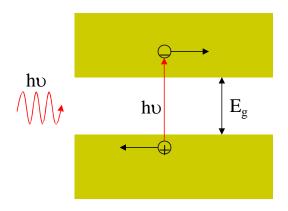
Photodiode detectors

- □ Background concepts
- □ p-n photodiodes
- □ Photoconductive/photovoltaic modes
- □ p-i-n photodiodes
- □ Responsivity and bandwidth

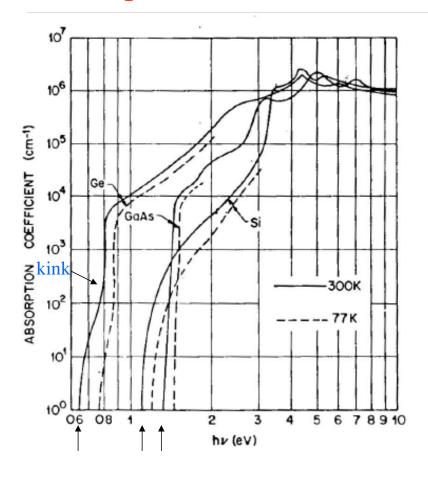
Electron-hole photogeneration

- Most modern photodetectors operate on the basis of the internal photoelectric effect – the photoexcited electrons and holes remain within the material, increasing the electrical conductivity of the material
- □ *Electron-hole photogeneration* in a semiconductor



- absorbed photons *generate* free electronhole pairs
- •*Transport* of the free electrons and holes upon an electric field results in a *current*

Absorption coefficient



Bandgaps for some *semiconductor* photodiode materials at 300 K

Bandgap (eV) at 300 K

	Indirect	Direct
Si	1.14	4.10
Ge	0.67	0.81
GaAs	-	1.43
InAs	-	0.35
InP	-	1.35
GaSb	-	0.73
$In_{0.53}Ga_{0.47}As$	-	0.75
$In_{0.14}Ga_{0.86}As$	-	1.15
$GaAs_{0.88}Sb_{0.12}$	-	1.15

Absorption coefficient

- \square E.g. absorption coefficient $\alpha = 10^3$ cm⁻¹
- □ Means an 1/e optical power absorption length of

$$1/\alpha = 10^{-3} \, \text{cm} = 10 \, \mu \text{m}$$

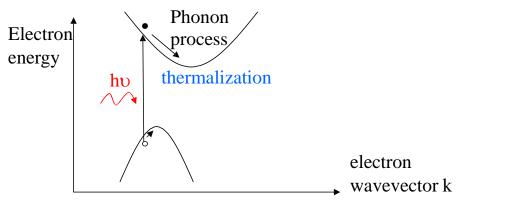
Likewise, $\alpha = 10^4 \text{ cm}^{-1} => 1/\text{e}$ optical power absorption length of 1 μ m.

 $\alpha = 10^5 \, \text{cm}^{-1} \Rightarrow 1/\text{e}$ optical power absorption length of 100 nm.

 $\alpha = 10^6 \, \text{cm}^{-1} \Rightarrow 1/\text{e}$ optical power absorption length of 10 nm.

Indirect absorption

- □ Silicon and germanium absorb light by both indirect and direct optical transitions.
- □ *Indirect* absorption requires the assistance of a *phonon* so that momentum and energy are conserved.
- □ Unlike the emission process, the absorption process can be sequential, with the excited electron-hole pair thermalize within their respective energy bands by releasing energy/momentum via phonons.
- □ This makes the *indirect absorption* <u>less efficient</u> than direct absorption where no phonon is involved.



Indirect vs. direct absorption in silicon and germanium

- □ Silicon is only weakly absorbing over the wavelength band 0.8 0.9 μm. This is because transitions over this wavelength band in silicon are due only to the indirect absorption mechanism. The threshold for indirect absorption (long wavelength cutoff) occurs at 1.09 μm.
- The bandgap for <u>direct</u> absorption in silicon is 4.10 eV, corresponding to a threshold of 0.3 μm.
- Germanium is another semiconductor material for which the lowest energy absorption takes place by <u>indirect</u> optical transitions. Indirect absorption will occur up to a threshold of 1.85 μm.
- However, the *threshold for direct absorption* occurs at 1.53 μm, for shorter wavelengths germanium becomes strongly absorbing (*see the kink in the absorption coefficient curve*).

Choice of photodiode materials

- □ A photodiode material should be chosen with a *bandgap* energy slightly less than the photon energy corresponding to the *longest* operating wavelength of the system.
- This gives a *sufficiently high absorption coefficient* to ensure a good response, and yet limits the number of *thermally generated* carriers in order to attain a low "*dark current*" (i.e. current generated with no incident light).
- Germanium photodiodes have relatively large dark currents due to their narrow bandgaps in comparison to other semiconductor materials. This is a major shortcoming with the use of germanium photodiodes, especially at shorter wavelengths (below 1.1 μm)

 hv_L

 hv_s

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 E_{σ} slightly less than $h\nu_L$

