here we need to find out water unit on each building



Note → first and last building have zero water unit

Yha par find out krene k liye Do chize required hai



condition if ($temp < 0$)
temp = 0

Note → we need to find out Max element in right part of array, and Max element of left Part of array

→ then other Part going to solve from a min calculation

$$\text{Min}(\text{Max_left}, \text{Max_Right}) - h[i] \Rightarrow \underline{\underline{\text{temp}}}$$

Code

```
int Rain-trapping ( int [] arr, int n )  
{  
    int Max-left = arr[0];  
    int Max-Right = max (arr, 1, n);  
    int ans = 0;  
  
    for (int i=1; i<n; i++)  
    {  
        int temp = min (Max-left, Max-Right) - arr[i];  
        if (temp < 0)  
            temp = 0;  
        ans = ans + temp;  
        Max-left = Math.max (Max-left, arr[i]);  
        Max-Right = Math.min (Max-Right, arr[i]);  
        if (Max-Right == arr[i])  
            Max-Right = max max (arr, i, n);  
    }  
}
```

return ans;

you
out
param

Step

String Parenthesis checker

you are given a string, you need to find out whether the given string is having valid parenthesis or not.

String \rightarrow "{(())?}" $\xrightarrow{\text{true}}$ this is a valid string

"{(())" \rightarrow this is an invalid

use stack

\rightarrow if you get opening bracket

\rightarrow Push

\rightarrow if closing bracket

\rightarrow check if top of stack is having minimum no corresponding open bracket

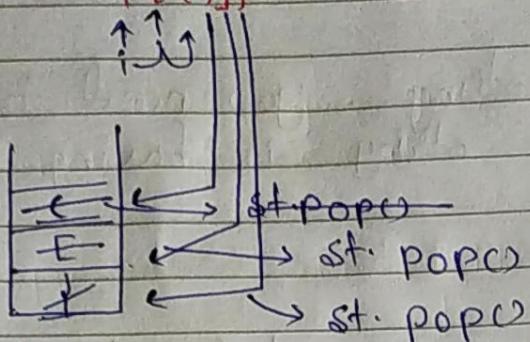
\rightarrow if yes

\rightarrow [st.pop]

\rightarrow false

\rightarrow return false

str → " { [()] } "



after loop

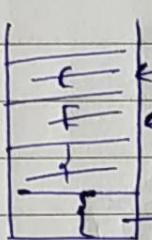
if (!st.isEmpty())

{ return false; } // if stack is not empty
which are some invalid
opening bracket

return true;

str → " { { [()] } }

↑↑↑



This character [opening bracket is occurring in invalid condition]
that's why

return false;

Note :- there can be three types of bracket

"{", ")", "("

→ considered as opening

"}", "}", ")" → considered as closing

Final code for star Parenthesis checking

class Solution {

```
    is Boolean is_Valid_Parenthesis( String str )  
    {  
        character character  
        stack<Integer> st = new stack<Integer>();  
  
        for (int i=0 ; i<str.length() ; i++)  
        {  
            char t = st.charAt(i);  
  
            if (t == '[' || t == '{' || t == '(') // for opening bracket  
                st.push(t);  
            else  
                if (st.isEmpty()) return false;  
                else  
                    if (t == ')' && st.pop() != '(')  
                        return false;  
                    else if (t == '}' && st.pop() != '{')  
                        return false;  
                    else if (t == ']' && st.pop() != '[')  
                        return false;  
        }  
        if (!st.isEmpty()) return false;  
        else return true;  
    }
```

Some invalid
Brackets

```
if (t == ')' && st.pop() != '(') return false;  
else if (t == '}' && st.pop() != '{') return false;  
else if (t == ']' && st.pop() != '[') return false;
```

if (!st.isEmpty())

return false;

extra opening bracket
return false.

Decode the string

You are given a string you need to decode it.

Input → "3[b2[ca]]"

↓
3 [bcaca]

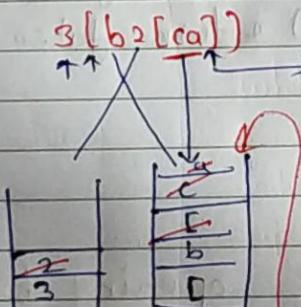
Output → bcaca bcaca bcaca

For solving this problem we need to store manage two stacks

- Integer array
- character array

3 [b2[ca]]
Integer array

character stack

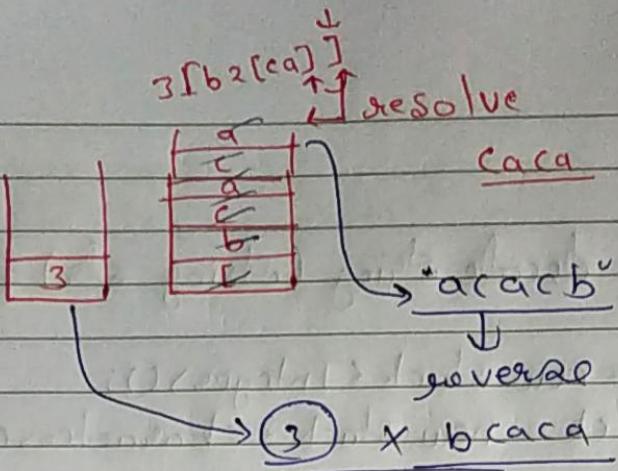


resolve
need to decode it
we will pop stack character

until we get opening bracket

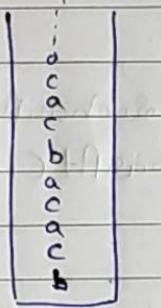
2 x ca
ca

2 x ca
ca



final op

stack



3 (bcaca)

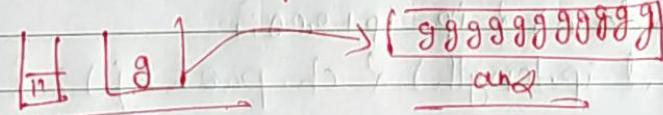
bcacabcacabca

at the end of loop we will
be having this stack
now we need to convert
into string and reverse and
that will be over final ans.

Note → we may have integers more than one digit, we need to manage that

11[g]

in this example



11 is considered as
single integer

class solution {
 static string decodeString(string str) {

 stack<Integer> st = new stack<Integer>();
 stack<Character> ch = new stack<Character>();

 string ip = "";
 string res = "";

 for (int i=0; i<str.length(); i++) {

 char t = str.charAt(i);

 if (Character.isDigit(t)) {

 string num = t + "";

 while (Character.isDigit((s.charAt(i+1))))

 num = num + str.charAt(i+1);

 i++;

 }

 st.push(Integer.parseInt(num));

 }

 character push { else if (t != ']') { ch.push(t); }

 else {

 res = "";

 while (!ch.isEmpty() && ch.peek() != '[') {

 res = ch.pop() + res; }

 ch.pop();

 ip = "";

 int n = st.pop();

 for (i=0 to n) { ip = ip + res; }

 for (j=0 to ip.length) { ch.push(j); }

converting
into digit ←
and pushing
in integer stack

character
push

resolving

String ans
while (!ch.
return

String ans = "";
while (!ch.isEmpty()) { ans = ch.pop() + ans; } Getting
ans
return ans;