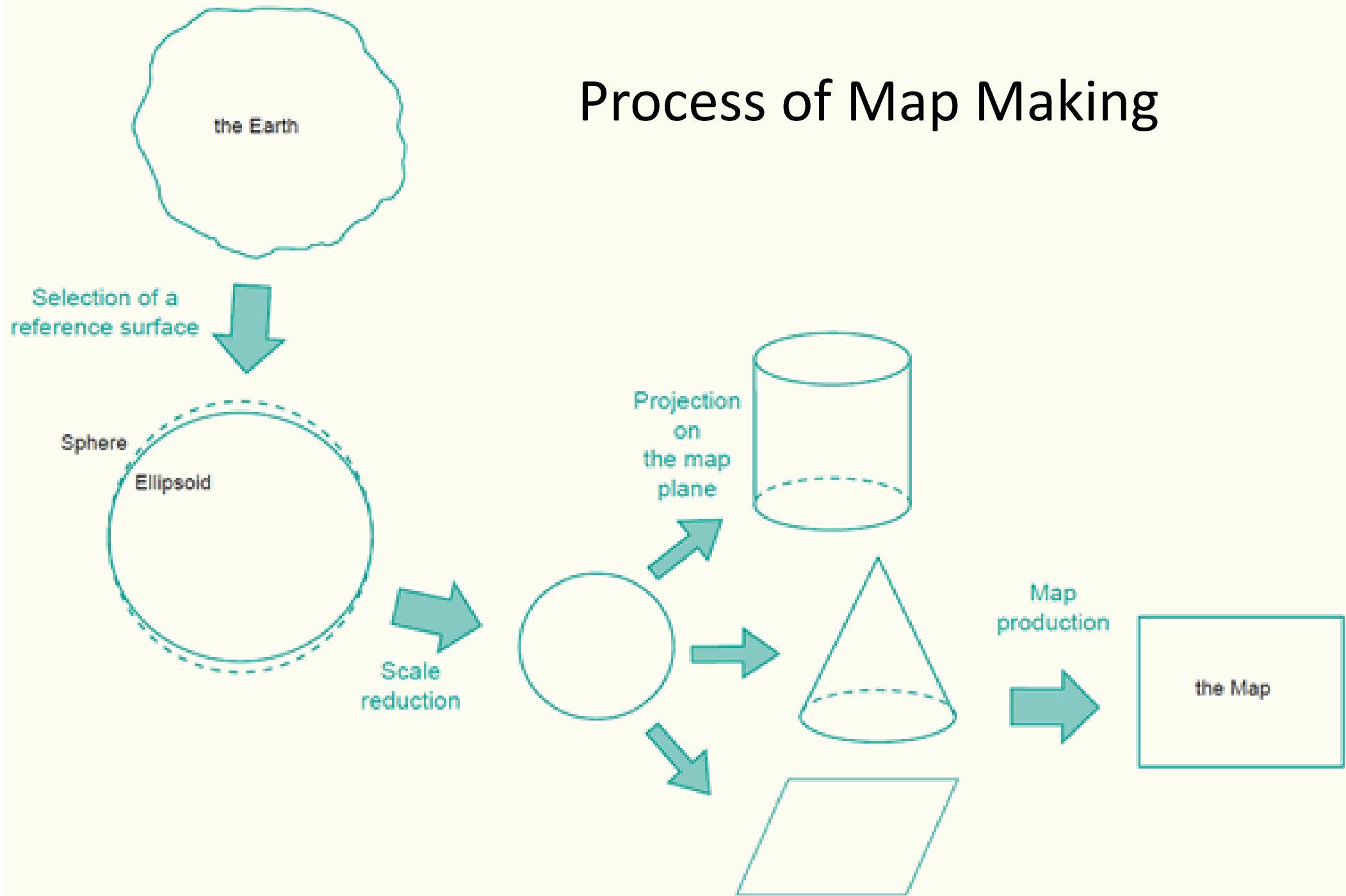


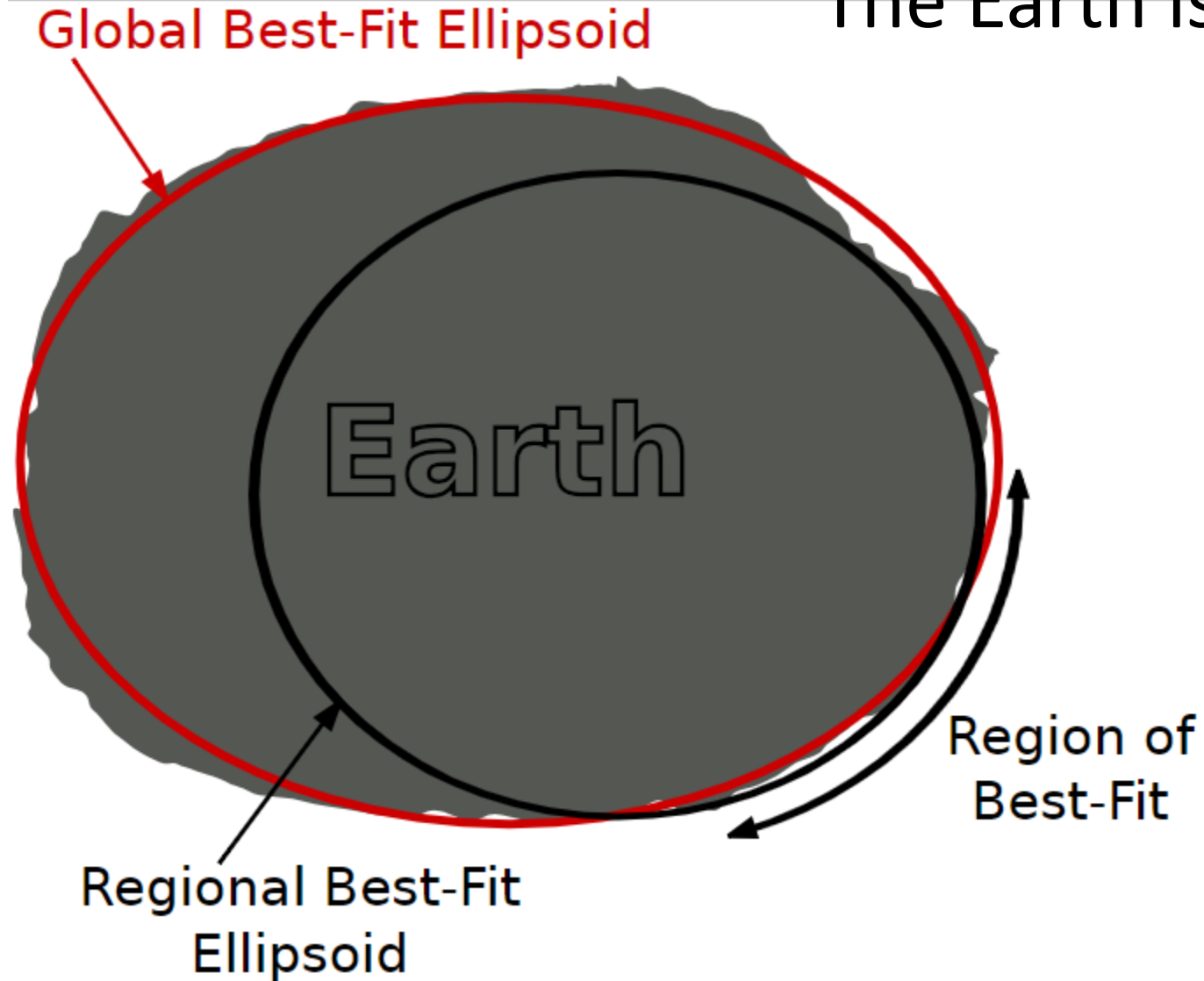
# Coordinate Reference Systems

Rolf Becker

# Process of Map Making

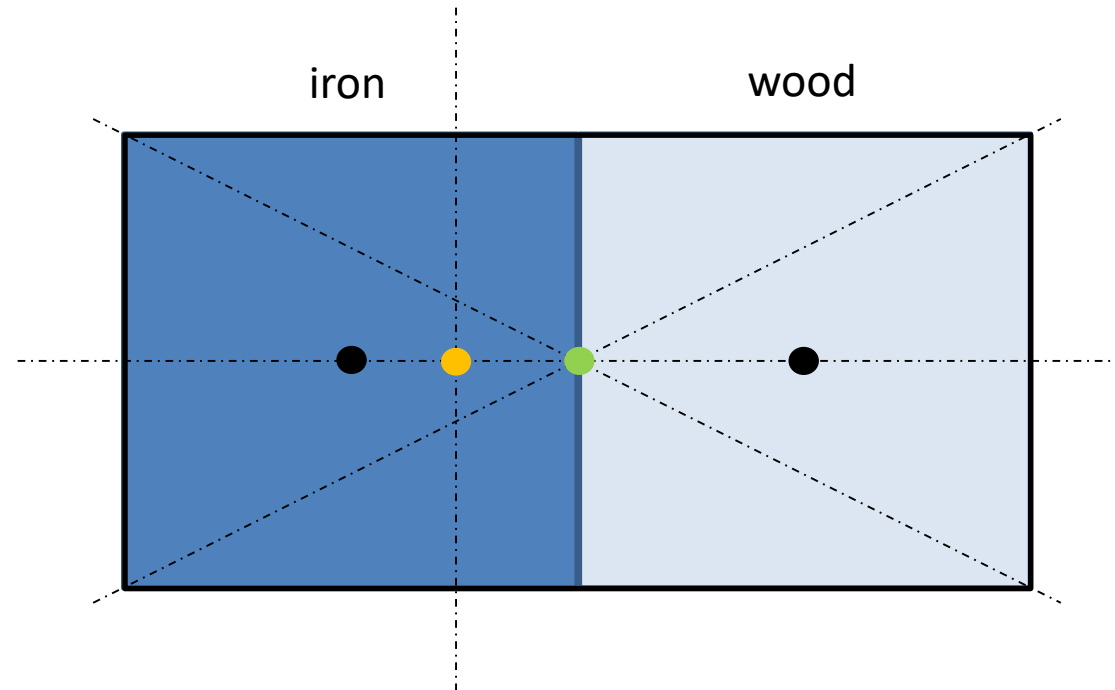


# The Earth is a Potato



# Global Ellipsoid: Center?

- Geometric Center (GC): green dot
- Center of Mass (CM), Center of Gravity: yellow dot
- Example: one block made of two materials, half iron, half wood