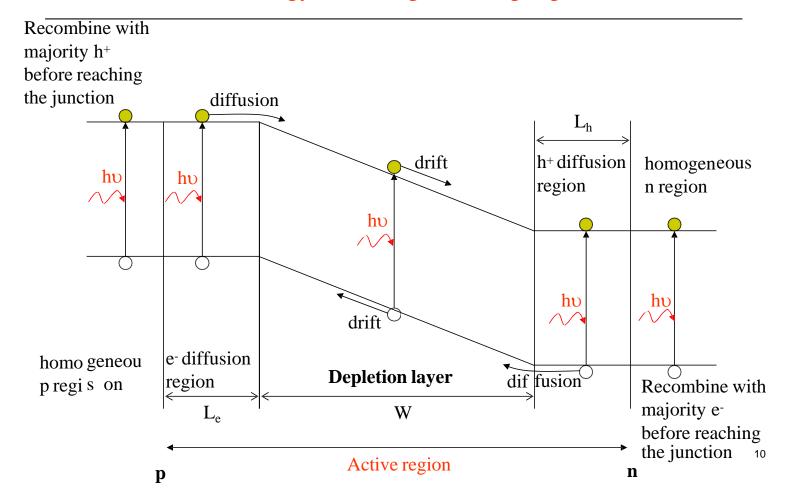
III-V compound semiconductors

- □ Direct-bandgap III-V compound semiconductors can be better material choices than germanium for the longer wavelength region.
- □ Their *bandgaps can be tailored* to the desired wavelength by changing the relative concentrations of their constituents (*resulting in lower dark currents*).
- They may also be fabricated in *heterojunction* structures (which *enhances their high-speed operations*).
- e.g. In_{0.53}Ga_{0.47}As lattice matched to InP substrates responds to wavelengths up to around 1.7 μm. (*most important for 1.3 and 1.55 μm*)

Junction photodiodes

- □ The *semiconductor photodiode detector* is a p-n junction structure that is based on the internal photoeffect.
- □ The photoresponse of a photodiode results from the *photogeneration of electron-hole pairs through band-to-band optical absorption*.
 - => The *threshold* photon energy of a semiconductor photodiode is the bandgap energy E_g of its active region.
- The *photogenerated* electrons and holes in the *depletion layer* are subject to the local electric field within that layer. The electron/hole carriers *drift* in opposite directions. This *transport* process induces an electric current in the external circuit.
- □ Here, we will focus on semiconductor *homojunctions*.

Photoexcitation and energy-band diagram of a p-n photodiode



- In the depletion layer, the internal electric field sweeps the photogenerated electron to the n side and the photogenerated hole to the p side.
 - => a *drift current* that flows in the *reverse* direction from the n side (cathode) to the p side (anode).
- □ Within one of the *diffusion regions* at the edges of the depletion layer, the photogenerated *minority* carrier (*hole in the n side and electron in the p side*) can reach the depletion layer by *diffusion* and then be *swept to the other side by the internal field*.
 - => a *diffusion current* that also flows in the *reverse* direction.
- In the p or n *homogeneous region*, *essentially no current is generated* because there is essentially no internal field to separate the charges and a minority carrier generated in a homogeneous region *cannot diffuse to the depletion layer before recombining with a majority carrier*.

Photocurrent in an illuminated junction

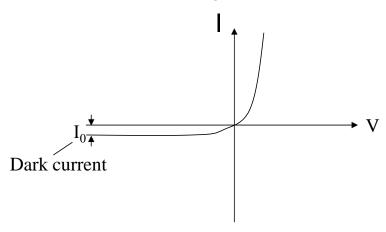
- If a junction of cross-sectional area A is uniformly illuminated by photons with hv > E_g, a photogeneration rate G (EHP/cm³-s) gives rise to a photocurrent.
- □ The number of holes created per second within a diffusion length L_h of the depletion region on the n side is AL_hG.
- □ The number of electrons created per second within a diffusion length L_e of the depletion region on the p side is AL_eG.
- Similarly, A*W*G no of carriers are generated within the depletion region of width W.
- □ The resulting junction photocurrent from n to p:
 I_p = eA (L_h + L_e + W) G

Diode equation

Recall the current-voltage (I-V) characteristic of the junction is given by the diode equation:

$$I = I_0(\exp(eV/k_BT) - 1)$$

- □ The current I is the injection current under a *forward* bias V.
- □ I₀ is the "saturation current" representing *thermal-generated* free carriers which flow through the junction (*dark current*).



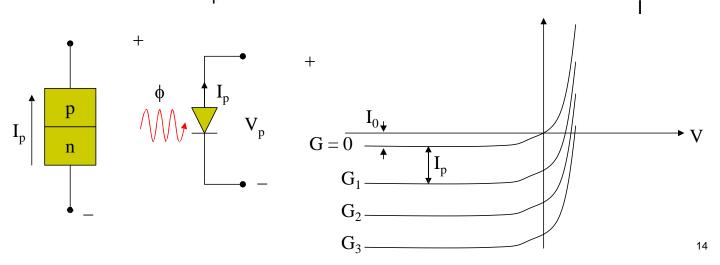
I-V characteristics of an illuminated junction

☐ The photodiode therefore has an I-V characteristic:

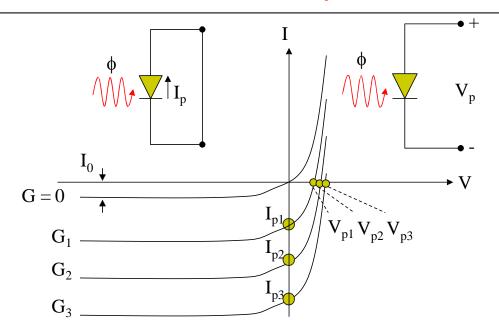
$$I = I_0(\exp(eV/k_BT) - 1) - I_p$$

Where, $I_p = eA (L_h + L_e + W) G$

☐ This is the usual I-V curve of a p-n junction with an added photocurrent —I_p proportional to the photon flux.

