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## **Undergraduate Honors Thesis**

# Predicting the Outcome of NFL Games Using Logistic Regression

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## 1. Introduction

The National Football League (NFL) is the highest grossing American professional sports league, generating over \$13.5 billion revenue in 2017 (Statista, 2018). This multi-billion-dollar league garners an unrivaled interest from spectators around the United States, making it the most popular spectator sport in the country. Viewers around the country support their teams by purchasing game tickets, player merchandise, team gear, and by numerous other means. However, there is a new way in which the NFL stands to benefit from viewer consumption and action. The introduction of the legal sports gambling arena has provided the NFL and other US sports leagues with a future projected revenue stream that will boost their success emphatically. According to a 2018 Nielsen study, the NFL stands to gain an estimated \$2.326 billion in annual revenue as a result of legal sports gambling (Garcia, 2018). This jump in revenue is due largely in part to the increase in consumption that forecasters are projecting as a result of people now having a larger rooting interest in games across the league. The additional interest in the NFL and other leagues will only increase the desire and need for those who can successfully predict the outcomes of their games.

Predicting the outcomes of NFL games is not a new activity, nor is it something that can be considered perfect science, but the importance and benefit cannot be understated. Engineering a prediction machine strong enough to reliably predict these outcomes would be of significance to consumers, NFL franchises, and the gambling industry alike. The unpredictability of the NFL has largely been attributed to the inability to measure or quantify the desire of the players on the field, or the number of intangibles that exist within each player, but that has not been a deterrent for those determined to understand which performance metrics and game attributes translate to victories.

The purpose of this research is to understand which statistics the best indicators of success are and use them to build a successful predictive model for determining the outcome of an NFL game. In particular, we explore the effectiveness and accuracy of Logistic Regression methodology in such prediction.

## 2. Literature Review

In this section we provide a brief review of the existing models in academic literature for predicting the outcome of sports games. We first focus on the models built using logistic regression, the technique we focus on in this paper, then we move on to other modeling techniques that are used to generate a similar prediction. The papers that use logistic regression particularly guide us in the set up and structure of our model, whereas those who explore other methods help us identify additional performance metrics that may be influential in our prediction and serve as benchmarks to compare the accuracy of our model.

## 2.1 Logistic Regression

Logistic regression is an extremely popular and quite successful technique for modeling the relationship between a number of independent variables and a dichotomous dependent variable (Kleinbaum, 2010, p.5). For problems in which one is trying to determine a probability of something happening, especially when there are only two possible outcomes (such as win or loss in a game, click or no click on an online ad, purchase or no purchase in response to an offered product, etc.), logistic regression is particularly appropriate and proven to be very powerful in various applications. The output from logistic regression is a value between 0 and 1. In many other types of models, such as linear regression, the output is not restricted to a value between 0 and 1, and so cannot be interpreted as a probability (Kleinbaum, 2010, p.6).

Willoughby (2002) used logistic regression to analyze and predict the outcomes of games in the Canadian Football League (CFL), a sport with extremely similar rules, statistics, and only a few differentiating factors from the NFL. The negligible differences between the sports are not significant enough to warrant ignoring the results and methods. The predictors chosen in this study were the head-to-head differences in a number of statistics. Rushing yardage differential, passing yardage differential, interception and fumble differential, and finally sack differential were the independent variables chosen. These indicators are meant to compare the two teams against one another and recognize who is superior in a specific category. Willoughby (2002) created three models, one for each of the three teams he wished to predict. The performance of each model was strong, but with some varying results. The three models

returned 85.9%, 90.2%, and 78.8% correct prediction rates, with 90.2% being an exceptionally strong performance, while 78.8% being only relatively strong.

Shanahan (1984) performed a logistic regression model to predict the outcome of college basketball games at the University of Iowa. While basketball and football are two vastly different sports, the modeling techniques, the predictors used, and the results can all provide meaningful insight that help shape the direction of this paper. In her paper, many of the strongest predictors were those which translated to possession. Strong rebounding and strong turnover numbers were both highly influential, which is important to know when creating our model for NFL games. The accuracy of the models differed only slightly between the men's and women's game, with the success rates of 88% and 90%, respectively.

Kolbush and Sokol (2017) used logistic regression, together with a Markov chain model, to predict the outcome of the NCAA Football rankings. There are a number of major differences between the NFL and NCAA football games in terms of rules, scheduling, conferences, etc. but they are essentially the same game in terms of how they are played and the rules of the game. The general ideas and principles are the same with largely differing strategies, which allows for lessons to be taken from this paper. To account for the evolution of the game as well as the roster turnover, the authors decided to use 4 year rolling samples for their data. The Markov chain model was paired with logistic regression to create a ranking system, as opposed to a simple binary output. In our paper, we only seek a binary win/loss prediction. Kolbush and Sokol (2017) also examined whether or not point differentials should be used as one of the predictors. Point differentials can often be skewed one way or another; in some games a team will run up the score and inflate that point differential number, while sometimes the score does not indicate how close or lopsided a game could be. Using metrics outside of point differential would seem to create a story that is more accurate and reliable than relying on point differentials. Although the authors only generated a ranking of the teams and did not predict wins vs. losses, the success rate of their model was only near 61%.

## 2.2 Other Techniques

Aside from logistic regression, there are several other modeling techniques in sports prediction. Despite the differences in methods, there are many consistencies when considering the data preparation, feature selections, and other steps necessary to produce a successful model.

Warner (2010) used a Gaussian process predictive model in an attempt to outperform Vegas line makers, i.e., those who determine the betting lines in Las Vegas, when predicting the margin of victory in NFL games. This study examined features that are outside of the scope of what we normally associate with the outcomes of NFL games, such as weather condition differences between what a team typically plays in and the game they will play. Warner (2010) also performed feature selection to only include the most influential variables to predict success. Although the main goal of this study is to predict the margin of victory, he then proceeds to covert these margins to a win vs. loss prediction. The success rate of his model, excluding the point spread and margin of victory, is 64% percent.

Hamadani (2005) aimed to generate a better prediction than a human could, using machine learning. This paper also provided a comparison between different methodologies and modeling techniques such as logistic regression and Support Vector Machine (SVM).

Surprisingly, the best performing model explored in this paper was one that employed logistic regression. The SVM results were similar but fell short of the accuracies generated using the regression analysis. Those accuracies were 65.83% for the 2005 season, 61.37% for the 2006 season and 67.08% for the 2007 season. Hamadani (2005) performed feature selection to generate a model that includes only the most influential variables. The overall success of the model was better than the compared accuracies of the 'expert' picks.

Silver (2014) runs a popular statistics website, FiveThirtyEight, which is well-known for its prediction machines and its relative accuracy for determining winners of all types. From presidential elections to sporting events, FiveThirtyEight has distinguished themselves as an industry leader in all things predictive in nature. The site uses a method that they developed that incorporates 'Elo', a rating system that they created from a variety of performance metrics to give a team a baseline rating, and then adjust based on their performance throughout the season. The 'average' team begins with an Elo rating of 1500 and most teams end the season

with a rating between 1300 and 1700. These ratings are used as a baseline to predict the outcomes but are generated using a lot of the same ideas we explore in this paper.

Although logistic regression is an appropriate method for our problem, much of the existing work surrounding this topic has used other modeling methods. Neural networks and other types of models that fall under the machine learning umbrella have been used with strong success to predict both point spreads and outcomes of NFL games, but we consider those methodologies outside of the scope of this paper.

## 3. Research Objectives

The focus of this paper is to create an accurate predictive model that would predict the outcome of an NFL game with high accuracy. As an integral part of developing such a model, we also aimed to provide answers to the following questions:

- Which attributes/metrics/statistics are the most useful for predicting NFL outcomes?
- With what accuracy can we predict the winner of each game?

## 4. Data

The data used for this work is a comprehensive NFL dataset by Armchair Analysis, spanning from 2001 to 2018. This data is comprised of many individual tables that contain data about every single play, game, player and more for each of the 32 NFL teams. For each team and game, we utilized the following statistics:

- Home vs. Away (H)
- Points Scored (PTS)
- Rushing Yards (RY)
- Rushing Attempts (RA)
- Passing Yards (PY)
- Passing Attempts (PA)
- Pass Completions (PC)
- Sacks Against (SK)
- INT's for Defense (INTS)
- Fumbles Lost (FUM)
- Punts (PU)
- Punt Returns (PR)
- Punt Return Yards (PRY)

- Kick Returns (KR)
- Kick Return Yards (KRY)
- Penalty Yards (Against) (PEN)
- Time-of-Possession (TOP)
- Touchdowns (TD)
- Field Goals Made (FGM)
- Field Goals Attempted (FGAT)
- Drives in Red Zone (RZA)
- Red Zone Drive TD's (RZC)
- Starting Field Possession (SFPY)
- Net Punt Yardage (NPY)

The complete data dictionary to what is available at the time of this writing can be found online at: <a href="mailto:armchairanalysis.com/2019">armchairanalysis.com/2019</a> AA Table Fields.pdf

## 5. Methodology

In this section we will elaborate on our logistic regression model, how we used Query Editor in Microsoft Excel along with R to drastically transform raw data into a workable state for regression analysis and discuss how we performed variable selection in conjunction with data partitioning and model validation to simplify our model and alleviate multicollinearity and overfit concerns.

## 5.1 Logistic Regression

Logistic regression is used widely to examine and describe the relationship between a binary response variable (e.g., 'success' or 'failure') and a set of predictor variables (G.M. Fitzmaurice, 2001). In our case, logistic regression is used to tell us whether or not a team would win (1) or lose (0). More specifically, the logistic regression model will return a probability between 0 and 1; this creates the need for a threshold of what will be considered a win or a loss. If the probability returned is greater than 0.5, then we would consider the prediction to be a win. The following mathematical equation represents the way in which the probability of a victory is determined:

$$Prob[Win] = \frac{1}{1 + e^{-U}}$$

where:

$$U = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \cdots$$

and  $x_i$  are the various independent variables (team performance metrics) chosen for the model.

The model coefficients,  $\beta_i$ , i.e., the weights by which the independent variables affect the outcome, are determined using Maximum Likelihood Estimation (MLE). For each variable (performance metric), the corresponding coefficient/weight can be interpret as follows: All else equal, each unit increase (decrease) in the variable  $x_i$  will multiply (divide) the odds of winning, i.e.,  $\frac{\text{Prob}[Win]}{\text{Prob}[Loss]}$ , by a factor of  $e^{\beta_i}$ . Therefore, a positive (negative) coefficient, indicates a positive (negative) relationship between that variable (performance metric) and the odds of winning. For further explanation on logistic regression, see Fitzmaurice (2001).

There are several ways we could use logistic regression: building a separate model for each pair of teams; a separate model for each team (against all others), or one model that explains all teams. We chose to use a separate model for each of the 32 NFL franchises because the performance metrics that best explain one team's success may not be optimal for another team. Therefore, a single model may not be able to accurately predict the outcome of games for all teams. On the other hand, fitting a separate model for each pair of teams would not be practical since a particular pair does not play against each other too often for us to have enough data points to fit a regression model properly. Creating a separate model for each of the teams strikes a balance between tailoring the models to unique attributes of each team, while having enough data to support the fitting and testing of each model. This approach is also consistent with the literature, for instance, the work of Willoughby (2002).

#### 5.2 Data Preparation

Before the regression could be performed there were a number of data preparation measures taken in order to merge, clean, preprocess, and transform the raw data into the necessary structure to carry out the analysis.

The relevant data fields (i.e., team performance metrics) that we were interested in using as our independent variables and the results of the games (which would be the dependent variables in our model), were spread across various tables. Using Query Editor in

Microsoft Excel, we were able to gather and merge all relevant data fields in to one table. This table showed, for every single game from 2001 to 2018, the season/year and game ID, home and away team IDs, a binary win/loss column (i.e., our dependent variable) indicating whether the home team won the game, and finally all of the performance metrics that we mentioned before in our Data section as realized during that game. This data was then loaded in R Studio for the remainder of transformations.