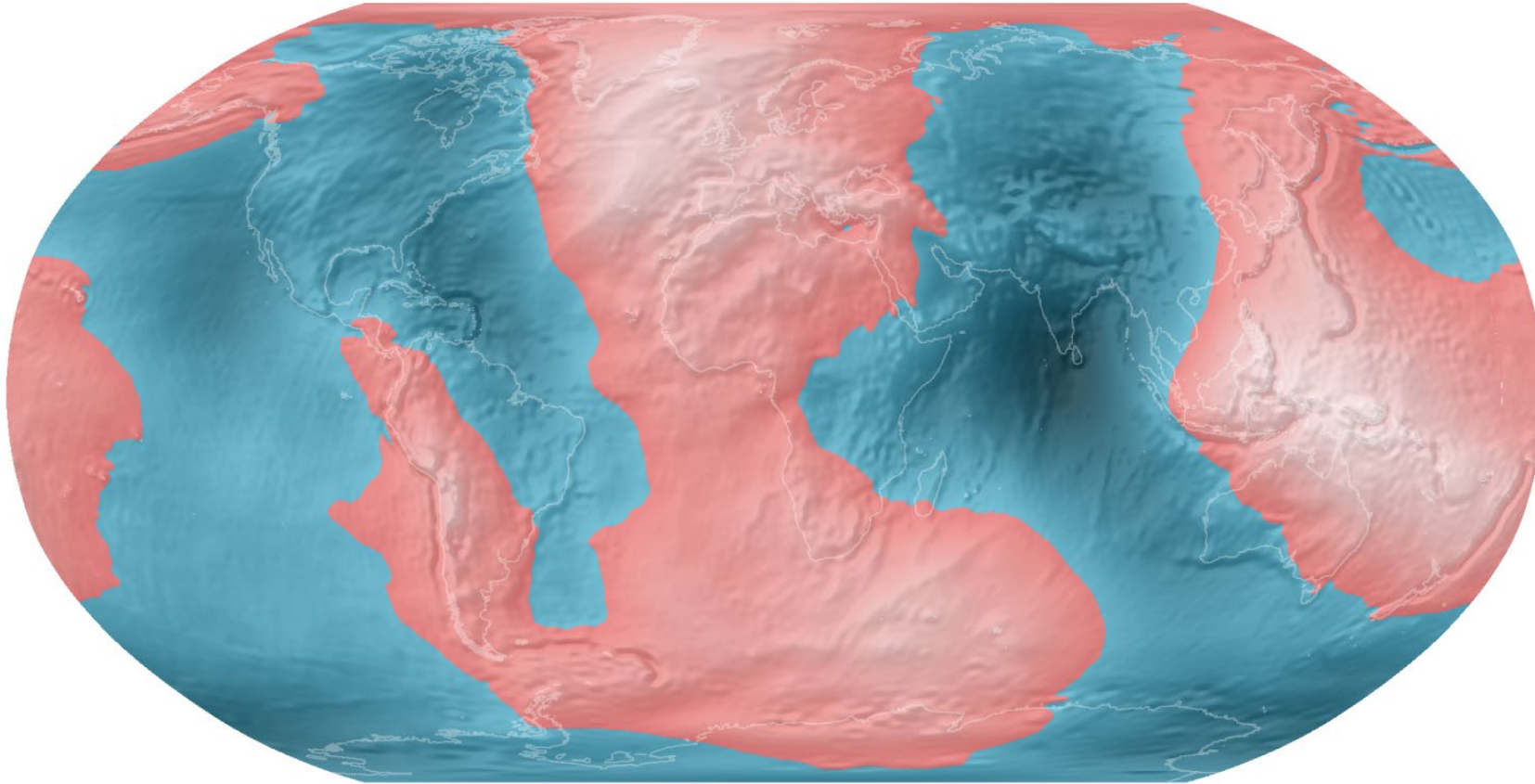


# GRS80

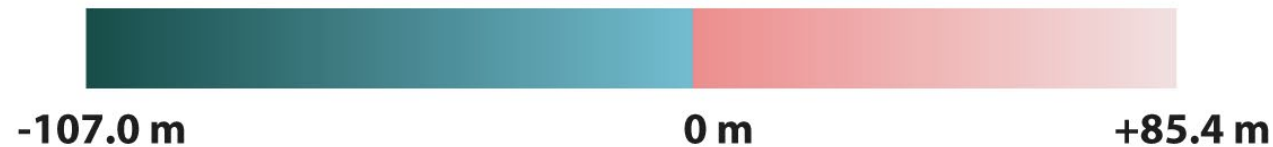
- GRS 80, or Geodetic Reference System 1980, is a geodetic reference system consisting of a **global reference ellipsoid** and a **gravity field model**.
- The reference ellipsoid is regular.
- The **geoid** (/ˈdʒiːɔɪd/) is the **shape that the surface of the oceans would take under the influence of Earth's gravity and rotation alone**, in the absence of other influences such as winds and tides.
- Gravitational equipotential surface
- The geoid is irregular.

# Deviation of the Geoid from the idealized figure of the Earth

(difference between the EGM96 geoid and the WGS84 reference ellipsoid)



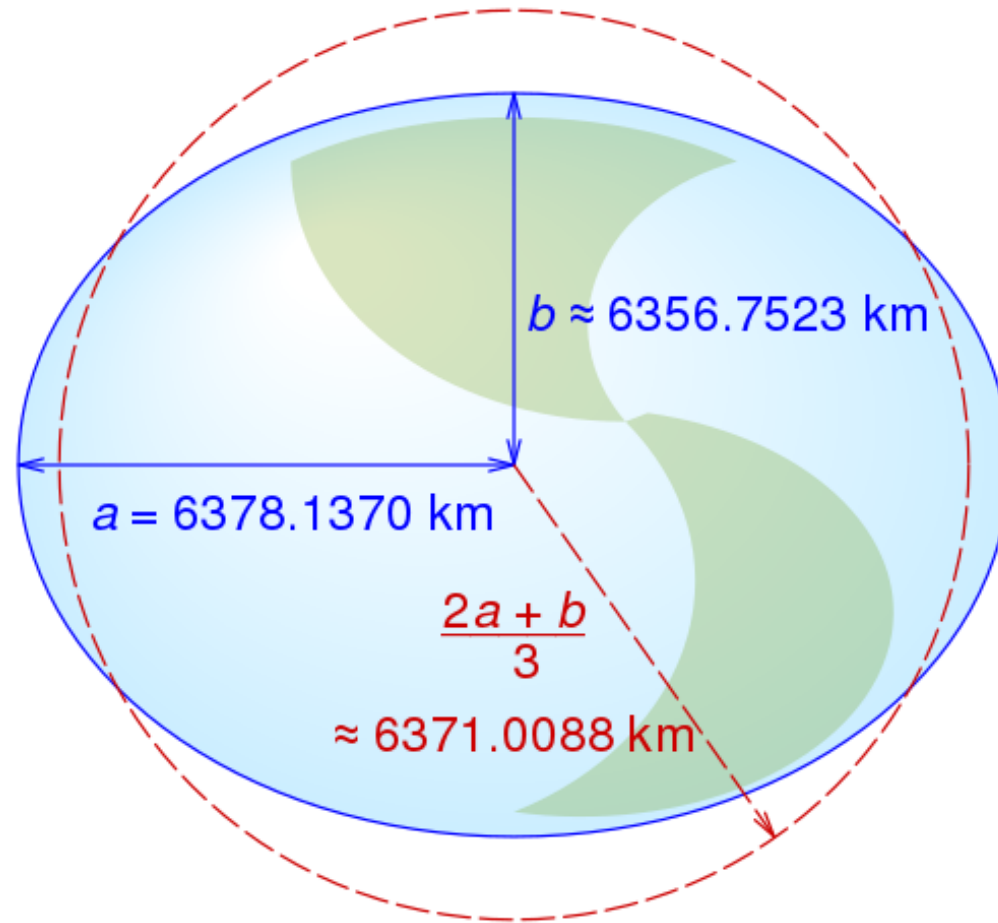
Red areas are above the idealized ellipsoid; blue areas are below.



[https://commons.wikimedia.org/wiki/File:Geoid\\_height\\_red\\_blue\\_averagebw.png](https://commons.wikimedia.org/wiki/File:Geoid_height_red_blue_averagebw.png)

# World Geodetic System WGS84 (EPSG:4326)

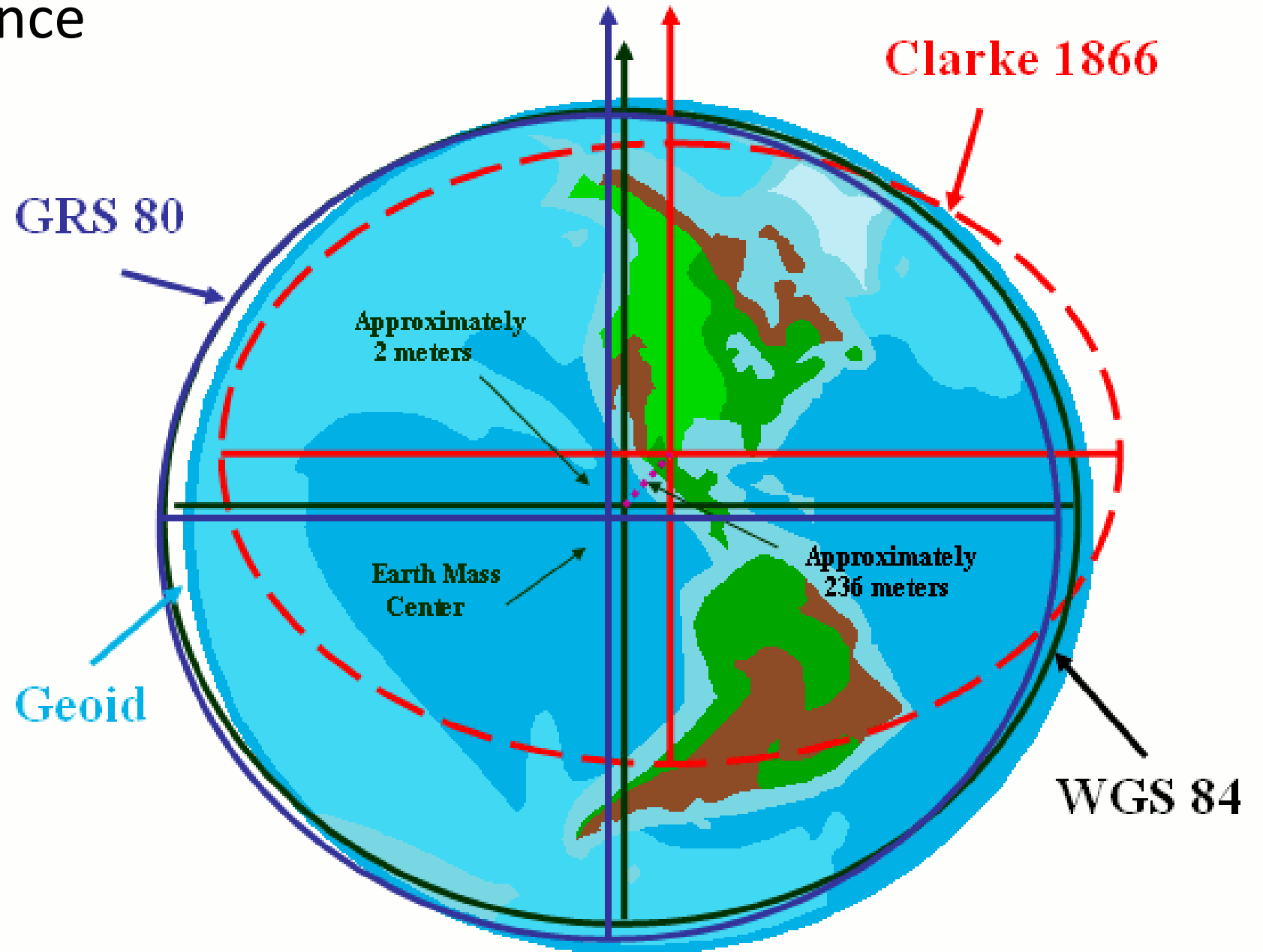
- Used by GPS
- Origin located in Earth's center of mass
- Ref. ellipsoid differs slightly from GRS80
- Equatorial (a), polar (b) and mean Earth radii as defined in the 1984 World Geodetic System revision (not to scale)



[https://commons.wikimedia.org/wiki/File:WGS84\\_mean\\_Earth\\_radius.svg](https://commons.wikimedia.org/wiki/File:WGS84_mean_Earth_radius.svg)  
[https://en.wikipedia.org/wiki/World\\_Geodetic\\_System#WGS84](https://en.wikipedia.org/wiki/World_Geodetic_System#WGS84)

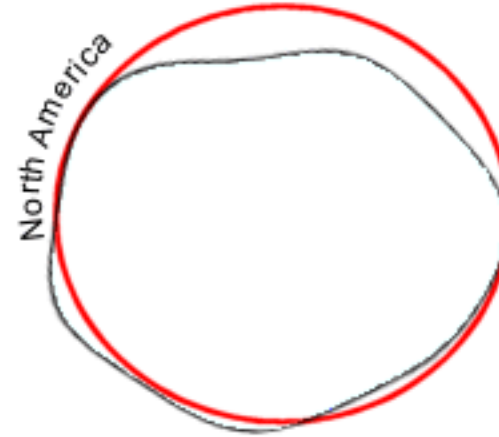
# Different Reference Ellipsoids

NOAA:  
National Oceanic  
and Atmospheric  
Agency

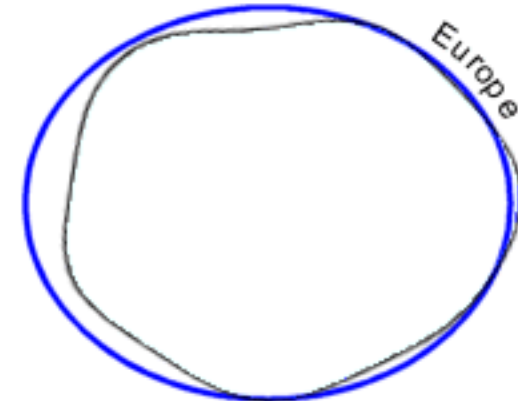




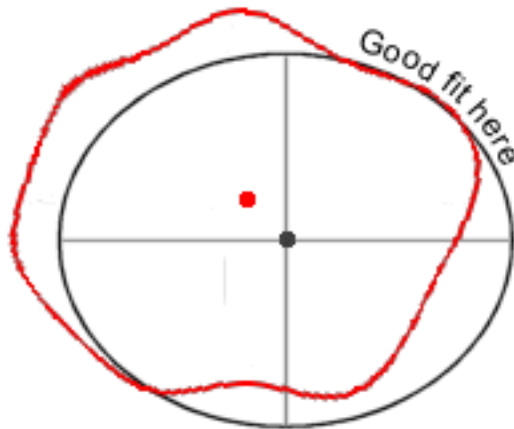
- Ellipsoid approximates geoid locally



The red ellipsoid fits the geoid well in North America.