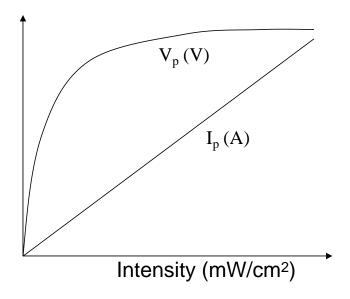


Short-circuit current and open-circuit voltage



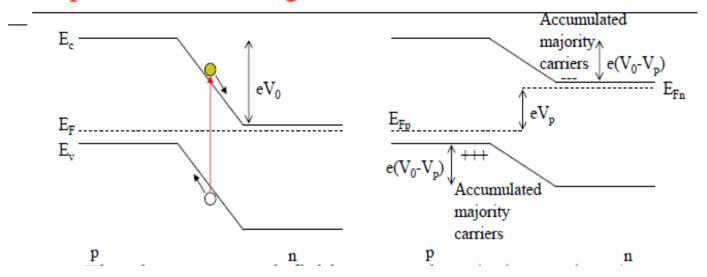
- \square The *short-circuit* current (V = 0) is the *photocurrent* I_p .
- The open-circuit voltage (I = 0) is the photovoltage V_p . $(I = 0) => V_p = (k_B T/e) \ln(I_p/I_0 + 1)$

Photocurrent and photovoltage



- □ As the light intensity increases, the short-circuit current increases linearly (I_p ∝ G);
- □ The open-circuit voltage increases only logarithmically (V_p
 ∞ In (I_p/I₀)) and limited by the equilibrium contact potential.

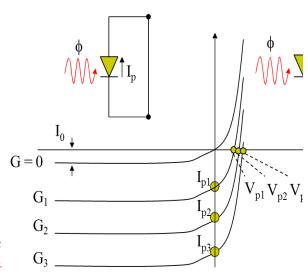
Open-circuit voltage



- □ The photogenerated, field-separated, majority carriers (+ve charge on the p-side, -ve charge on the n-side) forward-bias the junction.
- □ The appearance of a forward voltage across an illuminated junction (photovoltage) is known as the photovoltaic effect.
- The limit on V_p is the equilibrium contact potential V_0 as the contact potential is the maximum forward bias that can appear ¹⁷ across a junction. (drift current vanishes with $V_p = V_0$)

Photoconductive and Photovoltaic modes

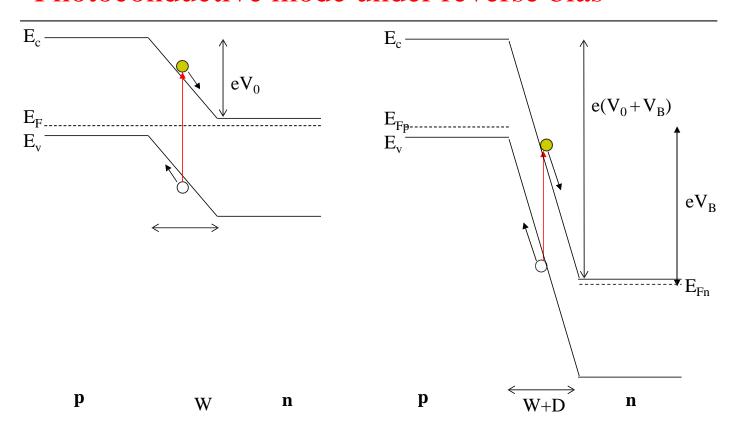
- □ There are two modes of operation for a junction photodiode: photoconductive and photovoltaic
- The device functions in *photoconductive* mode in the *third* quadrant of its current-voltage characteristics, including the *short-circuit condition* on the vertical axis for V = 0. (*acting as a current source*)
- ☐ It functions in *photovoltaic* mode in the *fourth* quadrant, including the *open-circuit condition* on the horizontal axis for I = 0. (acting as a voltage source with output voltage limited by the equilibrium contact potential)



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The mode of operation is determined by the *bias* condition and the external circuitry.

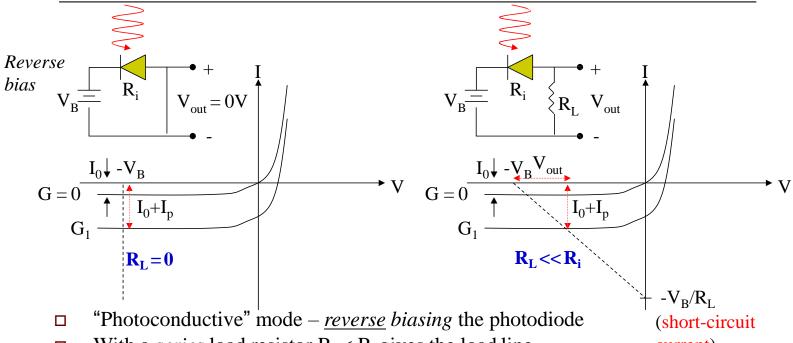
Photoconductive mode under reverse bias



(For silicon photodiodes, $V_0 \approx 0.7$ V, V_B can be up to -5 – -10 V)