There were three teams that required extra consideration due to either changing locations, or the expansion of the NFL. The Houston Texans were an expansion team prior to the 2002 season, thus not having a full season of data that the other teams did. For both the St. Louis Rams and the San Diego Chargers, who both moved to Los Angeles before the 2016 and 2017 seasons, respectively, we considered the teams to be the same before and after the move. To account for the difference in names, we assigned the team name of SDLA for the Chargers, and STLA for the Rams. We did not omit those teams from consideration or take any other steps to manipulate their data specifically and simply assumed they were the same team.

The classification model should not use the performance result of a game after it has happened to predict the outcome of that same game. The input variables to the model on any particular game should only be based on the performance of the two teams as observed up to and prior to that game. Therefore, the merged data is still not ready for fitting the model. In order to correct this, we wrote an R script to calculate 5-game moving averages (MA) and all-time cumulative averages (CA) of each metric up to (and excluding) each game. The MA and CA of each statistic became the initial candidates for independent variables. The very first 4 games played by each team in the history of our data were eliminated from the analysis due to not having a 5-game MA metric yet.

Our processed data table had the following structure: [Season, Year, Game ID, Home team ID, Visiting team ID, Home team win status (binary), Home team MA & CA statistics, Visitor team MA & CA statistics].

#### 5.3 Feature Generation

Feature generation is a common step in predictive modeling in which non-linear transformations of variables are created to form new additional independent variables. This

would allow the model to take advantage of possible nonlinear relationships between an input and the output which can often drastically improve the prediction accuracy. Simple linear transformations would only create an undesired multicollinearity in the model and would therefore be futile. It is hard to guess what specific transformations and on which variables would help increase the prediction accuracy, therefore, we choose to create as many transformations as we can think of and apply them to all variables, and let the variable section step, explained in the following section, to then trim the model down to only those variables that are significant.

In addition to the original moving and cumulative averages of teams' performance metrics, we wrote an R script to apply the following non-linear transformations to those MA and CA values and used them as additional independent variables: square, square root, logarithm, pairwise ratios and products. These transformations were not possible on every performance metric, e.g., some leaded to frequent division by zeros, and such cases were not generated in this process. Having these additional variables gave us a total of 505 independent variables to consider for our model.

#### 5.4 Feature Selection

Feature selection is often used in analytics as an easy and effective way of excluding variables that do not contribute, in a statistically significant manner, to the predicted outcome; thereby retaining only the most important metrics in the model. There are three main advantages in performing feature selection: i) having a smaller/simpler model to work with which would require less data to collect as input, ii) alleviating multicollinearity issues among independent variable, and iii) alleviating overfit issues, which could easily happen following the feature generation step. We will elaborate more on overfit issues in the next section.

There are a number of standard methodologies for performing variable selection which we explored to determine which would be appropriate for our case. The best subsets method tests every possible subset of variables returns the best model at any given number of predictors. Backwards elimination begins with all variables included in the model and iteratively eliminates the least impactful variable, one at a time, until the model is reduced to a desired number of predictors, or all the remaining variables are statistically significant. Similarly,

forward selection starts with only the intercept and iteratively adds the most impactful variable, one at a time, until there is no significant benefit from continuing. Lastly, sequential replacement replaces once variable at a time to check if any other possible variable would enhance the performance of that model.

The Best Subsets method is optimal, but it is also impractical for models that consider more than 20 variables as there would be a prohibitive number of variable subsets to fit and test. When comparing forward and backwards, we found that the final reduced models found through backwards elimination had a higher accuracy in our application. We then performed backward elimination down to 80 and then 20 variables and found that having about 20 variables in the model is the sweet spot for simplicity of the model, high accuracy, and having resolved most overfit concerns. These steps were looped in our R Script to produce models of both sizes for each of the 32 NFL franchises, with predictors that perform best for that team, independent of the others.

## 5.5 Data Partitioning and Model Validation

The primary goal of any predictive model is to produce an accurate prediction on new data which the model has not seen before. Consequently, only looking at the accuracy of the model within the same dataset that was used to fit the model is not sufficient for determining how well the model performs. Instances in which a model performs well on the dataset that was used to fit the model but does not perform well on new data is referred to as overfit. Excessive feature generation and including too many variables in a model can lead to significant overfit issues.

A common way to validate the model and ensure that there is not too much overfit is to partition the data into a training set and a testing set. The training data is used to fit the model, i.e., estimate the regression coefficients, while the test data is used to confirm that the model produces consistent accuracy rates when faced with new data. It is expected and normal that a model would perform better on the training data, since the model coefficients are particularly optimized to achieve that, however, we do not want the performance on test data to be drastically worse. When a model has overfit issues, variable selection is commonly used to reduce the number of features considered for the model and correct the overfitting.

We used the 2001-2016 data for training our models and held the 2017 and 2018 data for validation. This partitioning left us with an average of 300 games per team for training (i.e., fitting) each model and about 33 games for validation. This threshold was set in R studio and this process was made as an integral part of our R script loop for creating and testing the models for each of the 32 teams.

## 6. Results

In this section we will discuss the results of our models, with a section showing the various prediction accuracies, and a section highlighting the most commonly used predictors across the models.

## 6.1 Prediction Accuracy

The following table shows the prediction accuracies obtained for each team using a large model with 80 variables, and then a small model with only 20 variables, each measured on both training (2001-2016) and validation (2017-2018) data. These results are sorted in descending order by the accuracy of our test data from our small model. For a complete list of all coefficient information, please see the Appendix.

The results, for the most part, align with the consistency of the teams since the beginning of our dataset. Teams who were either consistently good, like the New England Patriots, or teams that were consistently bad, like the Cleveland Browns, had the best accuracies across the models. Similarly, teams that have been inconsistent from year to year, like the Carolina Panthers and the New Orleans Saints, had lower accuracy totals relative to the others.

	Large Model Accuracy (80 Vars)		Small Model Accuracy (20 Vars)	
Team	Train	Test	Train	Test
New England Patriots (NE)	0.900	0.500	0.823	0.763
Cleveland Browns (CLE)	0.944	0.781	0.787	0.719
New York Jets (NYJ)	0.864	0.688	0.731	0.688
Kansas City Chiefs (KC)	0.847	0.457	0.726	0.657
Dallas Cowboys (DAL)	0.887	0.471	0.715	0.647
Chicago Bears (CHI)	0.915	0.697	0.727	0.636
San Franciso 49ers (SF)	0.928	0.313	0.733	0.625
Oakland Raiders (OAK)	0.916	0.563	0.756	0.625
Indianapolis Colts (IND)	0.948	0.485	0.769	0.606
Pittsburgh Steelers (PIT)	0.848	0.545	0.759	0.606
Green Bay Packers (GB)	0.900	0.500	0.748	0.594
Minnesota Vikings (MIN)	0.883	0.471	0.734	0.588
Detroit Lions (DET)	1.000	0.531	0.772	0.563
Houston Texans (HOU)	1.000	0.500	0.773	0.563
Miami Dolphins (MIA)	0.860	0.516	0.708	0.548
Seattle Seahawks (SEA)	0.907	0.485	0.740	0.545
Baltimore Ravens (BAL)	0.907	0.515	0.730	0.545
Jacksonville Jaguars (JAC)	0.926	0.657	0.733	0.543
Atlanta Falcons (ATL)	0.910	0.529	0.752	0.529
Philadelphia Eagles (PHI)	0.846	0.595	0.723	0.486
Tennessee Titans (TEN)	0.908	0.529	0.744	0.471
Cincinati Bengals (CIN)	0.938	0.406	0.710	0.469
Buffalo Bills (BUF)	1.000	0.273	0.727	0.455
Washington Redskins (WAS)	0.941	0.452	0.717	0.452
Arizona Cardinals (ARI)	0.865	0.313	0.684	0.438
Denver Broncos (DEN)	0.849	0.563	0.727	0.406
Carolina Panthers (CAR)	0.904	0.576	0.762	0.394
San Diego/Los Angeles Chargers (SDLA)	0.887	0.382	0.764	0.353
St. Louis/Los Angeles Rams (STLA)	0.930	0.667	0.733	0.333
Tampa Bay Buccaneers (TB)	0.813	0.406	0.713	0.313
New Orleans Saints (NO)	0.905	0.278	0.669	0.278
New York Giants (NYG)	0.901	0.406	0.691	0.250

Examining the differences between the "Large Model" and "Small Model" accuracies, it is apparent that there was significant overfitting for the larger model. For example, when we look at the outputs for San Francisco (SF), the training accuracy for the "Full Model" is 92.8% and the testing accuracy is 31.3%. This clearly shows that the model was overfit to the training data and did not perform nearly as well on the test data. After feature selection was used to trim the number of variables further down to 20, those same accuracy outputs are much closer to one another, at 73.3% and 62.5%, respectively. This means we can now be confident that the smaller model delivers a similar level of accuracy when applied to new data, whereas the large model with 80 variables cannot be trusted on new data. For some of the teams, particularly in

the bottom half of the table, there is still a large gap between the train and test accuracies, which suggests a persistent overfit which could demand further variable elimination, maybe down to 10 variables. But in our tests, further variable elimination did not help with correcting the overfit in a noticeable way; It appears as if the recent performance of those teams during 2017-2018 simply could not be accurately explained based on their historic performance prior to 2017.

### 6.2 Statistically Significant Performance Metrics

Because we created a separate model for each team and performed feature selection independently for each of the 32 NFL franchises, there were different variables that were deemed statistically significant in predicting the probability of a win for each specific team. We combined the list of variables across all 32 (small) models, and using a pivot table in Excel, we generated a list of those most commonly found variables:

- Cumulative average of SFPY
- Cumulative average of PTS
- Squared cumulative average of SFPY
- Cumulative average of TOP
- Home or Away status (binary)
- Cumulative average of FGAT
- Cumulative average of PA
- Cumulative average of RY
- Squared cumulative average of PR
- Cumulative average of PR
- Square root of the cumulative average of PTS
- Squared cumulative average of TDs
- Squared cumulative average of PTS
- Square root of the cumulative average of PU
- Square root of the cumulative average of SFPY
- Cumulative average of KRY
- Cumulative average of TDs

The number of times that each of these predictors shows up among the 32 models is not drastically different from others, so we listed all variables that were considered a significant predictor for at least 7 of the 32 teams.

It is worth noting that none of the metrics listed above relate to the opposing team, nor are there any moving average metrics that made the list. They did appear in some models but were not consistently included. See the Appendix for a complete list of the variables used in each individual model.

Finally, we should point out that many of these variables are the result of our feature generation step, particularly through squaring or taking the square root of an original variable. It would have been hard to "guess" that such metrics would be significant predictors of a game outcome by intuition.

## 7. Conclusions and Future Work

We explored the effectiveness and accuracy of Logistic Regression methodology in predicting the outcome of NFL games. Our process began with transforming large amount of raw data, obtained from Armchair Analysis, into a format that was suitable for logistic regression. We wrote an R Script that applied moving averages and cumulative averages to each team performance metric we considered as independent variable for both the home and opposing teams, and then applied a number of non-linear transformations, which left us with a total of 505 independent variables to start the regression analysis. We then performed backward feature selection to trim those variables down to 80 and 20 for our two different sized models, while partitioning out data into training and validation sets to check for model overfit. After the previous steps were taken, various accuracy statistics were generated to show how well our models performed. Teams that were more consistent, either good or bad, like New England and Cleveland were predicted with the highest accuracies, above 70% on both training and test data. Teams that were more inconsistent over the same timeframe, like New Orleans and the New York Giants, showed near 70% accuracy on training data, but had the low accuracies near 30% on test data, which could be improved further through variable selection.

As mentioned in the introduction, one key limitation of any sports prediction is that it is impossible to measure the amount of desire a given player or team has. We try to assign value to all other measurables and metrics on the field, but often times the intangibles within players is the difference between a win and a loss. Furthermore, we left out the environmental aspects

of the games (such as stadium temperature and humidity) from our predictors, because our dataset contained too many missing values in those respects. Additionally, we did not explore an exhaustive list of non-linear transformations to generate our additional features. Exploring other transformations may help improve the accuracy further.

After comparing our results with those from previous works, it appears that more successful models can be generated using other modeling techniques. In this project, we did not explore other classification techniques such as neural networks, k-nearest neighbors or SVM. The viability of different classification methods is highly problem-specific and dependent on the data; therefore, any of those alternative methods may provide a stronger result. Given more time and a stronger understanding of additional methods, it would be valuable to test and see how those alternative techniques would compare to our models.

