

Digital Image Processing (MCS-80L)

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Unit - 1

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Introduction & Fundamentals

Motivation & Perspective, Applications, Component of image processing system, Element of visual perception, A simple image model, sampling & Quantization.

Image Enhancement in Frequency Domain

Fourier transform and the Frequency Domain, Basis of filtering in frequency domain, Filters - Low pass, High pass; correspondence b/w filtering in spatial & frequency domain
smoothing Frequency Domain filters - Gaussian low pass filters; sharpening Frequency Domain filters - Gaussian Highpass filters; Homomorphic filtering

Image:

An image is defined as 2D function, $f(x, y)$, where x & y are spatial (plane) coordinates, and the amplitude of f at any pair of coordinates (x, y) is called the intensity or gray level of the image at that point.

When x, y and the amplitude values of f are all finite, discrete quantities, then the image is known as digital image.

The processing of digital image by means of computer refers to Digital image processing.

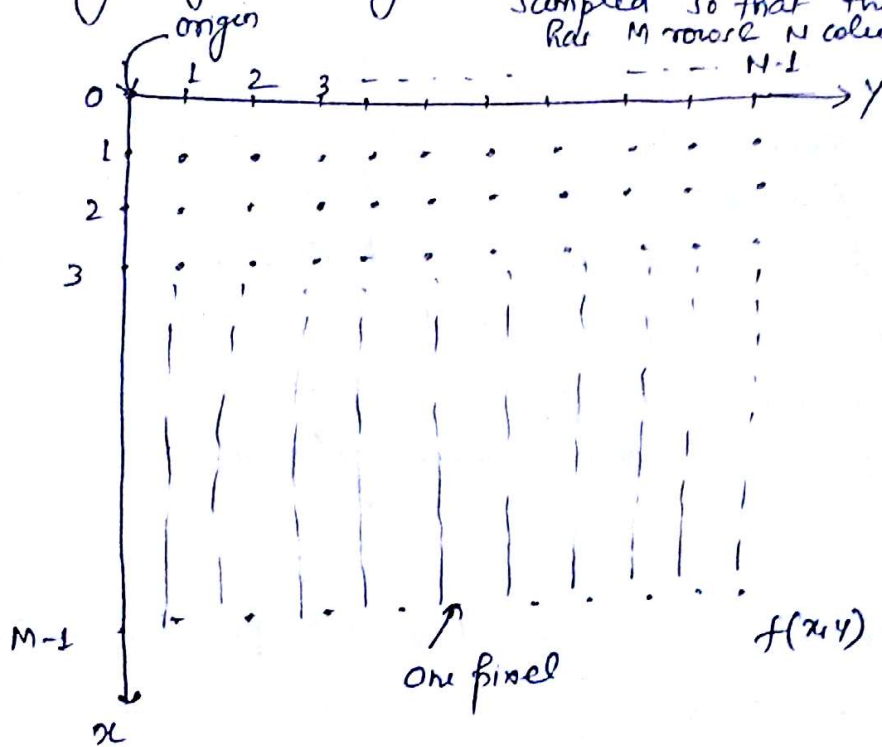
NOTE:

A digital image is composed of a finite number of elements, each of which has a particular location and values. These elements are referred to as picture elements, image elements, pels and pixels.

Pixel is the smallest unit of the digital image.

Representing Digital images:

Assume that an image $f(x,y)$ is sampled so that the resulting image has M rows & N columns.



Coordinate convention used to represent digital image

spatial coordinates that uses x to refer to columns & y to refer to rows.

Image as matrices:

$$f(x,y) = \begin{bmatrix} f(0,0) & f(0,1) & \dots & f(0,N-1) \\ f(1,0) & f(1,1) & \dots & f(1,N-1) \\ \vdots & \vdots & \ddots & \vdots \\ f(M-1,0) & f(M-1,1) & \dots & f(M-1,N-1) \end{bmatrix}$$

The right side of this eqn is a digital image by definition.

each element of this array is called an image element, or pixel.