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Basic circuitry and load line for the photoconductive mode

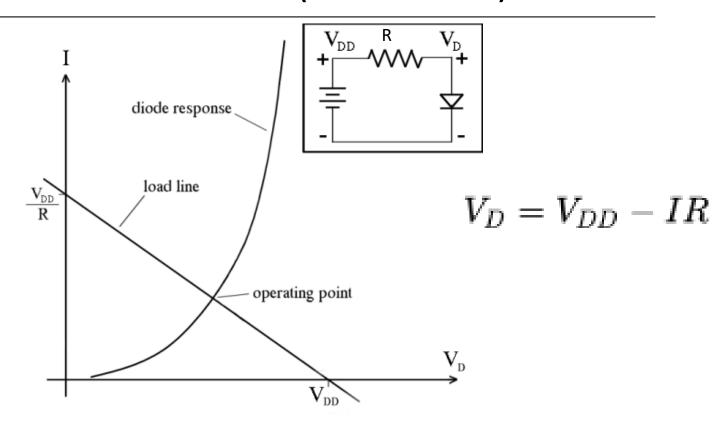


current)

- With a series load resistor R_L< R_i gives the <u>load line</u>
- Keep $V_{out} < V_B$ so that the photodiode is <u>reverse</u> biased $(V_R is sufficiently large)$
- Under these conditions and before it saturates, a photodiode has the following linear response: $V_{out} = (I_0 + I_p)R_L$ A **load line** curve represents the constraint put on

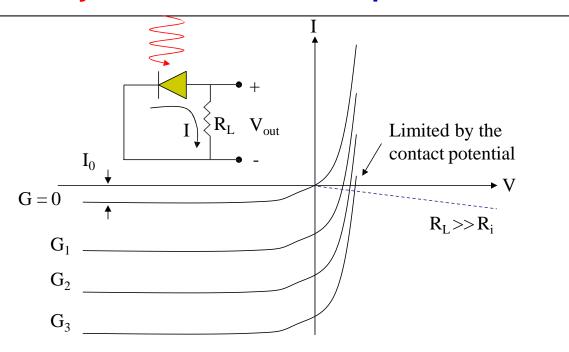
the voltage and current in the nonlinear device by the external circuit.

Load line (electronics)



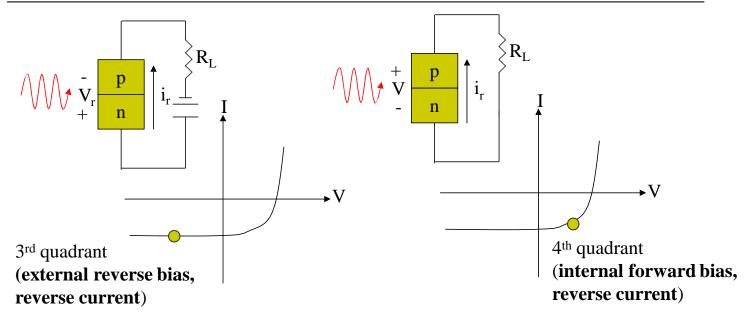
The **operating point** of the circuit will be at the **intersection of the curve with the load line**.

Basic circuitry and load line for the photovoltaic mode



- Does not require a bias voltage but requires a <u>large load</u> resistance.
- R_L >> R_i, so that the current I flowing through the diode, the internal resistance is negligibly small.

Operation regimes of an illuminated junction



Photoconductive:

Power (+ve) is delivered *to the device by the external circuit* (photodetector)

Photovoltaic:

Power (-ve) is delivered to the load by the device (solar cell/ energy harvesting)

Solar cell Parameters

Conversion of optical energy → electrical energy. (current and voltage)

For calculation of **important parameters**,

Open circuit mode, I= 0.

 $V_{oc} \rightarrow$ open circuit voltage.

$$\begin{split} I &= 0 = I_L - I_0 [exp \ (\frac{eV_{oc}}{mkT}) - 1] \\ V_{oc} &= \frac{mkT}{e} ln \ (1 + \frac{I_L}{I_0}) \end{split}$$

 $V_{oc} \approx 0.7 \text{ eV}$ for Si solar cell.

Short circuit mode, R = 0, V = 0.

Short circuit current, $I = I_{sc} = I_{L}$

Electrical power delivered to the load

$$P = IxV = I_LV - I_0 \left[exp \left(\frac{eV}{kT} \right) - 1 \right] V$$

P is maximum for (V_m, I_m) .