As the gambling industry grows and becomes more widely legalized, we expect that there would be a strong demand for predicting whether or not a team will cover a certain point spread against the opposing team. Being able to predict the point spread, instead of a binary win/loss, would enhance the value of our models to the gambling community, but in that case, we would need to use a method that produces a continuous output, like linear regression. In fact, all the data preparation and transformations that we performed in this study, as well as the data partitioning and model validation steps, would directly apply to the case of linear regression. The only difference would be that the point spread observed in each game would become the dependent variable, the model coefficients would be estimated using the Least Squares method, and the accuracy of the models would be measured using average distance metrics such as Mean Absolute Deviation (MAD), Mean Absolute Percent Error (MAPE), or Root Mean Square Error (RMSE).

While we certainly cannot quantify the heart of an athlete or foresee unpredictable events such as injuries, that did not deter us from attempting to search for and test available performance metrics which may be crucial indicators of a game's outcome. Our final model and findings provide the groundwork and template for those attempting to use logistic regression to predict outcomes of other sporting events. In fact, some of the performance metrics we

discover to be the most indicative of winning football had not been tested before in prior academic literature.

Moving forward, it would be interesting to apply the same techniques used in this paper to other sports. Much of the data preparation and modeling we performed could be applied in a similar fashion to NBA, NHL, or MLB games. It is possible that logistic regression is more suitable for a different sport than football, where there are more games played in a season and thus higher volume of data available to train and test the models. Having only 16 games in the regular season and a maximum of 4 additional playoff games, there are not nearly as many records in NFL as there would be in a baseball season of 162 games.

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## **Appendix: Coefficient Information and Confusion Matrices**

## for Individual NFL Teams

In this section, we will show the individual outputs for each model we created, as well as the confusion matrices associated with each. The variable names below are all comprised of performance acronyms defined in the 'Data' section 4, followed by either MA meaning the 5-game moving average, or CA meaning the cumulative average. A number "2" in the variable name indicates that this was a performance metric from the opposing team. Any prefix denotes the nonlinear transformation performed on the variable before its inclusion in the model, as introduced in the Feature Generation section 5.3: "Sq" means the squared term, "Sqrt" means the square root of the term, "log" means the logarithm of the term, "mult" means the pairwise product of the term, with "rat" meaning pairwise ratio of the term.

#### San Francisco 49ers

```
Coefficients:
                                         z value
                  Estimate Std. Error
                                                       Pr(>|z|)
            -6.814123e+03 3.320187e+03 -2.052331 4.013748e-02
(Intercept)
ra_MA -1.790999e-01 6.108105e-02 -2.932168 3.366042e-03
             3.023449e-01 9.848084e-02 3.070088 2.139954e-03 1.998080e+00 1.079014e+00 1.851765 6.405952e-02
top MA
sfpy_MA
pts_CA
             -1.875725e+00 6.129979e-01 -3.059921 2.213951e-03
py CA
             1.143662e+00 4.517209e-01 2.531790 1.134819e-02
pry CA
             -8.788293e+01 2.300658e+01 -3.819905 1.335032e-04
fgat CA
             -7.841214e+00 3.420111e+00 -2.292678 2.186653e-02
npy CA
             -8.448213e-01 3.418267e-01 -2.471490 1.345512e-02
ry MA2
             -1.423323e-02 5.243727e-03 -2.714335 6.640897e-03
sfpy_MA2
              7.613202e-03 3.287280e-03 2.315958 2.056057e-02
sfpy_CA2
             -3.591757e+01 1.794156e+01 -2.001920 4.529335e-02
             -9.754495e-04 5.227317e-04 -1.866061 6.203277e-02
Sq sfpy MA
Sq_py_CA
             -2.504012e-03 9.354697e-04 -2.676743 7.434166e-03
             -1.976662e+00 1.065976e+00 -1.854321 6.369322e-02
Sq_pr_CA
Sq_pry_CA
              1.099456e+00 2.739586e-01
                                         4.013221 5.989571e-05
                                         2.426849 1.523058e-02
Sq_npy_CA
              2.384951e-03 9.827355e-04
Sq_sfpy_CA2
              1.627145e-02 8.096936e-03 2.009582 4.447550e-02
Sqrt sfpy MA -4.906168e+01 2.653407e+01 -1.849007 6.445679e-02
              4.250272e+02 1.138533e+02 3.733112 1.891286e-04
Sqrt pry CA
Sqrt sfpy CA2 9.169754e+02 4.594690e+02 1.995729 4.596347e-02
Confusion Matrices:
Train:
p_data 0
    0 115 41
     1 33 88
Test:
p data 0 1
    0 15 5
     1 7 5
```

#### Atlanta Falcons

#### Coefficients:

```
Estimate
                                 Std. Error
                                                z value
                                                                Pr(>|z|)
              1.993485e+05 6.093261e+04 3.271623 1.069321e-03
(Intercept)
               -8.051473e-01 2.000572e-01 -4.024586 5.707563e-05
pr MA
               -8.477081e+00 2.784479e+00 -3.044405 2.331412e-03
rza MA
ints CA
               -2.596231e+02 1.230293e+02 -2.110254 3.483650e-02
pr CA
                2.324152e+02 1.273056e+02 1.825649 6.790319e-02
               -2.476361e+02 6.640297e+01 -3.729293 1.920174e-04
kr CA
               -4.341525e+02 1.010956e+02 -4.294476 1.751066e-05
td CA
               6.466145e+01 1.786002e+01 3.620458 2.940823e-04
rzc CA
               1.112997e+03 3.426770e+02 3.247947 1.162408e-03
sfpy CA
              1.089769e+02 5.818795e+01 1.872843 6.109006e-02
Sq_ints CA
               -5.161585e+01 2.906038e+01 -1.776159 7.570673e-02
Sq_pr_CA
               -5.132547e-01 1.602018e-01 -3.203801 1.356262e-03
Sq sfpy CA
Sqrt rza MA 3.062093e+01 9.852463e+00 3.107947 1.883921e-03
Sqrt ra CA
              -4.622948e+01 1.010425e+01 -4.575252 4.756476e-06
Sqrt_pa_CA
              6.959849e+01 2.128880e+01 3.269254 1.078313e-03
Sqrt_pc_CA
               -6.794042e+01 1.935634e+01 -3.509983 4.481347e-04

      Sqrt_kr_CA
      1.015286e+03
      2.707522e+02
      3.749873
      1.769239e-04

      Sqrt_td_CA
      1.203184e+03
      2.811870e+02
      4.278944
      1.877821e-05

      Sqrt_rzc_CA
      -7.876735e+01
      2.479704e+01
      -3.176482
      1.490732e-03

Sqrt sfpy CA -2.821570e+04 8.624997e+03 -3.271387 1.070214e-03
Sqrt pts MA2 -1.185779e+00 2.784878e-01 -4.257923 2.063350e-05
```

#### Confusion Matrices:

#### Train:

#### Test:

p\_data 0 1 0 0 0 1 16 18

#### Jacksonville Jaguars

```
Estimate Std. Error z value
(Intercept) -4.118014e+03 1.741090e+03 -2.365193 0.0180207009
-3.469286e+02 1.197358e+02 -2.897452 0.0037620707
top_MA
          -4.294714e+01 1.082238e+01 -3.968364 0.0000723677
pts CA
sk CA
          -1.463939e+01 9.952978e+00 -1.470855 0.1413302140
           1.682451e+02 5.457675e+01 3.082724 0.0020511511
fum CA
kr CA
          -3.232929e+02 9.222349e+01 -3.505538 0.0004556857
fgat CA
          -1.721349e+01 5.896504e+00 -2.919270 0.0035085226
           7.234229e-01 1.949601e-01 3.710620 0.0002067526
kr MA2
          -4.578858e+00 1.470074e+00 -3.114712 0.0018412475
fqm MA2
          -2.325502e-03 7.152547e-04 -3.251292 0.0011488181
Sq ry MA
Sq top MA
         1.903685e+00 6.642660e-01 2.865848 0.0041589393
Sq pts CA 1.005112e+00 2.598174e-01 3.868531 0.0001094929
          1.736280e+00 1.579601e+00 1.099189 0.2716855774
Sq sk CA
          -9.962653e+01 3.394486e+01 -2.934952 0.0033359935
Sq fum CA
```

```
Sq_kr_CA4.305161e+011.239920e+013.4721280.0005163495Sq_sfpy_CA1.437459e-044.496321e-053.1969670.0013888071Sq_fgm_MA21.405995e+004.621360e-013.0423830.0023471294Sqrt_ry_MA-2.317750e+017.201775e+00-3.2183040.0012895123Sqrt_top_MA2.543740e+038.737363e+022.9113360.0035988674
```

Train:

```
p_data 0 1
0 135 42
1 30 63
```

Test:

```
p_data 0 1
0 13 11
1 5 6
```

#### Cleveland Browns

Coefficients:

```
Estimate Std. Error z value
(Intercept) -2.140464e+02 2.152620e+02 -0.9943529 0.3200511011
pts_CA -2.293736e+01 2.909610e+01 -0.7883309 0.4305031795
              1.559315e-01 6.118222e-02 2.5486411 0.0108143535
kry CA
top CA
              -4.590509e+00 1.626202e+00 -2.8228400 0.0047600327
td CA
              2.131094e+02 1.861489e+02 1.1448328 0.2522784177
sk MA2
              -3.755335e+00 1.403706e+00 -2.6753001 0.0074662393
            -1.494119e+01 5.067453e+00 -2.9484614 0.0031935998
ra CA2
              1.389986e+01 1.843941e+01 0.7538127 0.4509617099
pr CA2
fgat CA2
              -3.501817e+00 1.625189e+00 -2.1547142 0.0311842056

      Sq_rzc_MA2
      -3.234472e-01
      1.086786e-01
      -2.9761806
      0.0029186291

      Sq_top_CA2
      1.227117e-02
      4.533972e-03
      2.7064950
      0.0067997611

      Sq_sfpy_CA2
      5.024277e-05
      2.050467e-05
      2.4503089
      0.0142733708

      Sqrt_pc_MA
      5.555754e-01
      4.396812e-01
      1.2635868
      0.2063783831

Sqrt_pts_CA 1.193874e+02 2.262902e+02 0.5275854 0.5977871614
Sqrt pu CA -5.402949e+01 2.618347e+01 -2.0634967 0.0390654615
Sqrt td CA -4.102422e+02 4.713867e+02 -0.8702879 0.3841430931
Sqrt rza CA 1.991409e+01 6.012423e+00 3.3121566 0.0009257971
Sqrt npy CA 7.042812e+00 3.403981e+00 2.0689929 0.0385467531
Sqrt sk MA2 1.248547e+01 4.337464e+00 2.8785188 0.0039954748
Sqrt ra CA2 1.572867e+02 5.369977e+01 2.9290006 0.0034005373
Sqrt pr CA2 -5.132402e+01 5.593060e+01 -0.9176376 0.3588086349
```

Confusion Matrices:

Train:

```
p_data 0 1
0 167 41
1 16 43
```

```
p_data 0 1
0 23 7
1 2 0
```

#### Philadelphia Eagles

#### Coefficients:

```
Estimate
                                Std. Error
                                              z value
                                                              Pr(>|z|)
             4.446042e+00 9.723650e+01 0.045724 9.635302e-01
(Intercept)
               7.285198e+01 3.722323e+01 1.957164 5.032818e-02
pu MA
              -2.045701e+00 8.641274e-01 -2.367361 1.791545e-02 1.650732e+00 5.955338e-01 2.771854 5.573812e-03 1.936807e+00 1.117671e+00 1.732896 8.311419e-02
npy MA
pa_CA
ints MA2
              -4.052167e-01 1.706710e-01 -2.374256 1.758436e-02
ra CA2
               1.187766e+01 5.607425e+00 2.118202 3.415798e-02
top CA2
               2.294813e-05 1.050957e-05 2.183545 2.899570e-02
Sq py MA
Sq_pu_MA
              -2.488601e+00 1.268410e+00 -1.961984 4.976438e-02
              1.941140e-03 7.947535e-04 2.442443 1.458825e-02
Sq npy MA
              -1.309755e-03 6.000363e-04 -2.182793 2.905102e-02
Sq pts MA2
Sq ints MA2 -7.198330e-01 4.874184e-01 -1.476828 1.397219e-01
              -1.919164e-01 9.238919e-02 -2.077260 3.777754e-02
Sq top CA2
              1.008923e+00 3.735308e-01 2.701044 6.912218e-03
Sq rzc CA2
              -2.120414e+02 1.086578e+02 -1.951460 5.100231e-02
Sqrt pu MA
Sqrt_npy_MA 3.579390e+01 1.536035e+01 2.330279 1.979140e-02
             -8.661804e+00 2.082220e+00 -4.159889 3.184024e-05 1.064122e+01 4.697897e+00 2.265103 2.350635e-02 9.459861e+00 2.991465e+00 3.162283 1.565373e-03
Sqrt_py_CA
Sqrt_kr_CA
Sqrt_rzc_CA
Sqrt sfpy CA -6.205313e+00 1.824466e+00 -3.401166 6.709911e-04
Sqrt pc CA2 -4.836417e+00 1.524532e+00 -3.172395 1.511875e-03
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
0 74 33
1 46 132
```

#### Test:

```
p_data 0 1
0 4 12
1 7 14
```

#### Dallas Cowboys

```
Estimate Std. Error z value
                                                                Pr(>|z|)
(Intercept) -2.515211e+02 1.182695e+02 -2.126678 3.344688e-02
              -1.563715e+00 6.899289e-01 -2.266487 2.342161e-02
pry_MA
               3.997774e+00 1.261799e+00 3.168314 1.533259e-03
ra_CĀ
top_CA
               -9.942917e+00 2.747515e+00 -3.618877 2.958842e-04

      4.468933e+00
      2.845115e+00
      1.570739
      1.162433e-01

      1.354195e+01
      4.977818e+00
      2.720458
      6.519154e-03

      1.353033e+00
      4.323827e-01
      3.129248
      1.752545e-03

fgat CA
rza CA
fum MA2
               -4.705128e-01 1.880344e-01 -2.502270 1.233999e-02
kr MA2
              -1.601564e+01 4.815720e+00 -3.325701 8.819648e-04
ra CA2
pa CA2
              -5.150535e-01 1.747318e-01 -2.947680 3.201678e-03
fum CA2
              -4.181784e+00 1.835873e+00 -2.277818 2.273740e-02
Sq_pry MA
              1.155055e-02 5.387551e-03 2.143932 3.203830e-02
               4.215639e-02 1.625601e-02 2.593280 9.506537e-03
Sq pa CA
Sq td CA
               -1.250630e+00 5.379224e-01 -2.324927 2.007585e-02
              1.534709e-04 4.127823e-05 3.717962 2.008365e-04
Sq py CA2
Sqrt pry MA 9.421229e+00 4.062424e+00 2.319115 2.038879e-02
Sqrt rza CA -1.331608e+01 6.825976e+00 -1.950795 5.108143e-02
```

```
Sqrt_ra_MA2 -1.710954e+00 4.752524e-01 -3.600095 3.181004e-04 Sqrt_py_MA2 -3.810650e-01 1.138816e-01 -3.346152 8.194137e-04 Sqrt_pts_CA2 -4.582284e+00 1.083702e+00 -4.228359 2.354015e-05 Sqrt ra_CA2 1.643931e+02 4.995098e+01 3.291089 9.980021e-04
```

Train:

p\_data 0 1 0 90 35 1 43 106

Test:

p\_data 0 1 0 2 0 1 12 20

#### New York Jets

Coefficients:

```
Estimate Std. Error z value
                                                       Pr(>|z|)
(Intercept) -4.884714e+02 2.266496e+02 -2.155183 3.114748e-02
              6.161815e+01 1.967014e+01 3.132572 1.732818e-03
rza MA
              2.292248e+01 1.981173e+01 1.157015 2.472661e-01
pts CA
pa_CA
             1.476794e+01 6.853572e+00 2.154780 3.117903e-02
pry_CA
             7.845661e-01 2.833968e-01 2.768437 5.632592e-03
rza CA
             -1.859419e+02 4.913983e+01 -3.783934 1.543686e-04
sfpy CA
             -1.582974e-01 5.297095e-02 -2.988381 2.804594e-03
             -3.639402e-01 1.738235e-01 -2.093734 3.628365e-02
py CA2
             2.578648e+00 1.077276e+00 2.393673 1.668061e-02
ints CA2
Sq pr MA
             1.949860e-01 4.730901e-02 4.121541 3.763468e-05
Sq_rza_MA
             -2.873572e+00 1.007051e+00 -2.853452 4.324705e-03
Sq_pts_CA
             -5.800449e-01 4.929710e-01 -1.176631 2.393429e-01
             -2.366490e-01 1.052506e-01 -2.248433 2.454858e-02 1.132325e+00 2.834764e-01 3.994425 6.485131e-05 2.064722e+01 5.184052e+00 3.982834 6.809832e-05
Sq_pa_CA
Sq kr CA
Sq_rza CA
             1.045046e-03 4.983564e-04 2.096986 3.599485e-02
Sq pa MA2
Sqrt rza MA -1.543278e+02 4.718014e+01 -3.271033 1.071553e-03
Sqrt rza CA
             2.680241e+02 7.522158e+01 3.563128 3.664612e-04
            -2.271113e+00 6.456549e-01 -3.517535 4.355755e-04
Sqrt td MA2
Sqrt_py_CA2
             1.089804e+01 5.127081e+00 2.125583 3.353797e-02
Sqrt fgm CA2 -6.955719e+00 3.002349e+00 -2.316759 2.051688e-02
```

Confusion Matrices:

Train:

```
p_data 0 1
0 112 42
1 33 92
```

```
p_data 0 1
0 17 4
1 6 5
```

#### Green Bay Packers

#### Coefficients:

```
Estimate Std. Error
                                       z value
                                                     Pr(>|z|)
(Intercept)
           2.287190e+03 7.627453e+02 2.9986289 2.711974e-03
             1.125077e+00 2.982138e-01 3.7727199 1.614775e-04
Home.1
            2.365230e-01 7.716012e-02 3.0653525 2.174136e-03 -3.709930e+00 9.101824e-01 -4.0760286 4.581139e-05
pc MA
ra_CA
pa_CA
            -1.499144e+02 4.302938e+01 -3.4840012 4.939772e-04
            -2.037046e+02 7.961594e+01 -2.5585903 1.050975e-02
td CA
            -6.172922e+01 6.032357e+01 -1.0233019 3.061651e-01
fgat CA
            -2.969577e+01 9.638951e+00 -3.0808091 2.064389e-03
rza CA
rza MA2
            2.611292e+00 1.271882e+00 2.0530925 4.006361e-02
            -8.685929e-02 3.972327e-02 -2.1866098 2.877102e-02
Sq rza MA
           1.377691e-05 6.106055e-06 2.2562701 2.405372e-02
Sq sfpy MA
            2.105457e+00 6.076792e-01 3.4647512 5.307222e-04
Sq pa CA
Sq fgat CA
           1.326244e+01 1.443471e+01 0.9187879 3.582065e-01
            5.673575e+00 1.679281e+00 3.3785731 7.286305e-04
Sq rza CA
Sq fqat MA2 -1.735179e-01 6.348847e-02 -2.7330621 6.274851e-03
Sq_rza MA2
            -4.517799e-01 2.048439e-01 -2.2054842 2.742014e-02
            2.938854e+01 1.246729e+01 2.3572514 1.841078e-02
Sqrt_fum_CA
```

#### Confusion Matrices:

#### Train:

#### Test:

```
p_data 0 1
0 12 6
1 7 7
```

#### Indianapolis Colts

```
Estimate Std. Error z value
(Intercept) -3.598390e+04 1.267026e+04 -2.840029 4.510943e-03
Home.1 9.667154e-01 3.101806e-01 3.116621 1.829364e-03
pa MA
            1.298771e-01 4.847825e-02 2.679079 7.382496e-03
fum MA
            -1.883355e+00 5.806071e-01 -3.243768 1.179600e-03
           -1.384712e+02 4.355941e+01 -3.178903 1.478334e-03 1.048749e+02 5.308927e+01 1.975445 4.821769e-02
fum CA
pu CA
fqm CA
            -4.371876e+04 1.557738e+04 -2.806555 5.007443e-03
           -1.091354e-01 3.297999e-02 -3.309141 9.358274e-04
pts MA2
            3.066275e+00 9.206231e-01 3.330652 8.664299e-04
pts_CA2
pry CA2
            -2.900893e-01 7.163469e-02 -4.049565 5.131302e-05
td CA2
           -2.234860e+01 6.585990e+00 -3.393354 6.904227e-04
           -3.926091e-01 1.899110e-01 -2.067332 3.870285e-02
sfpy CA2
           6.216387e-05 5.640637e-05 1.102072 2.704305e-01
Sq kry MA
            -1.468557e+01 6.936046e+00 -2.117283 3.423581e-02
Sq pu CA
           4.441890e+03 1.595779e+03 2.783524 5.377183e-03
Sq fgm CA
Sq fgat CA2 -1.953557e+00 6.795143e-01 -2.874932 4.041150e-03
Sq sfpy CA2 5.386083e-04 2.538939e-04 2.121391 3.388890e-02
```

```
      Sqrt_pr_MA
      1.155682e+00
      5.167798e-01
      2.236313
      2.533126e-02

      Sqrt_pts_CA
      -1.350652e+01
      4.647302e+00
      -2.906314
      3.657145e-03

      Sqrt_fum_CA
      2.599915e+02
      7.666253e+01
      3.391376
      6.954250e-04

      Sqrt_fgm_CA
      7.462721e+04
      2.648245e+04
      2.817987
      4.832578e-03
```

Train:

p\_data 0 1 0 63 24 1 43 160

Test:

p\_data 0 1 0 19 13 1 0 1

#### Kansas City Chiefs

Coefficients:

```
Std. Error z value
                   Estimate
                                                          Pr(>|z|)
(Intercept) -1.050834e+05 3.179127e+04 -3.305416 9.483553e-04
              7.377092e-01 2.045709e-01 3.606130 3.107971e-04
pu MA
              -4.174742e+00 1.723811e+00 -2.421810 1.544344e-02
sfpy MA
ry_CA
             2.684553e-01 8.445761e-02 3.178580 1.479983e-03
ra CA
             -3.055962e+00 6.392827e-01 -4.780299 1.750350e-06
             -1.463531e+00 8.260037e-01 -1.771822 7.642416e-02
py CA
pa CA
             -6.123738e+03 1.856125e+03 -3.299206 9.695858e-04
             -1.254572e+02 3.720524e+01 -3.372030 7.461644e-04
ints CA
npy_CA
             -2.849073e+00 6.440449e-01 -4.423718 9.701669e-06
             -1.444202e+00 5.778653e-01 -2.499202 1.244735e-02 1.996204e-03 8.089700e-04 2.467587 1.360273e-02 3.025461e-03 1.694258e-03 1.785715 7.414546e-02 2.974546e+01 9.030213e+00 3.293993 9.877483e-04
ry_MA2
Sq sfpy MA
Sq_py_CA
Sq pa CA
              6.338912e+01 1.801917e+01 3.517872 4.350225e-04
Sq ints CA
               8.390867e-03 1.872446e-03 4.481234 7.421286e-06
Sq npy CA
               2.209960e-03 8.375800e-04 2.638506 8.327229e-03
Sq ry MA2
Sqrt sfpy MA 1.032094e+02 4.313668e+01 2.392613 1.672887e-02
Sqrt pa CA 4.778829e+04 1.447823e+04 3.300699 9.644420e-04
            1.943059e+01 8.134018e+00 2.388806 1.690320e-02
Sqrt ry MA2
Sqrt ra MA2 -6.381652e-01 6.314589e-01 -1.010620 3.121981e-01
Sqrt pc MA2 -1.011249e+00 4.310790e-01 -2.345856 1.898345e-02
```

Confusion Matrices:

Train:

```
p_data 0 1
0 111 42
1 33 88
```

```
p_data 0 1
0 3 3
1 9 20
```

#### Seattle Seahawks

#### Coefficients:

```
Estimate
                             Std. Error z value
                                                           Pr(>|z|)
(Intercept) -1.364752e+03 9.786849e+02 -1.3944757 1.631740e-01
             1.498690e+00 2.958892e-01 5.0650370 4.083210e-07
Home.1
              -8.826661e-01 4.366933e-01 -2.0212496 4.325393e-02
ra MA
              6.186528e-02 4.556408e-02 1.3577645 1.745384e-01
pa MA
kry CA
              -2.232470e+01 1.562216e+01 -1.4290410 1.529924e-01
             -7.543524e-01 7.896303e-01 -0.9553235 3.394141e-01
top CA
              2.209049e+00 1.575835e+00 1.4018274 1.609668e-01
sfpy_CA
              4.782174e-01 1.807509e-01 2.6457266 8.151566e-03
sk MA2
td MA2
              2.936099e+01 1.703148e+01 1.7239251 8.472137e-02
              -7.233186e-02 3.341825e-02 -2.1644420 3.043044e-02
sfpy MA2
             -1.860984e+00 8.088124e-01 -2.3008846 2.139815e-02
pry CA2
kr CA2
              1.772851e+01 1.234567e+01 1.4360112 1.509992e-01
Sq ra MA
             1.727929e-02 7.665378e-03 2.2541988 2.418366e-02
Sq kry CA
              3.659079e-02 2.600792e-02 1.4069097 1.594542e-01
            -3.302028e-03 2.242214e-03 -1.4726641 1.408416e-01
Sq sfpy CA
Sq_tdMA2
              -2.149597e+00 1.185920e+00 -1.8125994 6.989364e-02
              9.987085e-05 4.647829e-05 2.1487636 3.165314e-02
Sq_sfpy_MA2
Sqrt_kry_CA 2.968028e+02 2.075536e+02 1.4300060 1.527153e-01 Sqrt_td_MA2 -5.817131e+01 3.442596e+01 -1.6897513 9.107554e-02 Sqrt_pry_CA2 1.724734e+01 7.458381e+00 2.3124778 2.075137e-02
Sqrt kr CA2 -7.092901e+01 4.987456e+01 -1.4221481 1.549833e-01
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
0 83 33
1 42 131
```

#### Test:

#### Miami Dolphins

```
Estimate Std. Error z value
                                                          Pr(>|z|)
              7.927035e+05 3.372202e+05 2.350700 1.873812e-02
(Intercept)
              2.302692e+00 9.879477e-01 2.330783 1.976479e-02
kr MA
              5.459567e+04 2.243078e+04 2.433962 1.493455e-02
top CA
sfpy_CA
             -4.927348e+00 1.522507e+00 -3.236338 1.210740e-03
             -4.476721e+02 1.658818e+02 -2.698742 6.960215e-03
npy_CA
              3.304920e+00 1.784836e+00 1.851665 6.407388e-02
3.678997e-01 3.135104e-01 1.173485 2.406014e-01
4.416924e+01 1.934162e+01 2.283637 2.239288e-02
pr MA2
sk CA2
fgat CA2
             -3.433921e-01 1.428767e-01 -2.403416 1.624268e-02
Sq kr MA
             1.167558e-01 3.575709e-02 3.265248 1.093684e-03
Sq rza MA
              2.082541e+01 4.586315e+00 4.540772 5.604867e-06
Sq fum CA
             1.095783e+00 2.736421e-01 4.004438 6.216522e-05
Sq kr CA
             -2.969403e+02 1.225372e+02 -2.423267 1.538161e-02
Sq top CA
Sq sfpy CA
            6.263577e-03 2.028668e-03 3.087532 2.018258e-03
Sq npy CA
             3.737790e-01 1.388568e-01 2.691831 7.106088e-03
Sq fgat CA2 -1.176555e+01 5.159108e+00 -2.280540 2.257571e-02
Sqrt top CA -4.029377e+05 1.651822e+05 -2.439352 1.471361e-02
```

```
Sqrt_rza_CA -1.419501e+01 3.255536e+00 -4.360268 1.299033e-05 Sqrt_npy_CA 8.425217e+03 3.118070e+03 2.702062 6.891097e-03 Sqrt_fum_MA2 2.046416e+00 6.059647e-01 3.377121 7.324881e-04 Sqrt_pr_MA2 -1.026074e+01 5.205893e+00 -1.970986 4.872550e-02
```

Train:

```
p_data 0 1
0 111 46
1 33 81
```

Test:

```
p_data 0 1
0 16 12
1 2 1
```

#### Chicago Bears

Coefficients:

```
Std. Error z value
                    Estimate
                                                              Pr(>|z|)
(Intercept) -3.459443e+04 1.204306e+04 -2.872562 4.071579e-03
kry CA
              -1.068090e+02 6.743843e+01 -1.583800 1.132393e-01
              -5.496604e+02 2.685266e+02 -2.046950 4.066302e-02
top CA
fgat CA
              -1.515548e+04 9.515959e+03 -1.592638 1.112415e-01
sfpy CA
              5.005769e-02 3.143518e-02 1.592410 1.112927e-01
pa MA2
              2.437118e-01 6.664489e-02 3.656872 2.553122e-04
              -3.459754e-01 9.051386e-02 -3.822347 1.321873e-04
pc MA2
pr_CA2
              -4.890251e+02 2.152519e+02 -2.271874 2.309414e-02
             9.551154e+00 2.589929e+00 3.687805 2.261965e-04 2.013222e-01 1.193988e-01 1.686132 9.177031e-02
Sq ints CA
Sq_kry_CA
            -4.008128e+00 1.177450e+00 -3.404075 6.638858e-04 1.431314e+03 8.908024e+02 1.606769 1.081050e-01 4.419205e+00 1.820950e+00 2.426868 1.522980e-02 9.366111e-02 3.296671e-02 2.841081 4.496085e-03
Sq_td_CA
Sq_fgat CA
Sq rzc CA
Sq_sk MA2
Sq_pr_CA2
              3.839405e+01 1.703502e+01 2.253830 2.420685e-02
Sqrt kr MA
             -5.486932e+00 1.323821e+00 -4.144769 3.401559e-05
Sqrt kry MA
              8.494290e-01 2.283948e-01 3.719125 1.999139e-04
              1.334098e+03 8.724498e+02 1.529140 1.262298e-01
Sqrt kry CA
Sqrt_top_CA
               5.946964e+03 2.894519e+03 2.054560 3.992151e-02
Sqrt fgat CA 2.679860e+04 1.691742e+04 1.584083 1.131748e-01
                9.400908e+02 4.144851e+02 2.268093 2.332353e-02
Sqrt pr CA2
```

Confusion Matrices:

Train:

```
p_data 0 1
0 102 38
1 36 95
```

```
p_data 0 1
0 8 4
1 8 13
```

#### Minnesota Vikings

#### Coefficients:

```
z value
                      Estimate
                                  Std. Error
                                                                    Pr(>|z|)
(Intercept) 1.719829e+04 5.042291e+03 3.4108095 6.477032e-04
               1.642190e+00 3.090199e-01 5.3141885 1.071337e-07

-1.102429e+02 3.664650e+01 -3.0082787 2.627320e-03

1.139034e+01 3.930244e+00 2.8981258 3.754000e-03

4.085470e+02 1.495720e+02 2.7314397 6.305827e-03

2.178480e+02 6.097724e+01 3.5726113 3.534392e-04
Home.1
pc CA
kry_CA
top CA
fgat CA
sfpy_CA
pen_MA2
               -8.762784e+00 3.760029e+00 -2.3305097 1.977923e-02
                2.741077e+00 1.272894e+00 2.1534207 3.128563e-02
pa_CA2
                2.890600e+02 1.560634e+02 1.8521966 6.399760e-02
                9.508719e-02 3.517509e-02 2.7032535 6.866435e-03
pen CA2
Sq_fgat CA
              -6.347071e+01 1.852540e+01 -3.4261445 6.122146e-04
Sq sfpy CA
              1.246504e-02 5.472570e-03 2.2777298 2.274268e-02
                2.076889e-06 8.907594e-06 0.2331593 8.156377e-01
Sq py MA2
Sq_pen MA2
               -9.387594e-03 4.174822e-03 -2.2486215 2.453659e-02
               -9.224310e-02 4.818269e-02 -1.9144448 5.556334e-02
Sq td MA2
Sq_pa_CA2
                -1.510407e+00 8.014697e-01 -1.8845466 5.949108e-02
Sqrt_pc CA
                9.777462e+02 3.289778e+02 2.9720734 2.957960e-03
Sqrt_kry_CA -2.117384e+02 7.534061e+01 -2.8104146 4.947772e-03 Sqrt_top_CA -4.497843e+03 1.646793e+03 -2.7312744 6.308991e-03
Sqrt pen MA2 -2.454975e+01 1.190549e+01 -2.0620532 3.920267e-02
Sqrt pa CA2 -2.174197e+03 1.184366e+03 -1.8357466 6.639514e-02
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
0 104 36
1 37 97
```

#### Test:

```
p_data 0 1
0 11 13
1 1 9
```

#### Tampa Bay Buccaneers

```
Estimate Std. Error z value
(Intercept) 8.670450e+03 2.590025e+03 3.347631 8.150534e-04
       1.952195e+00 1.173615e+00 1.663403 9.623180e-02
pts CA
pc CA
            7.077709e+02 2.819026e+02 2.510693 1.204943e-02
top_CA
           -8.448826e+00 2.017275e+00 -4.188238 2.811286e-05
           -1.738630e+01 7.943860e+00 -2.188646 2.862258e-02
td CA
rzc_CA
           -1.016184e+01 4.331595e+00 -2.345980 1.897712e-02 8.828733e+00 4.154464e+00 2.125120 3.357664e-02
npy_CA
             7.672146e-01 2.738250e-01 2.801843 5.081167e-03
rza MA2
           -6.941472e+00 3.222182e+00 -2.154277 3.121846e-02
ra CA2
           1.883860e-01 4.578021e-02 4.115010 3.871635e-05
Sq rza MA
Sq py CA
            8.435022e-04 2.601897e-04 3.241874 1.187466e-03
            -6.203828e+00 2.636664e+00 -2.352908 1.862724e-02
Sq pc CA
           1.536290e+01 6.157593e+00 2.494953 1.259739e-02
Sq kr CA
Sq pts MA2 -2.974804e-03 9.300759e-04 -3.198454 1.381668e-03
Sq pen CA2 6.432241e-04 2.891403e-04 2.224609 2.610748e-02
Sqrt pen MA 5.743616e-01 1.915316e-01 2.998782 2.710608e-03
Sqrt pc CA -4.086347e+03 1.581586e+03 -2.583702 9.774620e-03
```

```
Sqrt_pu_CA 1.575260e+02 3.958963e+01 3.978972 6.921389e-05 Sqrt_kr_CA -3.527852e+02 1.462553e+02 -2.412120 1.586008e-02 Sqrt_npy_CA -2.610107e+02 1.140001e+02 -2.289566 2.204647e-02 Sqrt_ra_CA2 7.250413e+01 3.382465e+01 2.143530 3.207059e-02
```

