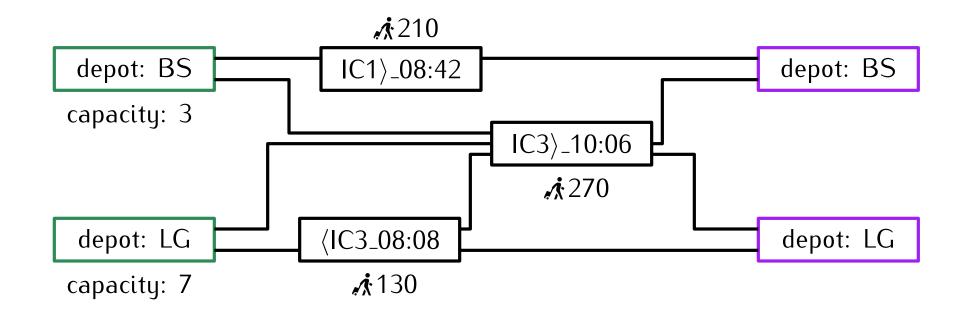
Collaboration SBB - ETH

RSSched

Rolling Stock Scheduling with Maintenance Regulations



by Leon Sering

Rolling Stock Scheduling

What does **rolling stock** mean?

rolling stock: "Vehicles that drive on rails."

for the project:

vehicle: multiple wagen that can drive by itself but are never

uncoupled (smallest unit)

formation: one or more vehicles that are coupled and form a train

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schedule: collection of tours, one for each vehicle

tour: sequence of activities covering one day

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• **service trip:** brings customers from a to b

• **dead-head trip:** driving from a to b without customers

• maintenance: maintenance check after given distance

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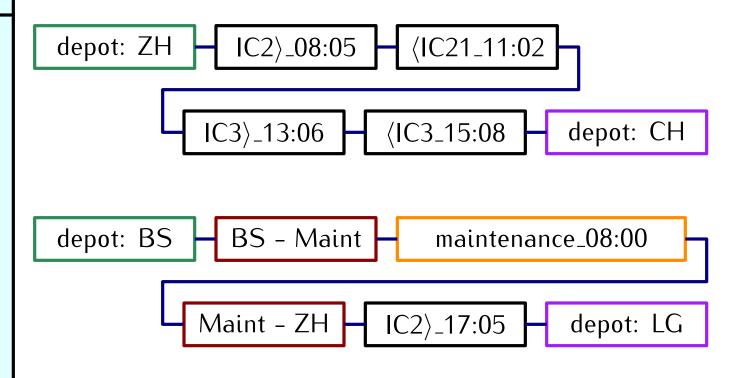
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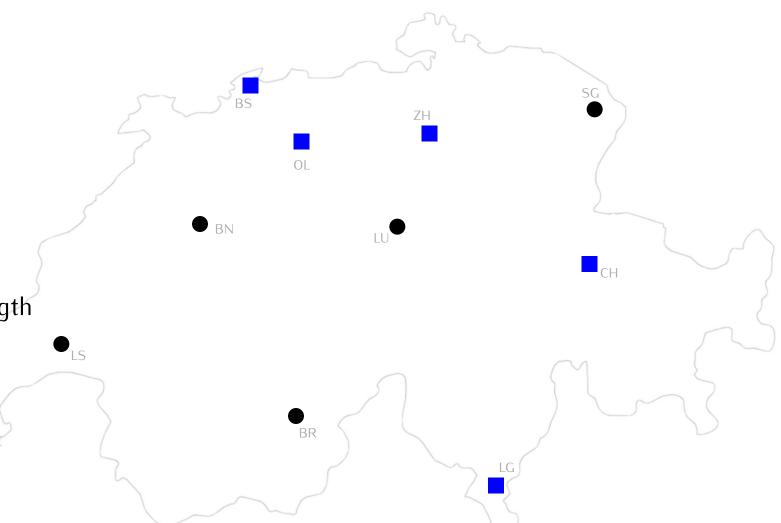
Phase 1 Basic Scheduling

input:

- **locations** (finite set *L*)
- depots: location, capacity
- routes origin, destination, distance, duration
- service trips route, departure time, passenger demand
- dead head trips:
 - distance matrix $\mathbb{R}^{L \times L}_{\geq 0}$
 - travel-time matrix $\mathbb{R}^{L \times L}_{>0}$
- vehicle type infos passenger capacity, max formation length

input:

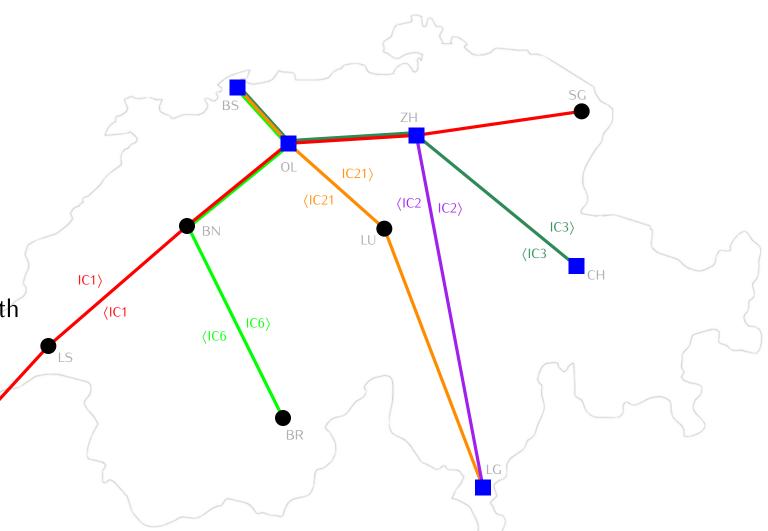
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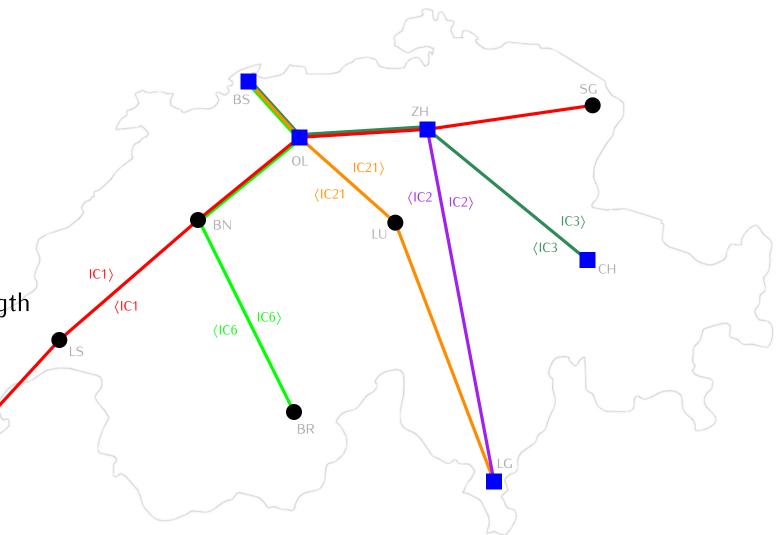
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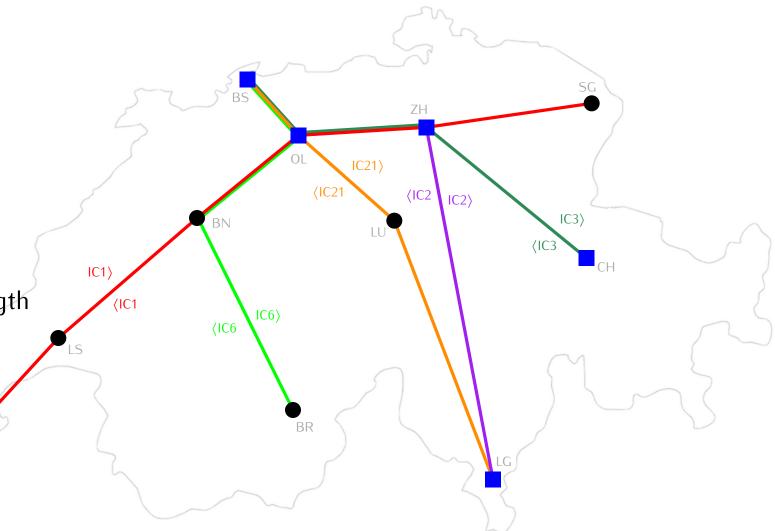


IC1>_05:42 IC1>_06:42	⟨IC1_05:07 ⟨IC1_06:07	\langle IC21_07:02 \langle IC21_08:02
IC1)_0 7 :42	⟨IC1_07:07	(IC21_09:02
: :	: :	: :
IC1>_20:42	⟨IC1_21:07	\langle IC21_22:02

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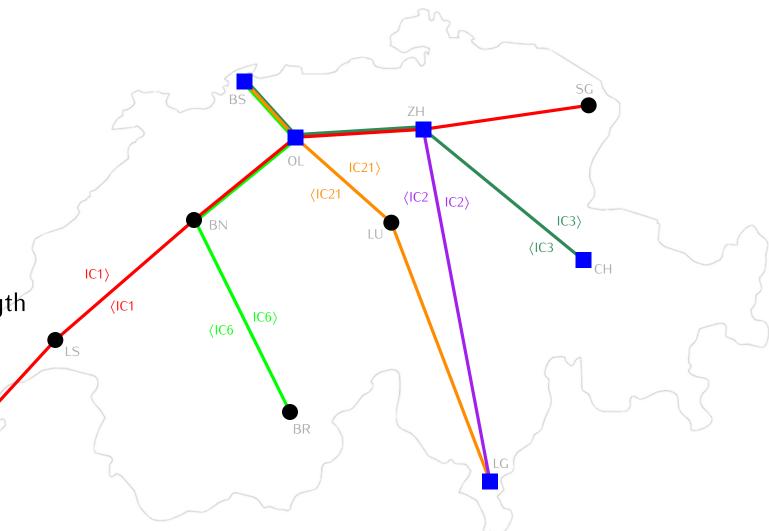


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output (schedule):

- a list of tours starting and ending at a depot
- cyclic (every day the same schedule)
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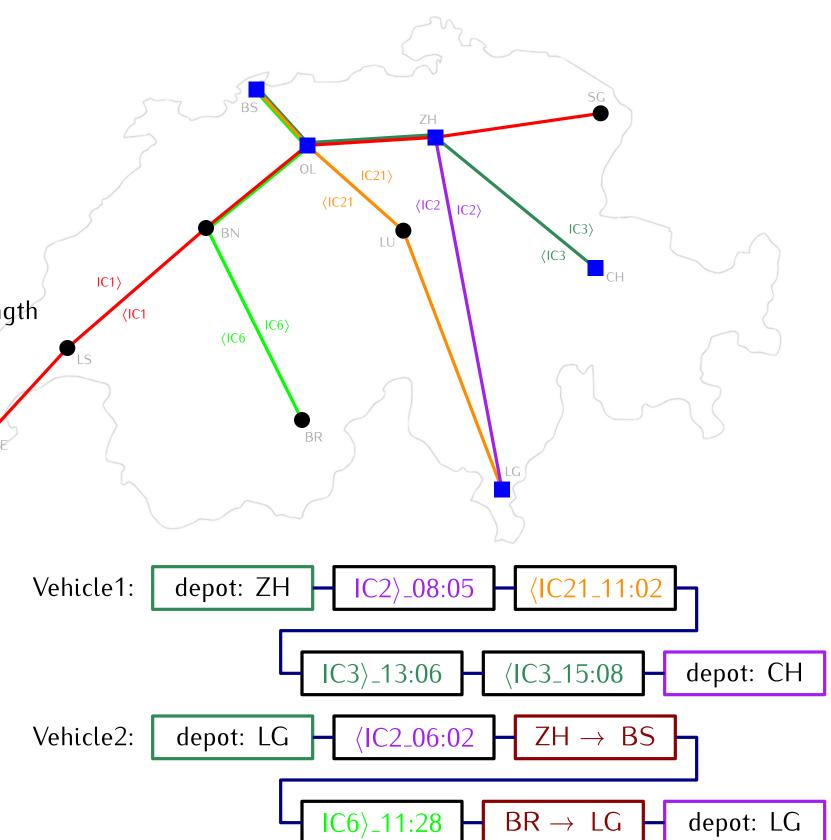
C1 >_05:42	⟨IC1_05:07 ♣ 20 ⟨IC1_06:07 ♣ 130 ⟨IC1_07:07 ♣ 310	 ⟨IC21_07:02
;	⋮	 :
:	⟨IC1_21:07 ⁂110	⟨IC21_22:02 ☆ 140