Digital image representation as a MATLAB matrix.

$$f = \begin{bmatrix} f(1,1) & f(1,2) & \dots & f(1,N) \\ f(2,1) & f(2,2) & \dots & f(2,N) \\ \vdots & \vdots & \ddots & \vdots \\ f(M,1) & f(M,2) & \dots & f(M,N) \end{bmatrix}$$

MATLAB functions :

Read the image : `imread('filename')`

`>> f = imread('deepak.jpg');`

← read the image from JPEG file into image array f
Beginning of command line

Display the image

`imshow(f)`

To keep the first image & o/p a second image use function

`>> figure, imshow(g)`

Write the image : Images are written to the current directory

using function `imwrite`,

`imwrite(f, 'filename')`

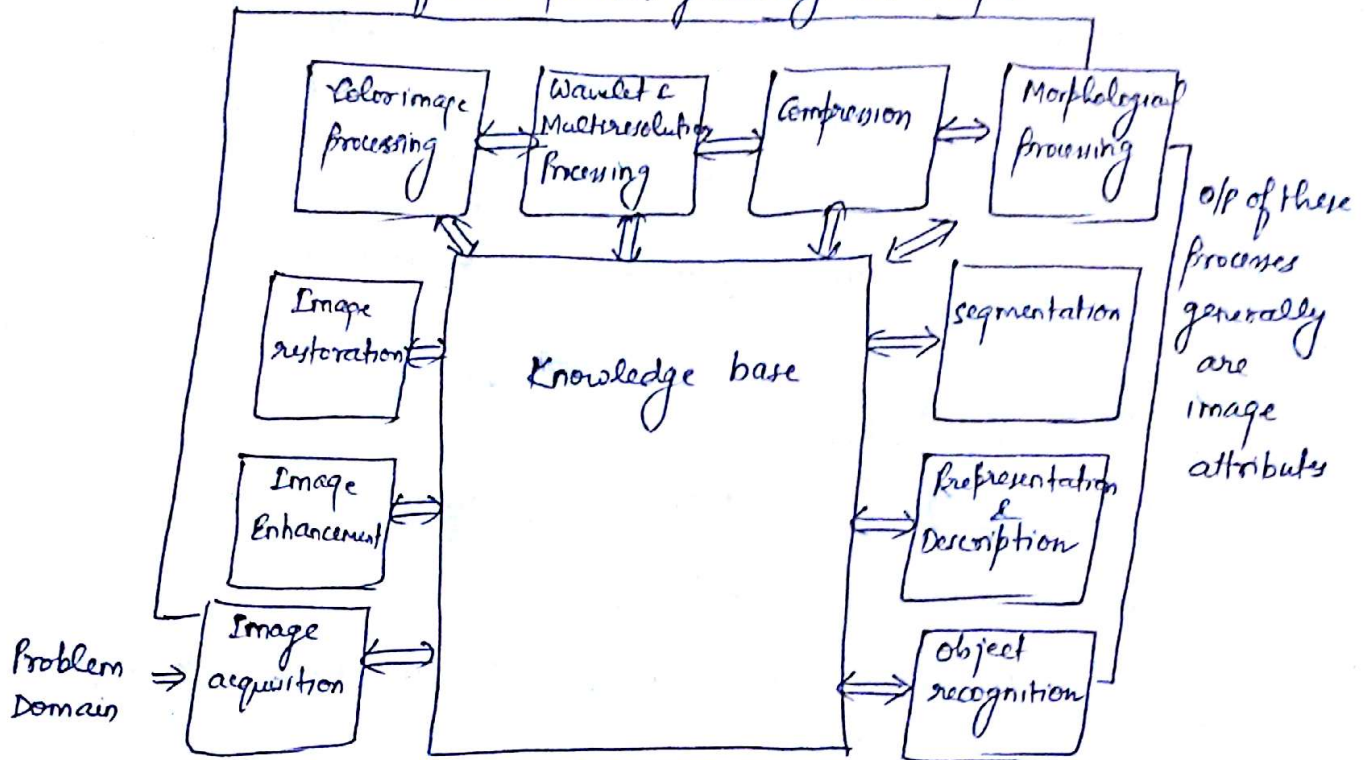
`imwrite(f, 'filename.jpg', 'quality', q)`

$q = 0 \text{ to } 100$

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Fundamental steps of Digital image processing:

O/P of these processes generally are images



Wavelet & multiresolution processing:

wavelets are the foundation for representing images in various degrees of resolution.

Morphological processing: It deals with tools for extracting image components that are useful in the representation & description of shape.