Train:

p\_data 0 1 0 119 46 1 32 75

Test:

p\_data 0 1 0 3 3 1 19 7

#### New England Patriots

Coefficients:

```
Estimate
                             Std. Error
                                          z value
                                                        Pr(>|z|)
              2.107935e+04 7.874893e+03 2.676779 0.007433366
(Intercept)
              9.118794e-01 3.116019e-01 2.926425 0.003428826
Home.1
             -1.174757e+02 4.593522e+01 -2.557420 0.010545183
ry_CA
             6.027860e+00 2.242823e+00 2.687621 0.007196293
py_CA
pu CA
             -2.219707e+02 7.241170e+01 -3.065398 0.002173803
kry CA
             2.936684e-01 1.197304e-01 2.452746 0.014177047
             -9.870478e+00 3.379868e+00 -2.920374 0.003496121
sfpy CA
             -1.028876e+02 6.855585e+01 -1.500785 0.133411097
ra_CA2
             -3.010825e+00 1.594988e+00 -1.887678 0.059069145
rza CA2
Sq sfpy CA
             1.267665e-02 4.385205e-03 2.890777 0.003842910
Sq_pts_CA2
            -5.258185e-03 2.155205e-03 -2.439761 0.014696979
            5.987446e-01 4.079698e-01 1.467620 0.142207553
4.217278e-01 3.385355e-01 1.245742 0.212859237
1.361107e+00 6.334669e-01 2.148663 0.031661112
Sq_ra_CA2
Sqrt_pts MA
Sqrt pa MA
              4.810449e+03 1.845592e+03 2.606453 0.009148548
Sqrt ry CA
             1.627850e+01 1.228797e+01 1.324751 0.185253878
Sqrt ra CA
Sqrt_py_CA
            -1.849338e+02 6.651274e+01 -2.780426 0.005428755
             9.743806e+02 3.151182e+02 3.092111 0.001987385
Sqrt_pu_CA
             7.311284e+02 4.831814e+02 1.513155 0.130240237
Sqrt ra CA2
Sqrt rza CA2 1.201269e+01 4.091755e+00 2.935828 0.003326582
log ry CA
             -1.232445e+04 4.631304e+03 -2.661119 0.007788149
```

Confusion Matrices:

Train:

```
p_data 0 1
0 29 6
1 47 218
```

Test:

p\_data 0 1 0 0 0 1 9 29

#### Detroit Lions

#### Coefficients:

```
Std. Error
                   Estimate
                                             z value
                                                            Pr(>|z|)
             2.983847e+04 8.724549e+03 3.420059 6.260763e-04
(Intercept)
              5.283601e-01 1.415880e-01 3.731674 1.902112e-04
3.373877e+00 2.188389e+00 1.541717 1.231423e-01
-1.000494e+01 3.822561e+00 -2.617339 8.861832e-03
pc MA
ints MA
pu MA
               6.003860e-02 1.911223e-02 3.141372 1.681585e-03 1.209541e+02 2.789144e+01 4.336603 1.447016e-05
pry MA
pts CA
              5.768270e+02 1.742222e+02 3.310870 9.300652e-04
ry CA
              1.271149e+02 4.546240e+01 2.796044 5.173242e-03
pa CA
rzc CA
              -2.137406e+01 6.651826e+00 -3.213262 1.312366e-03
rzc MA2
             -1.192630e+00 2.846267e-01 -4.190155 2.787634e-05
              5.043813e-05 2.428369e-05 2.077037 3.779814e-02
Sq_py_MA
              -7.322612e-03 1.647369e-03 -4.445034 8.787816e-06
Sq pa MA
Sq td MA
              -2.700387e-01 9.428503e-02 -2.864068 4.182386e-03
Sq pts CA
              -3.164613e+00 7.371084e-01 -4.293280 1.760525e-05
              -1.042653e+00 3.122226e-01 -3.339453 8.394369e-04
Sq ry CA
Sqrt_ints_MA -6.455960e+00 4.571815e+00 -1.412122 1.579141e-01
Sqrt_pu_MA 4.531553e+01 1.672622e+01 2.709251 6.743533e-03
              -7.376383e+03 2.239696e+03 -3.293475 9.895711e-04
Sqrt_ry_CA
Sqrt_py_CA
             -8.610193e+00 3.293228e+00 -2.614514 8.935439e-03
            -1.455389e+03 5.298428e+02 -2.746831 6.017413e-03
Sqrt pa CA
Sqrt sfpy CA -1.187910e+01 3.661422e+00 -3.244394 1.177009e-03
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
    0 155 41
    1 20 51
```

#### Test:

```
p_data 0 1
0 14 11
1 3 4
```

#### New Orleans Saints

```
Estimate Std. Error
                                            z value
                                                            Pr(>|z|)
               2.225088e+04 1.958023e+04 1.1363951 2.557912e-01
(Intercept)
              3.665816e+00 1.590596e+00 2.3046804 2.118448e-02
fgat MA
pts CA
              -1.486695e+02 7.942876e+02 -0.1871734 8.515247e-01
              -1.707697e+04 6.128744e+03 -2.7863735 5.330141e-03
pu_CA
              -4.090406e-01 1.556799e-01 -2.6274466 8.602834e-03
pen CA
              1.692289e+02 7.550403e+01 2.2413222 2.500521e-02
fgm_CA
              -5.788069e+00 1.564455e+00 -3.6997353 2.158244e-04 3.424708e+02 9.936910e+01 3.4464518 5.680000e-04 3.603006e+01 1.713696e+01 2.1024767 3.551154e-02
rzc CA
sfpy_CA
fgat_CA2
rza CA2
              1.122072e+00 5.963837e-01 1.8814599 5.990938e-02
Sq fgat MA
             -1.037292e+00 4.320856e-01 -2.4006632 1.636539e-02
              3.624952e-05 1.699952e-05 2.1323845 3.297525e-02
Sq_npy_MA
             1.158936e+00 5.699915e+00 0.2033252 8.388809e-01
Sq pts CA
Sq ints CA
             1.124072e+01 2.551584e+00 4.4053881 1.055947e-05
Sq pu CA
             6.242235e+02 2.234465e+02 2.7936152 5.212247e-03
             -1.565088e-01 4.536217e-02 -3.4502050 5.601611e-04
Sq sfpy CA
Sq fgat CA2 -9.951835e+00 4.704077e+00 -2.1155765 3.438084e-02
```

```
Sqrt_pts_CA 9.083459e+02 5.100246e+03 0.1780984 8.586457e-01 Sqrt_pu_CA 4.854794e+04 1.746292e+04 2.7800583 5.434914e-03 Sqrt_fgm_CA -3.943908e+02 1.818987e+02 -2.1681899 3.014424e-02 Sqrt_sfpy_CA -8.716077e+03 2.530224e+03 -3.4447843 5.715153e-04
```

Train:

Test:

p\_data 0 1 0 10 26 1 0 0

#### Arizona Cardinals

Coefficients:

```
Estimate Std. Error z value
                                                    Pr(>|z|)
             2.423468e+02 9.533461e+01 2.542065 0.0110199677
(Intercept)
             1.634740e-03 1.199845e-02 0.136246 0.8916268045
pen MA
             1.047171e+01 4.277000e+00 2.448377 0.0143501474
ints CA
             -2.987688e+00 2.372819e+00 -1.259130 0.2079833608
pry CA
kry_CA
             -4.384492e-01 1.472928e-01 -2.976719 0.0029135111
top CA
             -1.643553e+00 6.949463e-01 -2.365007 0.0180297335
pts MA2
             7.417148e-01 3.599468e-01 2.060624 0.0393389623
             2.936647e+00 8.890186e-01 3.303246 0.0009557238
pts CA2
             4.048956e+02 1.686921e+02 2.400205 0.0163858818
ints CA2
pr CA2
             2.067334e+01 9.385291e+00 2.202738 0.0276132065
fgm CA2
             -2.033446e+01 1.302779e+01 -1.560853 0.1185585518
Sq_npy_MA
             -2.923617e-05 8.878682e-06 -3.292850 0.0009917729
Sq_pry_CA
             8.838754e-02 6.366125e-02 1.388404 0.1650140386
             -6.726021e-02 2.025635e-02 -3.320450 0.0008987242
Sq pts CA2
             -5.718960e+01 2.600376e+01 -2.199282 0.0278578757
Sq ints CA2
             -4.566175e+00 2.065938e+00 -2.210219 0.0270899787
Sq pr CA2
              6.494785e+00 4.352339e+00 1.492252 0.1356332147
Sq fgm CA2
             3.676543e+01 1.325827e+01 2.773019 0.0055538883
Sqrt kr CA
Sqrt pts MA2 -6.914285e+00 3.287763e+00 -2.103036 0.0354626094
Sgrt ry CA2
            -6.884529e-01 3.596796e-01 -1.914073 0.0556108769
Sqrt ints CA2 -5.777215e+02 2.326328e+02 -2.483405 0.0130132866
```

Confusion Matrices:

Train:

```
p_data 0 1
0 111 46
1 41 77
```

```
p_data 0 1
0 12 9
1 9 2
```

#### New York Giants

#### Coefficients:

```
Estimate Std. Error
                                             z value
                                                            Pr(>|z|)
             4.891866e+04 1.186145e+04 4.124172 3.720700e-05
(Intercept)
fgat MA
               3.375386e+00 6.963141e-01 4.847505 1.250241e-06
              4.281439e+02 1.456260e+02 2.940024 3.281863e-03
-5.010677e+01 1.350501e+01 -3.710235 2.070667e-04
8.278232e+00 3.055266e+00 2.709496 6.738550e-03
ry CĀ
ra_CA
py_CA
              -1.292145e+01 7.976980e+00 -1.619843 1.052661e-01
pry CA
              -3.849732e-01 1.626247e-01 -2.367249 1.792088e-02
pen CA
              1.816787e+04 9.015542e+03 2.015172 4.388661e-02
td CA
Sq_pry_MA
              -1.587090e-03 4.966818e-04 -3.195385 1.396445e-03
Sq rzc MA
              -2.668883e-01 1.118617e-01 -2.385878 1.703839e-02
              -5.802926e-01 1.948994e-01 -2.977395 2.907094e-03
Sq_ry_CA
Sq ra CA
              7.689643e-01 2.195679e-01 3.502171 4.614829e-04
Sq td CA
              -1.349721e+03 6.504737e+02 -2.074982 3.798821e-02
Sq ints MA2
              4.305354e-01 1.532594e-01 2.809195 4.966562e-03
             1.536298e+00 5.400339e-01 2.844819 4.443673e-03
Sqrt pts MA
Sqrt_fgm_MA -8.129907e+00 1.787802e+00 -4.547431 5.430461e-06
Sqrt_ry_CA
              -6.320502e+03 2.164376e+03 -2.920242 3.497595e-03
             -2.402382e+02 8.959752e+01 -2.681304 7.333593e-03 1.261629e+02 7.102875e+01 1.776223 7.569616e-02
Sqrt_py_CA
Sqrt_pry_CA
Sqrt td CA -3.626860e+04 1.825734e+04 -1.986522 4.697539e-02
Sqrt fqat CA -6.069575e+01 1.442310e+01 -4.208233 2.573759e-05
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
0 83 40
1 47 112
```

#### Test:

```
p_data 0 1
0 0 0
1 24 8
```

#### San Diego/Los Angeles Charges

```
Estimate Std. Error z value
                                                          Pr(>|z|)
             5.491935e+05 2.111470e+05 2.601001 9.295229e-03
(Intercept)
             -4.287746e+01 1.581643e+01 -2.710944 6.709198e-03
pts CA
              4.308051e+00 1.949889e+00 2.209383 2.714803e-02 9.414301e+01 3.198035e+01 2.943777 3.242340e-03
ry_CA
sk_CA
              -3.233419e+02 9.633967e+01 -3.356270 7.900138e-04
pr_CA
             -1.718407e+01 5.459991e+00 -3.147271 1.648023e-03 3.756380e+04 1.417392e+04 2.650206 8.044265e-03
pen CA
top_CA
              -2.226085e+01 5.824514e+00 -3.821923 1.324149e-04
sfpy_CA
             -2.289384e-01 5.111826e-02 -4.478604 7.513294e-06
pry CA2
             -4.776299e-01 1.828295e-01 -2.612433 8.990031e-03
Sq ints MA
Sq sk CA
             -2.061190e+01 6.970816e+00 -2.956885 3.107640e-03
Sq_pr_CA
             6.488960e+01 1.889053e+01 3.435033 5.924811e-04
             1.578387e-01 4.847642e-02 3.255989 1.129980e-03
Sq pen CA
Sq top CA
             -2.110790e+02 7.909705e+01 -2.668607 7.616643e-03
Sq rza CA2
             -2.323957e-01 1.114463e-01 -2.085271 3.704470e-02
Sqrt pts CA 3.893046e+02 1.441030e+02 2.701573 6.901243e-03
             -8.352332e+01 3.971163e+01 -2.103246 3.544430e-02
Sqrt ry CA
```

```
Sqrt_top_CA -2.727547e+05 1.032790e+05 -2.640949 8.267404e-03 
Sqrt_fgm_CA 4.813511e+01 1.880120e+01 2.560215 1.046074e-02 
Sqrt_sfpy_CA 8.459552e+02 2.233445e+02 3.787670 1.520668e-04 
Sqrt_fum_MA2 2.000969e+00 6.112080e-01 3.273793 1.061141e-03
```