The conversion efficiency,

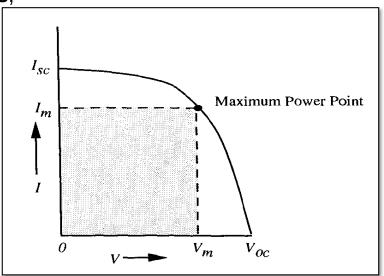


Fig. 45: The relationship between the current and voltage delivered by a solar cell. The open circuit voltage is Voc and the short circuit current is Isc. The maximum power is delivered at the point shown.

$$\begin{split} \eta_{conv} &= \frac{output\ electrical\ power}{input\ optical\ power} = \frac{P_m}{P_{in}} x 100\% \\ &= \frac{I_m V_m}{P_{in}} x 100\% \end{split}$$

Fill factor

$$F_f = \frac{I_m V_m}{I_{sc} V_{oc}} \approx 0.7 \ for \ most \ solar \ cell. \label{eq:ff}$$

Photons with $E > \hbar \omega$ will produce e-h pairs. $(\hbar \omega - E_g)$ excess is dissipated as

heat.

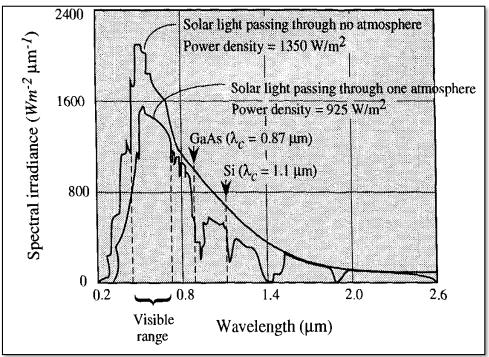
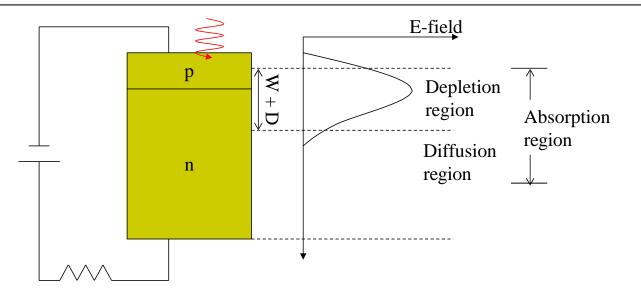


Fig. 46: The spectral irradiance of the solar energy. The spectra are shown for no absorption in the atmosphere and for the sea level spectra. Also shown are the cutoff wavelengths for GaAs and Si.

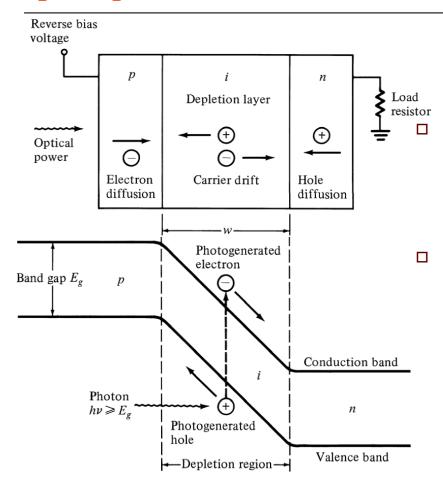
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A reverse-biased p-n photodiode



- It is important that the photons are absorbed in the depletion region. Thus, it is made as long as possible (say by decreasing the doping in the n type material). The depletion region width in a p-n photodiode is normally 1 3 μm.
- □ The depletion-layer width widens and the junction capacitance ²⁶ drops with reverse voltage across the junction.

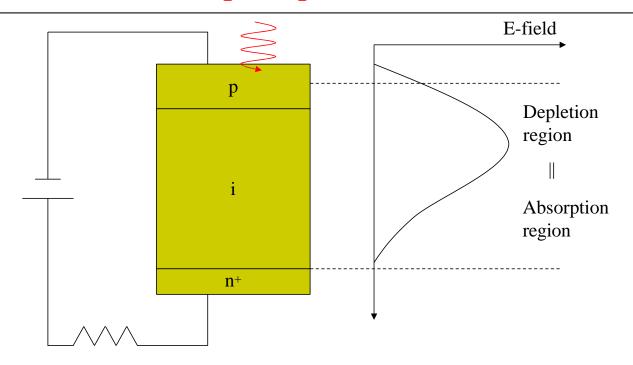
p-i-n photodiodes



A p-i-n photodiode consists of an *intrinsic* region sandwiched between heavily doped p⁺ and n⁺ regions. The *depletion layer* is almost completely defined by the intrinsic region.

In practice, the intrinsic region does not have to be truly intrinsic but only has to be highly resistive (lightly doped p or n region).

A reverse-biased p-i-n photodiode

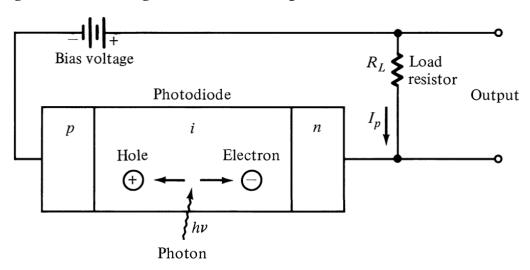


All the absorption takes place in the depletion region. The intrinsic region can be an n-type material that is lightly doped, and to make a low-resistance contact a highly doped n-type (n⁺) layer is added.

- □ The depletion-layer width W in a p-i-n diode does *not* vary significantly with bias voltage but is essentially fixed by the thickness, d_i , of the intrinsic region so that W $\approx d_i$.
- □ The internal capacitance of a p-i-n diode can be designed:

$$C_i = C_j = \varepsilon A/W \approx \varepsilon A/d_i$$

This capacitance is essentially independent of the bias voltage, remaining constant in operation.