The blue ellipsoid fits the geoid well in Europe.



Local datum



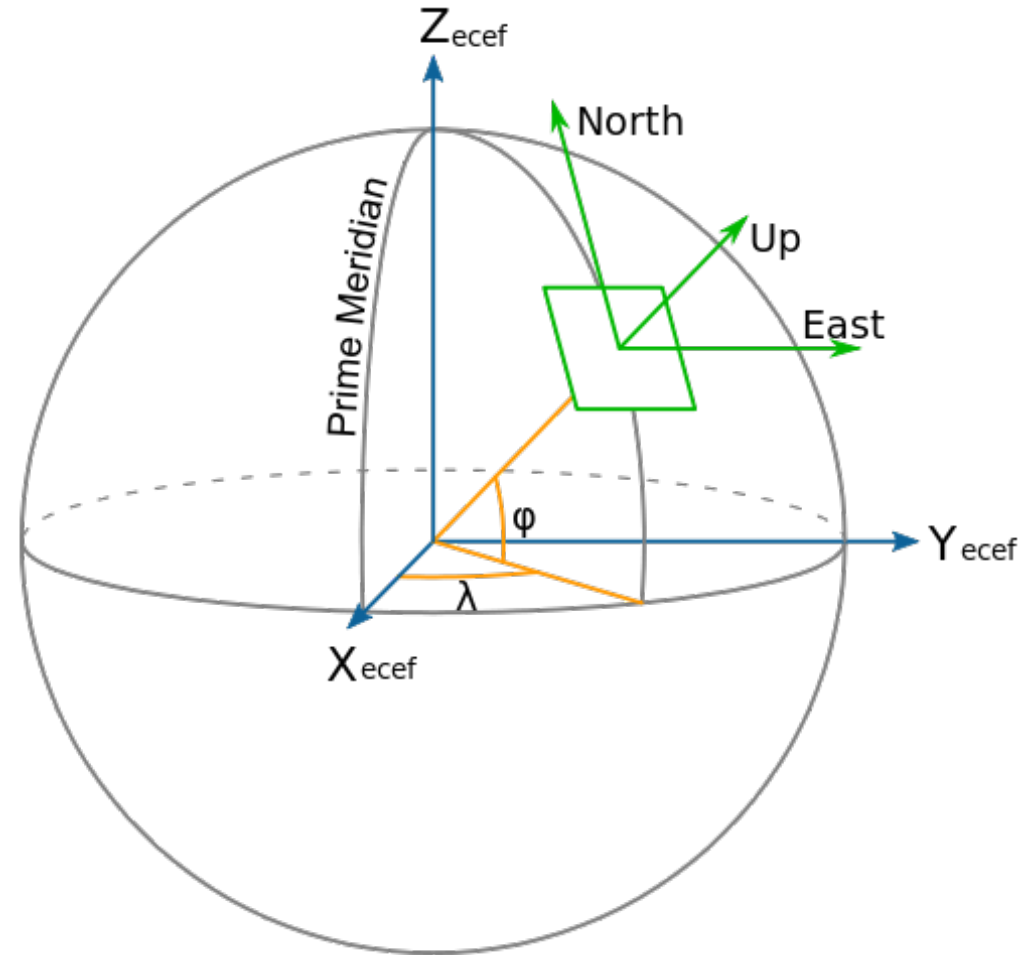
Earth-centered datum

- center of mass of geoid
- center of ellipsoid

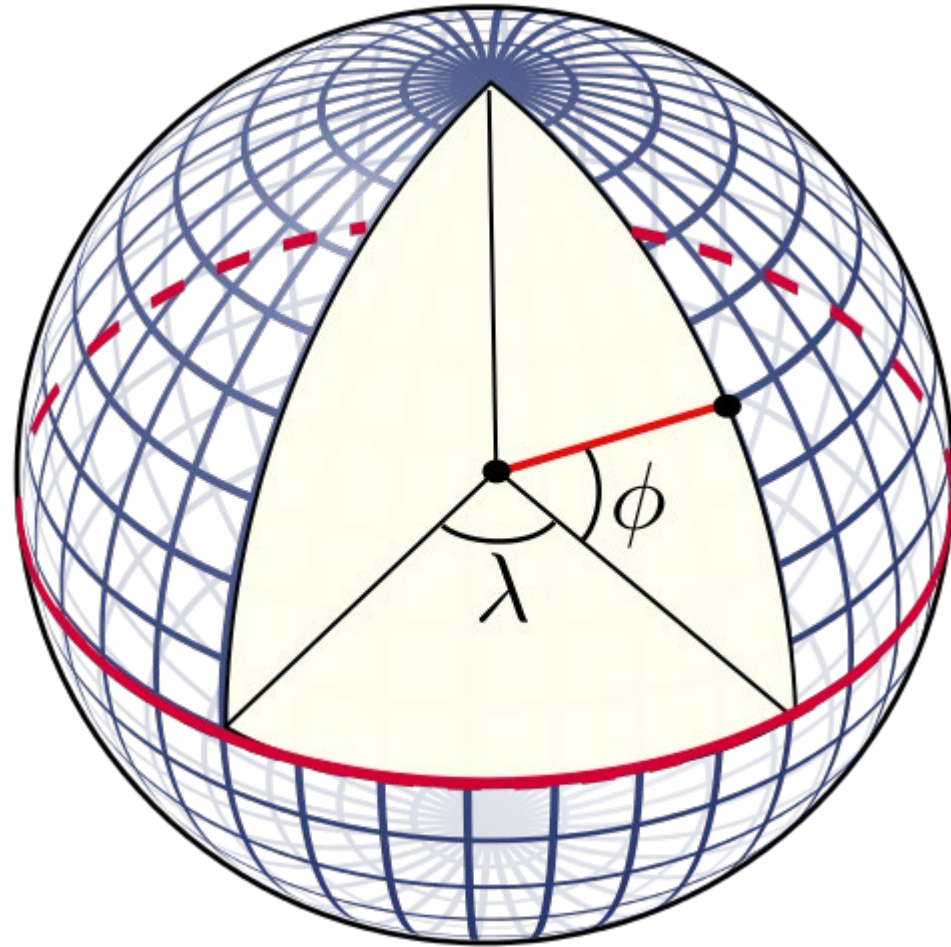
<http://www.geography.hunter.cuny.edu/~jochen/gtech361/lectures/lecture04/concepts/Datums/Components%20of%20a%20datum.htm>

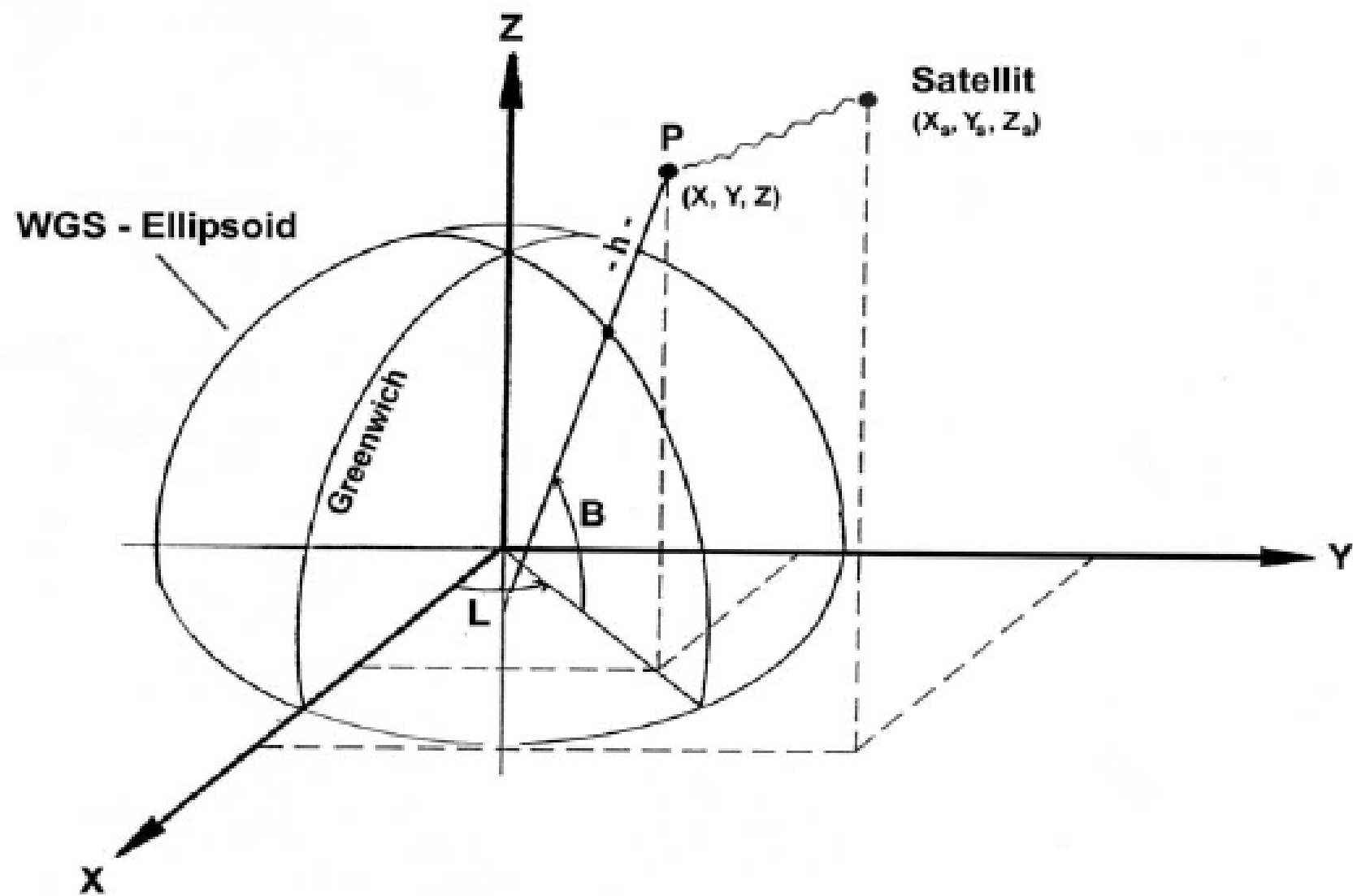
# WGS 84: Latitude, Longitude (lat, lon)

- Prime Meridian:  $\lambda = 0^\circ$  (approx. Greenwich)
- Latitude (Breite)  $\varphi$ ,  $\phi$  : measured from equator, North +, South -
- Longitude (Länge)  $\lambda$  : measured from PM, East +, West -

