

PH-211  
Electronics Lab.

Name - Rohit Ramabhadran

Roll no. 220121072

Experiment No - 5 .

Experiment Name - Filters .

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## Filter Circuits

Ques: To construct and study (a) the voltage gain as a function of frequency for low pass filter, (b) the voltage gain as a function of frequency for high pass filter and phase shift as well as cutoff frequency.

Equipments: DC power supply, (+/-) 15V, bread board, CRO, DMM, function generator.

→ Formulae

(a) Low pass filter .

$$A_{v/F} = \frac{A_{max}}{\sqrt{1 + (\frac{f}{f_c})^2}}$$

$A_{max} = 1 + \frac{R_f}{R_i}$  (gain of non-inverting amplifier).

$$f_c = \frac{1}{2\pi R_c} \quad (\text{cutoff frequency})$$

$f$  = operational frequency.

$A_v$  = voltage gain .

(b) High pass filter

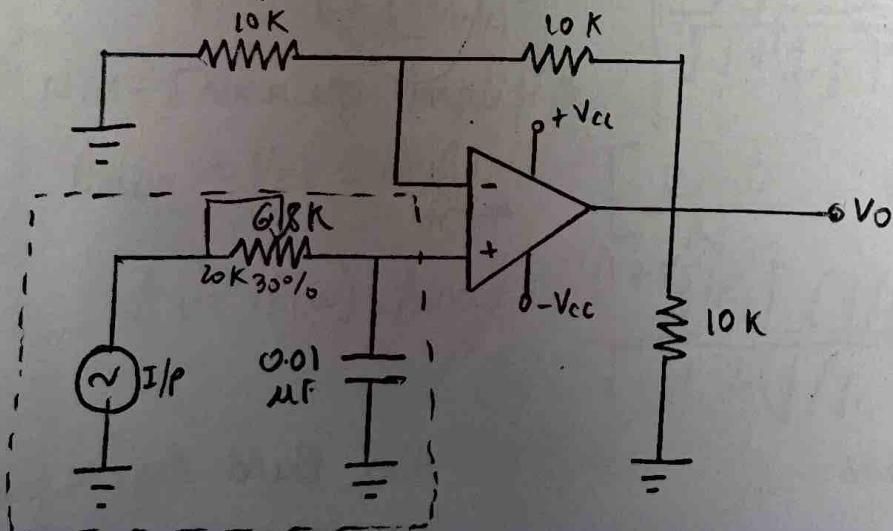
$$A_v = \frac{A_{max} (\frac{f}{f_c})}{\sqrt{1 + (\frac{f}{f_c})^2}}$$

$$A_{max} = 1 + \frac{R_f}{R_i}$$

$$f_c = \frac{1}{2\pi R_c}$$

Circuit diagrams and Analysis .

(a) Low Pass Filter .



Low pass Filter .

Non-inverting Amplifier .

Analysis:  $\frac{V_{in} - V_+}{R} = \frac{V_+ - 0}{1/SRC}$  (S = +j\omega)

$$\Rightarrow V_+ = \frac{V_{in}(1/SC)}{1 + \frac{1}{1/SC}} \Rightarrow \frac{V_+}{V_{in}} = \frac{1}{1 + SRC}$$

$$A(\omega) = \left| \frac{V_+}{V_{in}} \right| = \left| \frac{\frac{1}{1 + j\omega RC}}{1 + j\omega RC} \right| = \frac{1}{\sqrt{1 + (\omega RC)^2}}$$

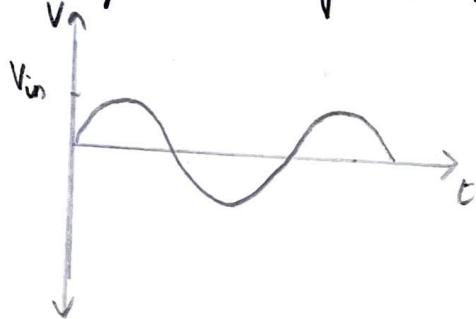
$\omega_c = \frac{1}{RC}$   $\rightarrow$  Cutoff frequency.