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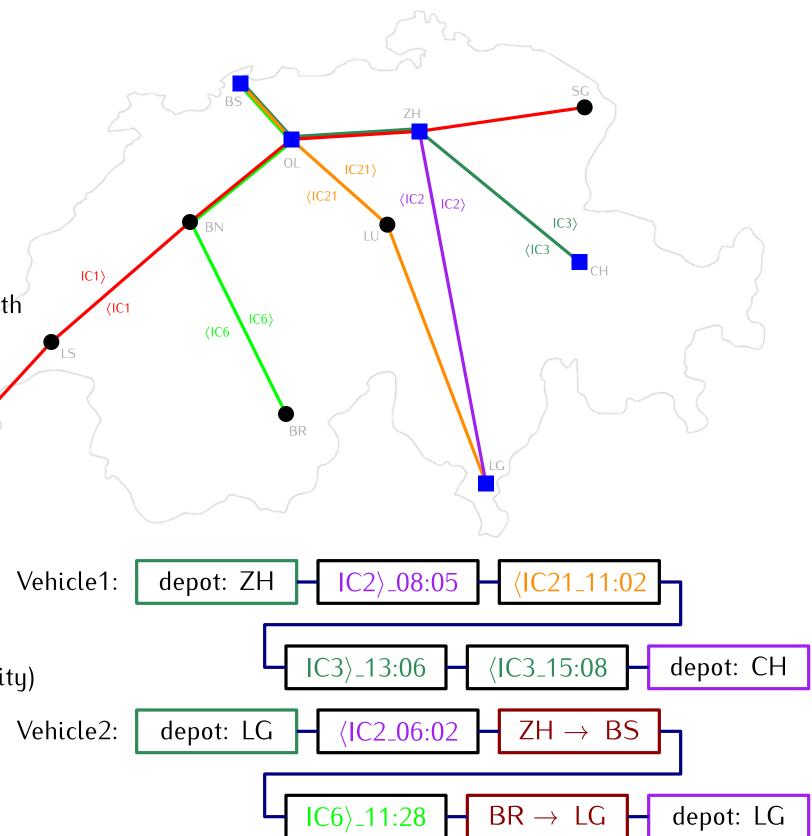
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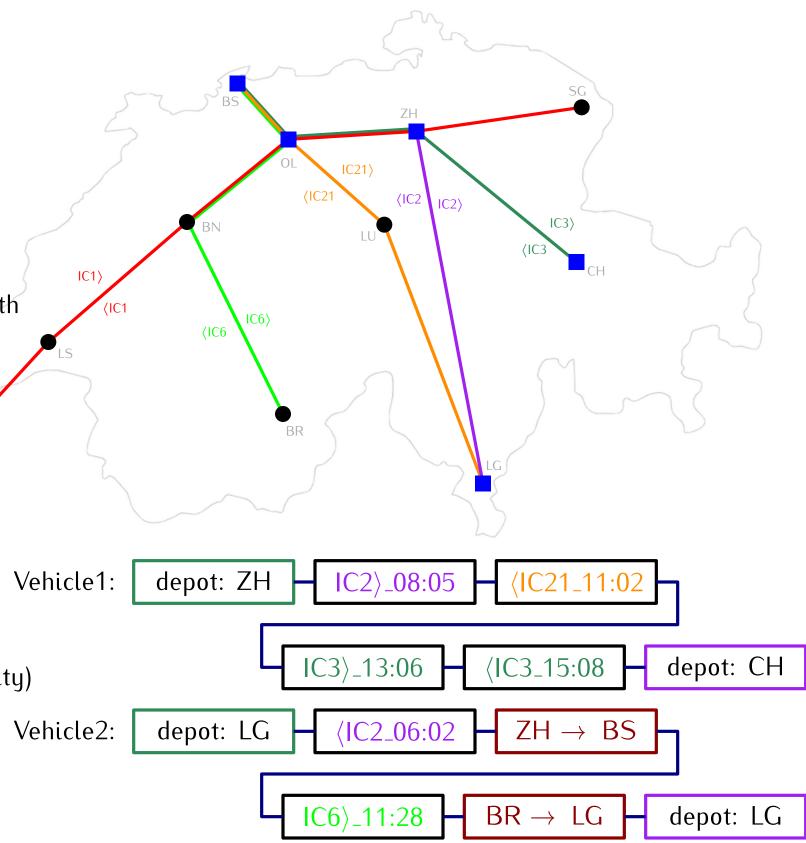
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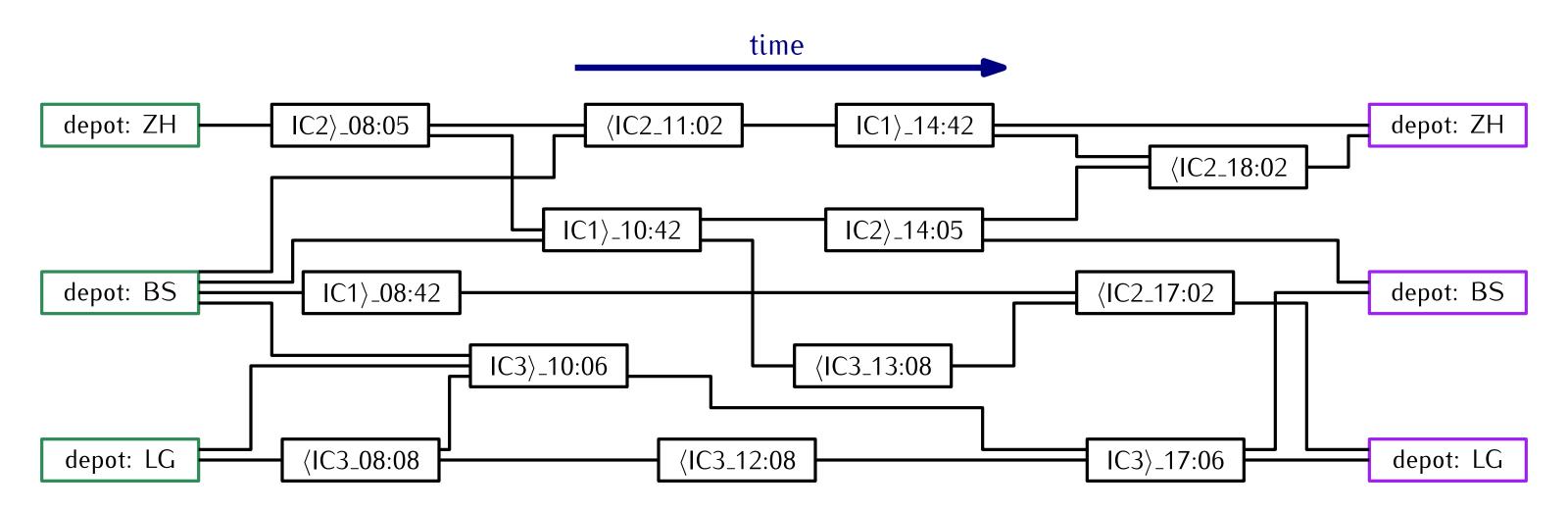
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hierachical objective: (to be minimized from top to bottom)

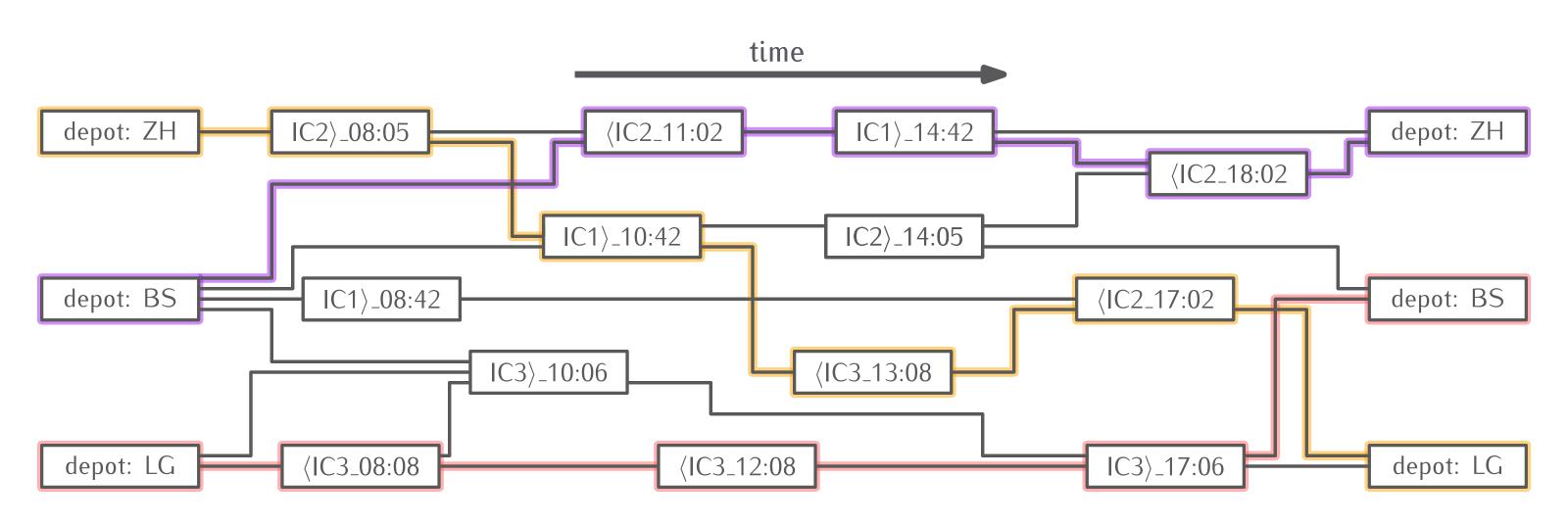
- 1. # unserved passengers
- 2. # number of vehicles
- 3. total distance traveled



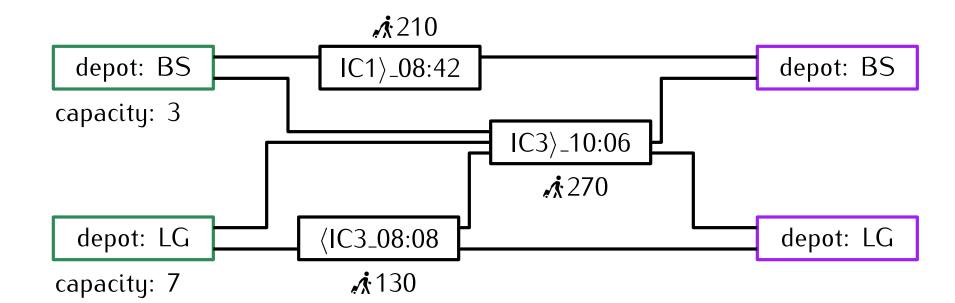
Phase 1 - Modeling



Phase 1 - Modeling



Model



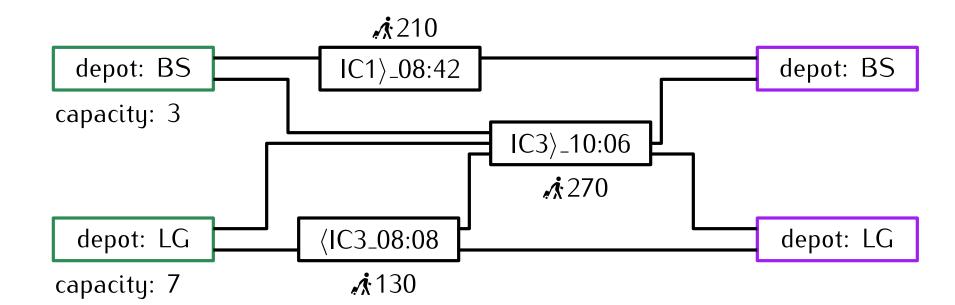
train info:

- passenger capacity per train: 200
- maximal vehicle in formation: 5

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Model



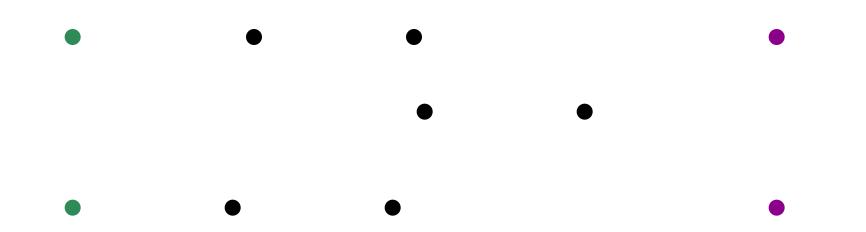
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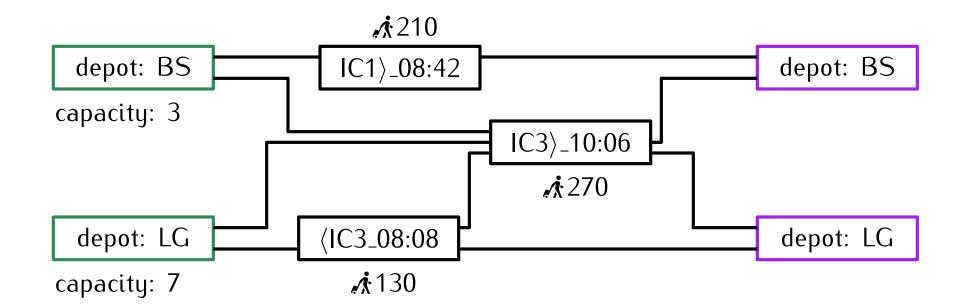
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Min-Cost-Circulation