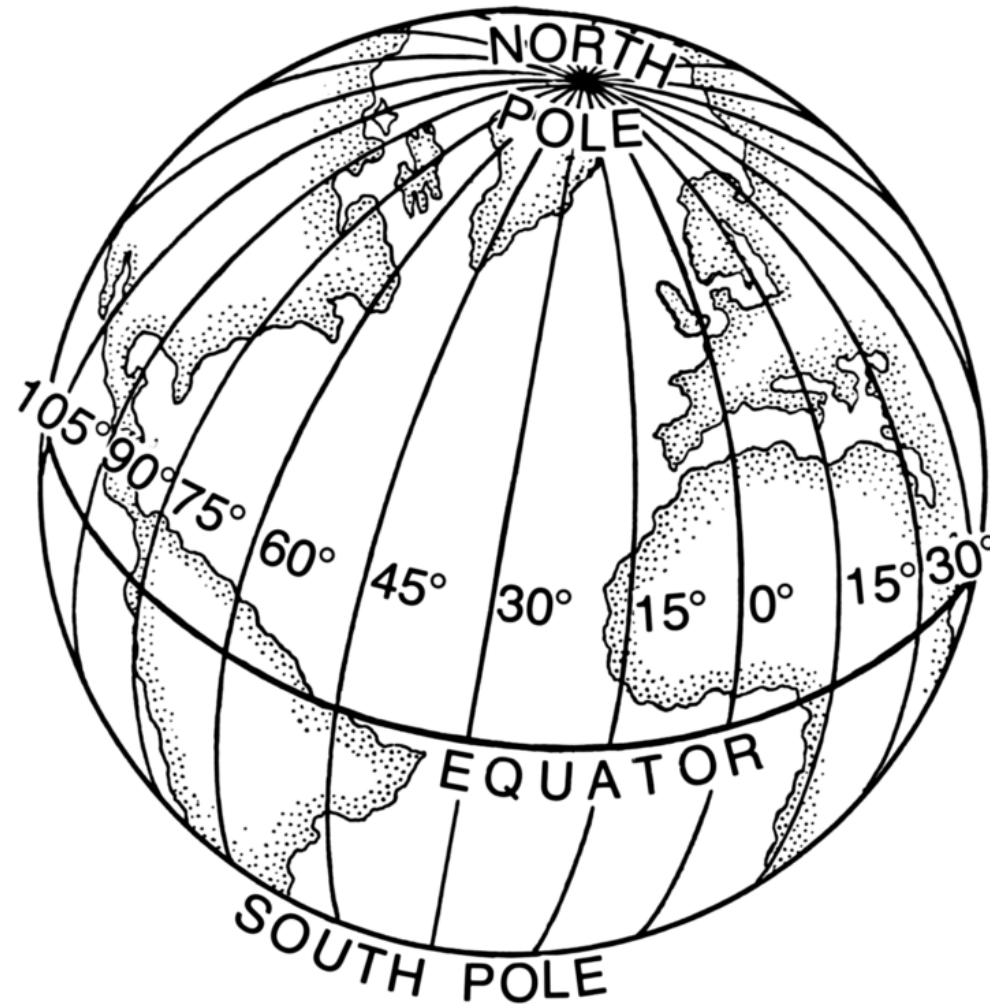


- Lat: N – S
- Lon: E – W





# Longitude



[https://commons.wikimedia.org/wiki/File:Longitude\\_\(PSF\).png](https://commons.wikimedia.org/wiki/File:Longitude_(PSF).png)

# Metropolis

Kamp-Lintfort:

- WGS84: 51° 30' 0" N 6° 32' 0" E
- WGS84: 51.5° 6.533333°
- UTM: 32U 328794 5708314

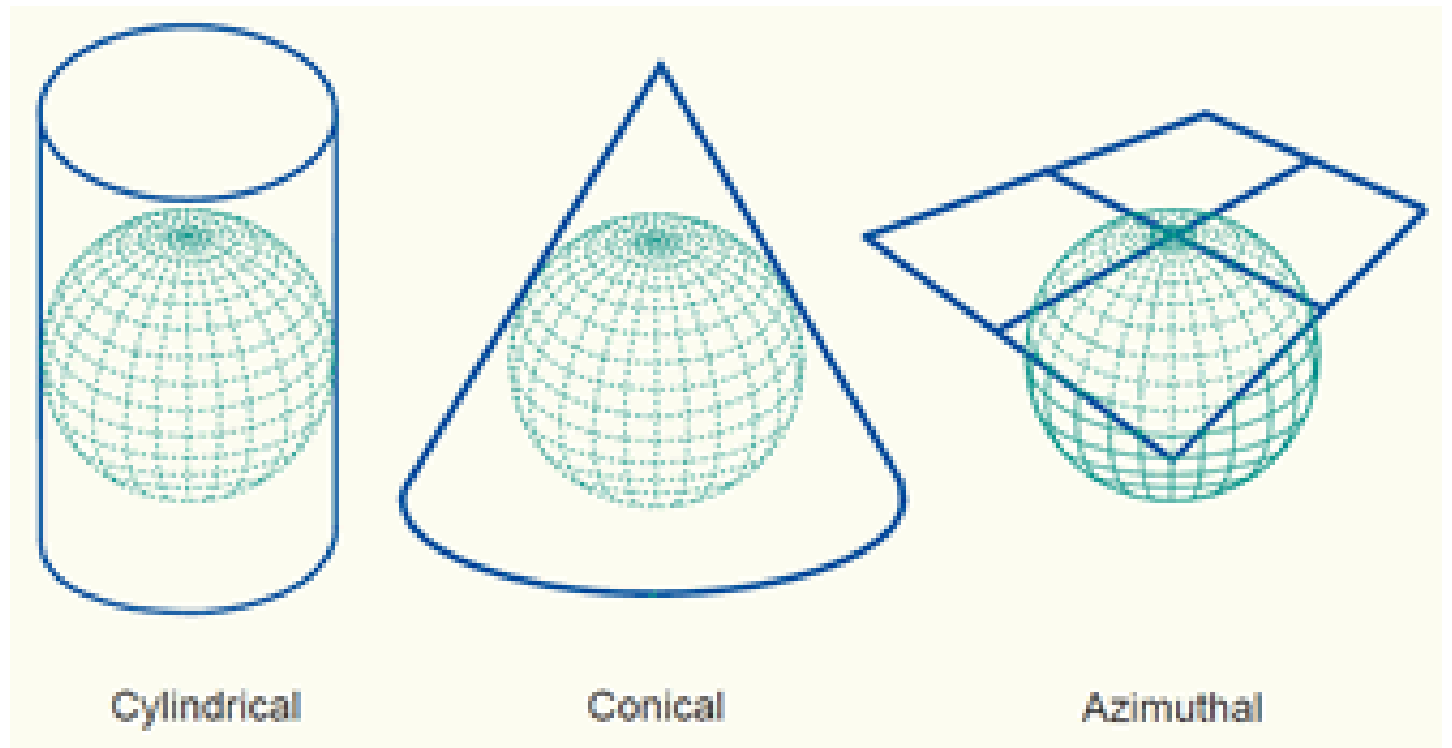
Which city?

- WGS84: 40° 42' 46" N 74° 0' 21" W
- WGS84: 40.712778° -74.005833°
- UTM: 18T 583973 4507349

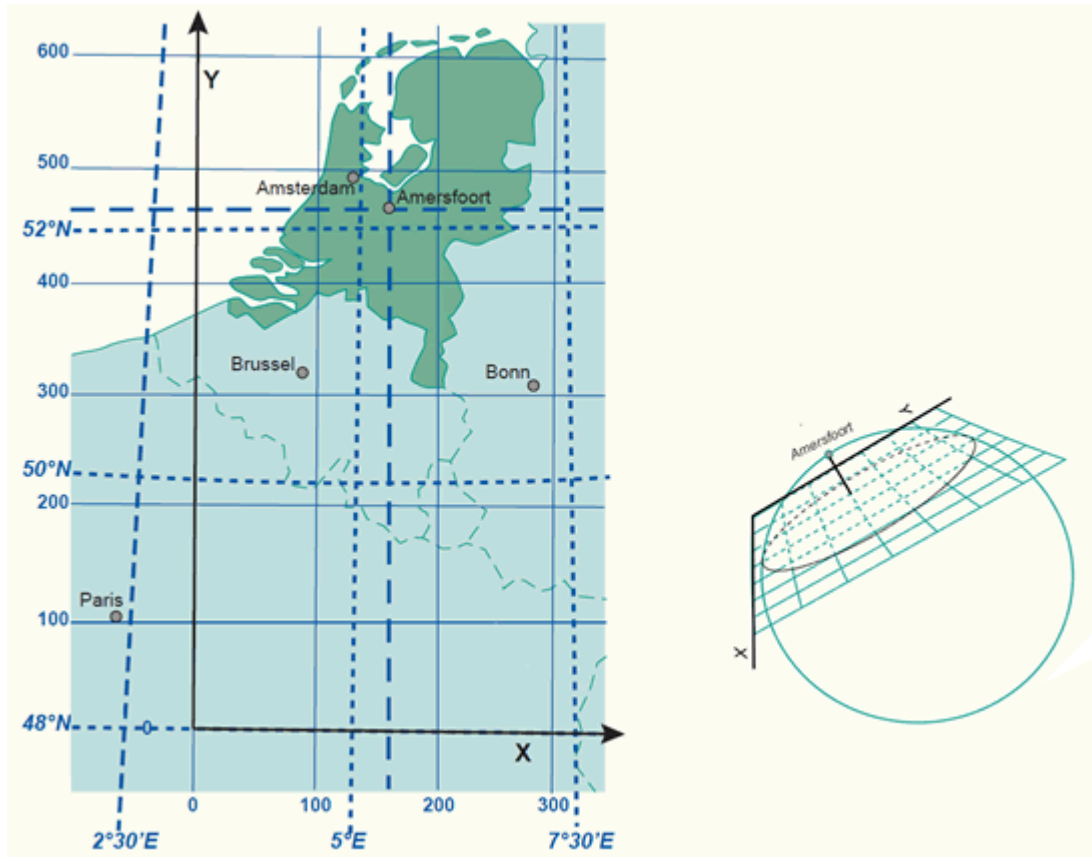
[https://tools.wmflabs.org/geohack/geohack.php?pagename=Kamp-Lintfort&language=de&params=51.5 N 6.533333333333333 E region:DE-NW type:city\(37346\)](https://tools.wmflabs.org/geohack/geohack.php?pagename=Kamp-Lintfort&language=de&params=51.5 N 6.533333333333333 E region:DE-NW type:city(37346))

# Map Projections

- Geographic coordinates:  
lat, lon (radius)
- Cartesian coordinates:  
x, y (z)
- Mostly optimized  
locally!