Recognition: It is the process that assigns a label (vehicle) to an object based on its descriptions.

Components of an image processing system:

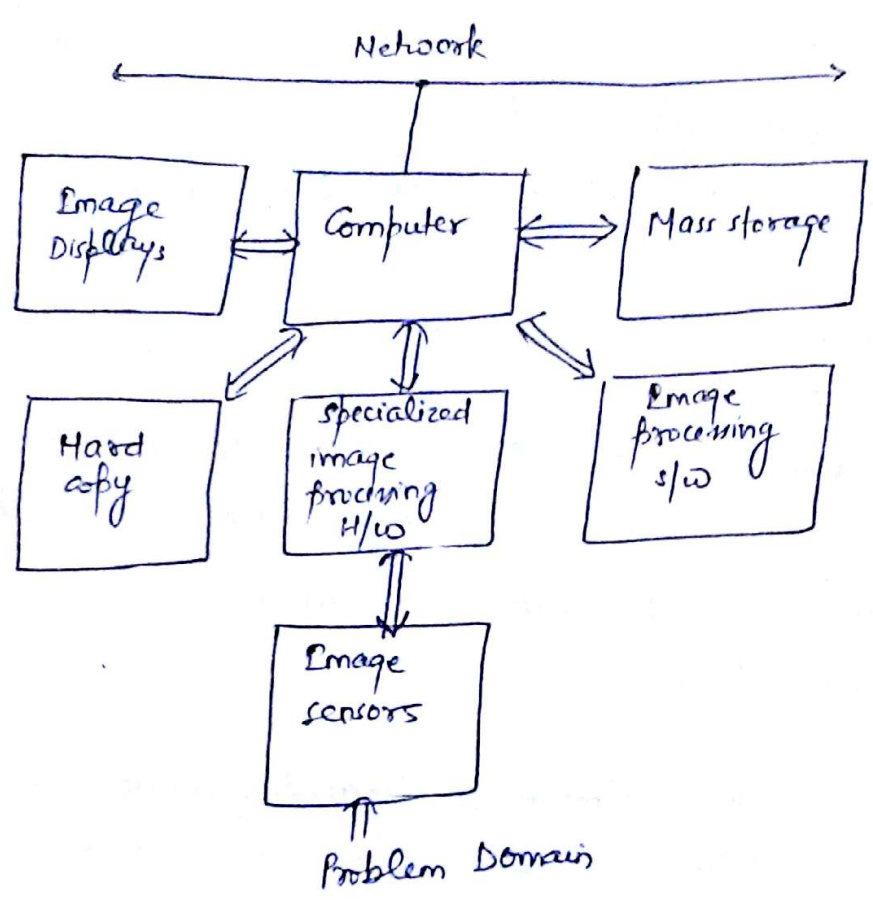


Image processing H/w It consist of digitizer plus H/w that performs other primitive operations such as an arithmetic logic unit (ALU) which perform arithmetic & logical operations in parallel on entire images. ex: image averaging as quickly as image digitized, for the purpose of noise reduction

Computer < General purpose computer (range from pc to a supercomputer)
 < specially designed computer

s/w It consist of specialized modules that perform specific tasks. A well designed package also include the capability for the user to write code that, as a minimum, utilizes the specialized modules

Mass storage : Digital storage for image processing application falls into 3 principal categories-

Short term storage for use during processing
Online storage for relatively fast re-call
Archival storage, characterized by infrequent access.

Image display : Color TV monitors

Hard copy devices : For recording images include laser printers, film cameras, heat sensitive devices, ~~inkjet~~ inkjet units, & digital units such as optical & CD Rom. disks.

Networking : It is almost a default function in any computer system. Because the large amount of data inherent in image processing applications, the key consideration in image transmission is bandwidth.