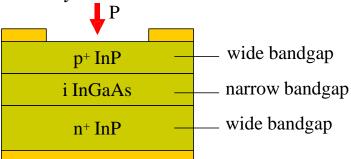


□ p-i-n photodiodes offer the following advantages:

- Increasing the width of the depletion layer (where the generated carriers can be transported by drift) increases the area available for capturing light
- Increasing the width of the depletion layer *reduces the junction capacitance* and *thereby the RC time constant*. Yet, the transit time increases with the width of the depletion layer.
- Reducing the ratio between the diffusion length and the drift length of the device results in a greater proportion of the generated current being carried by the faster drift process.

Heterojunction photodiodes

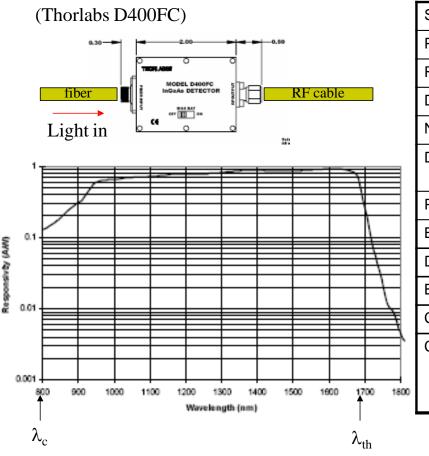
- □ Many III-V p-i-n photodiodes have heterojunction structures.
- Examples: p+-AlGaAs/GaAs/n+-AlGaAs, p+-InP/InGaAs/n+-InP, or p+-AlGaAs/GaAs/n+-GaAs, p+-InGaAs/InGaAs/n+-InP.
- \square AlGaAs/GaAs (0.7 0.87 μ m)
- □ InGaAs/InP (1300 1600 nm). A typical InGaAs p-i-n photodetector operating at 1550 nm has a *quantum efficiency* $\eta \approx 0.75$ and a *responsivity R* ≈ 0.9 A/W



Heterojunction photodiodes

- □ Heterojunction structures offer additional flexibility in optimizing the performance of a photodiode.
- □ In a heterojunction photodiode, the active region normally has a bandgap that is *smaller* than one or both of the homogeneous regions.
- □ A wide-bandgap homogeneous region, which can be either the top p+region or the substrate n region, serves as a window for the optical signal to enter.
- The *small bandgap of the active region* determines the *long-wavelength cutoff* of the photoresponse, λ_{th} .
- The large bandgap of the homogeneous window region sets the short-wavelength cutoff of the photoresponse, λ_c .
- => For an optical signal that has a wavelength λ_s in the range λ_{th} > λ_s > λ_c , the *quantum efficiency* and the *responsivity* can be optimized.

InGaAs fiber-optic pin photodetector



Spectral response	800 – 1700 nm
Peak response	0.95 A/W @ 1550 nm
Rise/fall time	0.1 ns
Diode capacitance	0.7 pF (typ)
NEP @ 1550 nm	1.0 x 10 ⁻¹⁵ W/√Hz
Dark current	0.7nA (typ), 1.0nA (max)
PD Active diameter	0.1 mm
Bandwidth	1 GHz (min)
Damage threshold	100 mW CW
Bias (reverse)	12V battery
Coupling lens	0.8" dia. Ball lens
Coupling efficiency	92% (typ) from both single- and multi- mode fibers over full spectral response

Application notes – output voltage

- The RF output signal (suitable for both pulsed and CW light sources) is the direct photocurrent out of the photodiode anode and is a function of the incident light power and wavelength.
- The *responsivity* $R(\lambda)$ can be used to estimate the amount of photocurrent.
- □ To convert this photocurrent to a voltage (say for viewing on an oscilloscope), add an external load resistance, R_L.
- \Box The *output voltage* is given as:

$$V_0 = P R(\lambda) R_L$$

Responsivity

□ The *responsivity* of a photodetector relates the electric current I_p flowing in the device circuit to the optical power P incident on it.

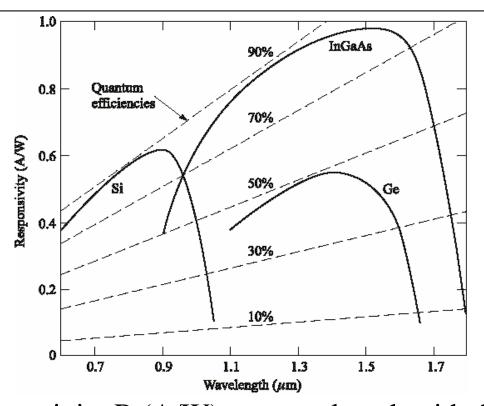
$$I_p = \eta \ e\Phi = \eta \ eP/h\upsilon \equiv R \ P$$
 η : quantum efficiency

Responsivity R =
$$I_p/P = \eta e/h\upsilon = \eta \lambda/1.24 [A/W]$$

The responsivity is *linearly proportional* to both the *quantum efficiency* η and the free-space wavelength λ .