Model



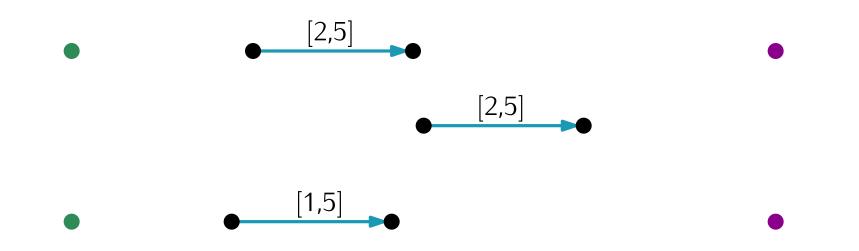
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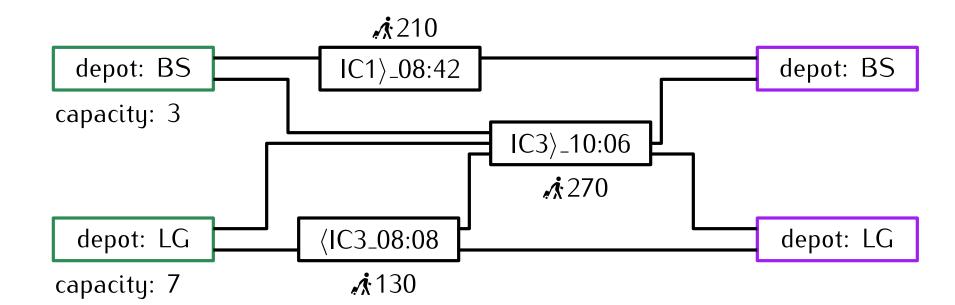
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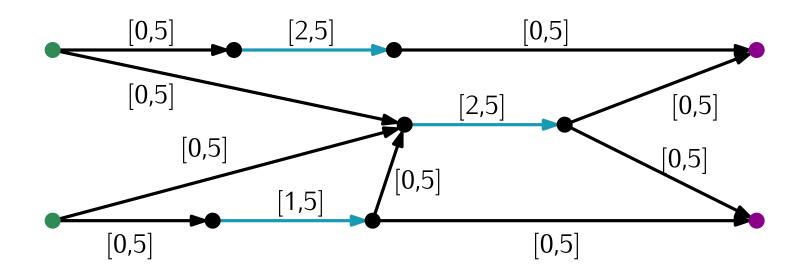
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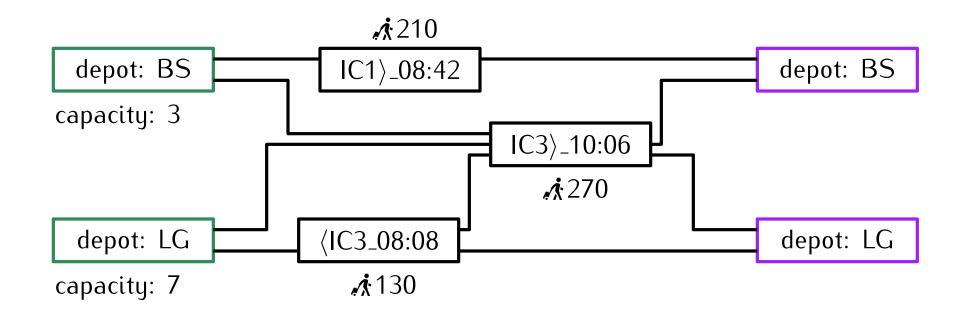
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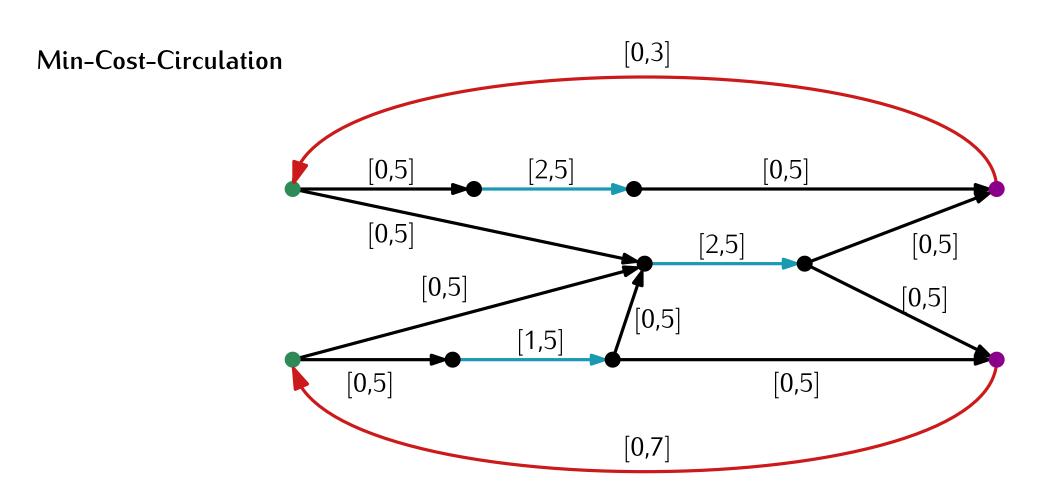
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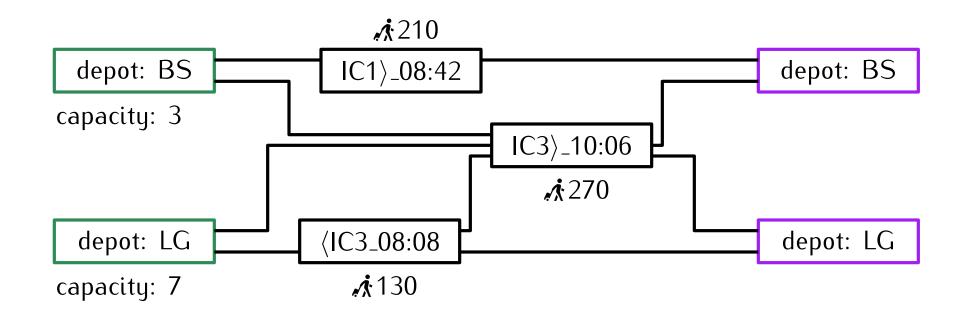
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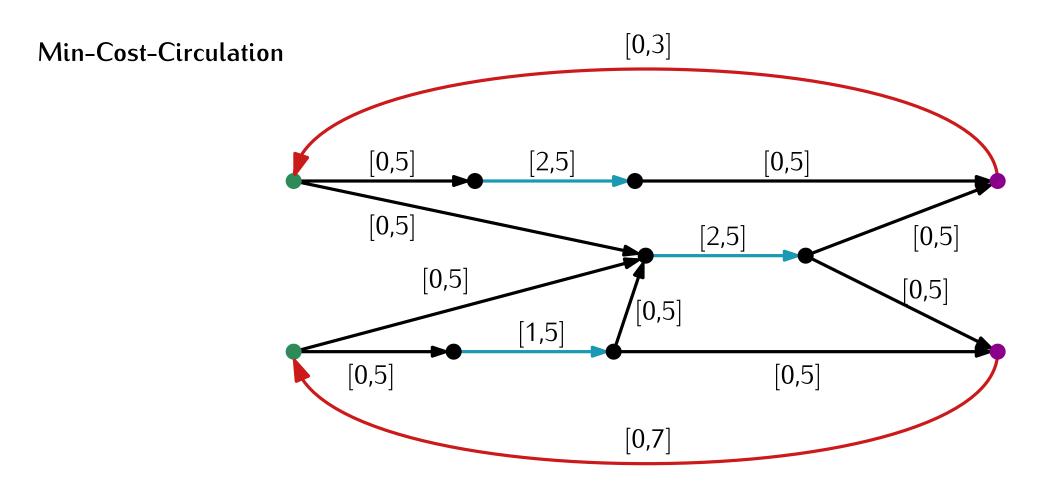


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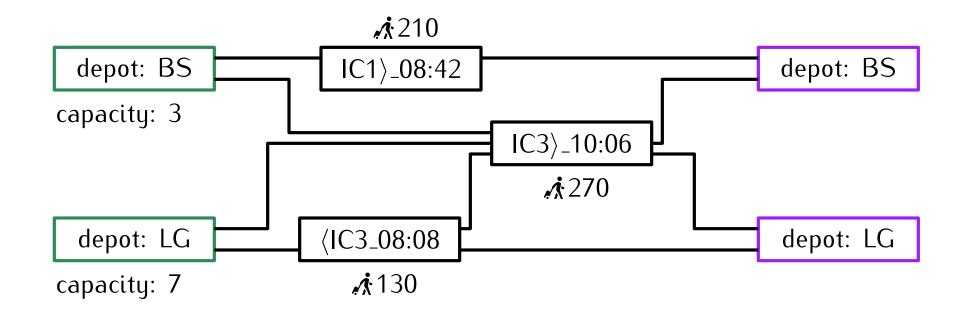
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costs:

- 1. forward arcs: distance traveled
- 2. depot arcs: sum of all distances

Model

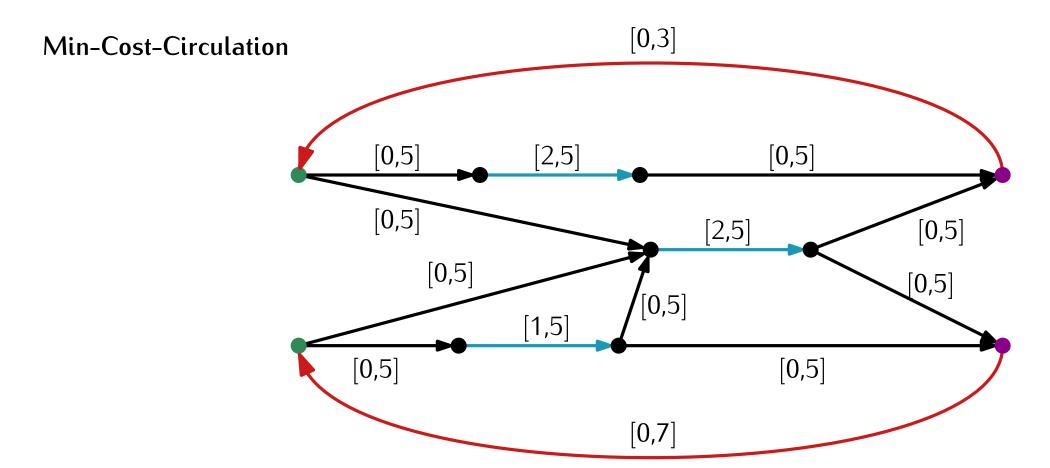


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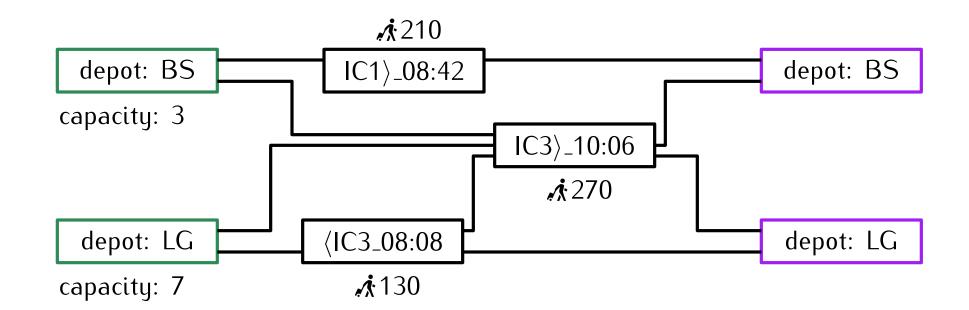
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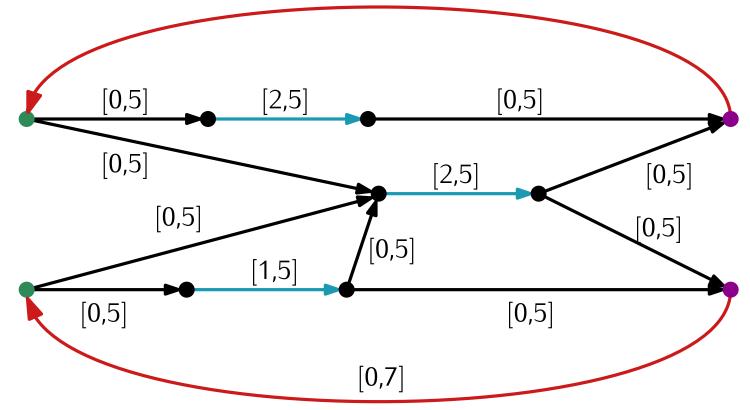
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Min-Cost-Circulation



[0,3]

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running time

- 1200 service trips
- 120 vehicle

- \Rightarrow 0.5 seconds
- Lenovo X1 Yoga

Phase 2 Model Extensions

seated / standing passengers

• assumption: passengers travelling < 15 minutes can stand (no seat needed)



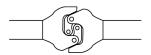
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strengthen / weaken train formation during a trip

- split service trips into segments
- within a segment: no coupling allowed
- between segments: vehicles can be (de-)coupled



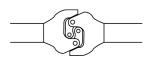
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 vehicles can be towed unused on a service trips (saves staff cost)



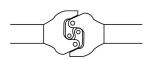
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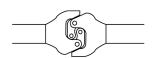
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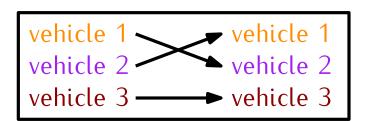






maintenance

- maintenance stations with multiple maintenance slots
- maintenance slots can be used by each type
- \bullet vehicles must go to maintenance every 15 000 km (\sim every 20 days)
- schedule is a single day repeated each day
- ullet map vehicles arriving at a depot in the evening to vehicles departure early in the morning (on the next day)



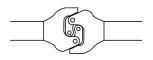
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old hierachical objective:

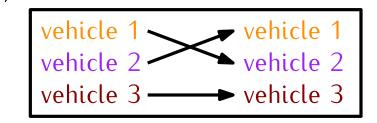
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new hierachical objective:

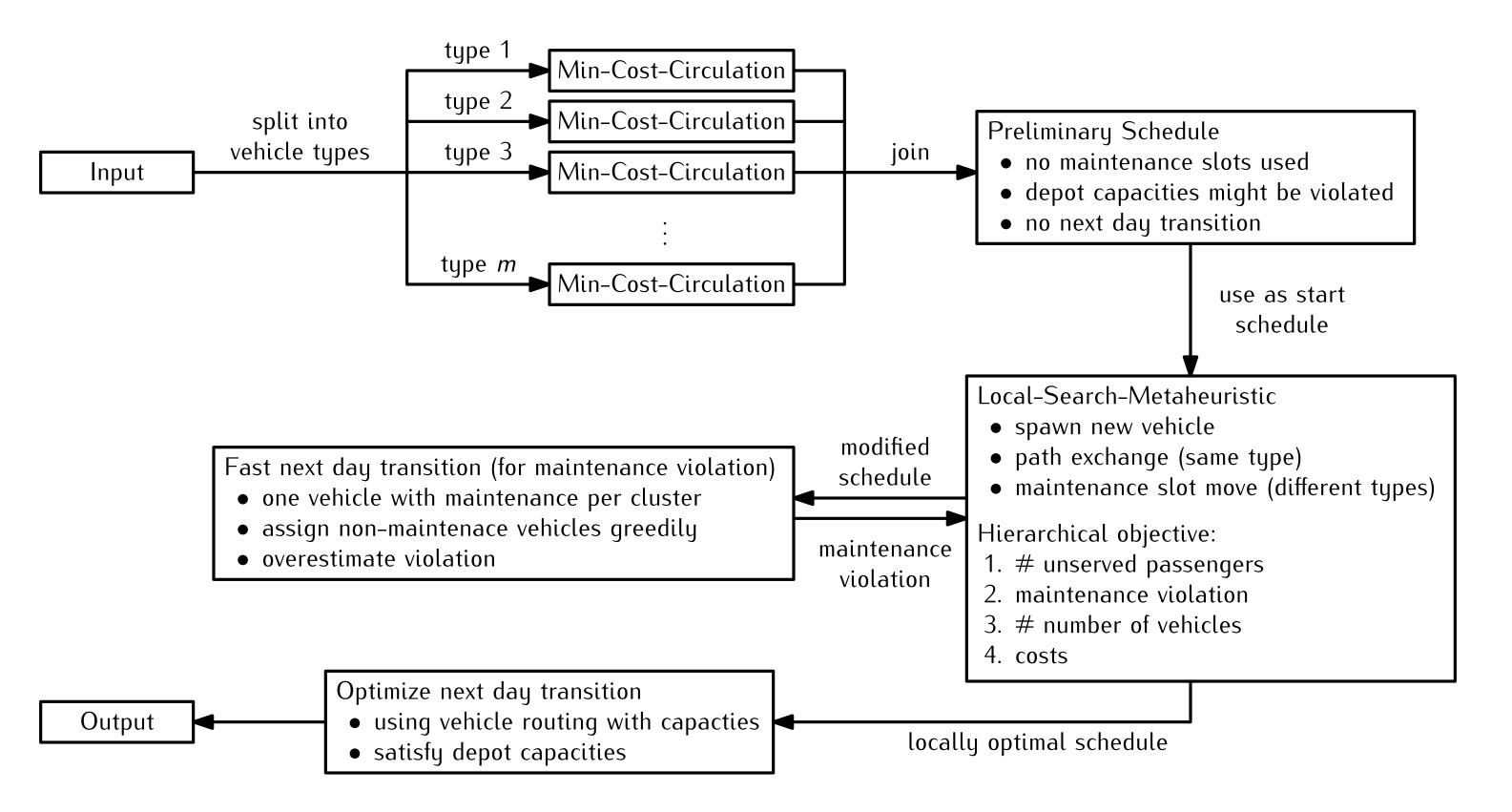
- 1. # unserved passengers
- 2. maintenance violation
- 3. # number of vehicles
- 4. costs

costs are a linear combination of

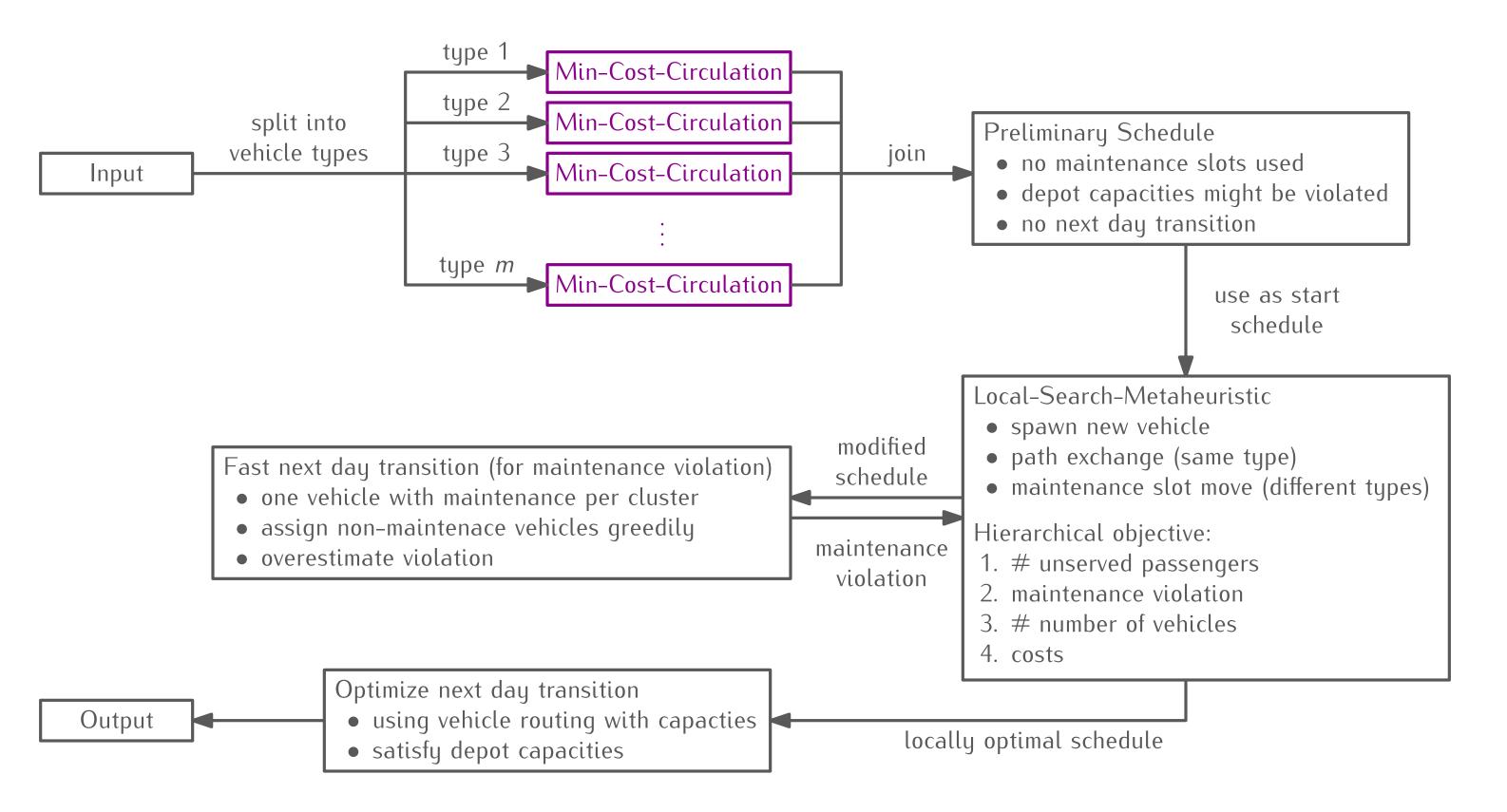
- total service trip duration
- total dead head trip duration
- mainteance duration
- idle duration
- staff cost (each train formation pays this only once)



Phase 2 - Algorithm Overview

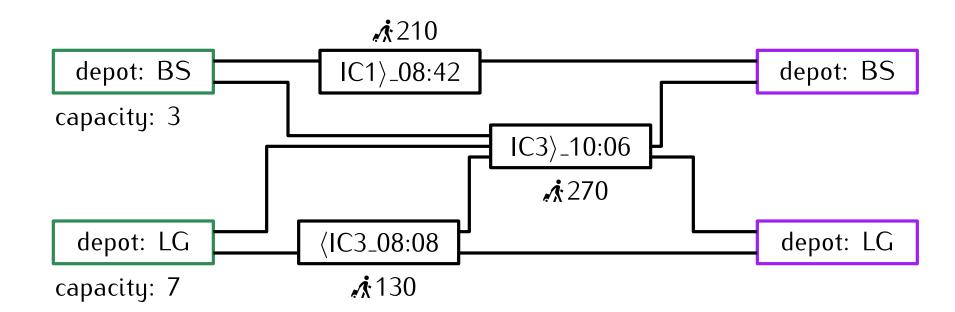


Phase 2 - Algorithm Overview

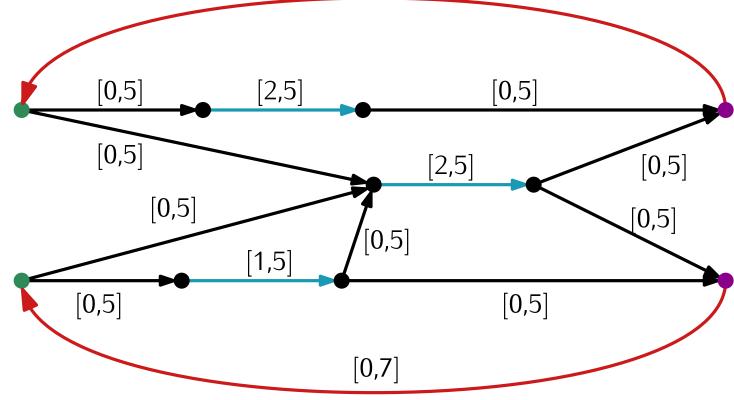


Min-Cost-Circulation

Model







[0,3]

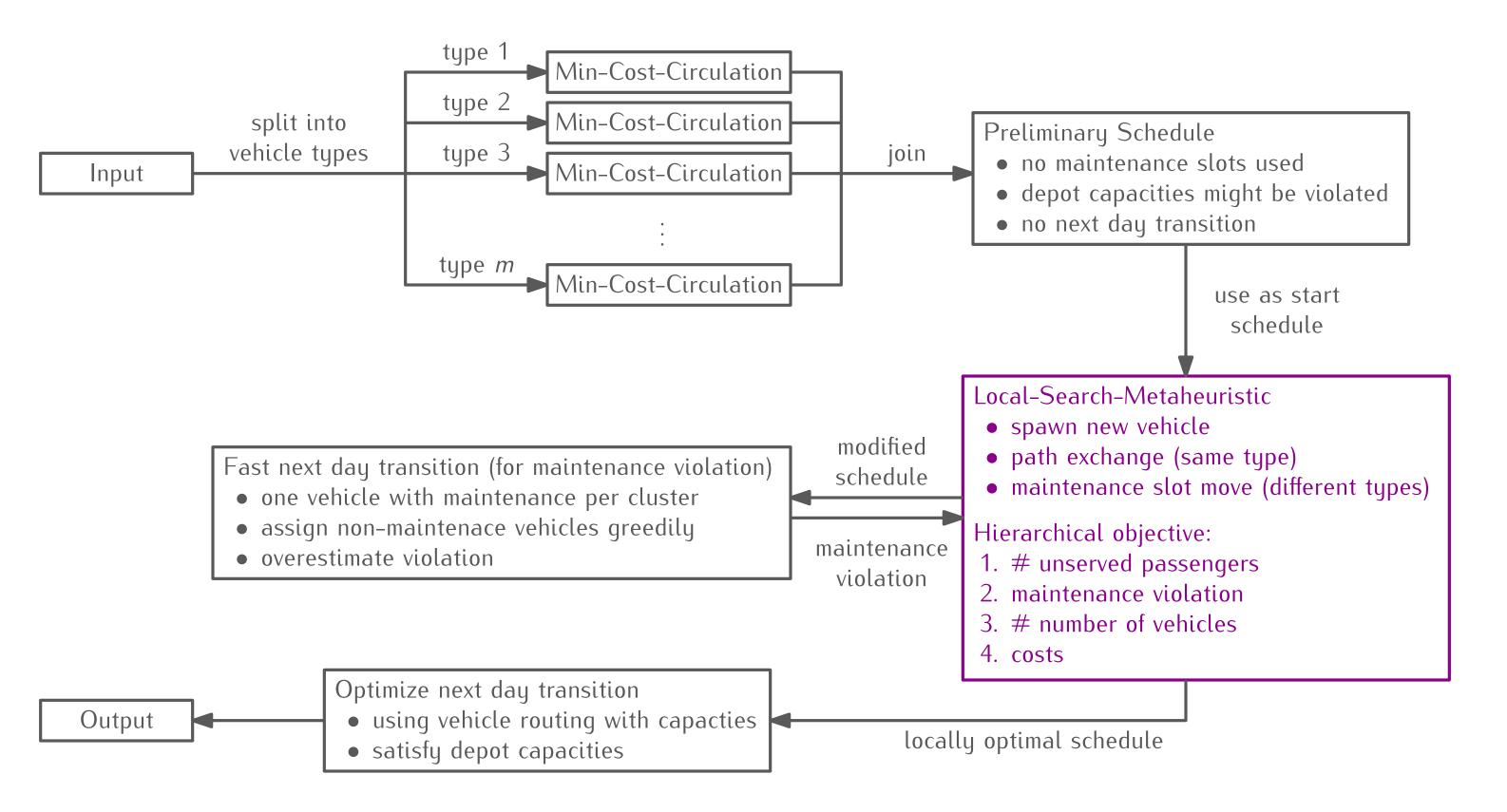
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costs:

- 1. forward arcs: new costs
- 2. depot arcs: sum of all costs

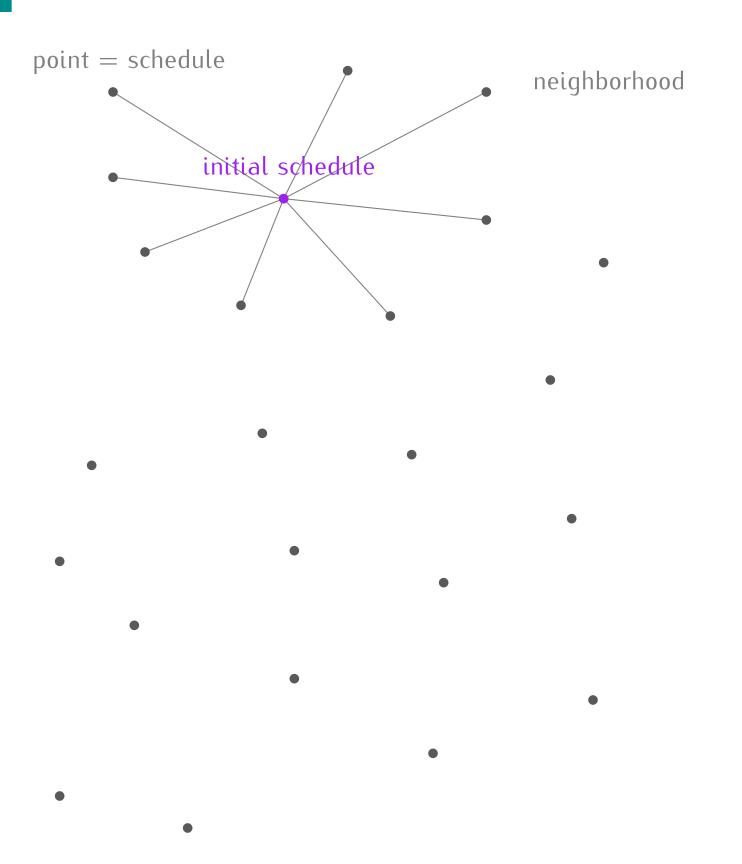
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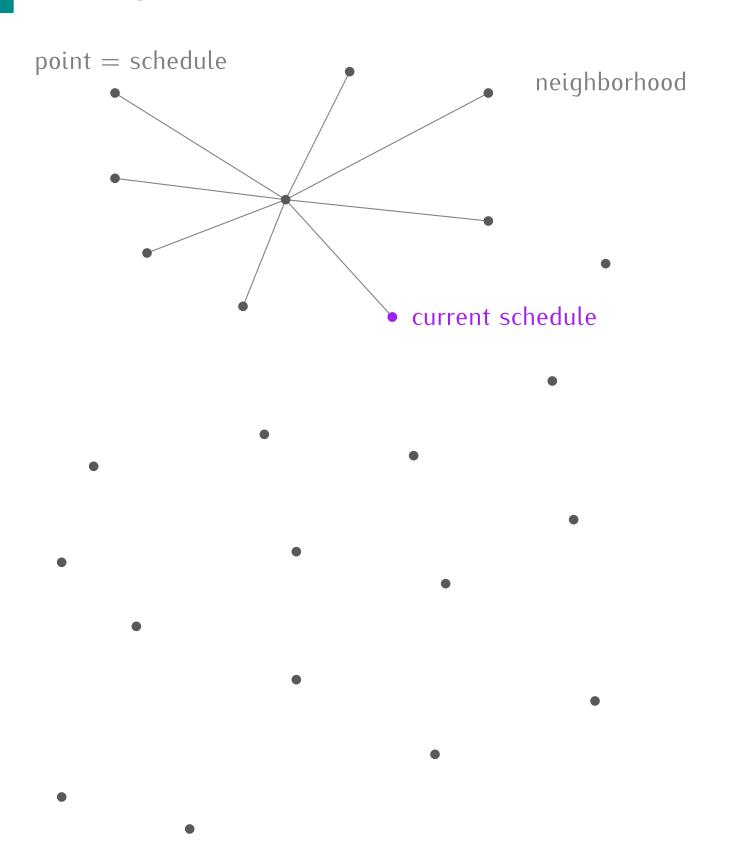


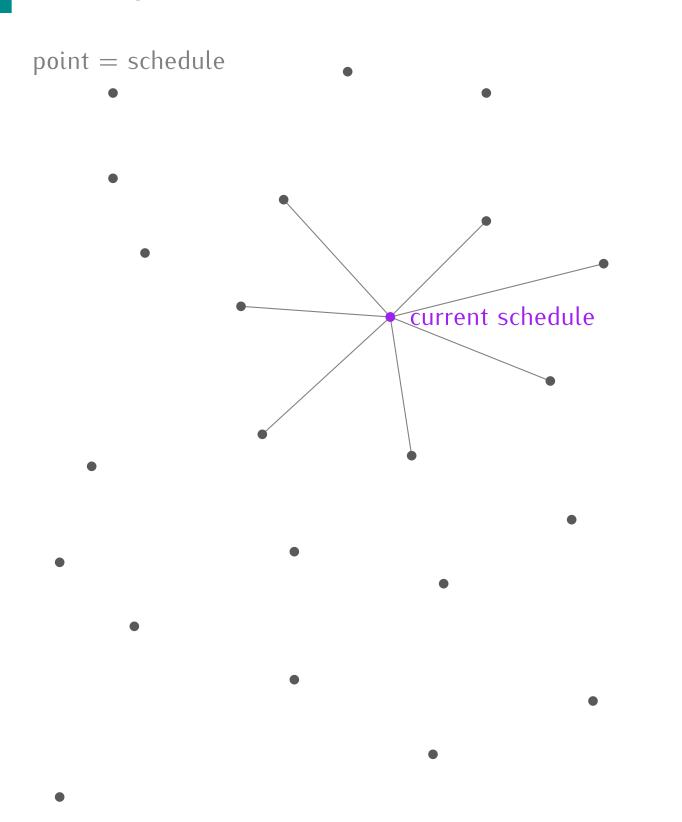
Local Search

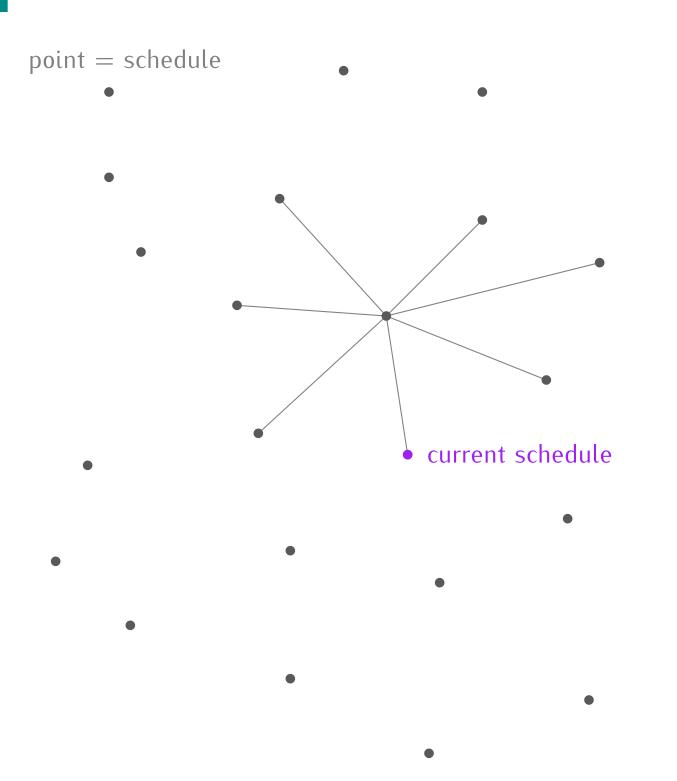
```
point = schedule
```

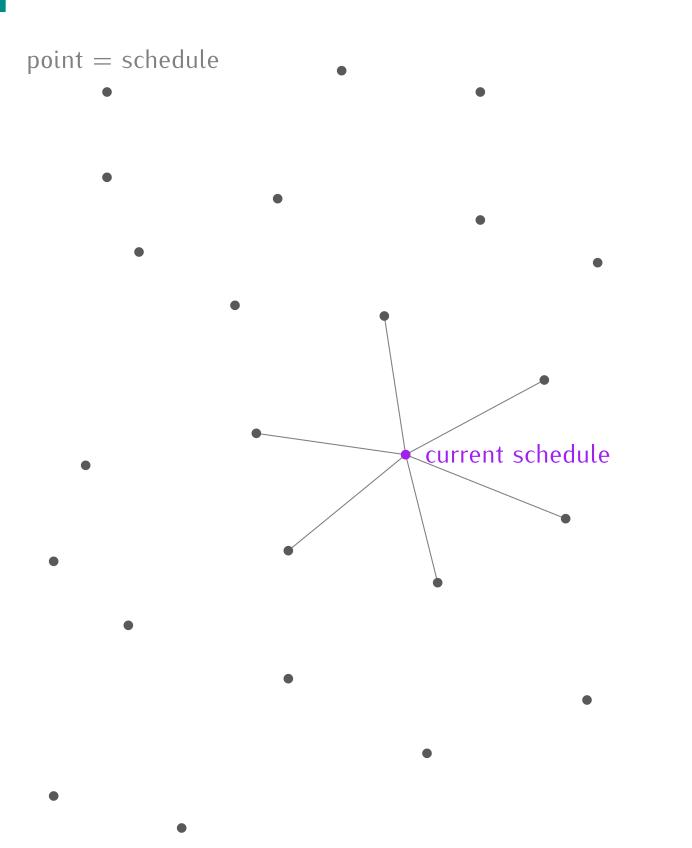
```
point = schedule
              initial schedule
```