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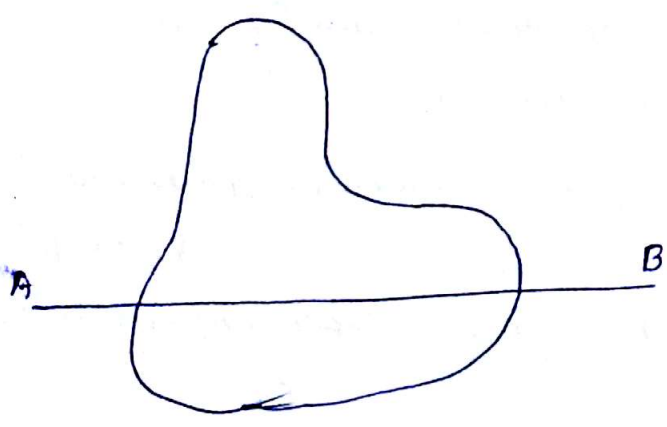
Image sampling and quantization process :-

The o/p of most sensor is a continuous voltage waveform whose amplitude and spatial behavior are related to physical phenomenon being sensed.

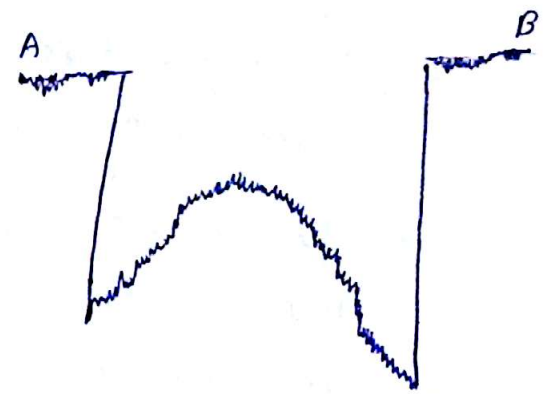
To create a digital image, we need to convert the continuous sensed data into digital form. this involve two processes-

- sampling (Digitizing the coordinate values)
- Quantization (Digitizing the amplitude values)

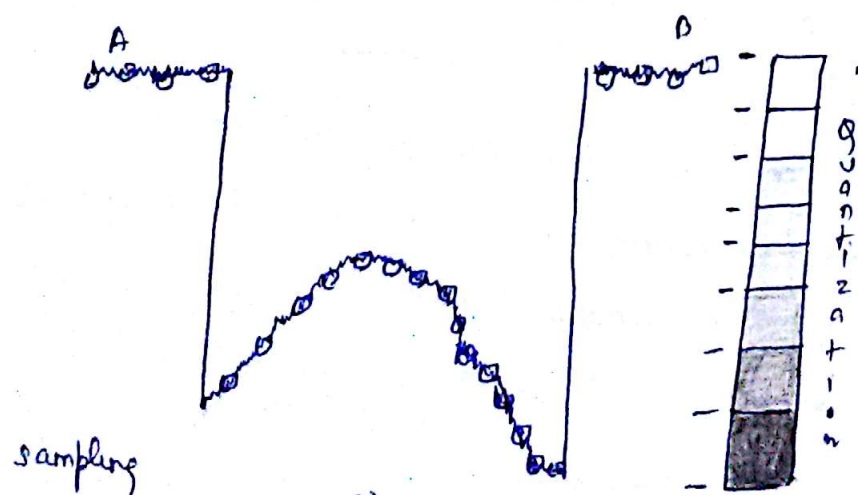
Basic concept in sampling & Quantization:



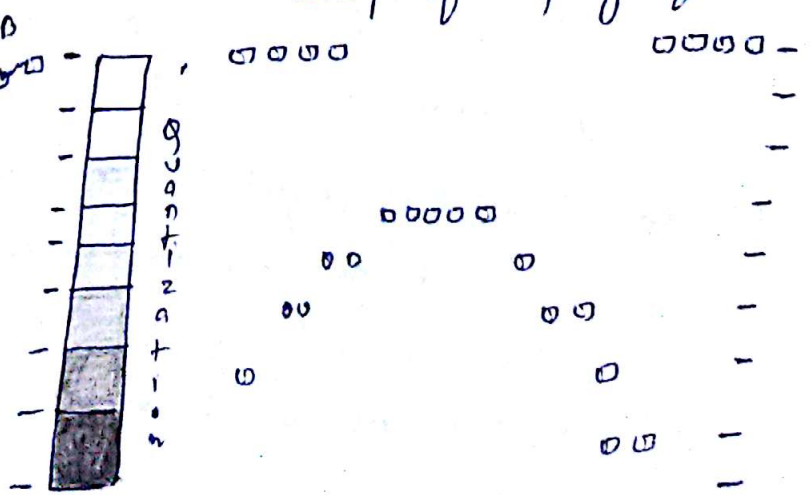
(a) Continuous image



(b) Scan line from A to B in continuous image, used to illustrate the concept of sampling & quantization.