$$|A(\omega)| = \frac{1}{\sqrt{1 + (\frac{\omega}{\omega_c})^2}} = \frac{1}{\sqrt{1 + (\frac{f}{f_c})^2}}$$

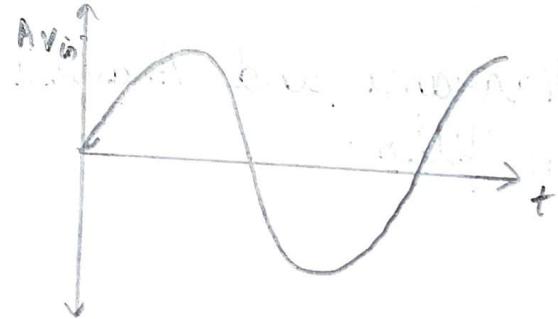
Non-Inverting Amplifier :  $A_{max} = \frac{V_o}{V_+} = 1 + \frac{R_f}{R_i} \quad [\because \frac{V_o - 0}{R_i} = \frac{V_o - V_+}{R_f}]$

$$A_v = |A(\omega)| A_{max} = \frac{1 + R_f/R_i}{\sqrt{1 + (f/f_c)^2}}$$

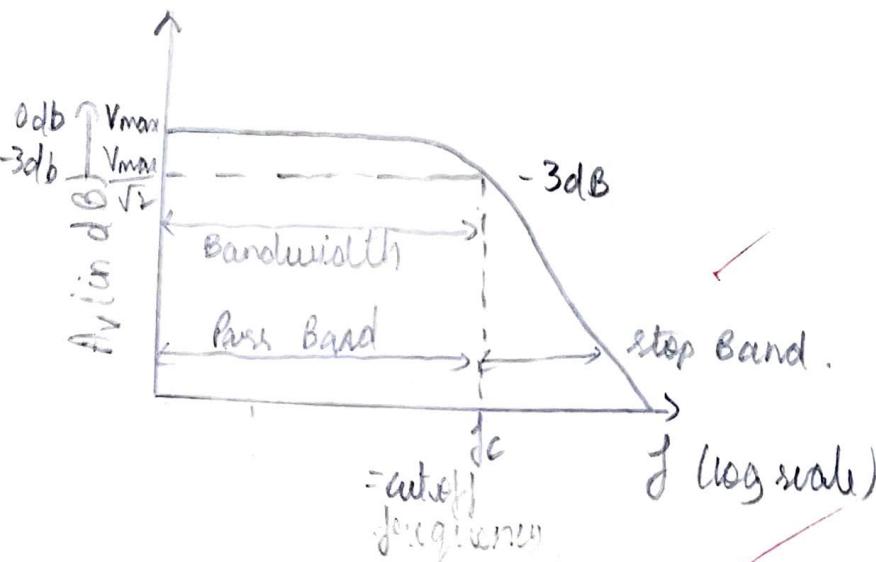
$\rightarrow$  Expected Waveform



Input



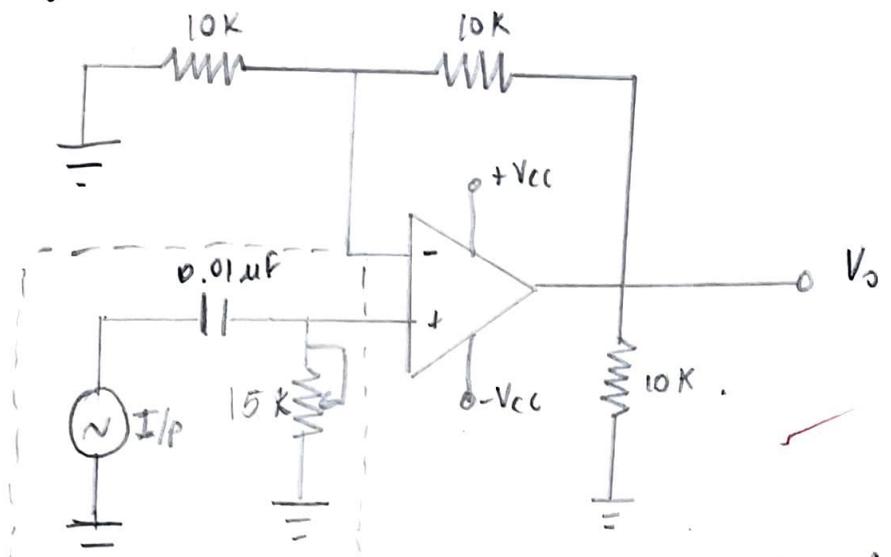
Output



Mid Band Region  
Waveform

It allows low frequencies  
to pass

## Q) High Bass filter



high pass filter

Non Inverting Amplifier

$$\text{Analysis: } \frac{V_{in} - V_-}{S_C} = \frac{V_t - 0}{R} \quad (S = j\omega)$$