(e.g. for
$$\eta = 1$$
, $\lambda = 1.24 \mu m$, $R = 1 \text{ A/W}$)

Responsivity vs. wavelength



Responsivity R (A/W) vs. wavelength with the quantum efficiency η shown on various dashed lines

Quantum efficiency

The *quantum efficiency* (*external quantum efficiency*) η of a photodetector is the probability that a single photon incident on the device generates a photocarrier pair that contributes to the detector current.

$$\eta(\lambda) = \zeta (1-R) [1 - \exp(-\alpha(\lambda)d)]$$

R is the optical power reflectance at the surface, ζ is the fraction of electron-hole pairs that contribute to the detector current, $\alpha(\lambda)$ the absorption coefficient of the material, and **d** the photodetector depth.

ζ is the fraction of electron-hole pairs that *avoid recombination* (often dominated at the material surface) and contribute to the useful photocurrent. Surface recombination can be reduced by careful material growth and device design/fabrication.

[1 – $\exp(-\alpha(\lambda)d)$] represents the fraction of the photon flux absorbed in the bulk of the material. The device should have a value of d that is sufficiently large. (d > $1/\alpha$, $\alpha = 10^4$ cm⁻¹, d > 1 μ m)

Dependence of quantum efficiency on wavelengths

- The characteristics of the semiconductor material determines the spectral window for large η .
- The bandgap wavelength $\lambda_g = hc/E_g$ is the *long-wavelength limit* of the semiconductor material.
- □ For sufficiently short λ , η also decreases because most photons are absorbed <u>near the surface</u> of the device (e.g. for $\alpha = 10^4$ cm⁻¹, most of the light is absorbed within a distance $1/\alpha = 1$ μm; for $\alpha = 10^5 10^6$ cm⁻¹, most of the light is absorbed within a distance $1/\alpha = 0.1 0.01$ μm).
- □ The recombination lifetime is quite short near the surface, so that the photocarriers recombine before being collected. (short-wavelength limit)
- In the near-infrared region, silicon photodiodes with *antireflection* coating can reach 100% quantum efficiency near $0.8 0.9 \mu m$.
- □ In the 1.0 1.6 µm region, Ge photodiodes, InGaAs photodiodes, and InGaAsP photodiodes have shown high quantum efficiencies.

Speed-limiting factors of a photodiode

- □ *High-speed photodiodes* are by far the most widely used photodetectors in applications requiring high-speed or broadband photodetection.
- □ The speed of a photodiode is determined by *two* factors:
 - The response time of the photocurrent
 - The RC time constant of its equivalent circuit
- □ Because a photodiode operating in *photovoltaic* mode has a large RC time constant due to the large internal <u>diffusion</u> <u>capacitance</u> upon internal forward bias in this mode of operation
 - => only photodiodes operating in a <u>photoconductive</u> mode are suitable for high-speed or broadband applications. ³⁹

Response time of the photocurrent (photoconductive mode)

- The response time is determined by two factors:
 - Drift of the electrons and holes that are photogenerated in the depletion layer
 - Diffusion of the electrons and holes that are photogenerated in the diffusion regions
- Drift of the carriers across the depletion layer is a fast process given by the transit times of the photogenerated electrons and holes across the depletion layer.
- Diffusion of the carriers is a slow process caused by the optical absorption in the diffusion regions outside of the high-field depletion region.

(diffusion current can last as long as the carrier lifetime)

- => a <u>long tail</u> in the impulse response of the photodiode
- => a *low-frequency falloff* in the device frequency response

Photodiode capacitance

Time constant incurred by the capacitance of the photodiode with its <u>load</u> – the junction capacitance

$$C_i = \varepsilon A/W$$

where ϵ is the permittivity of the semiconductor material and A is the diode junction area.

 A small depletion layer width W increases the junction capacitance.

(The capacitance of the photodiode C_{pd} is that of the junction together with the capacitance of the <u>leads</u> and <u>packaging</u>.

This capacitance must be *minimized* in order to reduce the ${}_{4}RC$ time constant. In ideal cases, $C_{pd} \approx C_{j.}$

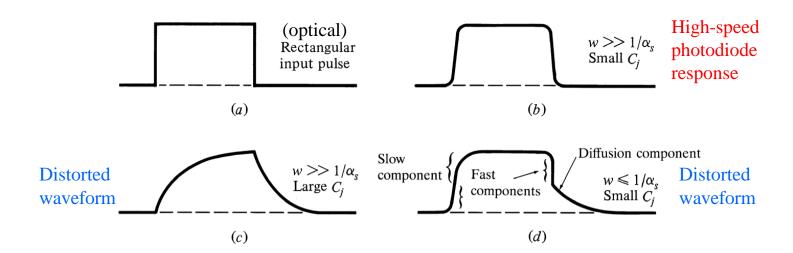
Remarks on junction capacitance

- □ *For pn junctions*, because the width of the depletion layer decreases with forward bias but increases with reverse bias, the junction capacitance increases when the junction is subject to a forward bias voltage but *decreases when it is subject to a reverse bias voltage*.
- □ **For p-i-n diodes**, the width of the depletion (*intrinsic*) layer is fixed => the junction capacitance is *not* affected by biasing conditions.
- e.g. A GaAs p-n homojunction has a 100 μ m x 100 μ m cross section and a width of the depletion layer W = 440 nm. Consider the junction in thermal equilibrium *without* bias at 300 K. Find the *junction* capacitance.

