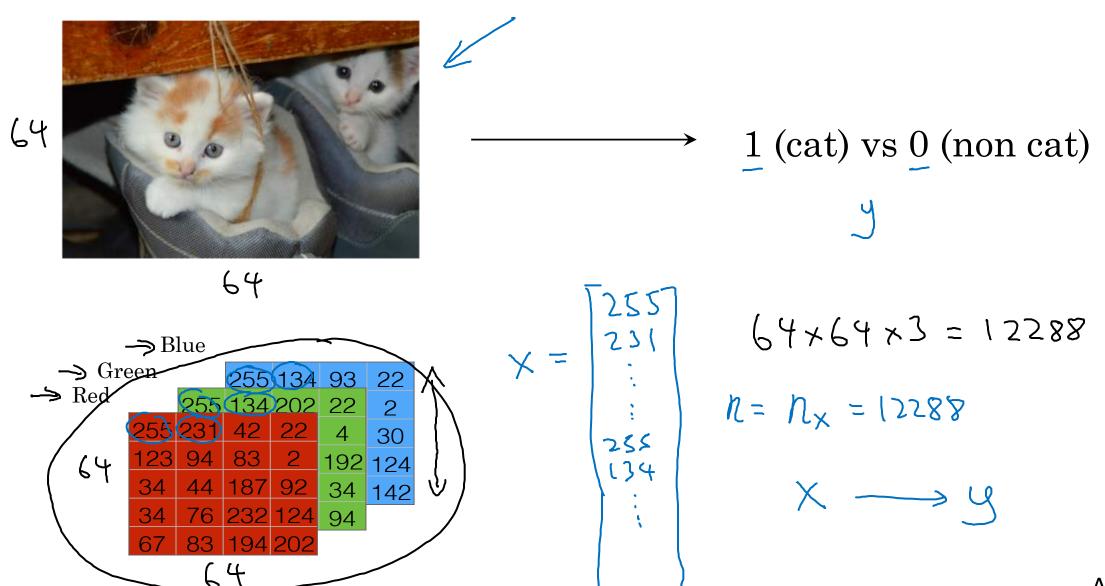


Basics of Neural Network Programming

Binary Classification

Binary Classification



Andrew Ng

Notation

$$(x,y) \times \mathbb{CR}^{n_{x}}, y \in \{0,1\}$$

$$m \text{ training evarples}: \{(x^{(1)},y^{(1)}), (x^{(1)},y^{(2)}), \dots, (x^{(m)},y^{(m)})\}$$

$$M = M \text{ train} \qquad M \text{ test} = \text{ $\#$ test examples}.$$

$$X = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X \in \mathbb{R}^{n_{x} \times m}$$



Basics of Neural Network Programming

Logistic Regression

Logistic Regression

Given
$$x$$
, want $y = P(y=1|x)$
 $x \in \mathbb{R}^{n}x$
Parareters: $w \in \mathbb{R}^{n}x$, $b \in \mathbb{R}$.
Output $y = \sigma(w^{T}x + b)$
Output $y = \sigma(x)$

$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$\hat{y} = 6 (0^{T}x)$$

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Basics of Neural Network Programming

Logistic Regression cost function

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Since $\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function: $\int_{\mathcal{C}} (\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$