$$\Rightarrow V_t = \frac{V_{in}}{1 + \frac{1}{S_C R}} \quad \Rightarrow \frac{V_t}{V_{in}} = \frac{j\omega R C}{1 + j\omega R C}$$

$$|A(\omega)| = \left| \frac{V_t}{V_{in}} \right| = \frac{\omega R C}{\sqrt{1 + (\omega R C)^2}} \quad (\omega_C = \frac{1}{R C})$$

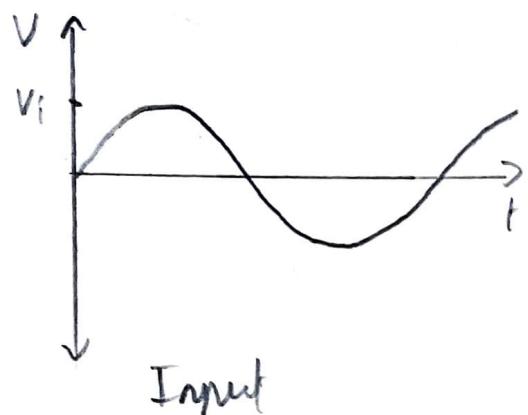
$$= \frac{\omega / \omega_C}{\sqrt{1 + (\omega / \omega_C)^2}} = \frac{f/f_C}{\sqrt{1 + (f/f_C)^2}}$$

⇒ Non-Inverting Amplifier

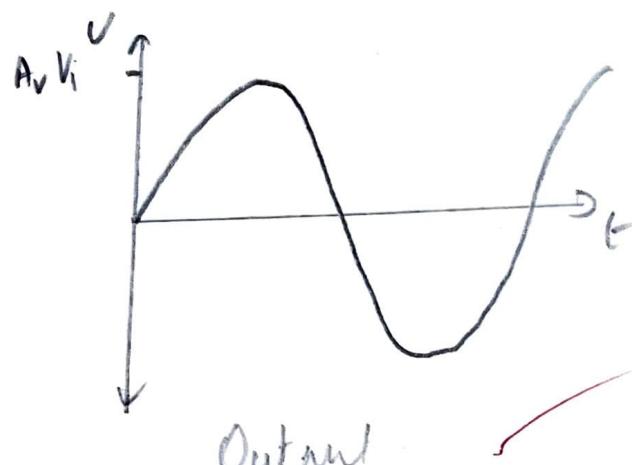
$$A_{max} = \frac{V_o}{V_i} = 1 + \frac{R_f}{R_i} \quad \left[ \frac{V_- - 0}{R_i} = \frac{V_o - V_-}{R_f} \right]$$

$$A_V = |A(\omega)| A_{max} = \frac{(1 + R_f/R_i) (f/f_C)}{\sqrt{1 + (f/f_C)^2}}$$