Train:

Test:

p\_data 0 1 0 12 22 1 0 0

#### Oakland Raiders

Coefficients:

```
Estimate Std. Error z value
                                                        Pr(>|z|)
             6.042588e+02 3.257462e+02 1.854999 6.359638e-02
(Intercept)
              -1.448229e+01 5.784126e+00 -2.503800 1.228675e-02
ra CA
              -4.407720e+00 1.331337e+00 -3.310747 9.304730e-04
pa CA
pc CA
              8.466341e+00 1.874801e+00 4.515862 6.305970e-06
pry CA
              5.633453e+00 2.245937e+00 2.508286 1.213184e-02
rzc CA
              -1.463609e+01 3.112642e+00 -4.702144 2.574437e-06
pry MA2
              -2.193309e-01 8.248014e-02 -2.659196 7.832735e-03
              9.233461e-01 4.454424e-01 2.072874 3.818400e-02
sk CA2
              6.541291e+02 3.376632e+02 1.937223 5.271807e-02 2.882367e-01 1.031377e-01 2.794679 5.195121e-03
fgat CA2
Sq_ra_CA
              -1.507737e-01 5.820495e-02 -2.590392 9.586658e-03 1.184289e+00 3.999780e-01 2.960885 3.067568e-03
Sq_pry_CA
Sq_kr_CA
Sq sfpy CA
              -3.296771e-04 8.142635e-05 -4.048776 5.148612e-05
Sq_pts_CA2
              -4.689551e-02 1.714297e-02 -2.735553 6.227547e-03
Sq pry CA2
              -4.213830e-03 1.291273e-03 -3.263315 1.101171e-03
Sq kry CA2
              -2.903587e-04 1.101717e-04 -2.635511 8.401074e-03
Sq_td_CA2
              2.833274e+00 1.063145e+00 2.664993 7.698995e-03
Sq fgat CA2
              -5.731889e+01 3.054781e+01 -1.876367 6.060495e-02
Sqrt pu CA
              6.205035e+01 1.854018e+01 3.346804 8.174901e-04
Sqrt pry MA2 2.225988e+00 7.816271e-01 2.847890 4.401018e-03
Sqrt fgat CA2 -1.181470e+03 6.093632e+02 -1.938860 5.251836e-02
```

Confusion Matrices:

Train:

```
p_data 0 1
0 145 45
1 22 63
```

```
p_data 0 1
0 18 8
1 4 2
```

#### Baltimore Ravens

#### Coefficients:

```
Estimate Std. Error
                                                         z value
                                                                             Pr(>|z|)
(Intercept) 2.541975e+02 1.294581e+02 1.9635502 4.958228e-02
                1.606568e+00 3.079412e-01 5.2171258 1.817209e-07
1.599366e+00 9.079025e-01 1.7616053 7.813601e-02
-6.884891e-03 1.513318e-02 -0.4549534 6.491428e-01
Home.1
kr MA
kry_MA
pry CA
                  -1.794127e-01 1.598919e-01 -1.1220871 2.618254e-01
pen CA
                  -1.576295e+01 4.516415e+00 -3.4901461 4.827565e-04
                  1.095283e+01 4.740300e+00 2.3105770 2.085623e-02
top CA2
rza CA2
                 -1.866419e+01 5.600870e+00 -3.3323739 8.610850e-04
Sq kr MA
                  -1.868975e-01 1.113138e-01 -1.6790153 9.314906e-02
                  2.096597e+00 6.096427e-01 3.4390578 5.837425e-04
Sq_sk_CA
                  1.531840e-01 4.360625e-02 3.5128906 4.432599e-04
Sq pen CA
Sq npy CA
                 8.077265e-04 2.600480e-04 3.1060667 1.895940e-03
                  -1.148334e-01 4.325870e-02 -2.6545739 7.940864e-03
Sq td MA2
Sq_kr_CA2
                 1.719530e-01 7.828185e-02 2.1965886 2.804984e-02
                 -1.709774e-01 7.665944e-02 -2.2303504 2.572419e-02
Sq top CA2
Sq_rza_CA2
                 2.132448e+00 7.209900e-01 2.9576669 3.099769e-03

      Sqrt_pu_CA
      -5.207265e+01
      1.758654e+01
      -2.9609380
      3.067037e-03

      Sqrt_kr_CA
      3.557909e+01
      1.293365e+01
      2.7508918
      5.943327e-03

      Sqrt_rza_CA2
      1.512654e+01
      5.546251e+00
      2.7273442
      6.384640e-03

      log_py_MA
      2.729835e+00
      1.273408e+00
      2.1437242
      3.205499e-02

                  -4.494590e+00 1.473444e+00 -3.0503971 2.285390e-03
log pa MA
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
0 79 35
1 43 132
```

#### Test:

```
p_data 0 1
0 5 6
1 9 13
```

#### Pittsburgh Steelers

```
Estimate Std. Error
                                             z value
                                                            Pr(>|z|)
             42.085799784 2.599775e+02 0.16188248 8.713984e-01
(Intercept)
            0.908497361 2.954240e-01 3.07523242 2.103386e-03
Home.1
               5.706800692 1.825629e+00 3.12593671 1.772397e-03
sk MA
              -0.018796282 5.239531e-03 -3.58739794 3.339944e-04 3.765838964 6.557352e+01 0.05742926 9.542033e-01
npy_MA
sk_CA
             -78.163391425 3.156141e+01 -2.47654936 1.326593e-02 4.244955900 1.158746e+00 3.66340474 2.488848e-04
pu CA
rza CA
sfpy CA
              -2.227890012 9.745864e-01 -2.28598522 2.225512e-02
              0.522872149 3.493363e-01 1.49675859 1.344561e-01
ra MA2
sk MA2
              -3.296941851 1.193312e+00 -2.76284916 5.729924e-03
              0.888414790 4.045319e-01 2.19615535 2.808083e-02
pry CA2
              -2.459006975 6.241258e-01 -3.93992174 8.150819e-05
rza CA2
              -0.081280496 3.686090e-02 -2.20506011 2.744988e-02
Sq pts CA
Sq td CA
              3.846207178 2.031278e+00 1.89349145 5.829254e-02
              0.002919089 1.301934e-03 2.24211730 2.495379e-02
Sq sfpy CA
              -0.009839669 6.104471e-03 -1.61187918 1.069882e-01
Sq ra MA2
             -16.762960453 5.602330e+00 -2.99214071 2.770285e-03
Sqrt sk MA
```

Train:

```
p_data 0 1
0 53 21
1 49 167
```

Test:

```
p_data 0 1
0 6 8
1 5 14
```

#### Carolina Panthers

Coefficients:

```
Estimate Std. Error z value
(Intercept) -5.773782e+04 1.641185e+04 -3.518058 4.347177e-04
                 -3.018250e+00 9.536083e-01 -3.165083 1.550386e-03 4.558140e+00 1.331484e+00 3.423354 6.185355e-04
kr MA
rzc MA
ry CA
                  -4.216211e+00 1.034750e+00 -4.074619 4.608979e-05
py CA
                 -1.115643e-01 5.318512e-02 -2.097659 3.593527e-02
                  5.163555e+00 1.390147e+00 3.714396 2.036896e-04
rza CA
                 -3.152483e+02 8.978983e+01 -3.510958 4.464950e-04
sfpy CA
                  7.506320e-01 3.116891e-01 2.408272 1.602825e-02
ints MA2
pu CA2
                  -1.306937e+03 5.088951e+02 -2.568186 1.022323e-02

      pq_CA2
      3.253347e+01
      1.183034e+01
      2.750003
      5.959471e-03

      Sq_kr_MA
      4.271847e-01
      1.397254e-01
      3.057315
      2.233292e-03

      Sq_sfpy_CA
      1.446516e-01
      4.088745e-02
      3.537799
      4.034776e-04

      Sq_sk_MA2
      8.543869e-02
      3.650613e-02
      2.340393
      1.926346e-02

      Sq_pu_CA2
      4.711615e+01
      1.791820e+01
      2.629513
      8.550719e-03

                -3.948100e-03 1.175464e-03 -3.358758 7.829371e-04
Sq pry CA2
Sq npy CA2
                -3.275812e-02 1.166178e-02 -2.809016 4.969317e-03
Sqrt rzc MA -1.073592e+01 3.211530e+00 -3.342929 8.289921e-04
Sqrt ry CA 7.895540e+01 2.016334e+01 3.915790 9.010867e-05
Sqrt sfpy CA 8.001007e+03 2.288745e+03 3.495806 4.726322e-04
Sqrt pu CA2 3.736895e+03 1.472903e+03 2.537096 1.117765e-02
Sqrt npy CA2 -5.562088e+02 2.045160e+02 -2.719634 6.535411e-03
```

Confusion Matrices:

Train:

```
p_data 0 1
0 105 32
1 35 109
```

```
p_data 0 1
0 6 11
1 9 7
```

#### Washington Redskins

#### Coefficients:

```
Estimate
                             Std. Error z value
                                                         Pr(>|z|)
(Intercept) -8.119719e+03 5.490259e+03 -1.478932 0.1391585603
             7.188100e+00 2.007012e+00 3.581493 0.0003416369
rzc MA
             -5.783479e+03 2.011051e+03 -2.875849 0.0040294200
pts CA
              3.650152e+03 2.423868e+03 1.505921 0.1320875433
pr_CA
top_CA
             -2.035938e+02 1.058476e+02 -1.923461 0.0544222005
             3.593541e+04 1.384567e+04 2.595427 0.0094473599
2.666607e-01 9.293066e-02 2.869459 0.0041117439
td CA
pry MA2
             -3.682035e+00 1.077705e+00 -3.416553 0.0006341930
top MA2
Sq_rzc MA
             -2.244131e+00 6.141708e-01 -3.653920 0.0002582673
             5.488989e+01 1.910841e+01 2.872551 0.0040717196
Sq pts CA
             -2.208150e+02 1.602942e+02 -1.377561 0.1683387906
Sq pr CA
Sq top CA
             3.310553e+00 1.729504e+00 1.914163 0.0555992970
Sq td CA
             -3.117272e+03 1.202968e+03 -2.591316 0.0095609559
Sq_top MA2
              6.287819e-02 1.796387e-02 3.500259 0.0004648061
Sqrt_pts CA
             3.227644e+04 1.122669e+04 2.874973 0.0040406245
             -7.976430e+03 5.120247e+03 -1.557821 0.1192756320
Sqrt_pr_CA
Sqrt_pry_CA -4.271919e+00 1.814537e+00 -2.354275 0.0185588519
Sqrt_td_CA -6.632190e+04 2.555832e+04 -2.594924 0.0094611888
Sqrt_ry_MA2 -4.627500e-01 1.503816e-01 -3.077173 0.0020897429
Sqrt pry MA2 -2.446458e+00 8.426352e-01 -2.903342 0.0036920309
Sqrt top CA2 -5.545396e+00 1.983371e+00 -2.795945 0.0051748216
```