The entropy of the second of the



Basics of Neural Network Programming

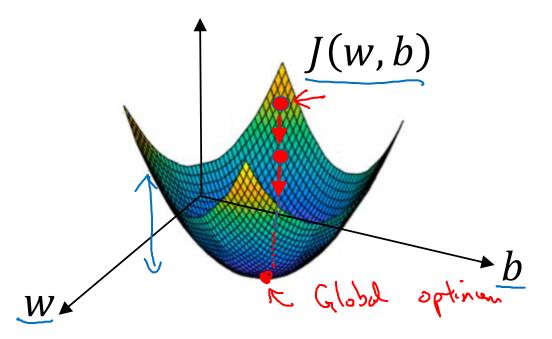
Gradient Descent

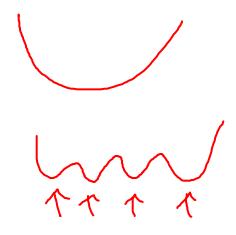
Gradient Descent

Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$

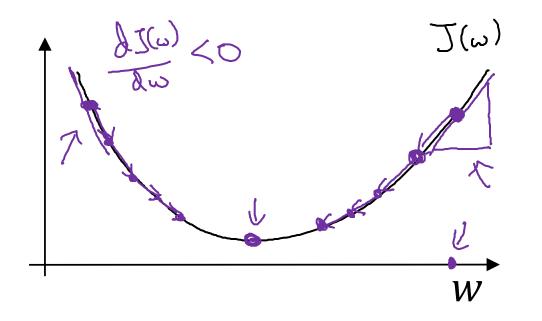
$$\underline{J(w,b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

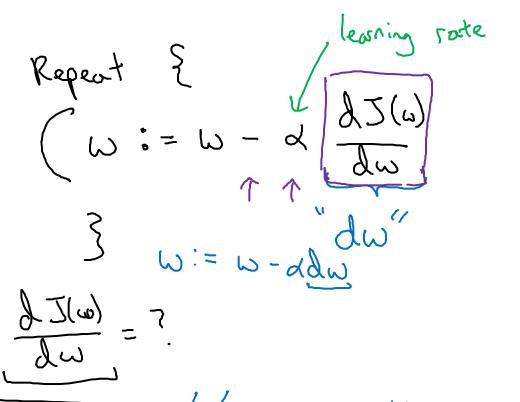
Want to find w, b that minimize J(w, b)





Gradient Descent





$$J(\omega,b)$$

$$b:=b-\lambda \frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

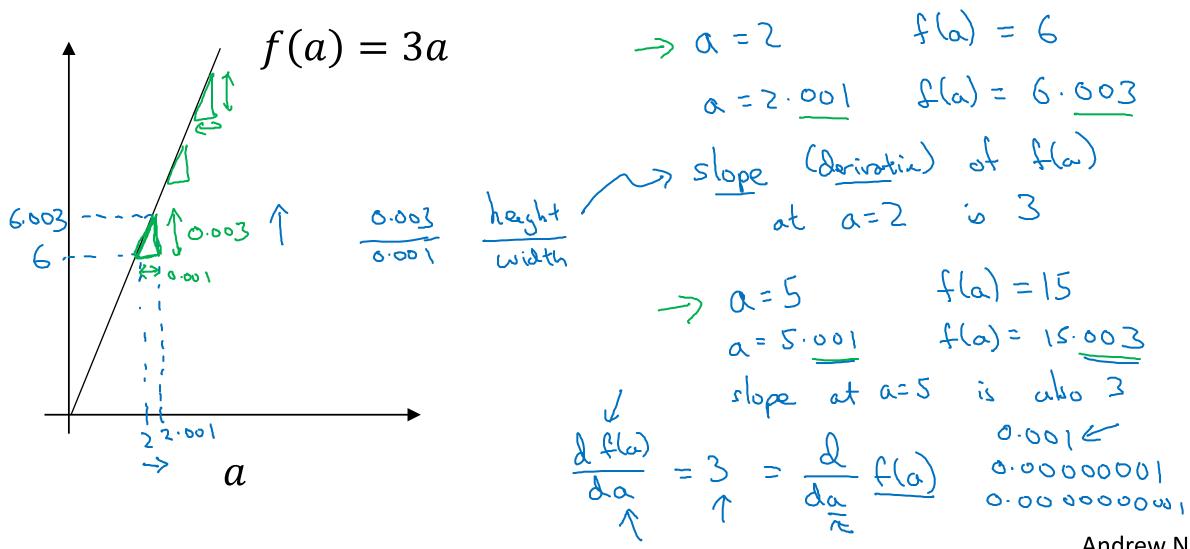
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Basics of Neural Network Programming

Derivatives

Intuition about derivatives



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Basics of Neural Network Programming