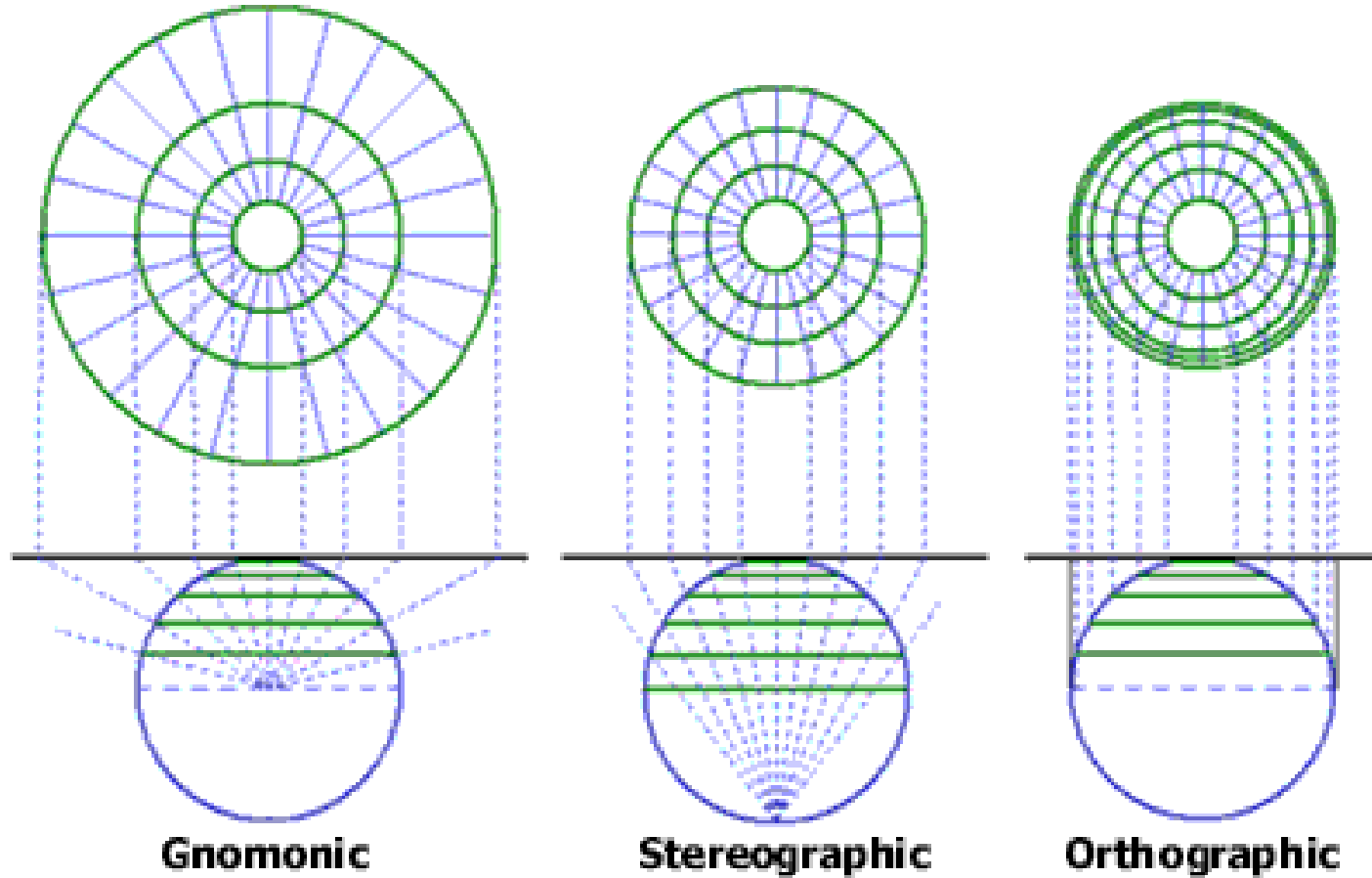
# Map Projections



The coordinate system of the Netherlands is derived from an oblique azimuthal stereographic projection.



# Different Azimuthal Projections

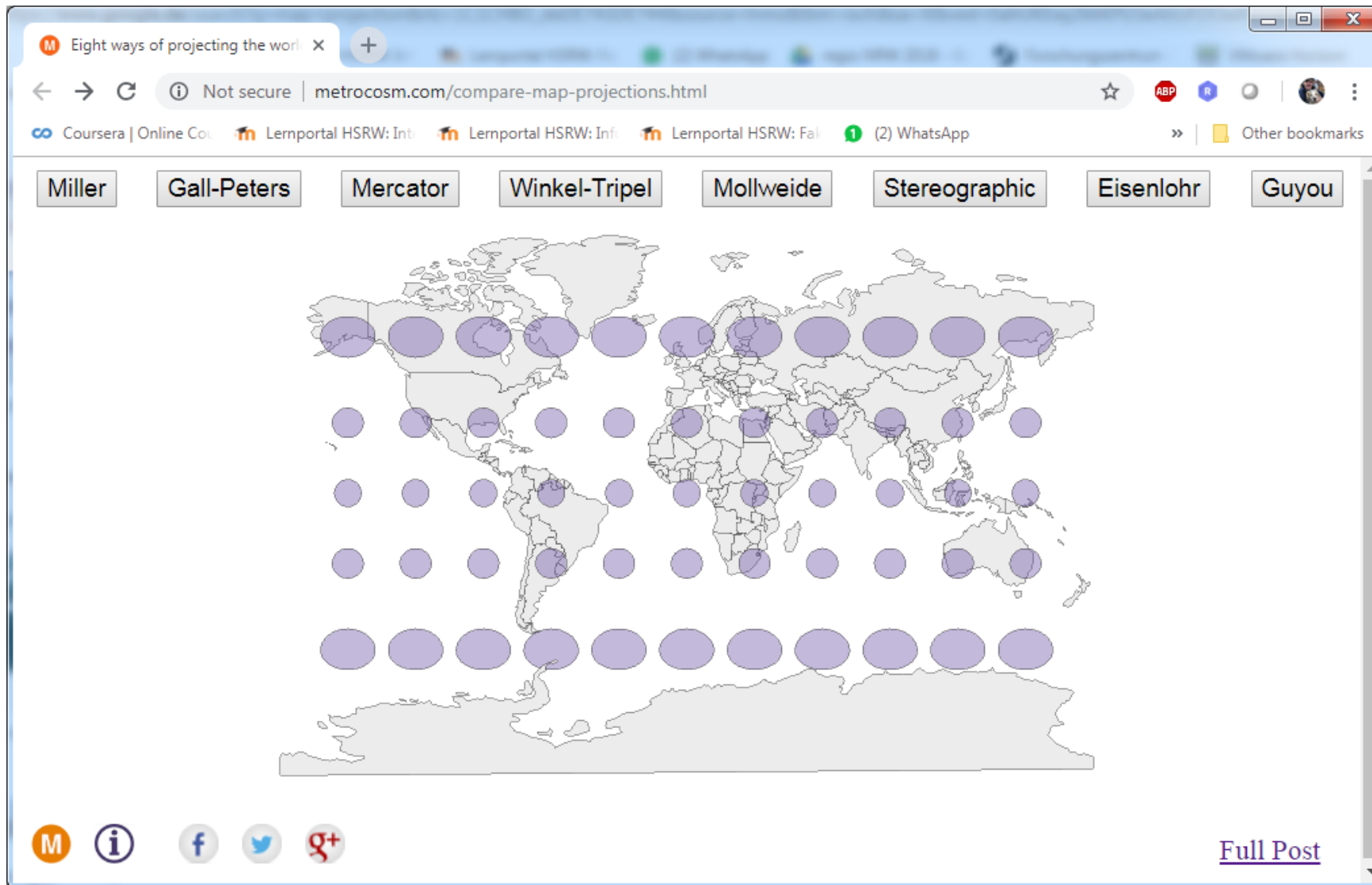


<http://www.geo.hunter.cuny.edu/~jochen/gtech201/lectures/lec6concepts/Map%20coordinate%20systems/Perspective.htm>

# Projection Invariants (what is preserved)

- Preserving direction (azimuthal or zenithal), a trait possible only from one or two points to every other point
- **Preserving shape locally (conformal or orthomorphic)**
- Preserving area (equal-area or equiareal or equivalent or authalic)
- Preserving distance (equidistant), a trait possible only between one or two points and every other point
- Preserving shortest route, a trait preserved only by the gnomonic projection
- Because the sphere is not a developable surface, it is impossible to construct a map projection that is both equal-area and conformal.

# Map Projection - Tissot's Indicatrices



<http://metrocosm.com/compare-map-projections.html>



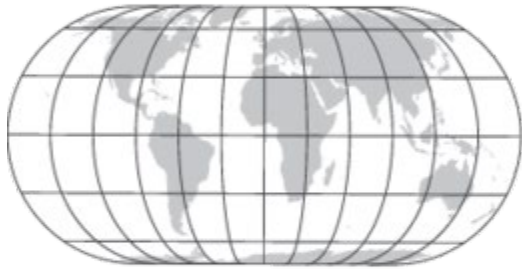
Robinson



Plate Carrée



Winkel Tripel



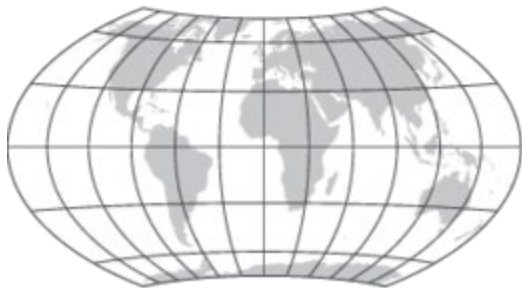
Eckert IV



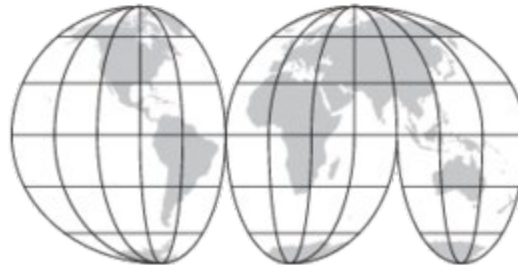
Mollweide



Mercator



Wagner VII

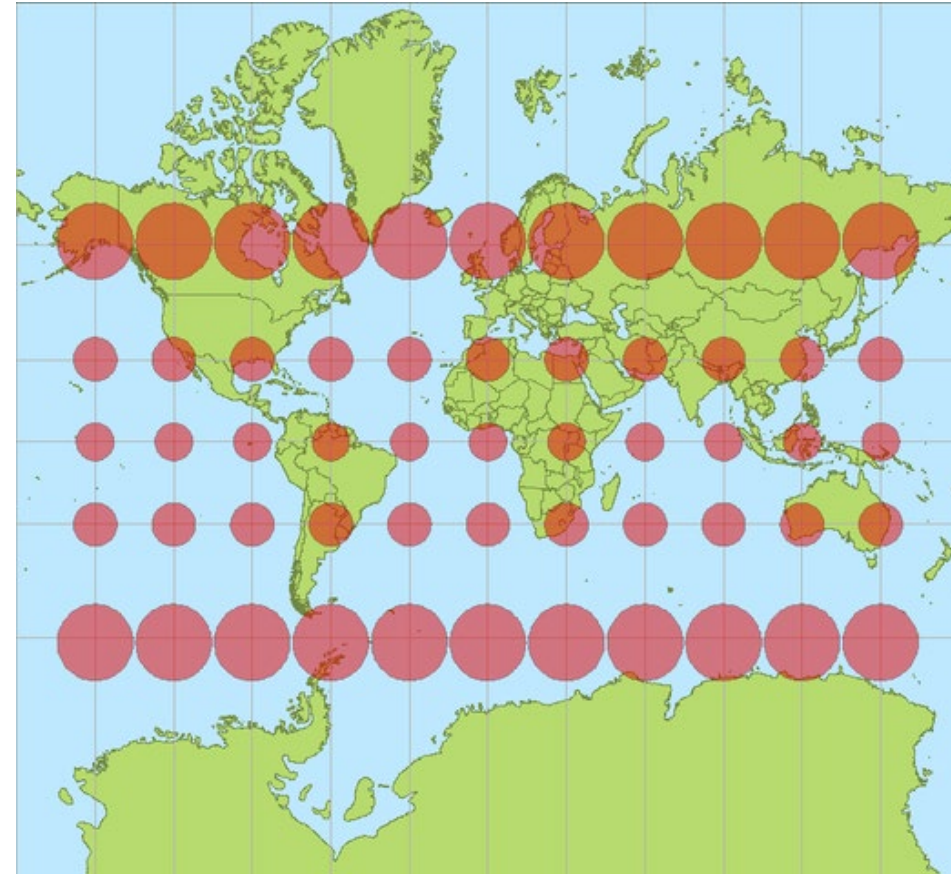
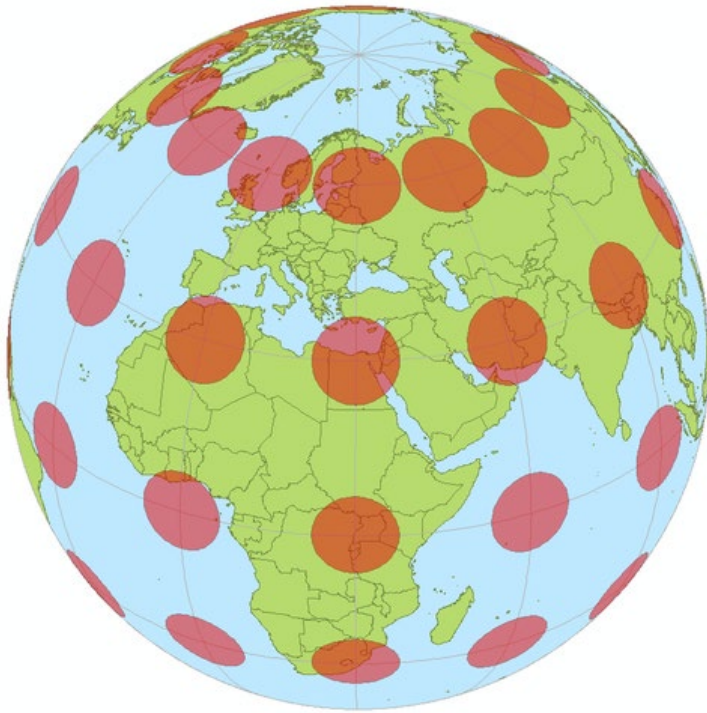