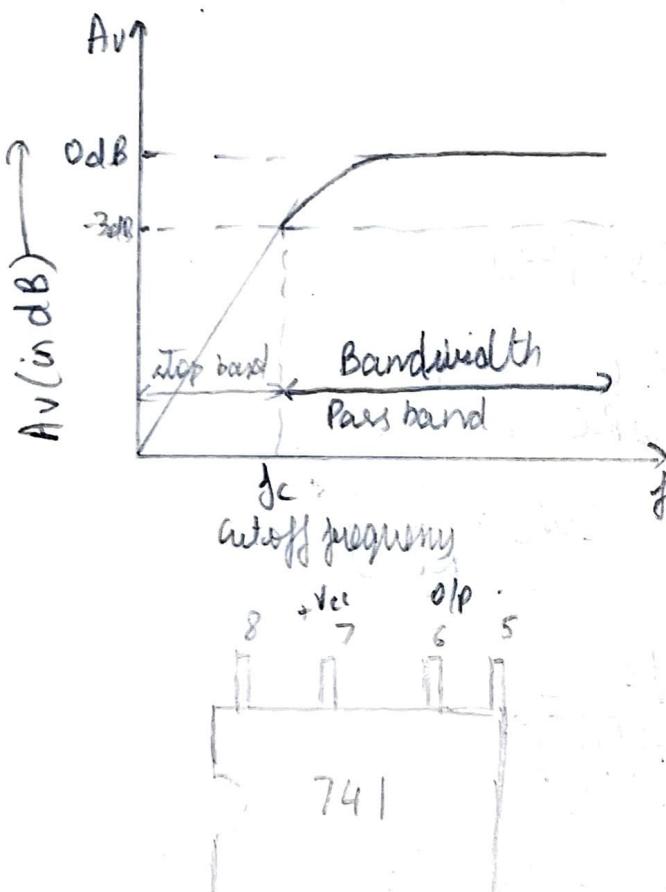
→ Expected Waveform



Input

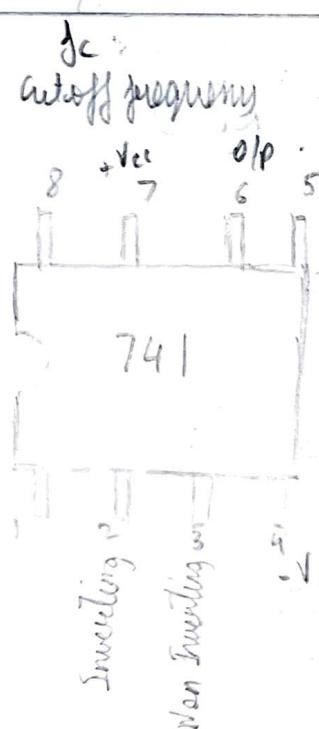


Output ✓



$$\frac{V_{max}}{\sqrt{2}}$$

If allows high frequencies to pass



$$I_P = \frac{10}{10}$$

Observation Table  
low pass filter

Biasing Voltage =  $\pm 15V$

No	Frequency	V <sub>in</sub> (V)	V <sub>out</sub>	A <sub>v</sub> = $\frac{20 \log (V_{out})}{V_{in}} (\text{dB})$	A <sub>v</sub>	Phase shift
1	5 Hz	1.5 V	3.0 V	6.02	2	-1.0°
2	10 Hz	1.5 V	3.0 V	6.02	2	-2.5°
3	20 Hz	1.5 V	3.0 V	6.02	2	-1.8°
4	30 Hz	1.5 V	3.0 V	6.02	2	-2.2°
5	100 Hz	1.5 V	3.0	6.02	2	3.0°
6	200 Hz	1.5 V	3.0	6.02	2	5.0°
7	300 Hz	1.5 V	3.0	6.02	2	7.2°
8	500 Hz	1.5 V	3.0	6.02	2	13.5°
9	1 KHz	1.5 V	2.8	5.42	1.87	25°
10	2 KHz	1.5 V	2.3	3.71	1.53	44°
11	3 KHz	1.5 V	1.8	1.58	1.2	54°
12	5 KHz	1.5 V	1.3	-1.24	0.87	64°
13	10 KHz	1.5 V	690 mV	-6.74	0.46	80°
14	20 KHz	1.5 V	370 mV	-12.16	0.25	90°
15	30 KHz	1.5 V	250 mV	-15.56	0.16	83°
16	50 KHz	1.5 V	160 mV	-19.44	0.11	88°
17	100 KHz	1.5 V	96 mV	-23.87	0.64	92°
18	200 KHz	1.5 V	60 mV	-27.96	0.04	101°/-79°
19	500 KHz	1.5 V	44 mV	-30.65	0.029	-177°/+177°
20	1 MHz	1.5 V	40 mV	-31.48	0.026	-179°/+179°