(c) Sampling & Quantization



(d) Digital scan line

fig(a) shows continuous ~~an~~ image along the line segment AB

fig(a) shows a continuous image, $f(x, y)$, that we want to convert to digital form. To convert it to digital form, we have to sample the function in both coordinates and in amplitude.

- ⇒ { Digitizing the coordinate values is called sampling.
Digitizing the amplitude values is called quantization
- ⇒ 1-D function shown in (b) is a plot of amplitude (gray level) values of the continuous image along the line segment AB. The random variation are due to noise.
- ⇒ To sample this function, we take equally spaced samples along line AB as shown in (c).
- ⇒ The location of each sample is given by a vertical tick mark in the bottom part of the figure. The samples are shown as small white squares superimposed on the the function.
- ⇒ The set of these discrete locations gives the sampled function. However the values of the samples still span (vertically) a continuous range of gray level values.
- ⇒ To form a digital function, the gray level values also must be converted (quantized) into discrete quantities. The right side of fig(c) shows the gray level scale divided into 8 discrete levels ranging from black to white.

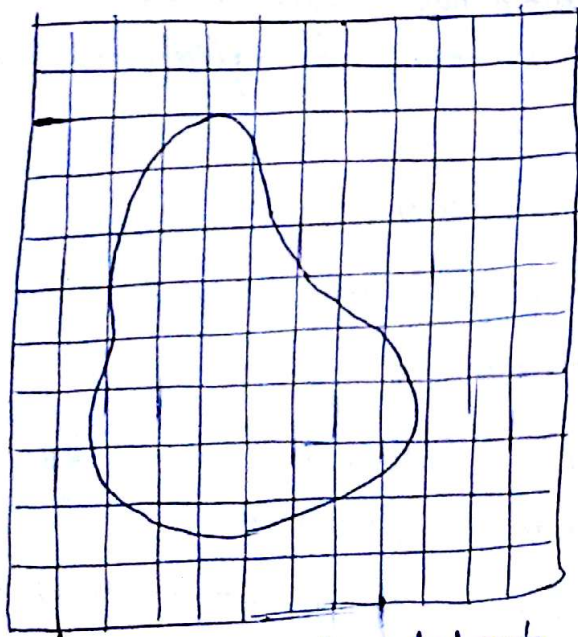
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⇒ The vertical tick mark indicate the specific value assigned to each of the 8 gray levels. The continuous gray levels are quantized simply by assigning one of the 8 discrete levels to each sample.

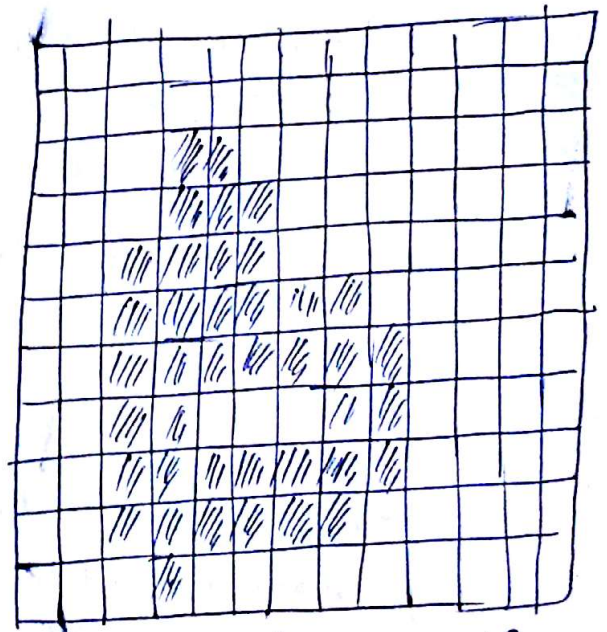
⇒ The assignment is made depending on vertical proximity of a sample to a vertical tick mark.

The digital samples resulting from both sampling & quantization are shown in fig (d).

Starting at the top of image and carrying out this procedure line by line produces a 2-D digital image.



a) Continuous image projected onto a sensor array



b) Result of image sampling & quantization

Simple image model :-

An image can be represented by 2D functions of the form $f(x, y)$. The value of f is known as amplitude or intensity.