More derivatives examples

Intuition about derivatives







More derivative examples

$$f(a) = a^2$$

$$f(\omega) = \alpha^3$$

$$\frac{\lambda}{\lambda a} (a) = 3a^{2}$$
 $3x2^{3} = 12$

$$\sigma = 5.001$$
 $t(r) = 8$

$$Q = 5.001 \quad \text{fm} \approx 0.64312$$

$$Q = 5.001 \quad \text{fm} \approx 0.64362$$



Basics of Neural Network Programming

Computation Graph

Computation Graph

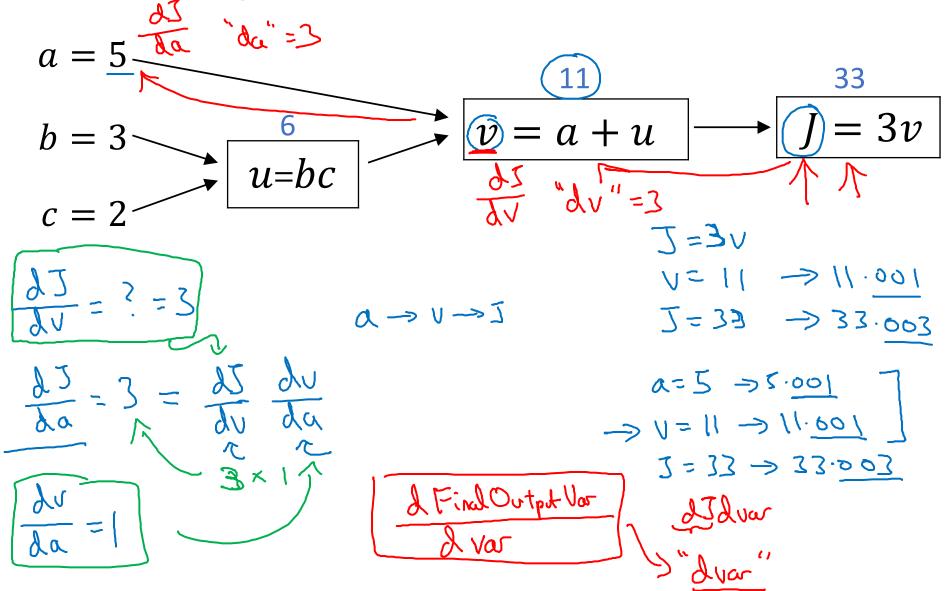
$$J(a,b,c) = 3(a+bc) = 3(5+3\pi^2) = 33$$
 $U = bc$
 $V = atu$
 $J = 3v$
 $V = a+u$
 $J = 3v$
 $V = a+u$
 $J = 3v$