Interrupted Mollweide



Goode Homolosine

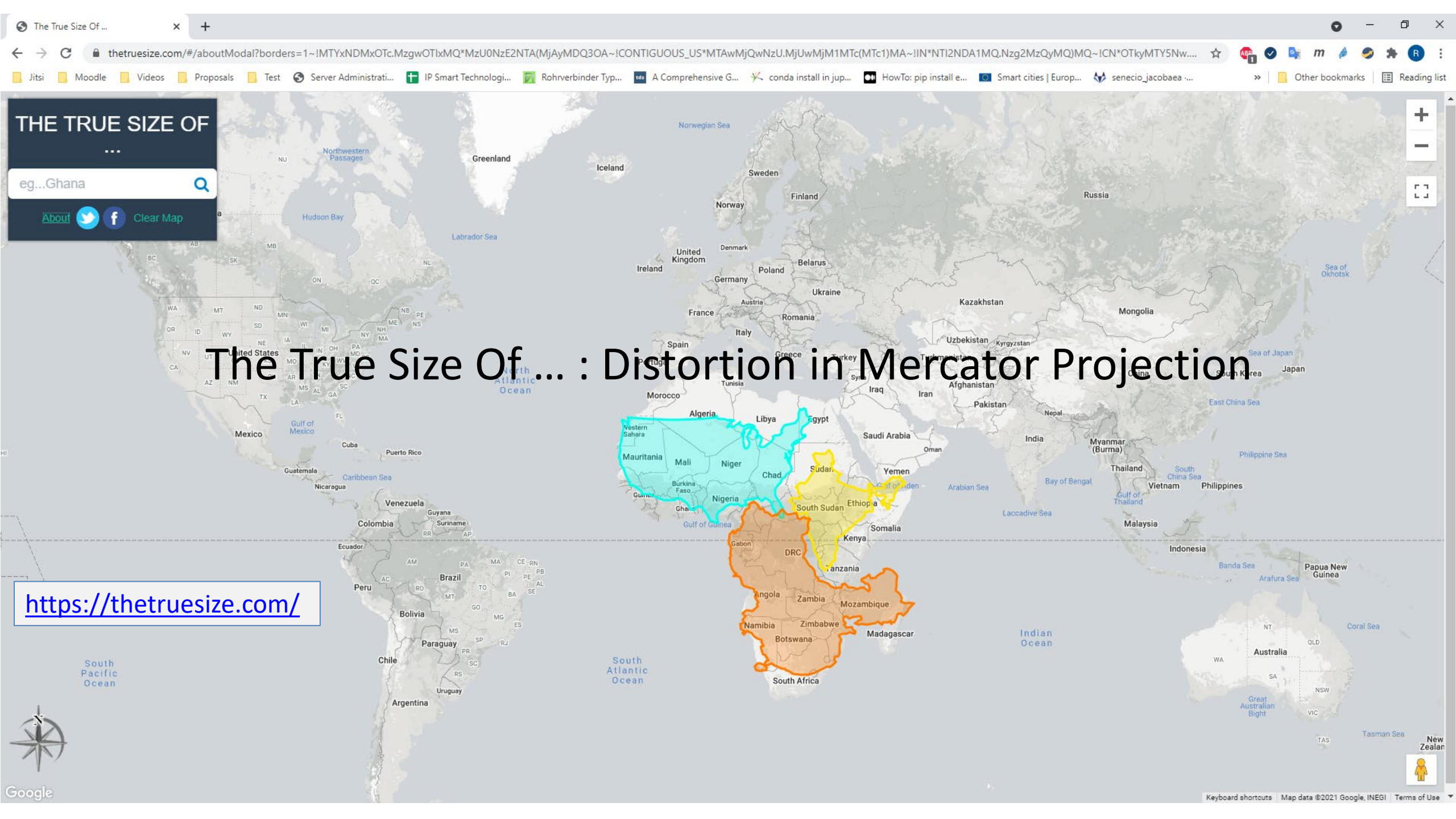
# Mecator Projection



Red Dots:  
Tissot's Indicatrix / Indicatrices

<https://de.wikipedia.org/wiki/Mercator-Projektion>



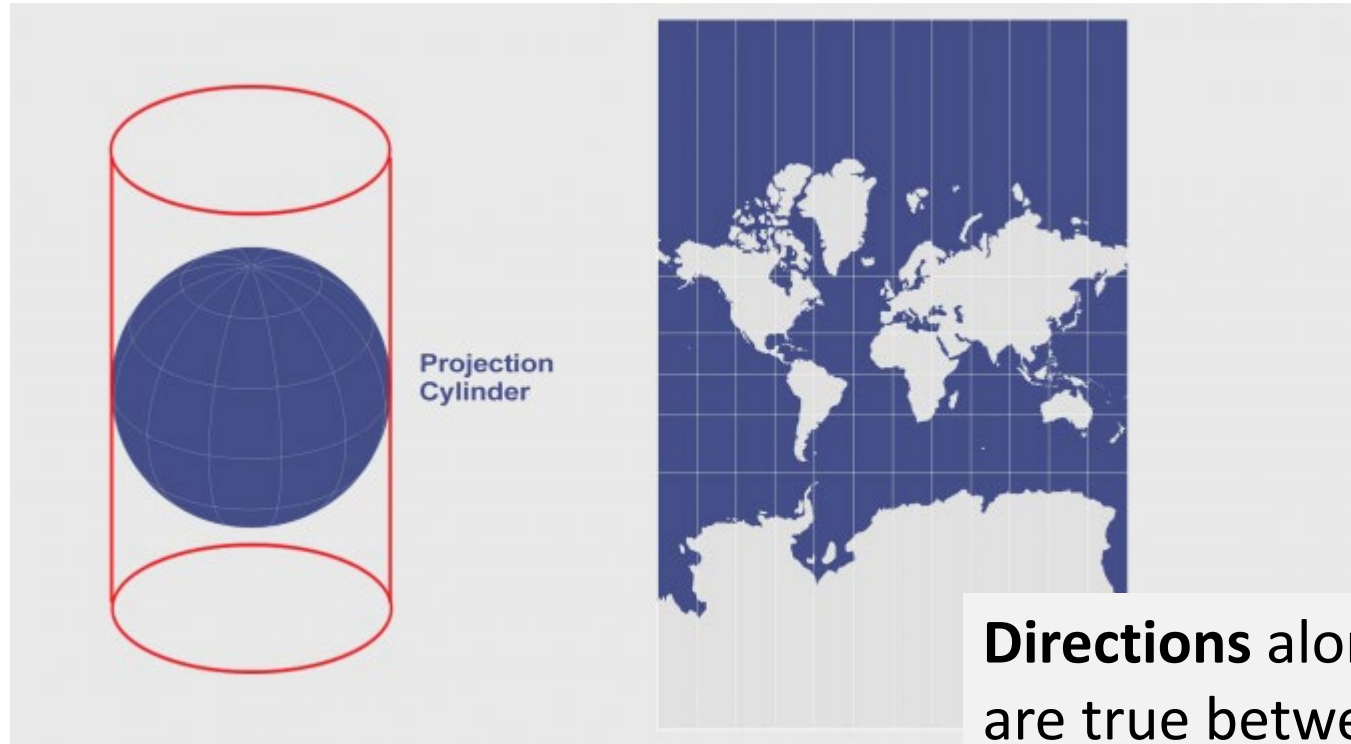


# The True Size Of... : Distortion in Mercator Projection

eg...Ghana

<https://thetruesize.com/>

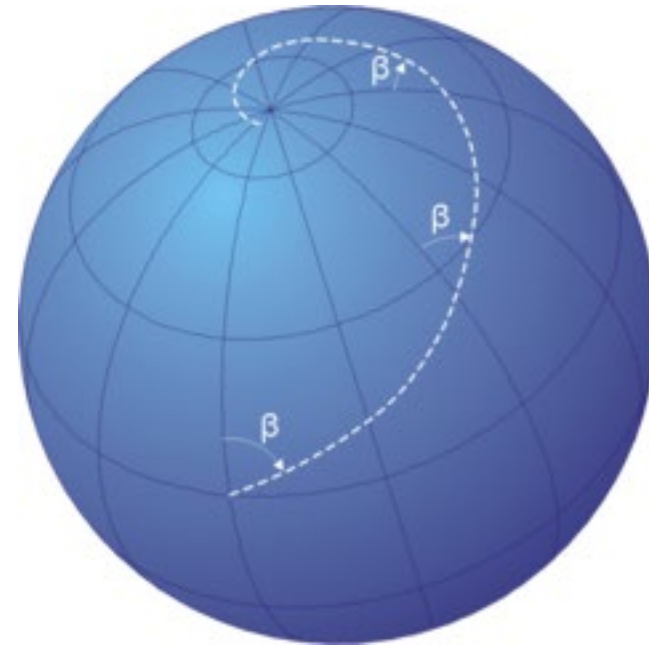
# Mercator Projection



**Directions** along a Rhumb line are true between any two points on a map. **Distances** are true only along the Equator. Although it has a **conformal** property, areas are greatly distorted increasing size at poles.

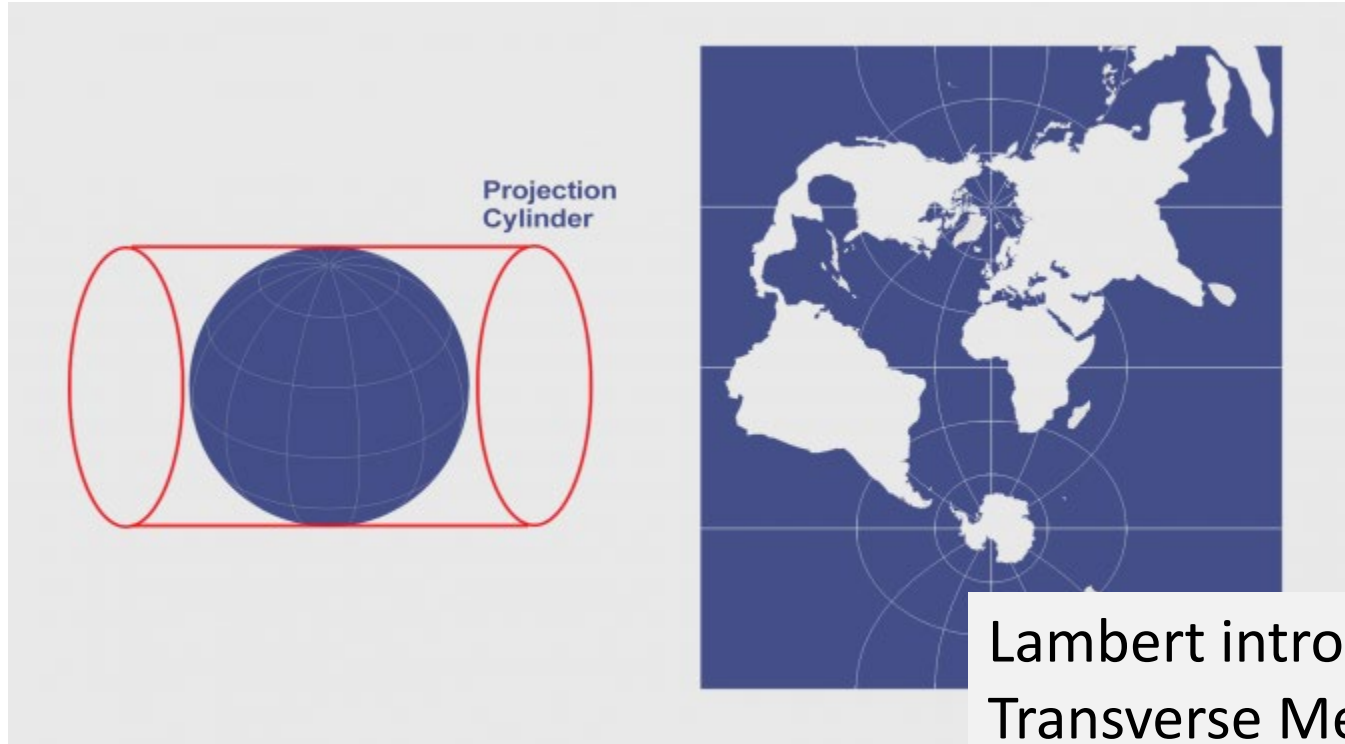
# Rhumb Line

- In navigation, a rhumb line, rhumb, (/rʌm/) or loxodrome is an arc crossing all meridians of longitude at the same angle, that is, a path with constant bearing as measured relative to true or magnetic north.