→ first write A<sub>v</sub>  
→ then A<sub>v</sub> (in dB)

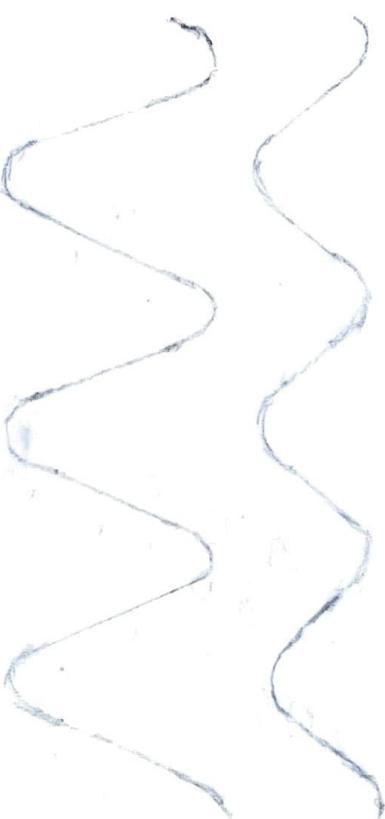
S No	Frequency	V <sub>in</sub>	V <sub>out</sub>	<del>A<sub>v</sub> = <math>\frac{V_{out}}{V_{in}}</math></del>	$A_v(\text{dB}) = 20 \log \frac{V_{out}}{V_{in}}$	$\text{phase shift } (\phi)$
1	5 Hz	2.5 V	85 mV	<del>37.72 (0.013)</del>	0.013	<del>-74.5° - 108°</del>
2	10 Hz	5.0 V	114 mV	0.023	-37.72	-95°
3	20 Hz	5.0 V	206 mV	0.041	-32.84	-95°
4	30 Hz	5.0 V	296 mV	0.059	-27.72	-91°
5	100 Hz	5.0 V	1.02 V	0.2	-24.55	-82°
6	200 Hz	5.0 V	2.0 V	0.4	-13.80	-79°
7	300 Hz	5.0 V	2.8 V	0.56	-7.96	-73°
8	500 Hz	5.0 V	4.6 V	0.92	-5.04	-64°
9	1 kHz	5.0 V	7.2 V	1.44	-0.72	-44°
10	2 kHz	5.0 V	9.1 V	<del>1.82</del>	3.161	-26°
11	3 kHz	5.0 V	9.8 V	1.96	5.20	-17°
12	5 kHz	5.0 V	10.2 V	2.04	6.19	-10°
13	10 kHz	5.0 V	10.4 V	2.08	6.36	-5°
14	20 kHz	5.0 V	10.4 V	2.08	6.36	0.7°
15	30 kHz	5.0 V	10.4 V	2.08	6.36	4.9°
16	50 kHz	5.0 V	8.4 V	1.68	4.50	35.1°
17	100 kHz	5.0 V	4.6 V	0.88	-1.11	66.8°
18	200 kHz	5.0 V	2.1 V	0.42	-7.54	81.9°
19	300 kHz	5.0 V	880 mV	0.176	-15.09	92.1°
20	1 MHz	5.0 V	480 mV	0.096	-20.35	-11.9°

(18)