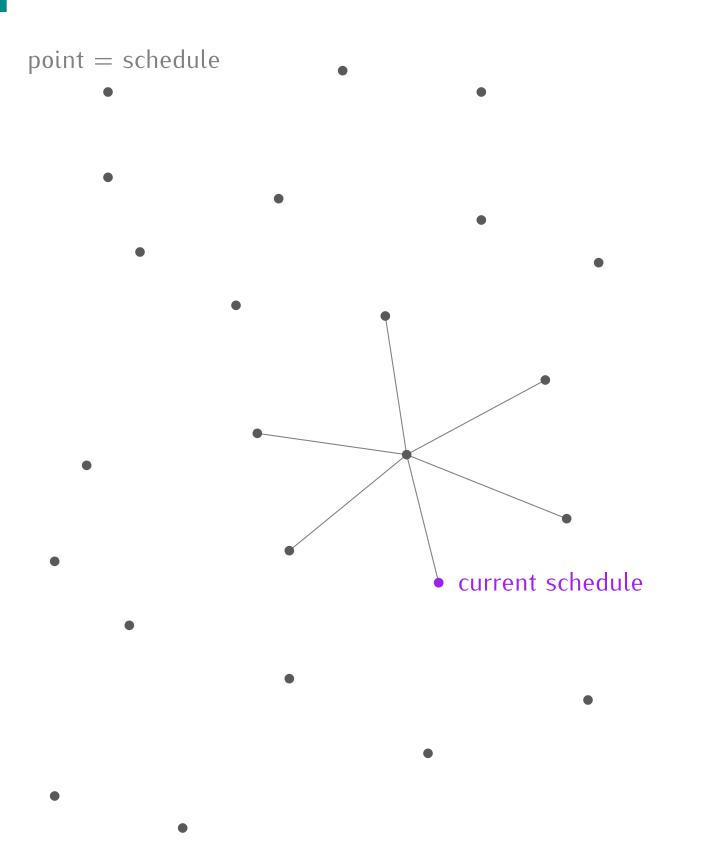


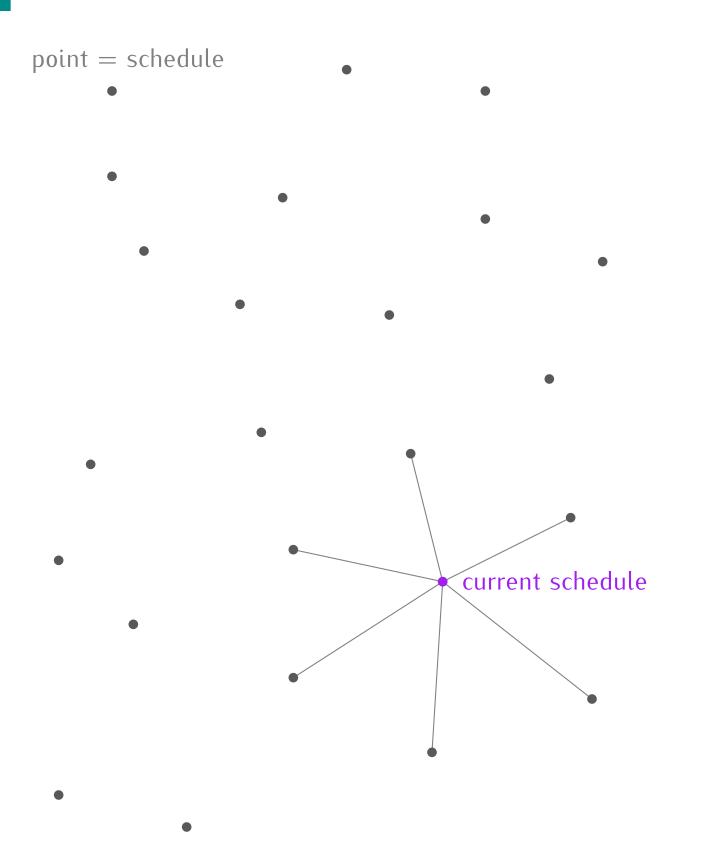


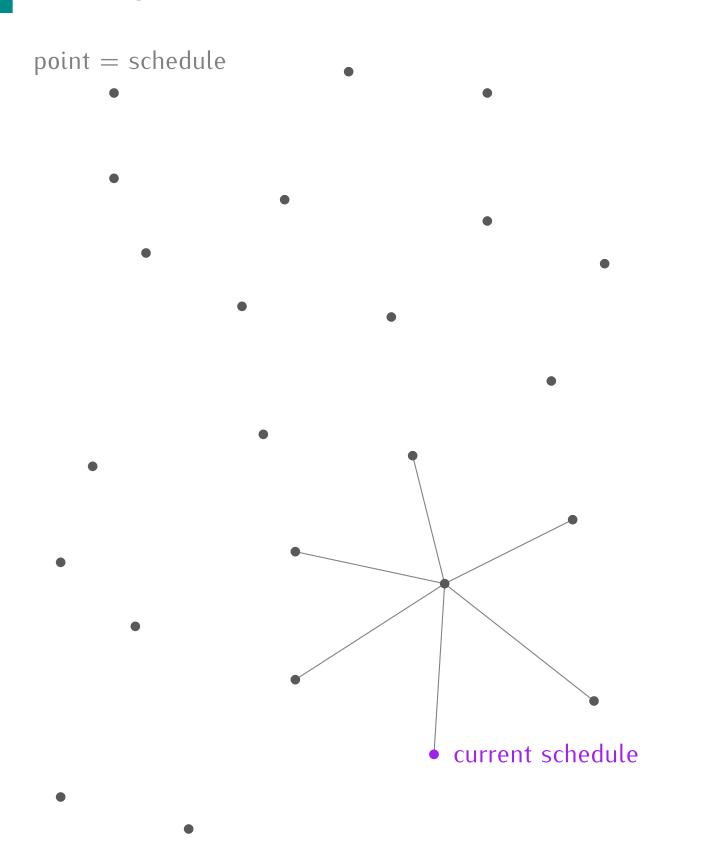


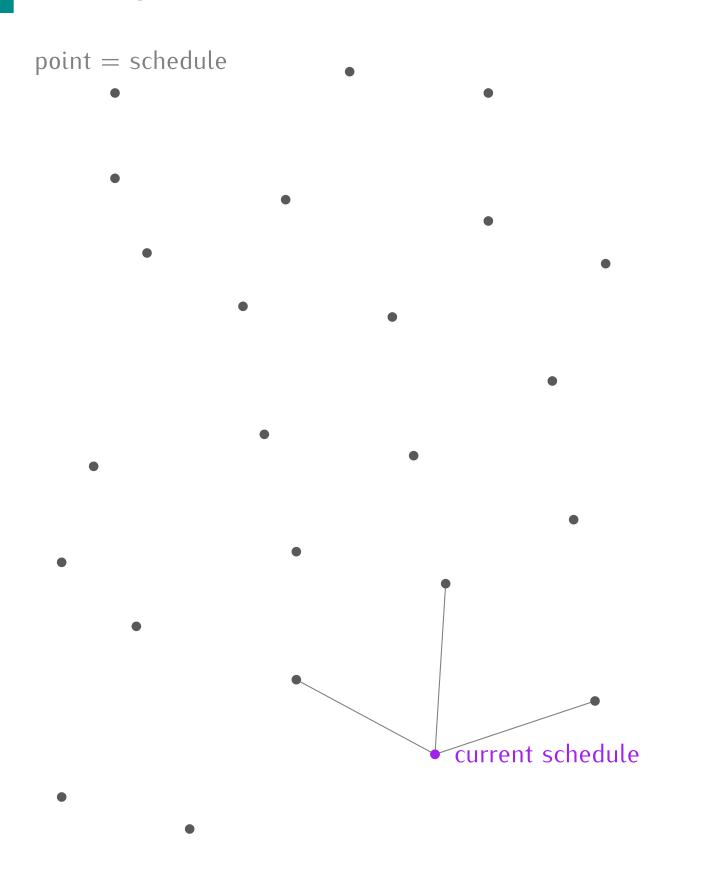


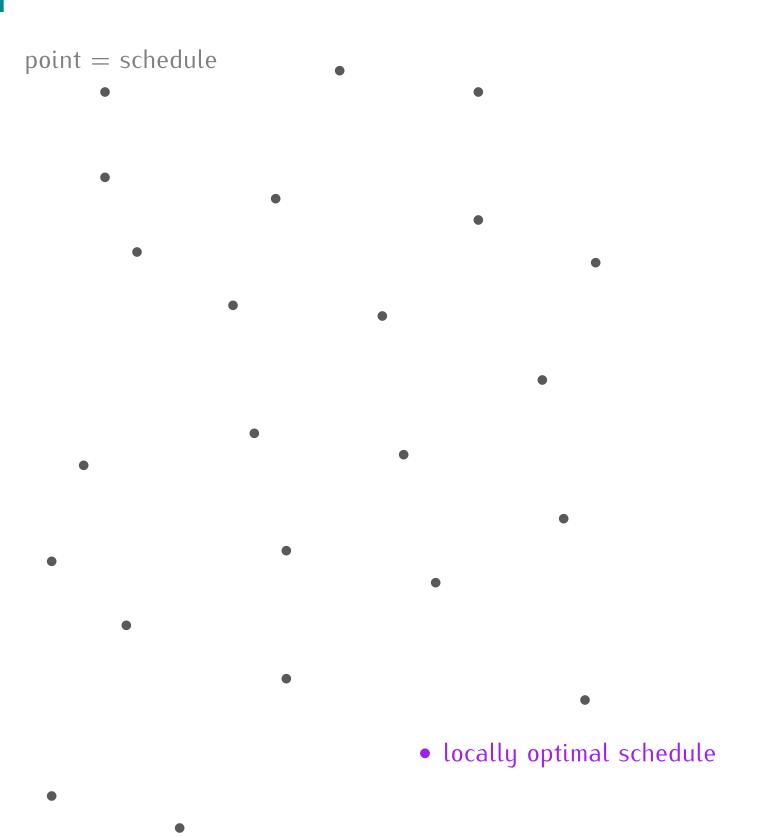




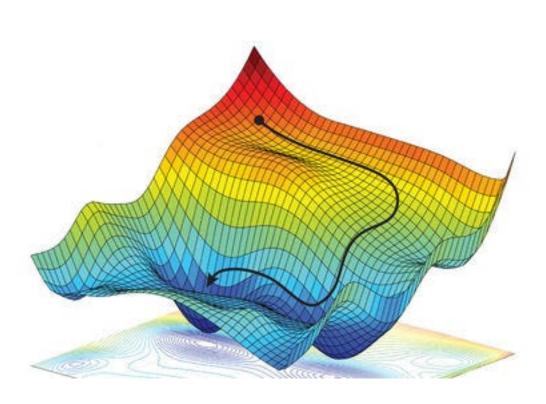


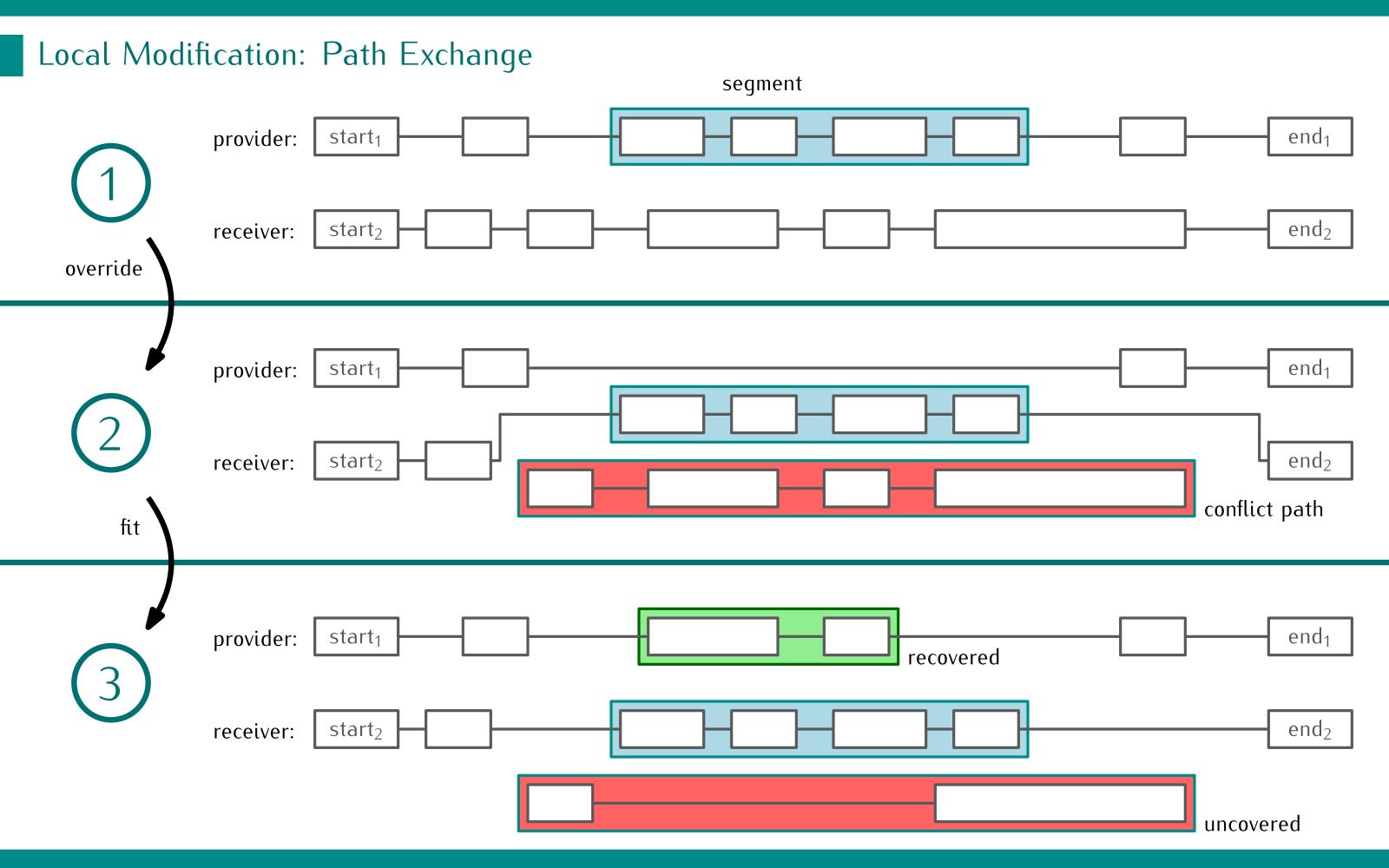




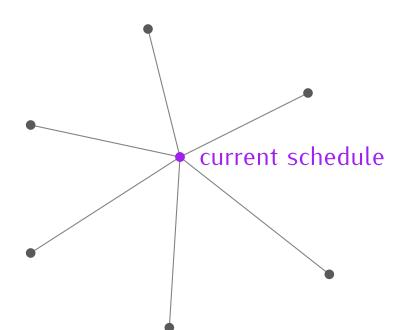






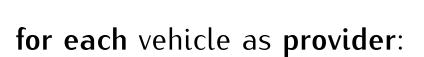


given the current schedule, consider the following modificaitons:



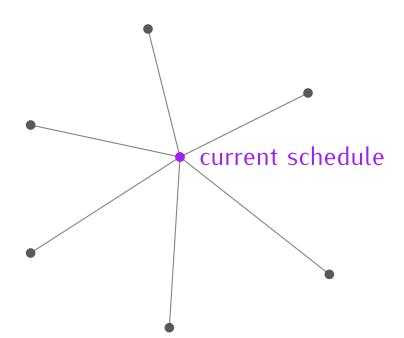
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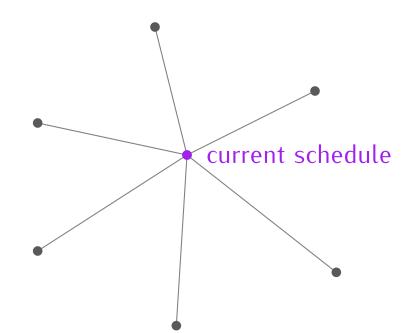


dead-head trips slower than service trips

for each segment of provider's tour that can be removed



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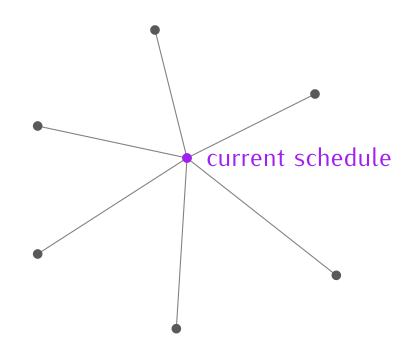
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(if segment is mainteance slot also different types are allwed)

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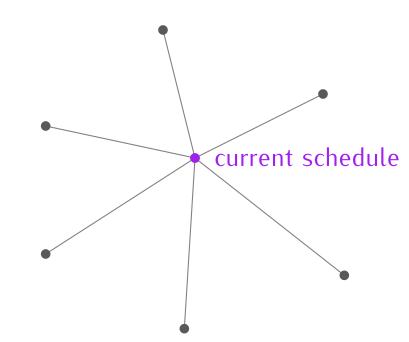
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(if segment is mainteance slot also different types are allwed)

PathExchange(segment, provider, receiver)

given the current schedule, consider the following modificaitons:

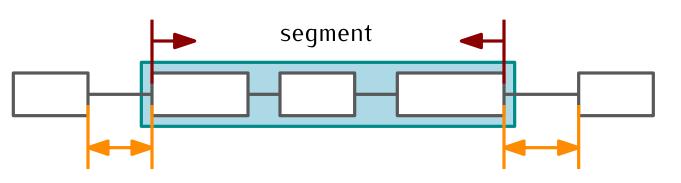


for each vehicle as provider:

dead-head trips slower than service trips

for each segment of provider's tour that can be removed

- restrict length: start of first node to end of last node
- restrict overhead time before and after