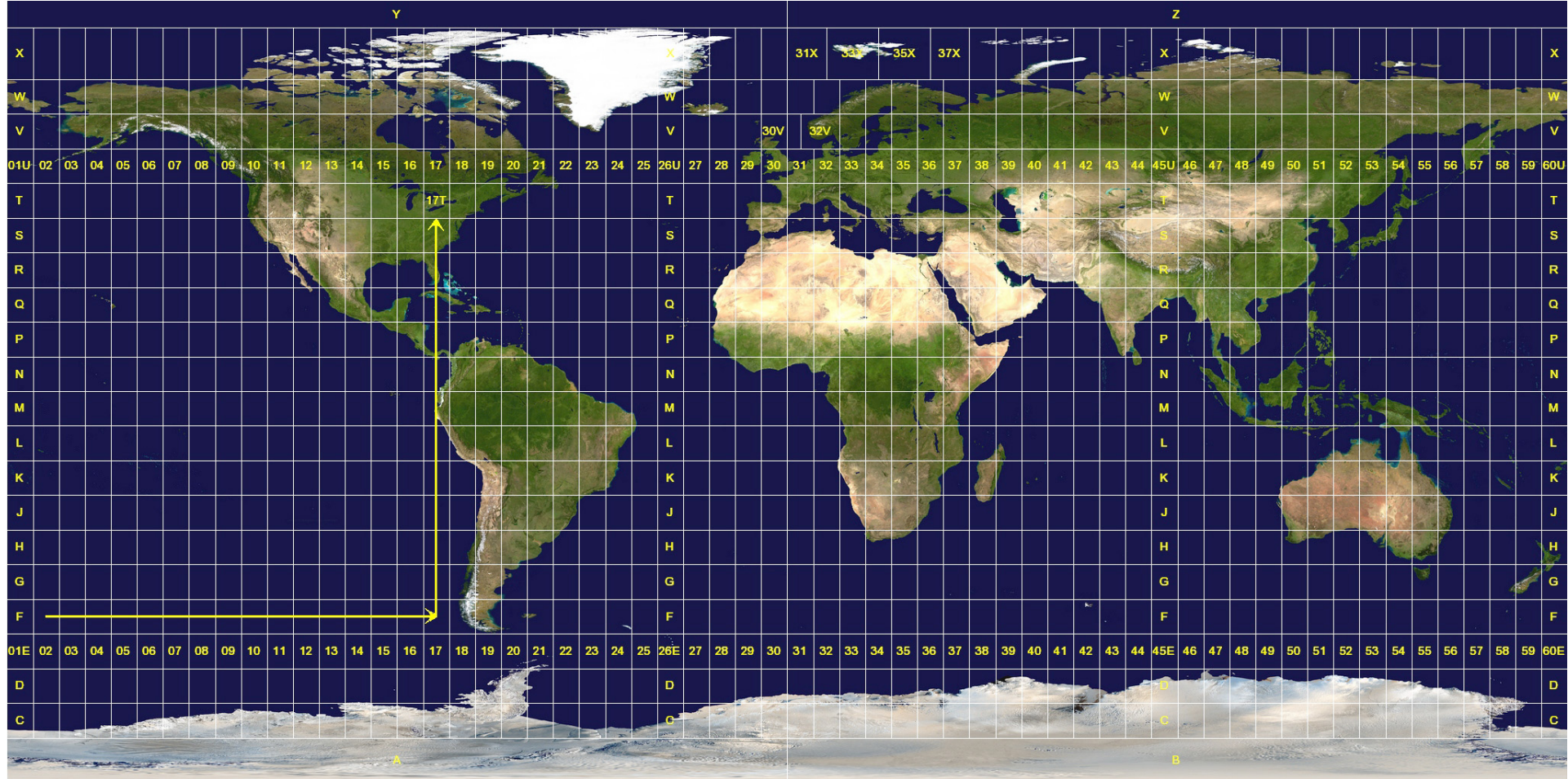


# Tranverse Mercator Projection



Lambert introduced the Transverse Mercator in 1772. It uses a horizontally oriented cylinder tangent to a Meridian. This is particular useful for mapping large areas that are mainly north-south in extent.

# Universal Transverse Mercator (UTM): Conformal Projection



[https://en.wikipedia.org/wiki/Universal\\_Transverse\\_Mercator\\_coordinate\\_system](https://en.wikipedia.org/wiki/Universal_Transverse_Mercator_coordinate_system)

# Nordrhein-Westfalen: ETRS89 / UTM, Realisation of WGS84

- ETRS89: European Terrestrial Reference System

Bezugssystem	Europäisch terrestrisches Referenzsystem 1989
Bezugsfläche	GRS80-Ellipsoid, Große Halbachse $a$ : 6 378 137 m und Abplattung $f$ : 1 : 298, 257 222 101
Datum/Lagerung	Fundamentalstationen des ITRS zum Zeitpunkt Januar 1989
Abbildung	Universale Transversale Mercatorabbildung (UTM)
Projektion	Schnittzylinder - siehe Abb. 2
Meridianstreifensystem	6° breite Meridianstreifen (Zonen)
Hauptmeridian	nicht längentreu, Maßstabsfaktor 0,9996
Netzgrundlage	ETRS89

Tab. 1: Wesentliche Merkmale von ETRS89/UTM

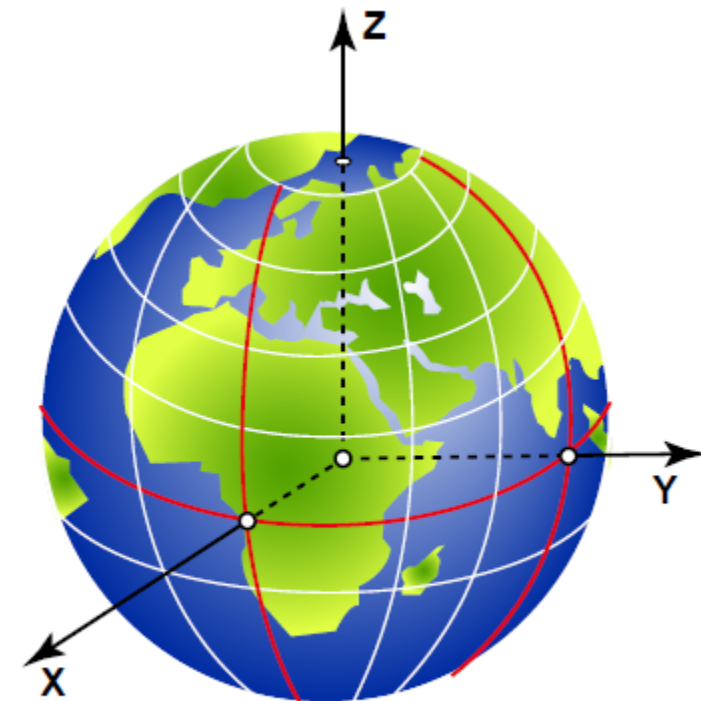


Abb. 1: Dreidimensionales kartesisches geozentrisches Koordinatensystem

[https://www.bezreg-koeln.nrw.de/brk\\_internet/publikationen/abteilung07/pub\\_geobasis\\_etr89.pdf](https://www.bezreg-koeln.nrw.de/brk_internet/publikationen/abteilung07/pub_geobasis_etr89.pdf)

