

# Computer vision and machine learning for the material scientist

## Lecture 9. *Object Detection*

Romain Vo



\*slides adapted from [CS231n](#)

# Computer Vision Tasks

## Classification



**DOG**



Classify the image

# Computer Vision Tasks

Classification

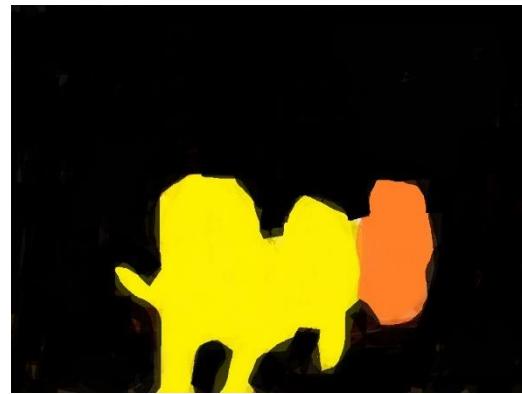


**DOG**



Classify the image

Semantic  
segmentation



**DOG,CAT,BG**



Classify each pixel

# Computer Vision Tasks

Classification

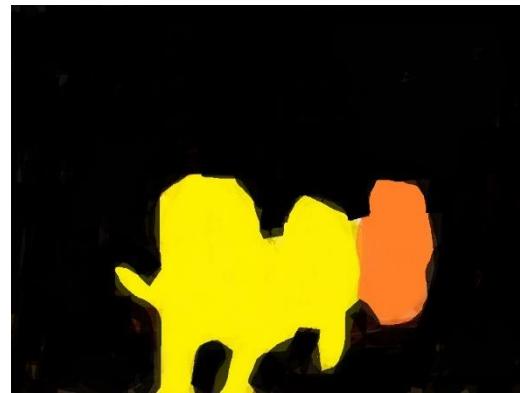


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**DOG,CAT,BG**



Classify each pixel

Instance  
Segmentation



**SMTH, SMTH,  
SMTH**



Segment independent  
instances

Panoptic  
segmentation



**DOG,DOG,CAT**



Segment & Classify independent  
instances

# Computer Vision Tasks

Classification

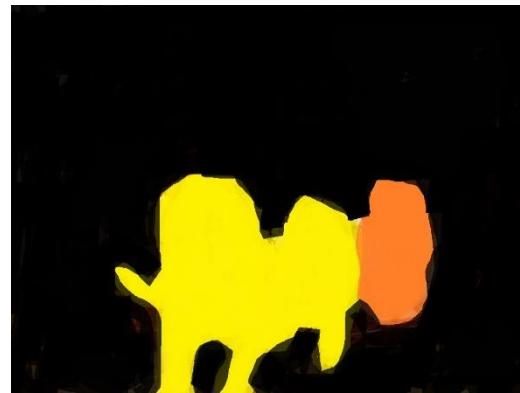


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Classify the image

Semantic  
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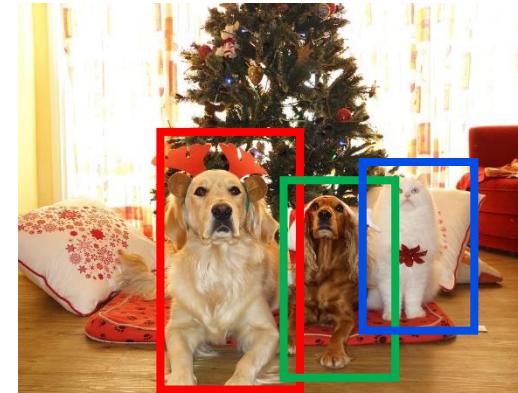


**DOG,CAT,BG**



Classify each pixel

Instance  
Detection



**SMTH, SMTH,  
SMTH**



Detect independent  
instances

Panoptic  
segmentation



**DOG,DOG,CAT**



Segment & Classify independent  
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# Computer Vision Tasks

