

Roland Carter
CSC 376
Chapter 11

Part I	Present state				Next state			
	a	b	c	d	a	b	c	d
9	1	0	0	1	1	0	0	0
8	1	0	0	0	0	1	1	1
7	0	1	1	1	0	1	1	0
6	0	1	1	0	0	1	0	1
5	0	1	0	1	0	1	0	0
4	0	1	0	0	0	0	1	1
3	0	0	1	1	0	0	1	0
2	0	0	1	0	0	0	0	1
1	0	0	0	1	0	0	0	0
0	0	0	0	0	1	0	1	0
10	1	0	1	0	1	0	1	1
11	1	0	1	1	1	1	0	0
12	1	1	0	0	1	0	0	1

← sorry for the misalignment, it was easier to write up

D_A

AB \ CD	00	01	11	10
00	1	0	0	0
01	0	0	0	0
11	1	x	x	x
10	0	1	1	1

$$D_A = \bar{A}\bar{B}\bar{C}\bar{D} + ABC + AD + AC$$

D_B

AB \ CD	00	01	11	10
00	0	0	0	0
01	0	1	1	1
11	0	x	x	x
10	1	0	1	0

$$D_B = BD + BC + ACD + \bar{A}\bar{B}\bar{C}\bar{D}$$

D_C

AB \ CD	00	01	11	10
00	1	0	1	0
01	1	0	1	0
11	0	x	x	x
10	1	0	0	1

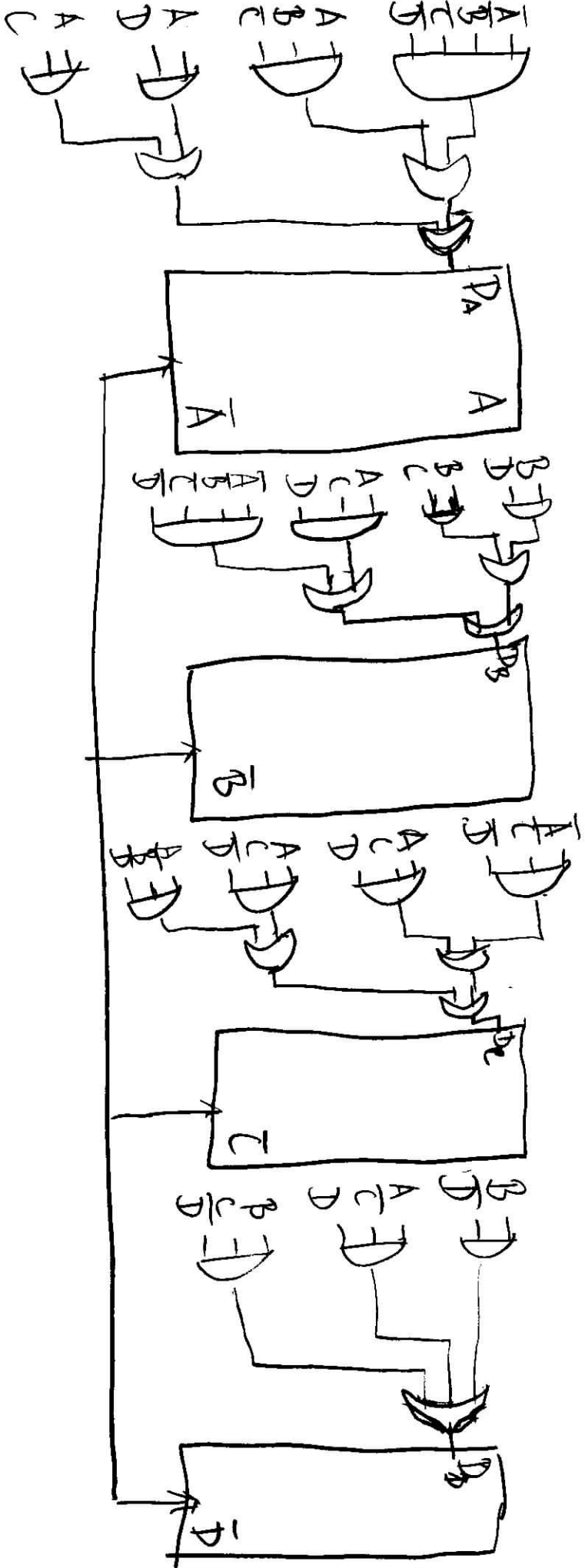
$$D_C = \bar{A}\bar{C}\bar{D} + ACD + AC\bar{D} + A\bar{B}\bar{D}$$