#### Confusion Matrices:

#### Train:

```
p_data 0 1
0 133 52
1 25 62
```

#### Test:

```
p_data 0 1
0 4 4
1 13 10
```

#### Tennessee Titans

```
Estimate Std. Error z value
                                                         Pr(>|z|)
(Intercept) -8.232232e+04 3.189576e+04 -2.580980 9.852036e-03
             -9.738242e+02 4.493457e+02 -2.167205 3.021921e-02
ry_CA
kry CA
             1.850567e-01 7.200199e-02 2.570160 1.016515e-02
sfpy_CA
             -1.192363e+02 6.889715e+01 -1.730642 8.351569e-02
             8.345559e+00 4.404324e+00 1.894856 5.811152e-02
pts CA2
             -5.463182e+01 3.074322e+01 -1.777037 7.556219e-02
td CA2
             -4.001323e+00 9.741480e-01 -4.107510 3.999469e-05 3.956264e-03 1.157835e-03 3.416949 6.332705e-04 1.328460e+00 6.159560e-01 2.156745 3.102557e-02
rza CA2
Sq pa MA
Sq_ry_CA
              5.117295e-02 2.972148e-02 1.721750 8.511486e-02
Sq sfpy CA
             2.422447e-01 8.169374e-02 2.965279 3.024084e-03
Sq sk CA2
            4.665698e+00 9.965173e-01 4.682004 2.840833e-06
Sqrt ra MA
Sqrt top MA -6.281597e+00 1.771359e+00 -3.546202 3.908267e-04
Sqrt_ry_CA 1.434258e+04 6.604573e+03 2.171614 2.988482e-02
Sqrt pa CA -1.169185e+01 5.883722e+00 -1.987151 4.690561e-02
Sqrt pr CA -1.888005e+01 8.288992e+00 -2.277726 2.274292e-02
Sqrt sfpy CA 3.128538e+03 1.803893e+03 1.734326 8.286028e-02
```

```
Sqrt_td_MA2   -3.984184e+00   1.113576e+00   -3.577828   3.464613e-04   Sqrt_rzc_MA2   3.214560e+00   1.077750e+00   2.982657   2.857580e-03   Sqrt_pts_CA2   -7.483223e+01   3.884511e+01   -1.926426   5.405122e-02   Sqrt_td_CA2   1.711831e+02   9.189739e+01   1.862763   6.249558e-02
```

Train:

p\_data 0 1 0 107 34 1 36 96

Test:

p\_data 0 1 0 13 16 1 2 3

#### Buffalo Bills

Coefficients:

```
Std. Error
                 Estimate
                                       z value
           3.837520e+03 1.936403e+03 1.981778 4.750412e-02
(Intercept)
            8.322395e-01 3.058629e-01 2.720956 6.509341e-03
Home.1
pts CA
            -1.399563e+01 4.999697e+00 -2.799295 5.121438e-03
pr CA
            3.405271e+03 1.712745e+03 1.988196 4.679007e-02
fqm CA
            3.650933e+01 1.531412e+01 2.384030 1.712422e-02
pu MA2
            1.568565e+02 4.249265e+01 3.691380 2.230405e-04
           -6.335438e-01 2.442222e-01 -2.594129 9.483096e-03
rza MA2
npy_MA2
           -2.777018e+00 8.868654e-01 -3.131274 1.740498e-03
Sq pu CA
            -1.253271e+00 3.541746e-01 -3.538567 4.023049e-04
Sq_pr_CA
           -2.512605e+02 1.246825e+02 -2.015202 4.388347e-02
             2.142923e+01 7.786969e+00 2.751935 5.924426e-03
Sq_td_CA
Sq_pu MA2
            -5.702319e+00 1.523371e+00 -3.743224 1.816742e-04
Sq pen MA2
            -3.077965e-04 1.054540e-04 -2.918775 3.514098e-03
           2.877995e-01 8.117705e-02 3.545330 3.921211e-04
Sq_fgat MA2
            2.776650e-03 8.517726e-04 3.259849 1.114716e-03
Sq npy MA2
Sq fgat CA2
           -1.428693e+00 3.233377e-01 -4.418579 9.935218e-06
Sqrt_pa_CA
           1.300995e+01 4.463232e+00 2.914917 3.557828e-03
           -6.792400e+03 3.442774e+03 -1.972944 4.850193e-02
Sqrt pr CA
Sqrt npy CA 1.248631e+01 3.077701e+00 4.057024 4.970195e-05
Sqrt pu MA2 -4.396838e+02 1.210928e+02 -3.630964 2.823641e-04
Sqrt npy MA2 4.687706e+01 1.542285e+01 3.039455 2.370067e-03
```

Confusion Matrices:

Train:

```
p_data 0 1
0 132 47
1 25 60
```

```
p_data 0 1
     0 5 5
     1 13 10
```

#### Denver Broncos

#### Coefficients:

```
Estimate Std. Error
                                            z value
                                                            Pr(>|z|)
             3.408619e+03 1.627309e+03 2.094635 3.620341e-02
(Intercept)
              -1.323829e-01 5.137047e-02 -2.577023 9.965532e-03
ra MA
              -2.251889e-01 7.793338e-02 -2.889504 3.858495e-03
pry MA
             -5.152739e-01 3.154516e-01 -1.633448 1.023748e-01 8.600888e-01 1.920728e-01 4.477930 7.537016e-06 4.343441e+00 9.748341e-01 4.455569 8.367079e-06
rzc_MA
ry_CA
pa CA
              -4.243861e+02 1.280248e+02 -3.314875 9.168411e-04
pr CA
              2.639293e+03 1.357415e+03 1.944352 5.185296e-02
fgat CA
              4.366137e-01 9.914013e-02 4.404006 1.062702e-05
npy CA
pry MA2
              -4.163020e-02 1.498788e-02 -2.777591 5.476348e-03
              2.112792e-01 8.175935e-02 2.584160 9.761654e-03
top MA2
              -4.471432e-02 2.131777e-02 -2.097513 3.594815e-02
Sq pu MA
Sq pry MA
              4.718071e-03 1.631235e-03 2.892330 3.823955e-03
Sq pr CA
             9.740242e+01 2.927461e+01 3.327197 8.772422e-04
              1.601977e-03 4.062221e-04 3.943600 8.026756e-05
Sq kry CA
              -1.776899e+02 9.729453e+01 -1.826309 6.780366e-02
Sq fgat CA
              -3.198599e-03 1.327282e-03 -2.409887 1.595747e-02 5.430596e-01 1.628432e-01 3.334863 8.534154e-04
Sq_pc_MA2
Sq ints MA2
Sqrt_pts_CA -1.939439e+01 4.112522e+00 -4.715936 2.406016e-06
Sqrt fgat CA -5.480505e+03 2.748293e+03 -1.994149 4.613576e-02
Sqrt ry MA2 -3.722849e-01 1.600822e-01 -2.325586 2.004064e-02
```

#### Confusion Matrices:

#### Train:

#### Test:

```
p_data 0 1
0 5 3
1 16 8
```

#### St. Louis/Los Angeles Rams

```
Estimate Std. Error z value
            1.040525e+04 3.429205e+03 3.034305 2.410906e-03
(Intercept)
             -8.333317e+01 3.721109e+01 -2.239471 2.512527e-02
pa CA
pr_CA
             7.307056e+03 2.795608e+03 2.613763 8.955125e-03 1.408031e+02 3.869817e+01 3.638495 2.742359e-04
kr_CA
             -3.746284e+00 9.426766e-01 -3.974093 7.064803e-05
top_CA
pc MA2
             -1.996639e+01 8.410122e+00 -2.374090 1.759225e-02
             4.450557e-01 1.951686e-01 2.280365 2.258603e-02
kr MA2
             2.547537e-01 8.699526e-02 2.928363 3.407522e-03
top MA2
fgat MA2
             -1.135061e+00 3.266790e-01 -3.474545 5.117213e-04
             6.219783e+02 2.610582e+02 2.382527 1.719425e-02
kr CA2
             -1.307764e+00 4.755325e-01 -2.750104 5.957637e-03
pen CA2
             1.168229e+00 5.151215e-01 2.267871 2.333707e-02
Sq pa CA
Sq_pr CA
             -5.516568e+02 2.182490e+02 -2.527648 1.148293e-02
             -1.589608e+01 4.298807e+00 -3.697788 2.174861e-04
Sq kr CA
             1.584225e-01 6.811328e-02 2.325867 2.002563e-02
Sq pc MA2
             -2.482450e+01 1.095433e+01 -2.266181 2.344029e-02
Sq kr CA2
```

Train:

```
p_data 0 1
0 141 51
1 22 59
```

Test:

```
p_data 0 1
0 9 23
1 1 3
```

#### Houston Texans

Coefficients:

```
Estimate Std. Error z value
                                                    Pr(>|z|)
(Intercept) -1.264912e+02 384.5053985 -0.3289711 7.421776e-01
            1.304969e+00 0.3429893 3.8046926 1.419804e-04
Home.1
ra MA
            2.295650e+00 1.0482931 2.1898931 2.853199e-02
ints MA
           1.317120e+00 0.4899986 2.6880074 7.187981e-03
kr MA
           -8.690203e-01 0.3139809 -2.7677486 5.644497e-03
sk CA
           5.128120e+02 124.4190784 4.1216509 3.761669e-05
           -1.971397e+01 5.7486147 -3.4293427 6.050451e-04
ints\_CA
fum CA
           3.874269e+01 9.5429302 4.0598314 4.910817e-05
rza_CA
           -1.164422e+03 391.8219755 -2.9718143 2.960457e-03
rzc_CA
           -4.684305e+01 10.7603430 -4.3533044 1.341007e-05
ry_CA2
           -3.586186e-02 0.0179812 -1.9944084 4.610744e-02 2.410190e-01 0.5897160 0.4087035 6.827573e-01
pu CA2
           -2.882774e+00 1.0752066 -2.6811347 7.337298e-03
rza CA2
           -1.504889e+00 0.4130284 -3.6435493 2.689041e-04
Sq fum MA
Sq_sk_CA
           -1.850649e+01 4.7430573 -3.9018067 9.547741e-05
Sq pu CA
           -6.445085e-01 0.2151157 -2.9961016 2.734553e-03
Sq fgat CA -1.007940e+01 2.1273339 -4.7380446 2.157904e-06
Sq rza CA
           8.063439e+01 28.9018871 2.7899352 5.271859e-03
Sqrt ra MA -2.669027e+01 11.4379544 -2.3334825 1.962284e-02
Sqrt sk CA -1.446164e+03 341.9219774 -4.2295133 2.341975e-05
Sqrt rza CA 2.437217e+03 784.5009368 3.1067106 1.891815e-03
```

Confusion Matrices:

Train:

```
p_data 0 1
0 110 31
1 24 77
```

```
p_data 0 1
0 16 12
1 2 2
```

#### Cincinnati Bengals

#### Coefficients:

```
Estimate Std. Error z value
                                                                                      Pr(>|z|)
(Intercept) 6.210411e+02 1.990207e+03 0.3120485 0.755003632
                    1.309660e+03 4.473996e+02 2.9272724 0.003419492

-1.402161e+02 5.616404e+01 -2.4965450 0.012540977

-1.738445e+01 6.328826e+00 -2.7468683 0.006016729

4.327728e+03 1.477282e+03 2.9295195 0.003394865
pts CA
sk CA
ints CA
pr CA
                    -8.727761e+03 3.343587e+03 -2.6102989 0.009046315
td CA
                    -8.522874e+03 3.457652e+03 -2.4649310 0.013703962
fgat CA
                    -1.676336e+00 6.289140e-01 -2.6654452 0.007688647
pa MA2
Sq_pts CA
                    -1.334648e+01 4.683082e+00 -2.8499344 0.004372825
                     7.934078e-02 3.321110e-02 2.3889842 0.016895030
Sq pc CA
Sq_pr_CA
                    -3.024478e+02 9.873315e+01 -3.0632847 0.002189217
Sq td CA
                    7.857725e+02 3.098266e+02 2.5361687 0.011207272
Sq fgat CA
                  8.825961e+02 3.727883e+02 2.3675529 0.017906161
                    -1.268930e-01 3.945173e-02 -3.2164109 0.001298048
Sq_td MA2
                     7.983711e-04 2.972007e-04 2.6863026 0.007224763
Sq pen CA2
Sqrt_pts_CA -6.889970e+03 2.355644e+03 -2.9248779 0.003445914
Sqrt_sk_CA 4.003177e+02 1.695594e+02 2.3609298 0.018229180

      Sqrt_pr_CA
      -8.814628e+03
      3.087625e+03
      -2.8548252
      0.004306052

      Sqrt_td_CA
      1.537159e+04
      5.905615e+03
      2.6028777
      0.009244492

      Sqrt_fgat_CA
      1.422150e+04
      5.708461e+03
      2.4913022
      0.012727583

      Sqrt_pa_MA2
      1.924016e+01
      7.175164e+00
      2.6814943
      0.007329415
```

#### Confusion Matrices:

#### Train:

p\_data 0 1 0 98 35 1 44 95

#### Test: