

Indian Institute of Technology
PH205 (Nov 2023)
End-semester Examination

Full marks: 50

Time: 3 hours

Section I: Write the answer(s) for each question in your answer script. Each question carry one mark.

1. In a doped semiconductor sample of cross-sectional area A and length L , the doping density, N_D , varies with distance (x) as $N_D(x) = N_0 \exp\left(-\frac{x}{L}\right)$, where N_0 is a constant. Assuming that the mobility μ of the majority carrier remains constant, the electrical conductivity (σ) of the sample is given by (expression) $\sigma = \dots\dots\dots$

2. The energy $E(\mathbf{k})$ of electrons of wave vector \mathbf{k} in a solid is given by $E(\mathbf{k}) = A\mathbf{k}^2 + B\mathbf{k}^4$, where A and B are constants. The effective mass (m^*) of the electron at $|\mathbf{k}| = k_0$ is given by $m^* = \dots\dots\dots$

3. When the PN junction is forward biased, the sequence of events (among diffusion, drift, injection and recombination) that take place are:

(a) $\dots\dots\dots$, (b) $\dots\dots\dots$, (c) $\dots\dots\dots$

4. The junction capacitance (C) of linearly graded p-n junction varies with the applied reverse bias, V_R , as $C \propto \dots\dots\dots$

5. A GaAs LED emits light in the $\dots\dots\dots$ region and GaN emits light in the $\dots\dots\dots$ region of spectrum.

6. The sensitivity of a photo diode depends on parameters, such as : $\dots\dots\dots$, $\dots\dots\dots$

7. Match items in Group I with items in Group II, most suitably.

Group I

P. LED Q. Avalanche Photodiode R. tunnel diode S. LASER

Group II

1. Heavy doping, 2. Coherent radiation, 3. Spontaneous emission, 4. Current gain

P - $\dots\dots\dots$, Q - $\dots\dots\dots$, R - $\dots\dots\dots$, S - $\dots\dots\dots$

8. Given that for GaAs, bandgap $E_g = 1.43$ eV, and for AlAs, $E_g = 2.75$ eV, using virtual crystal approximation, the bandgap of $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ alloy will be

$E_{g, \text{ alloy}} = \dots\dots\dots$ eV

9. Construction wise, MOSFETs can be categorized into four types as follows:

(a) $\dots\dots\dots$ (b) $\dots\dots\dots$
(c) $\dots\dots\dots$ (d) $\dots\dots\dots$

10. Transconductance (g) of a JFET is defined as (formula): $g = \dots\dots\dots$ and its unit is $\dots\dots\dots$

Section 2

11. A semiconductor sample is n-type doped. Briefly describe an experimental technique with schematic to determine its bandgap energy (E_g) and the donor energy level (E_D). Use a graphical method for the determination of E_g and E_D . [3]
12. Draw the schematic diagram of a quantum well laser for low threshold operation and briefly explain its working principle. [2+2]
13. The absorption coefficient near the band-edge of Si is $\sim 10^3 \text{ cm}^{-1}$. What is the minimum thickness (in cm unit) of a sample that can absorb 90% of the incident light? [3]
14. In a p-type GaAs sample, electrons are injected from a contact. If the electron mobility is $4000 \text{ cm}^2/\text{V-s}$ at 300K, calculate the diffusion length for electrons. Take recombination time as 0.6 ns. [3]
15. A Si diode is being used as a thermometer by operating it at a fixed forward (bias) current. The voltage is then a measure of the temperature. At 300K, the diode voltage is found to be 0.6V. How much will be the *voltage change* if the temperature changes by 1 K? [4]
16. Consider a semiconductor laser having an optical confinement factor of unity. If the threshold carrier density is $1.32 \times 10^{18} \text{ cm}^{-3}$ and the active layer thickness is $20 \mu\text{m}$, calculate the threshold current density (J_{th}) for the lasing action to start. Assume a radiative recombination time of 2.4 ns. [3]
17. A Schottky barrier is formed between a metal having a work function of 4.3 eV and p-type Si (electron affinity $\chi = 4 \text{ eV}$). The acceptor doping in the Si is $10^{17} / \text{cm}^3$. (a) Calculate the work function of the semiconductor (ϕ_s). (b) Draw the equilibrium band diagram, showing numerical value of qV_0 . [3+2]
18. Consider a Si solar cell with area = 1 cm^2 , acceptor doping density = $5 \times 10^{17} \text{ cm}^{-3}$, donor doping density = 10^{16} cm^{-3} and photocurrent of 25 mA. If $D_n = 20 \text{ cm}^2/\text{s}$, $D_p = 10 \text{ cm}^2/\text{s}$, $\tau_n = 3 \times 10^{-7} \text{ s}$, $\tau_p = 10^{-7} \text{ s}$, calculate the open circuit voltage (V_{oc}) of the solar cell operated at 300K. [4]
19. Consider a GaAs p-n LED with the p-region on the top to emit light, and $D_n = 30 \text{ cm}^2/\text{s}$, $D_p = 15 \text{ cm}^2/\text{s}$, $N_a = 5 \times 10^{16} \text{ cm}^{-3}$ and $N_d = 5 \times 10^{17} \text{ cm}^{-3}$, $\tau_n = 10 \text{ ns}$, $\tau_p = 100 \text{ ns}$. Calculate the diode injection efficiency (γ_{inj}). [3]
20. A Si p-n junction with cross-sectional area, $A = 0.001 \text{ cm}^2$ is formed with $N_a = 10^{15} \text{ cm}^{-3}$, $N_d = 10^{17} \text{ cm}^{-3}$. Calculate (a) built-in potential, V_0 , (b) current I with a forward bias of 0.5 V. Assume that the current is diffusion dominated. Assume $\mu_n = 1500 \text{ cm}^2/\text{V-s}$, $\mu_p = 450 \text{ cm}^2/\text{V-s}$, $\tau_n = \tau_p = 2.5 \mu\text{s}$. [2+3]
21. For the given circuit below for a Si NPN transistor with $\beta = 100$, calculate the I_B , I_C and V_{CE} . [3]

Useful Formula:

$$\gamma_{inj} = \frac{J_n}{J_n + J_p}, \quad L_n = \sqrt{D_n \tau_n}, \quad J_n = \frac{e D_n n_p}{L_n}$$

$$V_{oc} = \frac{mkT}{e} \ln\left(1 + \frac{I_L}{I_0}\right), \quad I_0 = A \left[\frac{e D_n n_p}{L_n} + \frac{e D_p p_n}{L_p} \right]$$

$$\alpha_{loss} = -\frac{1}{L} \ln R, \quad R = \frac{(n_2 - n_1)^2}{(n_2 + n_1)^2}, \quad n_{th} = \frac{J_{th} \tau_r}{e d_{laser}}$$

$$I = I_0 \left[\exp\left(\frac{eV}{kT}\right) - 1 \right]$$

$$n_i = 1.5 \times 10^{10} / \text{cc for Si}$$

$$V_0 = \frac{kT}{e} \ln\left(\frac{N_a N_d}{n_i^2}\right)$$