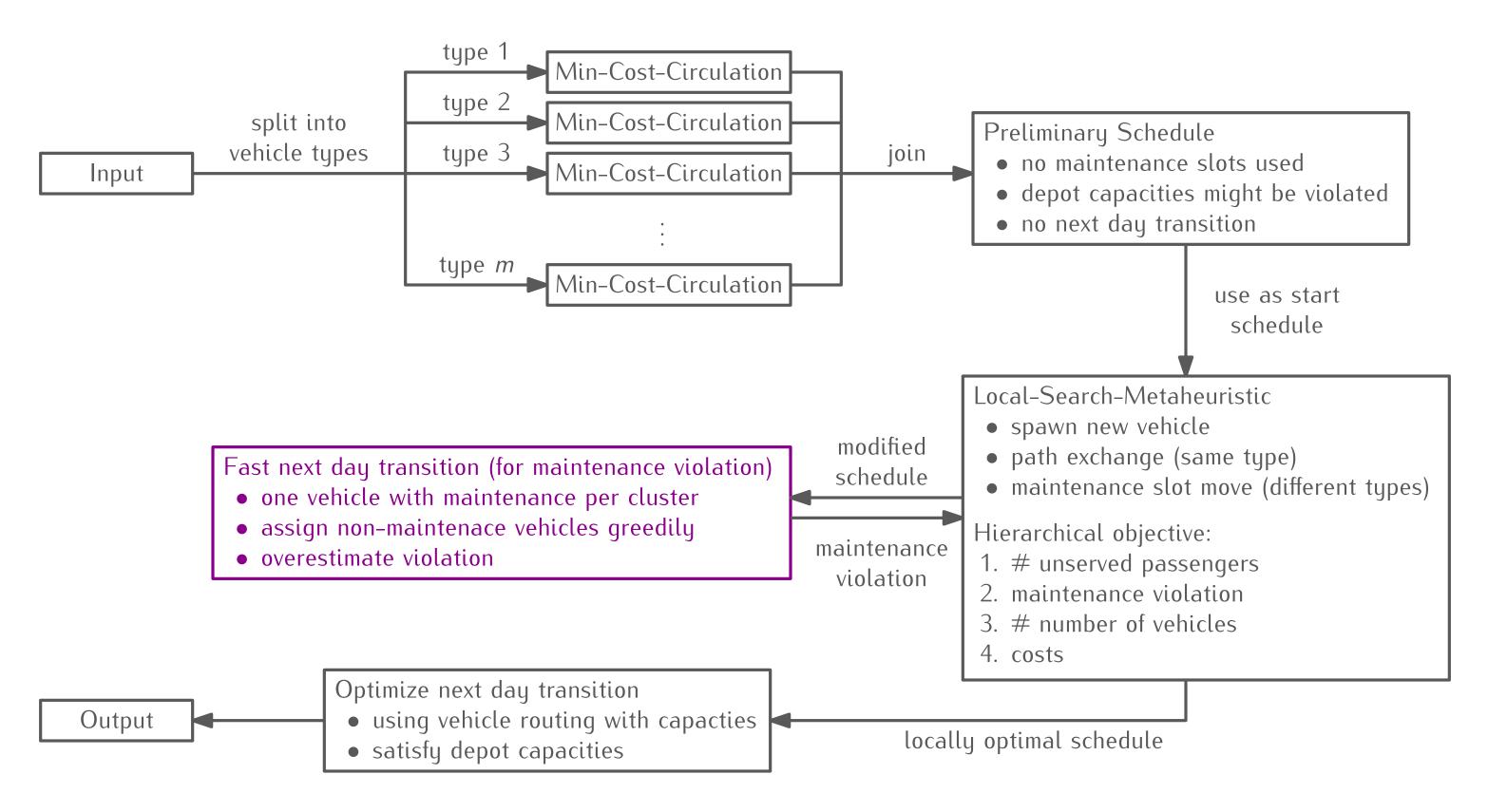


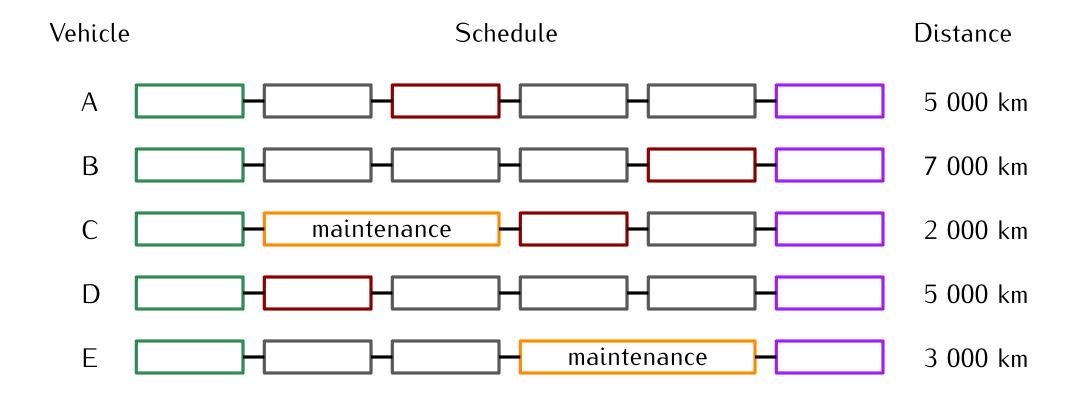
for each vehicle of the same type (that is not the provider) as receiver:

(if segment is mainteance slot also different types are allwed)

PathExchange(segment, provider, receiver)

Phase 2 - Algorithm Overview





maintenance all 15 000 km

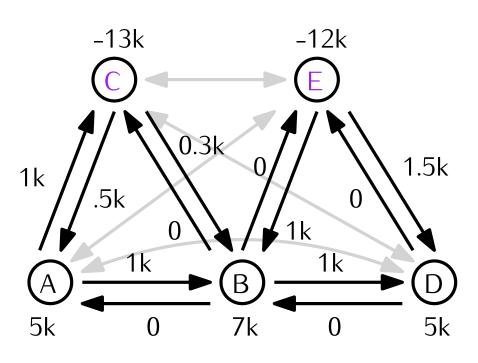
Vehicle	Schedule	Distance	Maintenance Counter	
А		5 000 km	= 5 000 km	
В		7 000 km	= 7 000 km	
С	maintenance — — — — — — — — — — — — — — — — — — —	2 000 km - 15 000 km	= - 13 000 km	
D		5 000 km	= 5 000 km	
Ε	maintenance	3 000 km - 15 000 km	= - 12 000 km	

maintenance all 15 000 km

Vehicle	Schedule	Distance	Maintenance Counter	
А		5 000 km	= 5 000 km	
В		7 000 km	= 7 000 km	
С	maintenance — — — — — — — — — — — — — — — — — — —	2 000 km - 15 000 km	= - 13 000 km	
D		5 000 km	= 5 000 km	
Е	maintenance	3 000 km - 15 000 km	= - 12 000 km	

Model

- consider types individually
- fully connected directed graph
 - one node per vehicle labeled with maintenance counter
 - arcs (v_1, v_2) are labelled with dead-head-distance between end depot of v_1 to start depot of v_2



maintenance all 15 000 km

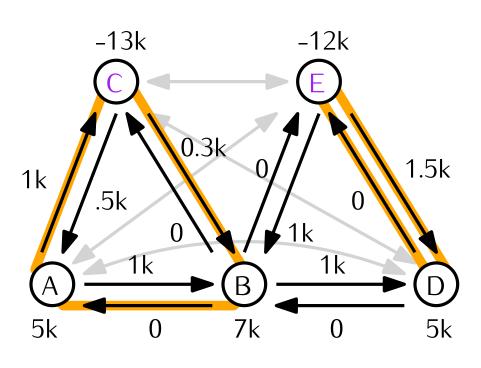
Vehicle	Schedule	Distance	Maintenance Counter
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Next Day Transition

- a set of disjoint cycles
- all nodes are covered



maintenance all 15 000 km

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А		5 000 km	= 5 000 km	
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Model

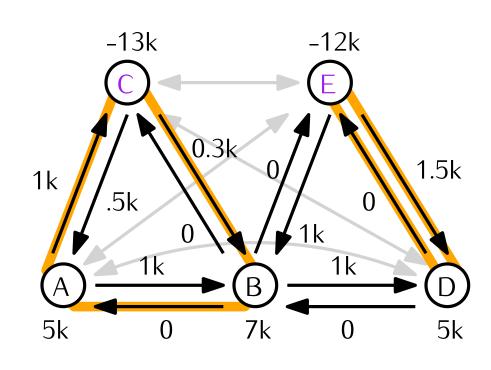
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Next Day Transition

- a set of disjoint cycles
- all nodes are covered

Objective:

• minimize maintenance violation: $\max_{C \in \mathcal{C}} (\max \{ d(C), 0 \})$ where $d(C) = \sup$ over all node and arc labels of cycle C



- 1. put all maintenance vehicles in a cycle (and sort them)
- 2. for each non-maintenance vehicle (in decreasing order):
 - (a) put vehicle into the first fitting cycle (or the last if none are fitting)
 - (b) resort cycles

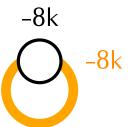
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maintenance vehicles: (decreasing)		-8k	-11k	-14k	
non-maintenance vehicles:	O 7k	O	O	O	O
(decreasing)		5k	4k	4k	3k

Algorithm

- 1. put all maintenance vehicles in a cycle (and sort them)
- 2. for each non-maintenance vehicle (in decreasing order):
 - (a) put vehicle into the first fitting cycle (or the last if none are fitting)
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maintenance vehicles:
(decreasing)



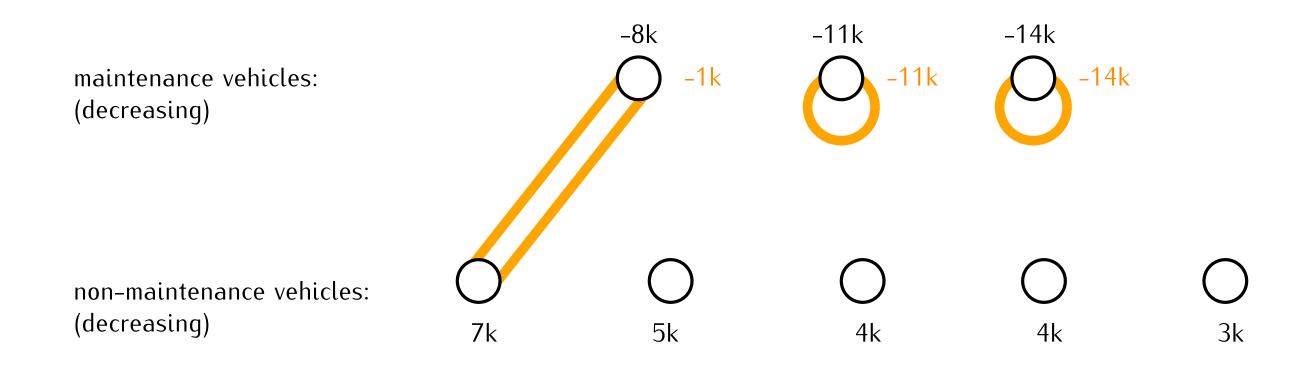
non-maintenance vehicles:
(decreasing)

