

26/05/23

DAY 5:

## I. Machine Learning

Applications

(sound/speech recognition)

↳ +vs voltage wave.

(emotions, accent, speed detected)

of an AI system: (FEATURE EXTRACTION)

written problem vs expected outcome

↓  
this accuracy is very high.

naturally → no idea how its done.

$$y = f(x)$$

learn f  
code f

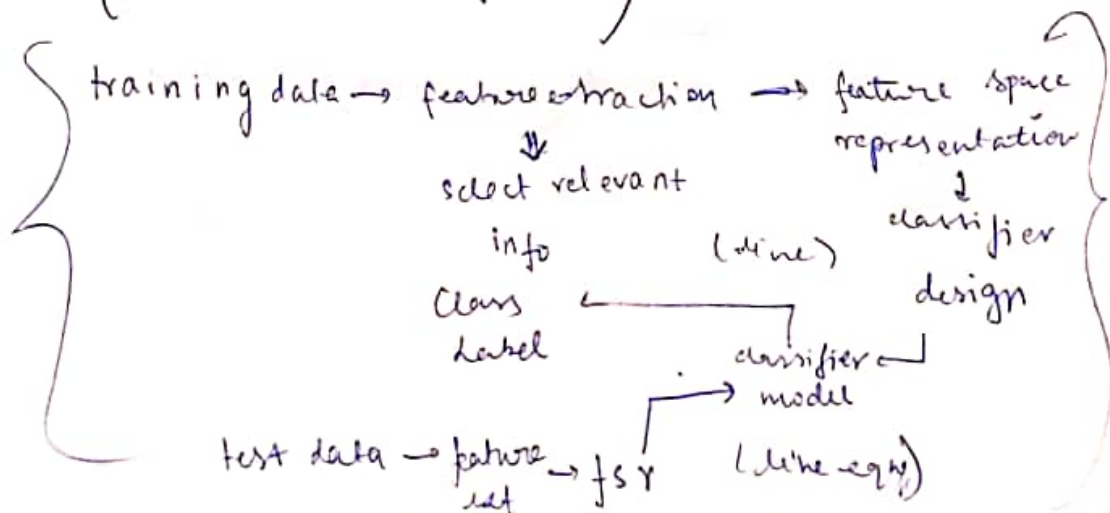
Classification → int y

clustering → unsupervised.

Regression → real no. f

Time series prediction → eg. predict future weather based on past 5 days

\* (formulate real world problem) \*



not correctness, its accuracy  
imp.

either decide an eqn that divides | fit a model for different  
generative | discriminative. classes.

1) Classifier - k-NN (find k nearest neighbours  
image  $\rightarrow$  feature vector  
 $\rightarrow$  most common class is the answer)  
(majority)  
most frequent label.

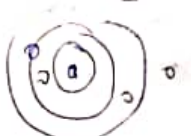
for multiple classes  $\rightarrow$  voronoi tessellation. (between nearest neighbours)  
piecewise linear boundary  $\rightarrow$  final product.  
(course  $\perp$  bisector)

sklearn.neighbors.

Training is trivial. (no learning effectively).

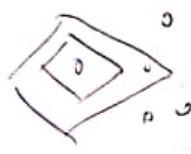
\* Bayesian classifier known to be most ideal

what is nearest (theoretical proof)

L2 1) Euclidean Distance  $\rightarrow \sum (x_1 - x_2)^2$   
iso surfaces  $\rightarrow$   } draw circles.

L1 2) Manhattan distance (no sq.).

$\sum |x_1 - x_2|$   
iso surface

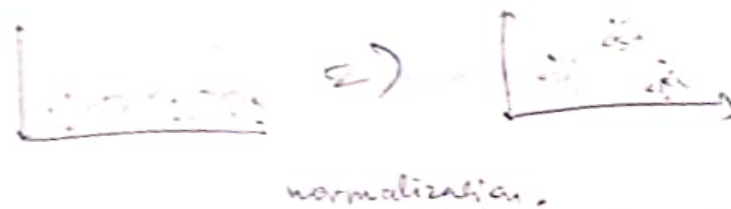
 } draw rhombus.

L0 distance?

3) Minkowski dist  
 $\sum (x_1 - x_2)^r$

$r = 2 = \bigcirc$   $r = \infty = \square$   
 $r = 1 = \diamond$   
 $r = 1.25 = \text{rounded diamond}$

if features have different variances  
 ↳ some feature will dominate  
 ↳ so req. to normalize.



normalization.

4) Mahalanobis Dist.

$$d(P, Q) = (P - Q)^T S^{-1} (P - Q)$$

weight distance for  $\frac{1}{2}$  accounting for features that change less/more.

5) Hamming distance.