When an image is generated from a physical process, its intensity values are proportional to energy radiated by a physical source (eg Electromagnetic waves).

$f(x, y)$ must be non zero and finite, i.e.

$$0 < f(x, y) < \infty \quad \text{--- ①}$$

The function $f(x, y)$ may be characterized by two components

- 1) The amount of source illumination incident on the scene being viewed. This is known as illumination component $i(x, y)$.
- 2) The amount of illumination reflected by the objects in the scene. This is known as reflectance component $r(x, y)$.

$$\text{so } f(x, y) = i(x, y) r(x, y)$$

$$\text{where } i: 0 < i(x, y) < \infty \quad \text{--- ②}$$

$$r: 0 < r(x, y) < 1 \quad \text{--- ③}$$

eqn ③ indicates that reflectance is bounded by 0 (total absorption) and 1 (total reflectance).

$i(x, y)$ is determined by the illumination source and $r(x, y)$ is determined by the characteristics of the imaged objects.

This expression also applicable to images formed via transmission of the illumination through a medium such as chest X ray.

In this we would deal with transmissivity instead of reflectivity function, but the limits would be the same.

Let the intensity (gray level) of a monochrome image at any coordinates (x_0, y_0) be denoted by

$$l = f(x_0, y_0)$$

l lies in the range

$$L_{\min} \leq l \leq L_{\max}$$

$$\text{in theory } \left. \begin{array}{l} L_{\min} > 0 \\ L_{\max} < \infty \end{array} \right\}$$

$$\text{in practical } L_{\min} = l_{\min} \eta_{\min}$$

$$L_{\max} = l_{\max} \eta_{\max}$$

for office illumination

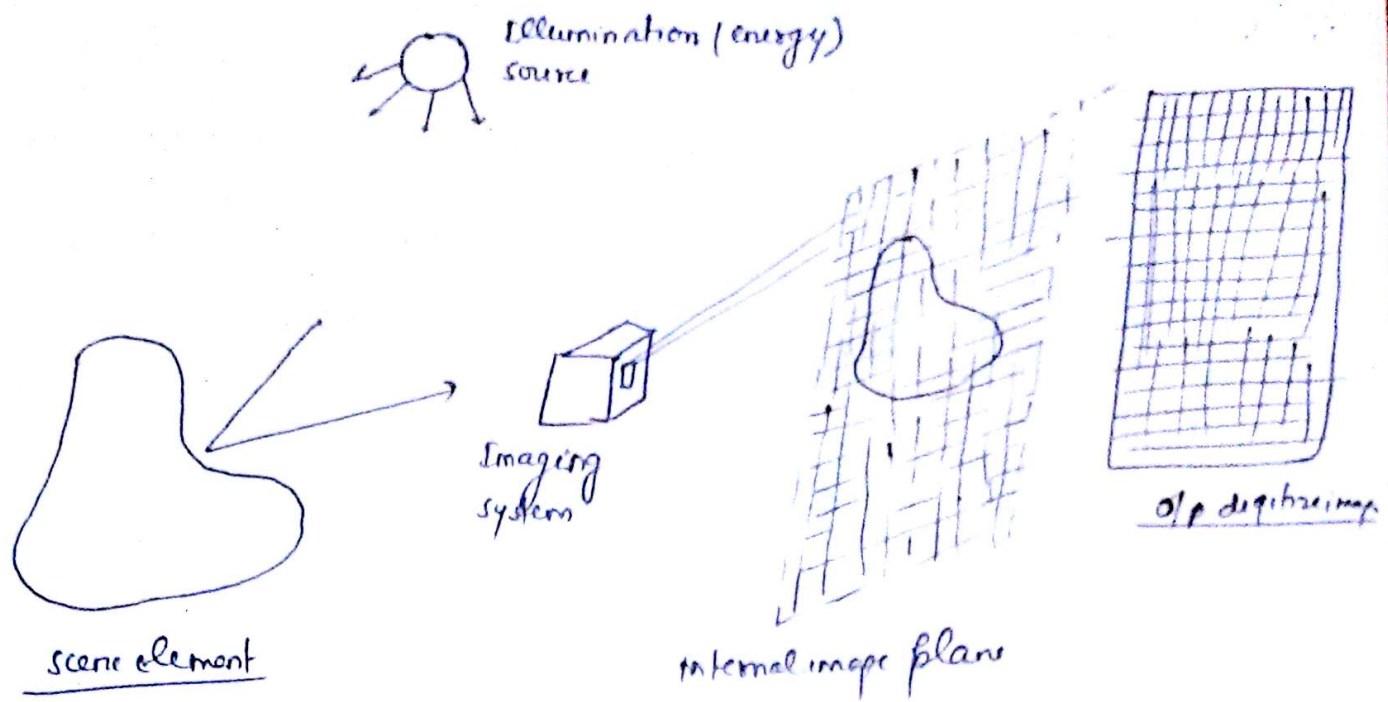
$$\left. \begin{array}{l} L_{\min} \approx 10 \\ L_{\max} \approx 1000 \end{array} \right\} \text{ limit for indoor value in absence of additional illumination}$$