$$\epsilon = 13.18\epsilon_0 \text{ for GaAs, } \epsilon_0 = 8.854 \text{ x } 10^{-12} \text{Fm}^{-1}$$

$$\Rightarrow C_j = 13.18 \text{ x } 8.854 \text{ x } 10^{-12} \text{ x } 1 \text{ x } 10^{-8} / (440 \text{ x } 10^{-9}) = 2.65 \text{ pF}$$

Photodiode response to rectangular optical input pulses for various detector parameters



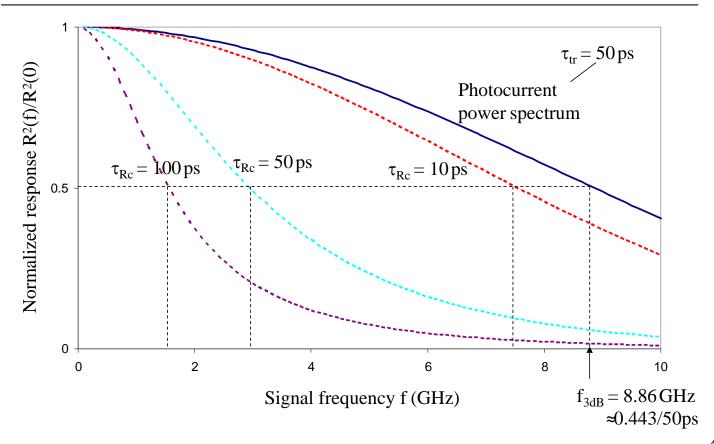
- \gg W >> 1/α (all photons are absorbed in the depletion layer) and small C_i. High speed response.
- \gg W >> 1/ α , large photodiode capacitance, RC time limited
- \triangleright W ≤ 1/α, (some photons are absorbed in the diffusion region) diffusion component limited

Transit-time-limited

- Thus, for a high-speed photodiode, diffusion mechanism has to be eliminated (by reducing the photogeneration of carriers outside the depletion layer through design of the device structure).
- When the diffusion mechanism is eliminated, the frequency response of the photocurrent is only limited by the transit times of electrons and holes.
- In a semiconductor, electrons normally have a higher mobility (smaller electron effective mass), thus a smaller transit time, than holes.
- □ For a good estimate of the detector frequency response, we use the <u>average</u> of electron and hole transit times:

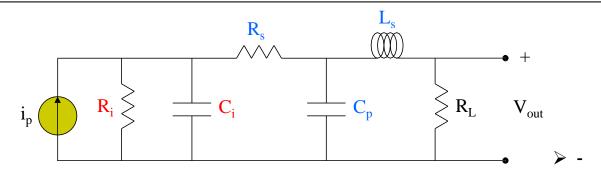
$$\tau_{tr} = \frac{1}{2}(\tau_{tr}^{e} + \tau_{tr}^{h})$$

Total frequency response



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Small-signal equivalent circuits



- A photodiode has an internal resistance R_i and an internal capacitance C_i across its junction.
- The series resistance R_s takes into account both resistance in the homogeneous regions of the diode and parasitic resistance from the contacts.
- ➤ The external parallel capacitance C_p is the parasitic capacitance from the contacts and the package.
- ➤ The series inductance L_s is the parasitic inductance from the wire or transmission-line connections.
- ➤ The values of R_s, C_p, and L_s can be minimized with careful design, processing, and packaging of the device.

- \square Both R_i and C_i depend on the *size* and the *structure* of the photodiode and *vary with the voltage across the junction*.
- In *photoconductive* mode under a *reverse* voltage, the diode has a *large* R_i normally on the order of $1 100 \text{ M}\Omega$ for a typical photodiode, and a *small* C_i dominated by the junction capacitance C_i .
- As the reverse voltage increases in magnitude, R_i increases but C_i decreases because the depletion-layer width increases with reverse voltage.
- In *photovoltaic* mode with a *forward* voltage across the junction, the diode has a *large* C_i dominated by the <u>diffusion capacitance</u> C_d .
- □ It still has a large R_i , though smaller than that in the photoconductive mode.

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Frequency response of the equivalent circuit

- □ The **frequency response** of the equivalent circuit is determined by
 - The *internal* resistance R_i and capacitance C_i of the photodiode
 - The *parasitic* effects characterized by R_s , C_p , and L_S
 - \blacksquare The *load* resistance R_L
- □ The *parasitic effects must be eliminated* as much as possible.
- □ A high-speed photodiode normally operates under the condition that $R_i >> R_L$, R_s .
 => equivalent resistance $\approx R_L$
- In the simple case, when the parasitic inductance/capacitance are negligible, the speed of the circuit is dictated by the RC time constant $\tau_{RC} = R_L C_i$.

RC-time-limited bandwidth

e.g. In a silicon photodiode with $W=1~\mu m$ driven at saturation drift velocity,

$$\tau_{tr} \approx 10^{-4} \text{ cm}/10^7 \text{ cm s}^{-1} \approx 10 \text{ ps}$$

Suppose, the diode capacitance = 1 pF and a load resistance of 50Ω ,

$$\tau_{\rm RC} \approx 50 \, \rm ps$$

$$\Rightarrow$$
 $f_{3dB} \approx 1/2\pi\tau_{RC} \approx 3.2 \text{ GHz}$

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