(binary vectors)

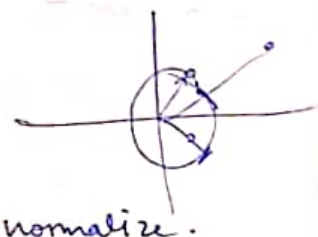
$$d(P, Q) = \sum I(P_i \neq Q_i)$$

↳ Indicator funct. (T=1, F=0)

6) cosine distance

$$d(P, Q) = \cos \theta = \frac{\vec{P} \cdot \vec{Q}}{\|\vec{P}\| \|\vec{Q}\|} = \frac{P \cdot Q}{\|P\| \cdot \|Q\|}$$

(hypersphere - 4D+)



normalize.



feature vectors need not  
 be of same length.

non metric, edit, jaccard dist.

## ② Linear Classifier

linear decision boundaries.

pt, line, plane, hyperplane.

$$w_1 + w_2 x_1 + w_3 x_2 - \dots - w_d x_d = 0$$

(d dimension-space line).

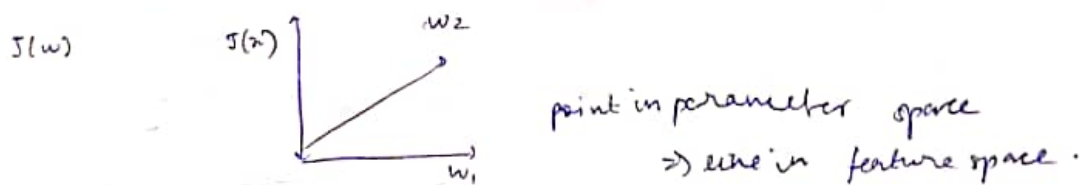
$$f(x) = 0.$$

goal  $\rightarrow$  learn parameters  $w_i$  so training samples are separated.

linear banding  $\rightarrow$  better to compute.

understanding is simplifying.

minimizing loss func.



iteratively modify  $w_i$  to reduce  $J(w)$ .

what modifications reduce  $J(w)$ ?

$$\frac{\partial J}{\partial w_i} \uparrow \quad \left. \begin{array}{l} \text{gradient descent} \\ \text{slope} \end{array} \right\}$$

$$\frac{\partial J}{\partial w} \quad \left. \begin{array}{l} \text{gradient} \\ \text{(vector)} \end{array} \right\} \text{ (ascent)}$$

$$-\frac{\partial J}{\partial w} \quad \left. \begin{array}{l} \text{gradient descent} \end{array} \right\}$$

$$w = \frac{\partial J}{\partial w}$$

gd algorithm.

$$w^{t+1} = w^t - \eta \frac{\partial J}{\partial w}$$

Loss function  $J(w)$   
 ↳ no. of misclassified samples.  
 (not differentiable).

$$y_i(w^T x_i) > 0 \text{ for all samples}$$

$$J(w) = -y_i(w^T x_i) \text{ (for misclassified samples)}$$

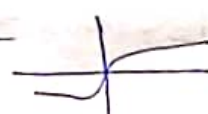
$$\nabla J = -y_i x_i$$

↳ called perceptron update rule.

so  $w^{t+1} = w^t + \eta \sum_{i \in X} y_i x_i$  (already negative.)

$\begin{array}{c|c} 1 & 0 \\ \hline 0 & 1 \end{array}$  } linear classifier doesn't work,  
 no way to separate.

$$\begin{matrix} x_1 & w_1 \\ x_2 & w_2 \\ \vdots & \vdots \end{matrix} \quad \begin{matrix} \text{bias} \\ \sum_{i=1}^n (w_i x_i) + b \end{matrix} \quad \begin{matrix} \text{output} \\ \downarrow \\ \text{threshold} \end{matrix} \quad \left. \begin{matrix} i \cdot j > T \\ \downarrow \\ \text{activation function} \end{matrix} \right\} \phi(\cdot) = y$$

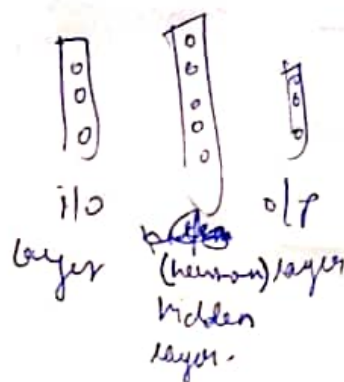
hyperbolic tangent  $\tanh$   } most popular

ReLU



determine

$$w, b$$



neural networks help in creating cloud boundaries (highly complex),

determining w/b is very very difficult.

Only 1 hidden layer suffices.

> 2 hidden layers  $\Rightarrow$  vanishing gradient descent.  
(back propagation).

hyperparameters = no. neurons  
 $\downarrow$

user pics,

MLP