# Nordrhein-Westfalen: ETRS89 / UTM

UTM projection strip 32

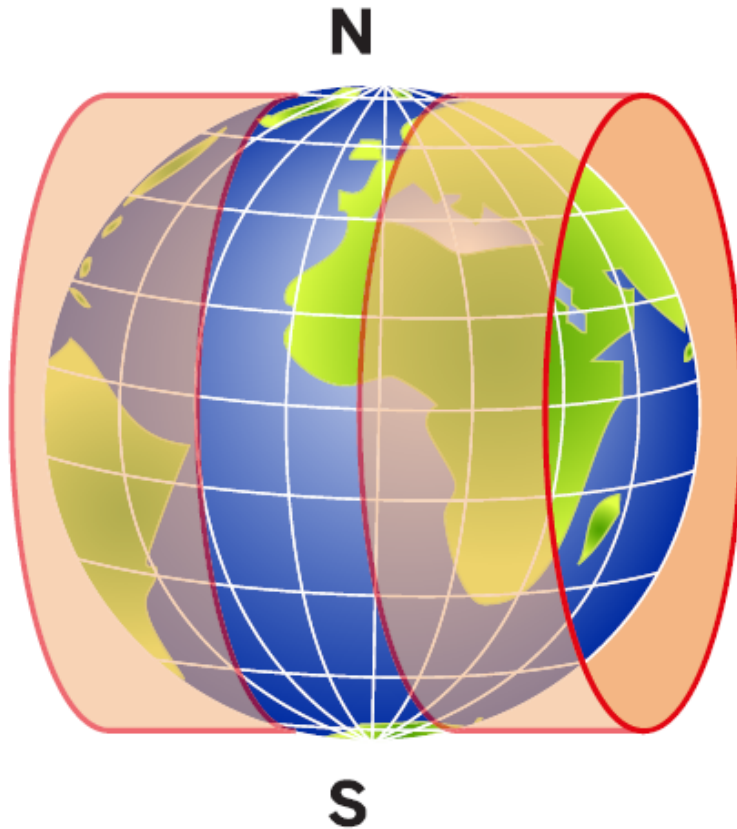


Abb. 2: Schnitzylinder der UTM-Abbildung

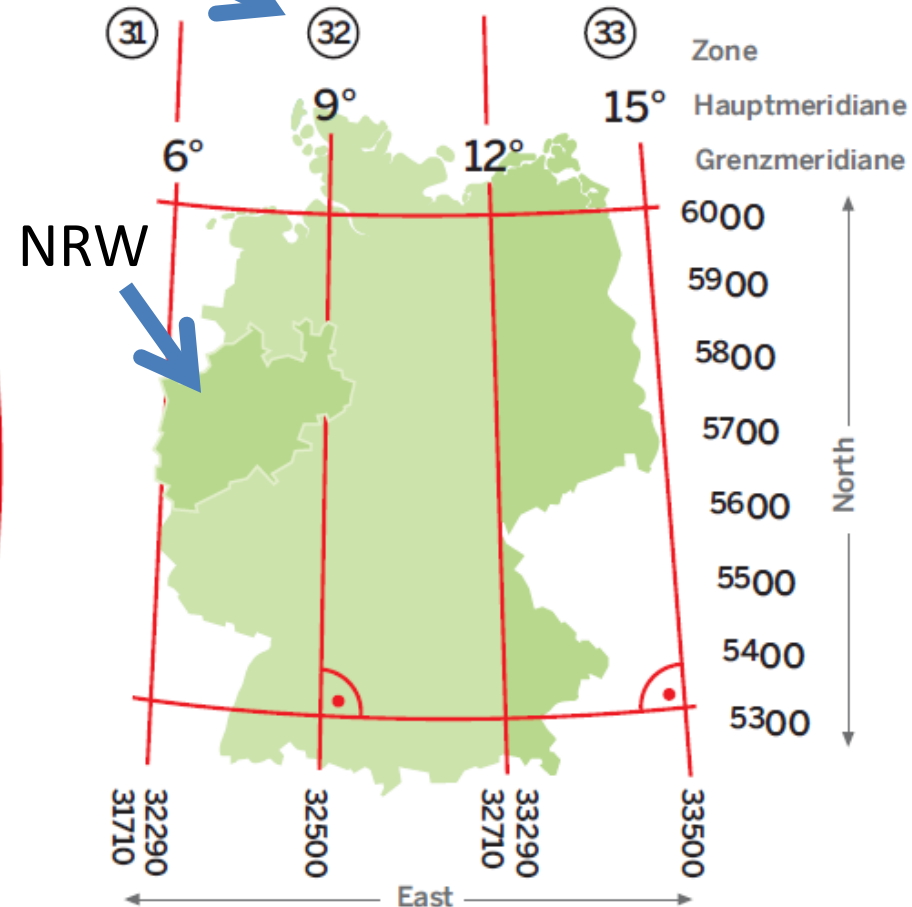


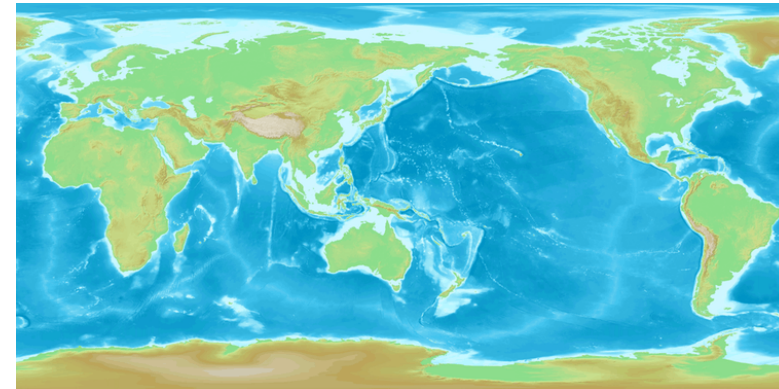
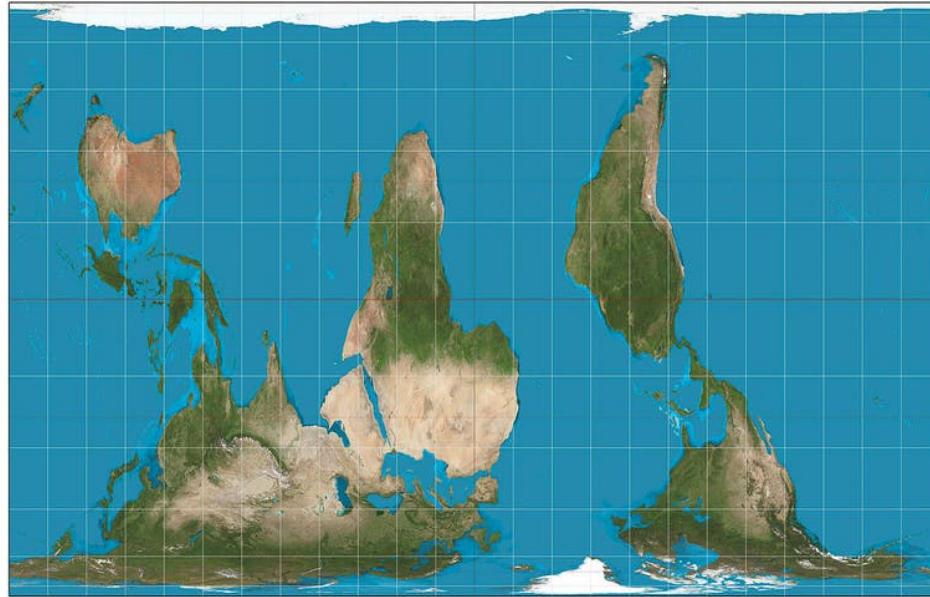
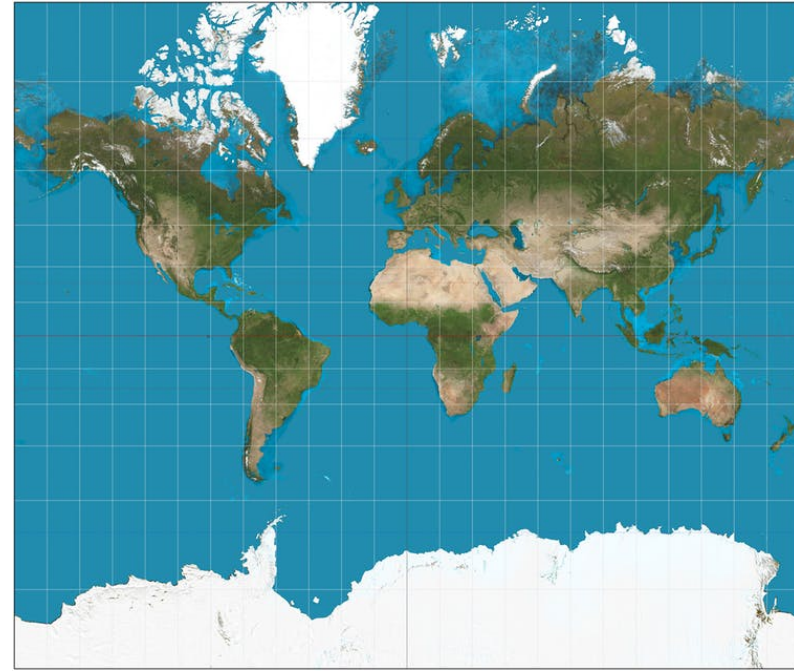
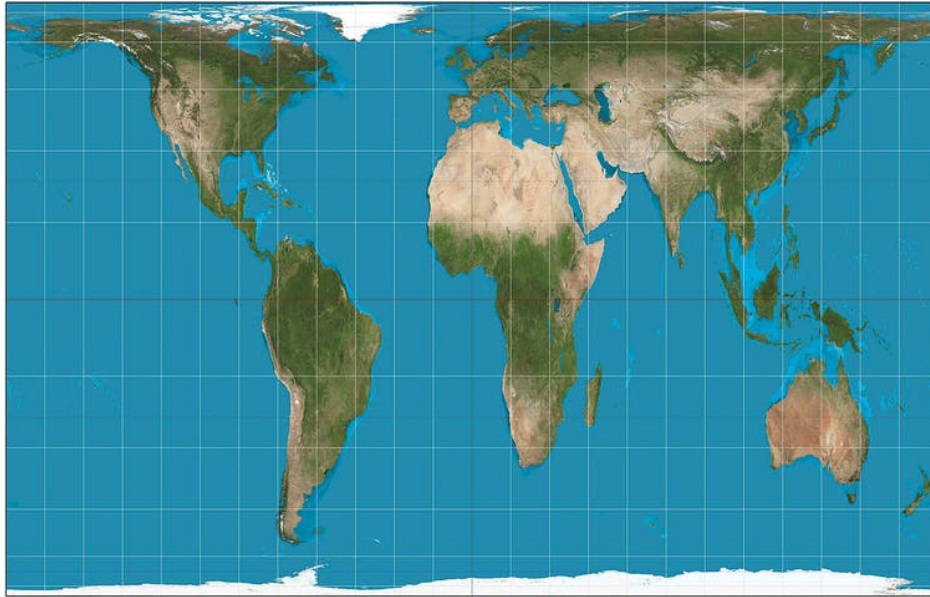
Abb. 3: Die Lage von NRW in der UTM-Zone 32

[https://www.bezreg-koeln.nrw.de/brk\\_internet/publikationen/abteilung07/pub\\_geobasis\\_etr89.pdf](https://www.bezreg-koeln.nrw.de/brk_internet/publikationen/abteilung07/pub_geobasis_etr89.pdf)

# EPSG: Unique ID for CRS

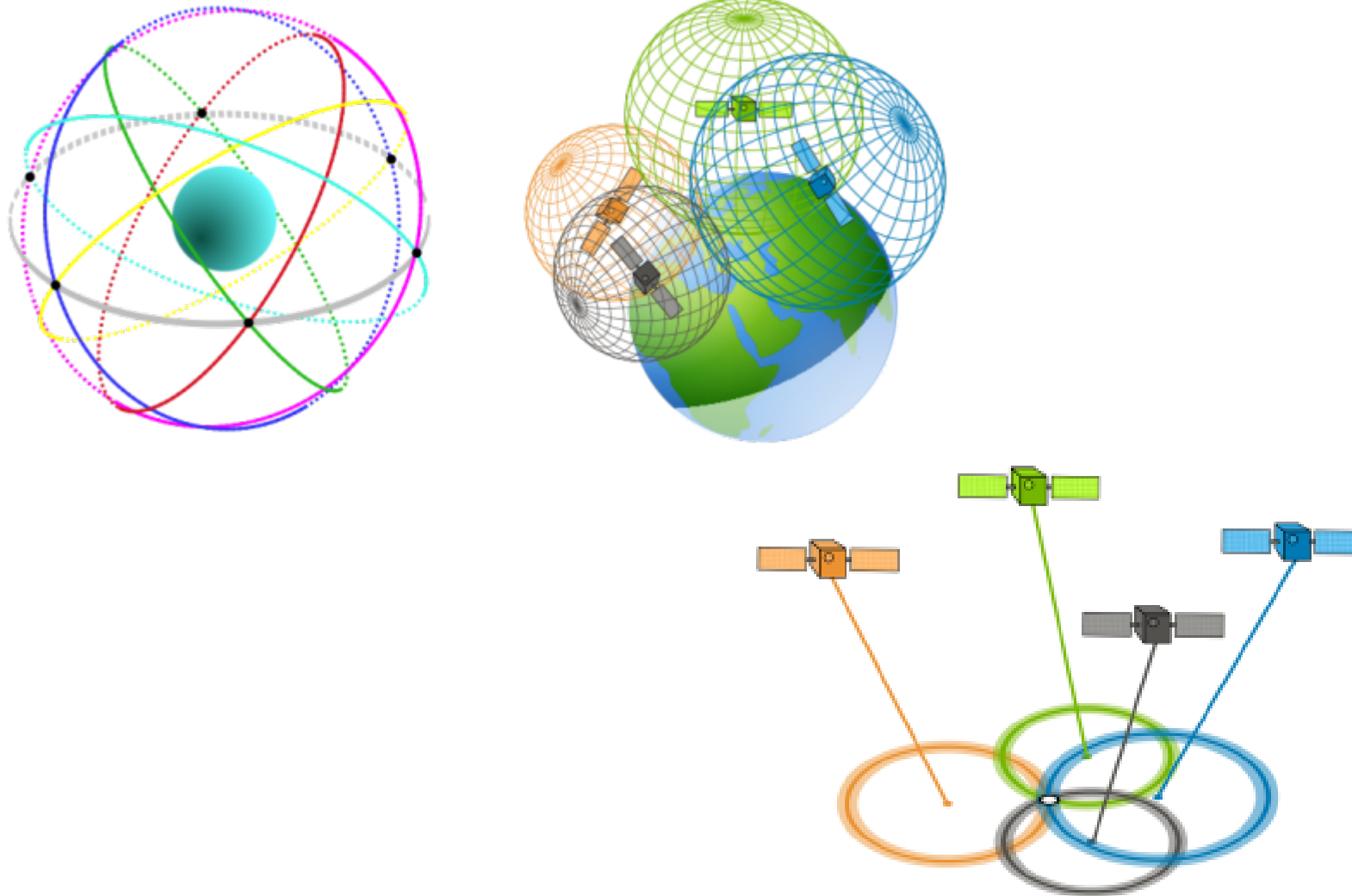
- EPSG: European Petroleum Survey Group Geodesy
- Provides a unique numeric key for all registered CRS
- **EPSG:4326** -> WGS84 (GPS coord.), <https://epsg.io/4326>
- **EPSG:25832** -> ETRS89 / UTM zone 32N, <https://epsg.io/25832>
  - Ka-Li coord: 327896.29, 5710585.12
- **EPSG:4647** -> ETRS89 / UTM zone 32N (zE-N), <https://epsg.io/4647>
  - Ka-Li coord: **32**327896.29, 5710585.12
  - Remarks: Variant of ETRS89 / UTM zone 32N (CRS code 25832) in which **easting has zone prefix**.
- EPSG:3857 -> WGS 84 / Pseudo-Mercator, <https://epsg.io/3857>
  - Spherical Mercator, Google Maps, OpenStreetMap, Bing, ArcGIS, ESRI





<http://theconversation.com/five-maps-that-will-change-how-you-see-the-world-74967>

# WGS 84: GPS Trilateration



<https://gisgeography.com/wgs84-world-geodetic-system/>

# Geoid, Ellipsoid, Topography