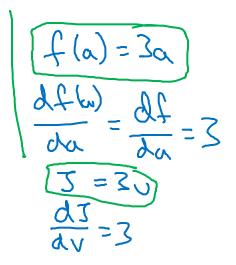


Basics of Neural Network Programming

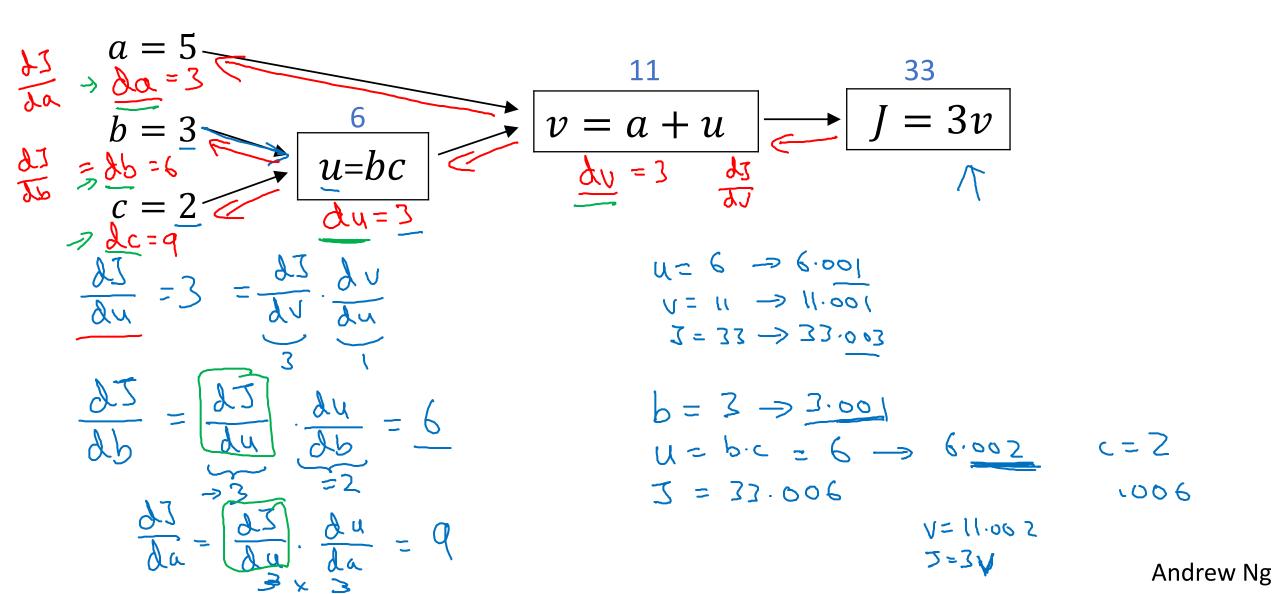
Derivatives with a Computation Graph

Computing derivatives





Computing derivatives





Basics of Neural Network Programming

Logistic Regression Gradient descent

Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

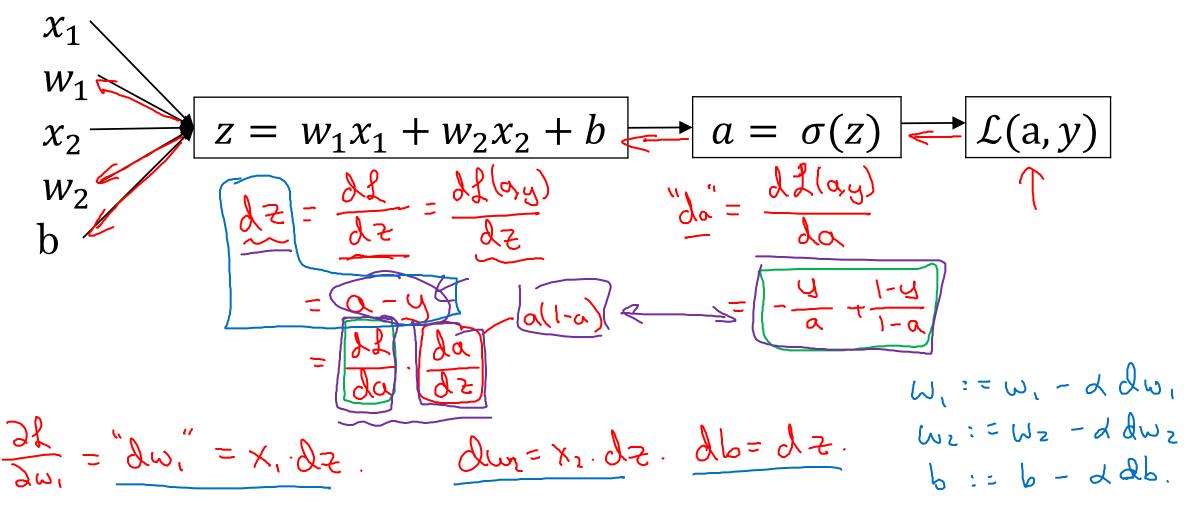
$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

Logistic regression derivatives





Basics of Neural Network Programming

Gradient descent on m examples

Logistic regression on m examples

$$\frac{J(u,b)}{J(u,b)} = \frac{1}{m} \sum_{i=1}^{m} f(a^{(i)}, y^{(i)}) \\
\Rightarrow a^{(i)} = f(x^{(i)}) = G(x^{(i)}, y^{(i)}) \\
\frac{\partial}{\partial u_i} J(u,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial u_i} f(a^{(i)}, y^{(i)}) \\
\frac{\partial u_i}{\partial u_i} - (x^{(i)}, y^{(i)})$$

Logistic regression on m examples

$$J=0$$
; $d\omega_{1}=0$; $d\omega_{2}=0$; $db=0$
 $Z^{(i)}=\omega^{T}x^{(i)}+b$
 $Z^{$

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$
 $\omega_1 := \omega_1 - d d\omega_1$
 $\omega_2 := \omega_2 - \alpha d\omega_2$
 $b := b - d db$

Vectorization