* Illumination level in commercial office is about 1000 lm/m^2

$$L = f(x, y) =$$

The interval $[L_{\min}, L_{\max}]$ is called the grayscale.

Elements of visual perception :-



Digital image acquisition

Elements of visual perception :-

- ① Structure of the Human Eye
- ② Image formation in the eye
- ③ Brightness adaptation & Discrimination

Que. If we want to resize a 1024×768 image to one that is 600 pixel wide with the same aspect ratio as the original image, what should be the height of the resize image?

$$\text{Aspect ratio} = \frac{\text{width}}{\text{Height}} \Rightarrow \frac{1024}{768} = 1.33$$

$$\begin{aligned} \text{Height} &= \frac{\text{width}}{\text{Aspect ratio}} = \frac{600}{1.33} \\ &= 451 \end{aligned}$$

resized image will be 600×451

Que. A common measure of transmission for digital data is the baud rate, defined as the number of bits transmitted per second. Transmission is accomplished in packets consisting of a start bit, a byte (8 bits) of information and a stop bit

- How many minutes would it take to transmit a 1024×1024 image with 256 gray levels if we use a 56K baud modem?
- What would be the time required if we use a 750K baud transmission line?

Physical Resolution :

The number of pixels per unit length is referred to as the resolution of the displaying device.

Thus 3x2 inch image at a resolution of 300 pixels per inch would have total no. of pixels

$$(3 \times 300) \times (2 \times 300)$$

$$= 900 \times 600$$

$$= 540000 \text{ pixels}$$

$$\begin{array}{lcl} \text{Image size} = & \begin{array}{cc} \text{width} & \text{Height} \\ 1024 & \times 1024 \end{array} & \begin{array}{l} \text{Total no. of pixels in} \\ \text{vertical direction} \end{array} \\ & \downarrow & \\ & \text{Total no. of pixels in Horizontal direction} & \end{array}$$

Aspect ratio :

The ratio of the image's width to its height, measured in unit length or number of pixels is referred to as its aspect ratio.

Ex: 3x3 inch or 128x128 image have the aspect ratio 1

$$\boxed{\text{Aspect ratio} = \frac{\text{width}}{\text{Height}}}$$

Que.

Compute the physical size of a 640 x 480 image when printed by a printer at 240 pixels per inch

$$\left\{ \frac{640}{240} \text{ by } \frac{480}{240} \right\}$$

Soln

256 gray levels, we need 8 bits for representing each pixel.

along 8 bits, we also have a start bit & stop bit

Hence we have 10 bits per pixel.

Total no. of bits for transmission are

$$N = 1024 \times 1024 \times 10 \\ = 10485760 \text{ bits}$$

These bits are transmitted at 56 K baud rate.

In 1 sec ——— 56 K bits

re 56 K bits ——— = 1 sec

$$\therefore 1 \text{ ———} = \frac{1}{56K}$$

$$\therefore 10485760 \text{ ———} = \frac{1}{56K} \times 10485760$$

$$\Rightarrow 187.25 \text{ sec} \approx 3.1 \text{ minutes}$$

(b)

if the baud rate is 750 K

$$\text{then time} = \frac{10485760}{750K} = \frac{10485760}{750 \times 10^3} \\ \Rightarrow 13.90 \text{ sec}$$