

## Operation Research

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Q. A Company has a current shipping schedule, which is being questioned by the management. as to whether or not it is optimal. The firm has 3 factories & 4 warehouse. The necessary data in terms of transportation cost in  $\pi$  per unit from a factory to a destination  $f$  factory capacities  $f$  warehouse requirements are as follows.

Warehouse	$w_1$	$w_2$	$w_3$	$w_4$	Requirement
factory					
$F_1$	19	30	50	10	720
$F_2$	40	30	40	60	900
$F_3$	40	<del>20</del>	70	20	1800
Capacity	500	800	700	1400	

Solve for a basic feasible shipping schedule in terms of lowest possible shipping cost.

Sol<sup>n</sup> As  $\sum \text{Capacity} = \sum \text{Requirements}$  The above problem is balanced.

We will use Vogel's Approximation Method to solve the above problem.

$$\begin{aligned} \text{Requirements} &= 700 + 900 + 1800 = 3400 \\ \text{Capacity} &= 500 + 800 + 700 + 1400 = 3400 \end{aligned}$$

### Iteration 1:-

Warehouse factory	W1	W2	W3	W4	Requirements	Penal
$f_1$	19	30	50	10	700	9
$f_2$	40	30	40	60	900	10
$f_3$	40	80	70	20	1000	12
Capacity	500	800	700	1400	3400	-
penalties	21	22	10	10	-	-

### Iteration 2:-

Warehouse factory	W1	W3	W4	Requirements	Penalties
$f_1$	19	50	10	700, 200	9
$f_2$	40	40	60	900	20
$f_3$	40	70	20	1000	20
Capacity penalties	500	700	1400	2400	-
penalties	21	10	10	-	-

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### Iteration 3:-

warehouse factory	W3	W4	Requirements	Penalties
$f_1$	50	10	200	40
$f_2$	40	60	700	20
$f_3$	70	20	1000	50 ←
Capacity penalties	700	1400	2100	-
penalties	10	10	-	-

### Iteration 4:-

Warehouse factory	W3	W4	Requirements	
$f_2$	40	60	900	-
Capacity	700	200	900	-
penalties	-	-	-	-



Iteration 5:-

Warehouse	W3	W4	
factory			
$F_2$	40	60	9000
Capacity	700	200	1900
Penalties			

Iteration 5:-

Warehouse	W3	W4	Requirement
factory			
$F_2$	40	60	9000
Capacity	700	200	1900
Penalties			

Warehouse	W1	W2	W3	W4	Requirement
Factory					
$F_1$	19	30	50	10	70
$F_2$	40	30	40	60	90
$F_3$	40	2	70	20	180
Capacity	500	800	700	1400	

$$\begin{aligned}
 \text{Total cost} &= 19 \times 500 + 10 \times 200 + 40 \times 700 + 60 \times 200 \\
 &\quad + 8 \times 300 + 20 \times 1000 \\
 &= 9500 + 2000 + 2800 + 12000 + 6400 \\
 &\quad + 2000 \\
 &= 52700
 \end{aligned}$$