$$O_{4k}$$

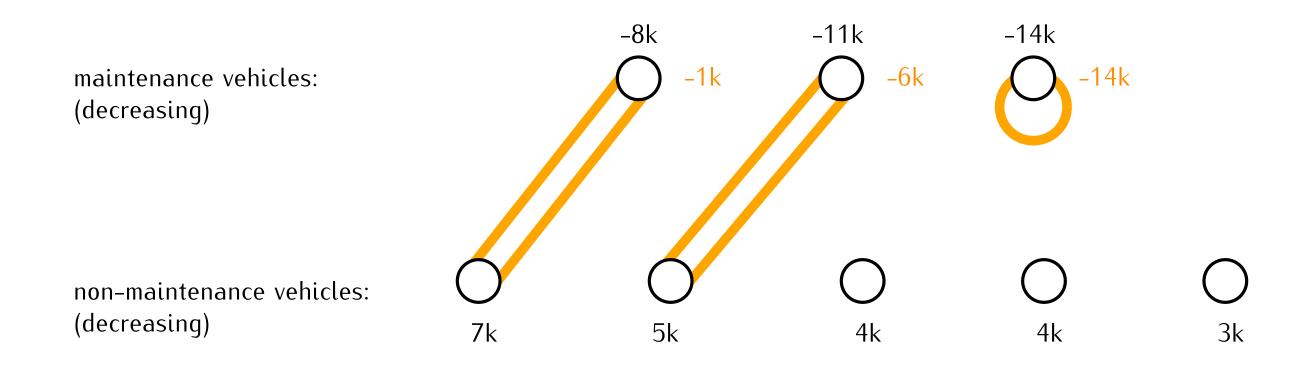
$$\bigcirc$$

$$\frac{1}{3k}$$

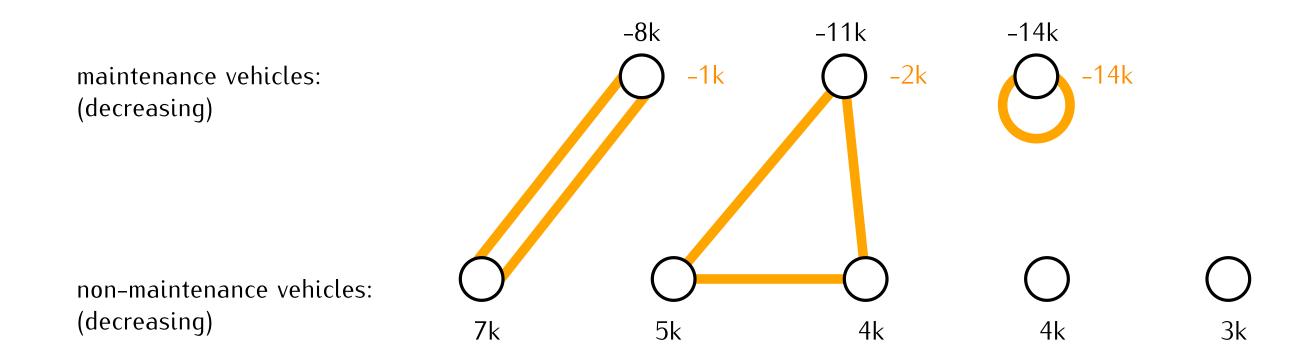
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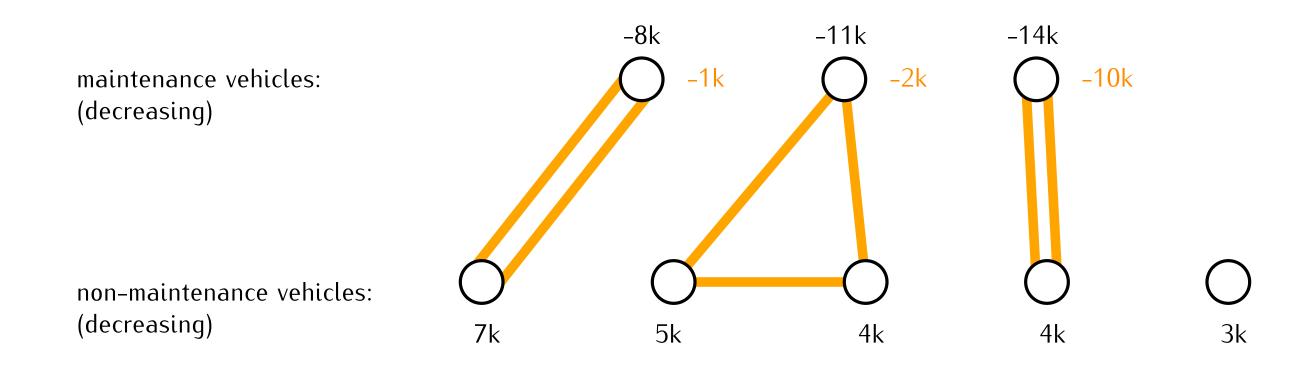
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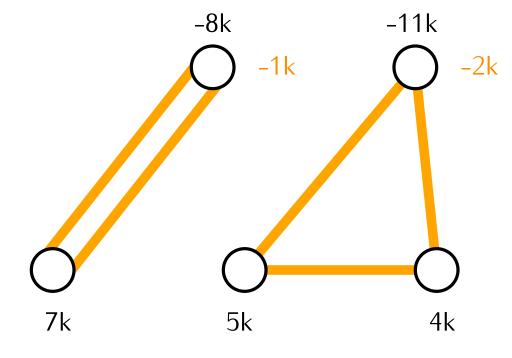


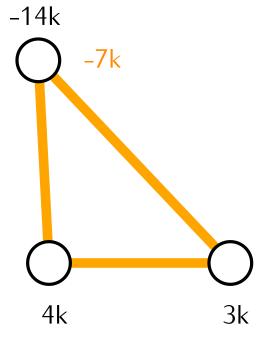
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maintenance vehicles:
(decreasing)

non-maintenance vehicles:
(decreasing)



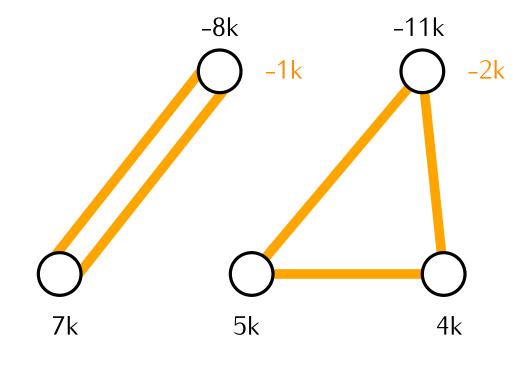


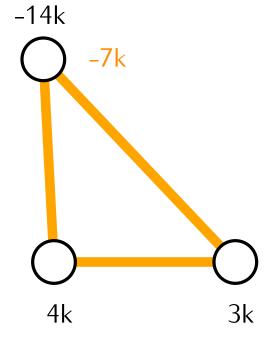
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(decreasing)

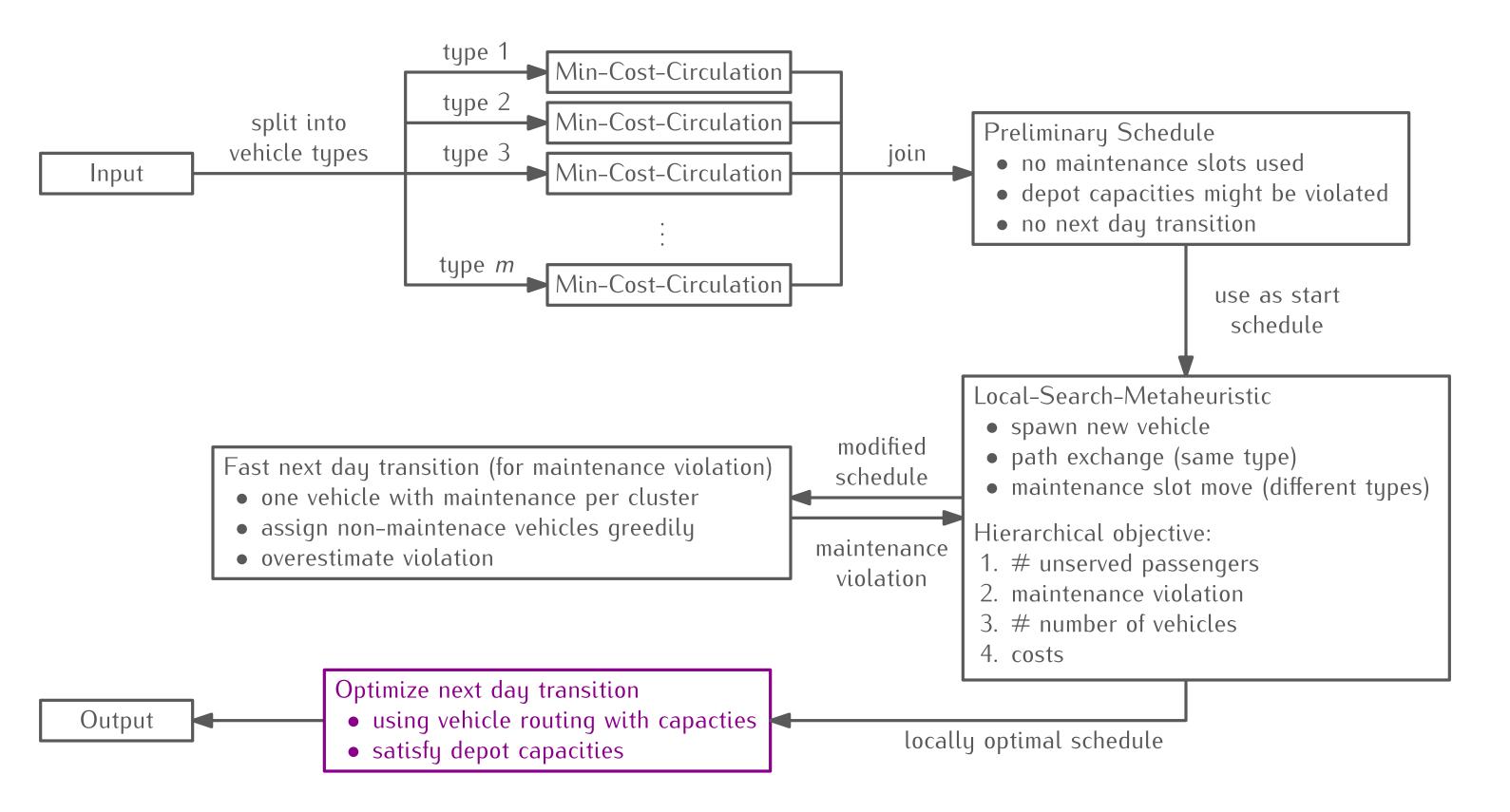
non-maintenance vehicles:
(decreasing)





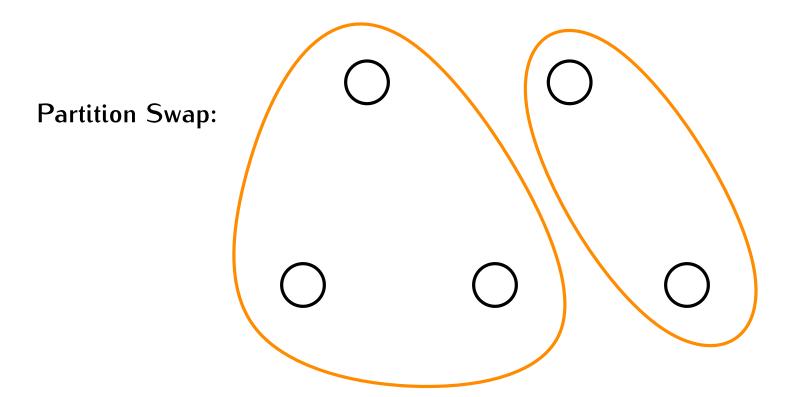
(dead-head trips between the depots are ignored for the slides)

Phase 2 – Algorithm Overview

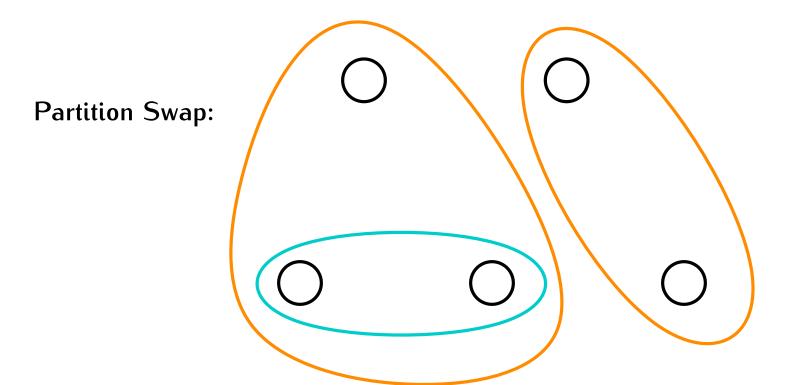


- still: only one maintenance vehicle per cycle
- ignore dead-head-trips between depots
- store partition instead of cycles
- cycles are computed afterwards for each component

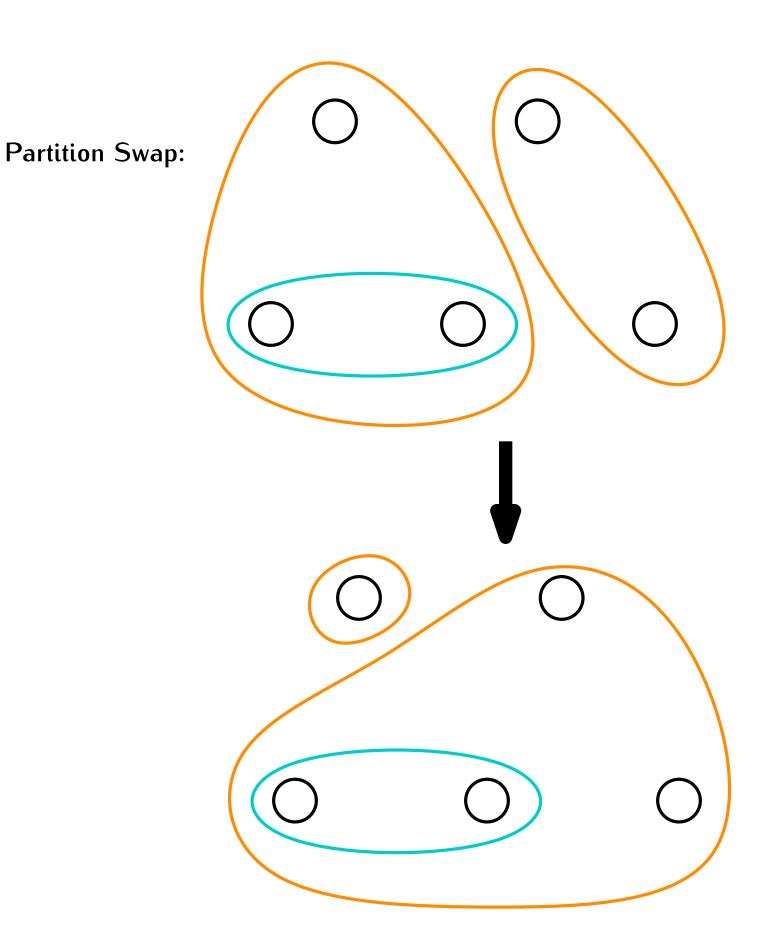
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- still: only one maintenance vehicle per cycle
- ignore dead-head-trips between depots
- store partition instead of cycles
- cycles are computed afterwards for each component



Local Search (again):

- still: only one maintenance vehicle per cycle
- ignore dead-head-trips between depots
- store partition instead of cycles
- cycles are computed afterwards for each component

Neighborhood:

for each component as provider:

for each other component as receiver:

for each subset of provier's vehicles

PartitionSwap(subset, provider, receiver)

recompute cycles for provider and receiver