(a) Low Pass Filter

V<sub>in</sub>

V<sub>out</sub>



Frequency = 500 Hz

Phase shift = 135°

V<sub>in</sub> = 1.5 V

V<sub>cc</sub> = ±15 V

V<sub>out</sub> = 3.0 V

A<sub>v</sub> = 2.0

$$A_v(10\text{dB}) = 6.02$$

At cutoff

Cutoff  
Region

frequency = 1000 Hz

phase diff = 45.0°

V<sub>in</sub> = 1.5 V

V<sub>out</sub> = 2.30 V

A<sub>v</sub> = 1.57 dB

Rohit Rambabu

220121072

(b) High Pass Filter

At saturation

frequency = 1000 Hz  
V<sub>in</sub> = 5.0 V  
V<sub>cc</sub> = 10.0 V



A<sub>v(10\text{dB})</sub> = 6.36  
phase shift = -50°

A<sub>v</sub> = 2.08

frequency = 1 kHz  
V<sub>in</sub> = 5.0 V

V<sub>out</sub> = 7.28 V

A<sub>v</sub> = 1.4

At cutoff

## Calculation

a) Low Pass Filter  
from the graph

$$\text{Cut-off frequency } (f_c) = 2.3 \text{ kHz}$$

$$\begin{aligned} \text{Theoretical } f_c &= \frac{1}{2\pi RC} = 2340.5 \text{ Hz} \\ A_{max} &= 1 + \frac{f_c}{R_i} = 2 \\ 45^\circ \phi \text{ at } f &= 2.3 \text{ kHz} \quad V_{max} = 3V \\ A_V &= 1.44 \quad \frac{V_{max}}{\sqrt{2}} = 2.12V \end{aligned}$$

∴ allowed frequency band for low pass filter  $\omega = f_H - f_L$

$$f_H = 2.3 \text{ kHz}$$

$$= 2.3 \text{ kHz} - 5 \text{ Hz}$$

$$f_L = 5 \text{ Hz}$$

$$= 2.295 \text{ kHz}$$

(b) High Pass filter  
from the graph

$$\text{Cut-off frequency} = 1.0 \text{ kHz}$$

$$\text{Theoretical } f_c = \frac{1}{2\pi RC} = 1.06 \text{ kHz}$$

$$A_{max} = 1 + \frac{f_c}{R_i} = 2$$

$$V_{max} = 10.4V$$

$$\frac{V_{max}}{\sqrt{2}} = 7.35V$$

∴ allowed frequency band for high pass filter  $\omega = f_H - f_L$

$$f_H = 30 \text{ kHz}$$

$$= 30 \text{ kHz} - 1 \text{ kHz}$$

$$f_L = 1 \text{ kHz}$$

$$= 29 \text{ kHz}$$

⑩

## Result

- ① The cut-off frequency for low pass filter is 2.3 kHz
- ② The allowed frequency band for it is 2.295 kHz
- ③ Cut-off frequency for high pass filter is 1 kHz
- ④ The allowed frequency band for it is 29 kHz.
- ⑤ The theoretical v/s Actual values is

low pass

$$f_c = 2340.5 \text{ Hz}$$

$$f_H - f_L = 2340.5 \text{ Hz}$$

$$f_c = 1.06 \text{ kHz}$$

High pass

$$f_c = 2.3 \text{ kHz}$$

$$f_H - f_L = 2.295 \text{ kHz}$$

$$A_{max} = 2 \quad V_{max} = 3V$$

$$A_V = 1.44 \quad \frac{V_{max}}{\sqrt{2}} = 2.12V$$

$$f_c = 1 \text{ kHz}$$

$$f_H - f_L = 29 \text{ kHz}$$

$$A_{max} = 2$$

$$A_V = 1.37$$

Actual

$$\begin{aligned} V_{max} &= 10.4V \\ \frac{V_{max}}{\sqrt{2}} &= 7.35V \end{aligned}$$

### Precautions:

1. Make sure that all connection are tight -
2. Do not apply too large biasing voltage to the op-amp
3. Switch off the power supply when handling the circuit
4. Wait for the values in oscilloscope to reach equilibriums
5. Ensure the ground is connected between the power supply and breadboard.

### Discussion

1. There is a phase shift in all the three circuits
2. phase difference increase with the increase in frequency.
3. Breakdown for low pass filter was observed for  $14\text{MHz}$
4. Breakdown for high pass filter was observed for  $1800\text{kHz}$   
~~increase and then~~
5. Volt for low pass filter was observed to remain constant  
and then decrease
6. Volt for High pass filter was observed to increase first  
then remains constant and then decrease