D_D

AB \ CD	00	01	11	10
00	0	0	0	1
01	1	0	0	1
11	1	x	x	x
10	1	0	0	0

$$D_D = B\bar{D} + A\bar{C}\bar{D} + B\bar{C}\bar{D}$$

Circuit Diagram



Part II

A ₁	A ₀	B ₁	B ₀	Q ₁	Q ₀	R ₁	R ₀	E
0	0	0	0	x	x	x	x	1
0	0	0	1	0	0	0	0	0
0	0	1	0	0	0	0	0	0
0	0	1	1	0	0	0	0	0
0	1	0	0	x	x	x	x	1
0	1	0	1	0	1	0	0	0
0	1	1	0	0	0	0	1	0
0	1	1	1	0	0	0	1	0
1	0	0	0	x	x	x	x	1
1	0	0	1	1	0	0	0	0
1	0	1	0	0	1	0	0	0
1	0	1	1	0	0	1	0	0
1	1	0	0	x	x	x	x	1
1	1	0	1	1	1	0	0	0
1	1	1	0	0	1	0	1	0
1	1	1	1	0	1	0	0	0

$E = B_1 B_0$

$A_1 A_0$	$B_1 B_0$	00	01	11	10
00	1	1	0	0	0
01	1	1	0	0	0
11	1	1	0	0	0
10	1	1	0	0	0

$Q = A_1 + \bar{B}_1$

$A_1 A_0$	$B_1 B_0$	00	01	11	10
00	X	0	0	0	0
01	X	0	0	0	0
11	X	1	0	0	0
10	X	1	0	0	0

$Q_0 = A_1 A_0 + A_0 \bar{B}_1 + A_1 B_1 \bar{B}_0$

$A_1 A_0$	$B_1 B_0$	00	01	11	10
00	X	0	0	0	0
01	X	1	0	0	0
11	X	1	1	1	1
10	X	0	0	1	1

$R_1 = A_1 \bar{A}_0 B_1 B_0$

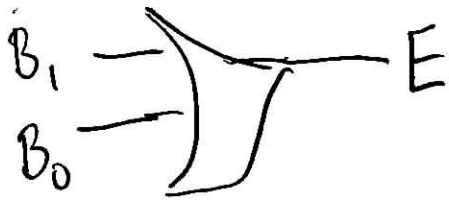
$A_1 A_0$	$B_1 B_0$	00	01	11	10
00	X	0	0	0	0
01	X	0	0	0	0
11	X	0	0	0	0
10	X	0	1	1	1

R_2 ~~B_2~~

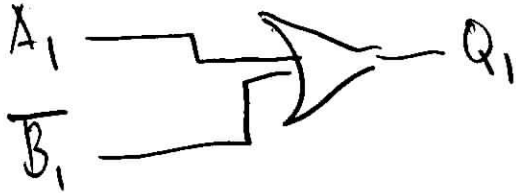
$A_1 A_0$	00	01	11	10
00	x	0	x	0
01	x	0	1	1
11	x	0	0	1
10	x	0	0	0

$$R_2 = \overline{A_1} A_0 B_1 + A_0 B_1 B_0$$

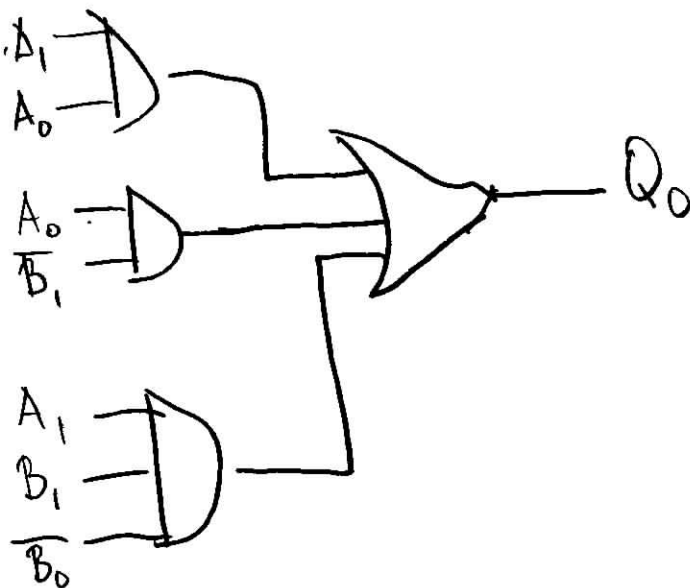
E.)



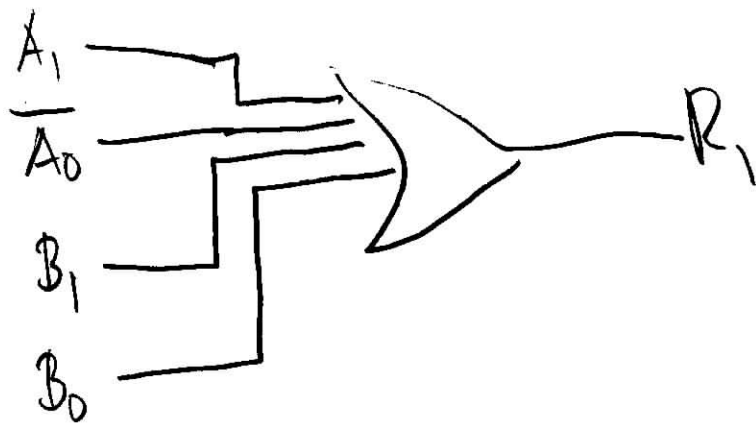
Q_1)



Q_0 .)



Q₁)



Q₂)