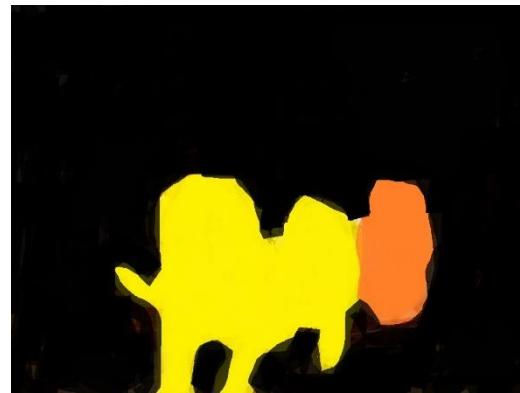
Classification



**DOG**

Classify the image

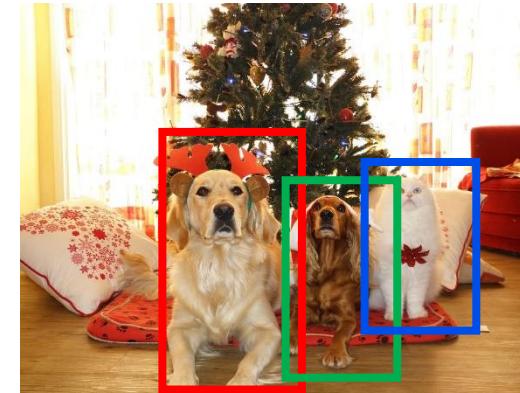
Semantic segmentation



**DOG,CAT,BG**

Classify each pixel

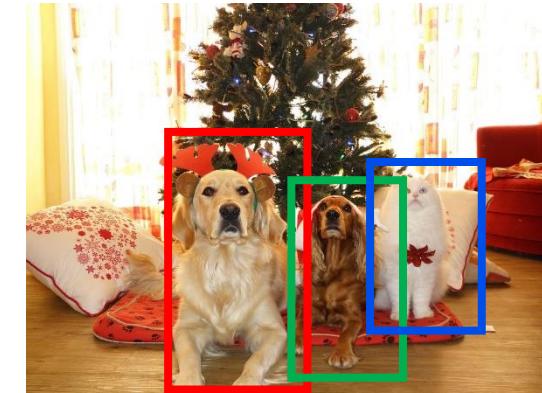
Instance  
Detection



**SMTH, SMTH,  
SMTH**

Detect independent  
instances

Panoptic  
Detection



**DOG,DOG,CAT**

Detect & Classify independent  
instances

# Computer Vision Tasks

Classification

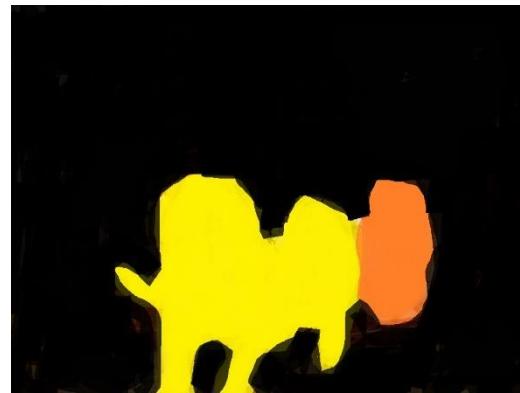


**DOG**



Classify the image

Semantic  
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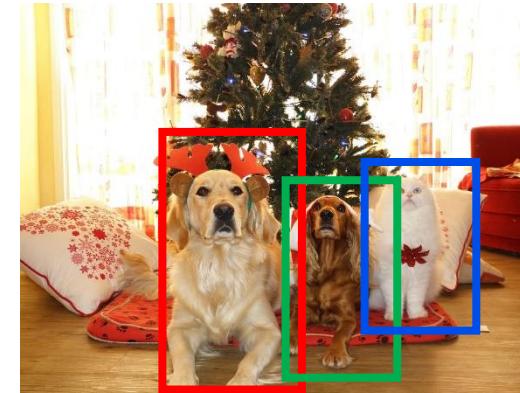


**DOG,CAT,BG**



Classify each pixel

Instance  
Detection

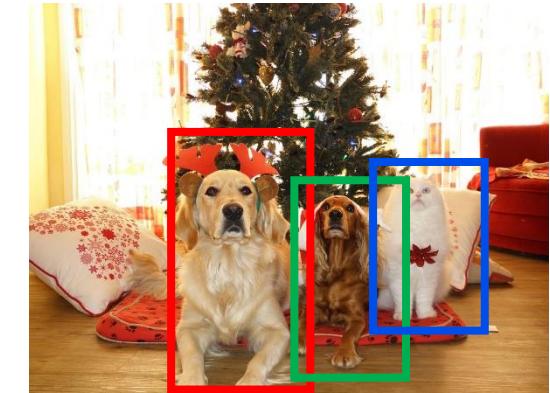


**SMTM, SMTM,  
SMTM**



Detect independent  
instances

Object  
Detection



**DOG,DOG,CAT**



Detect & Classify independent  
instances

# Object Detection

Classification

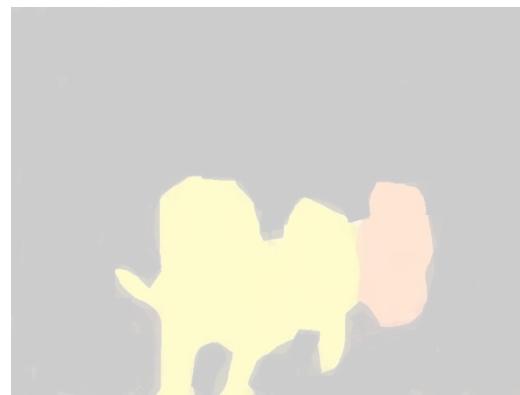


DOG



Classify the image

Semantic  
segmentation

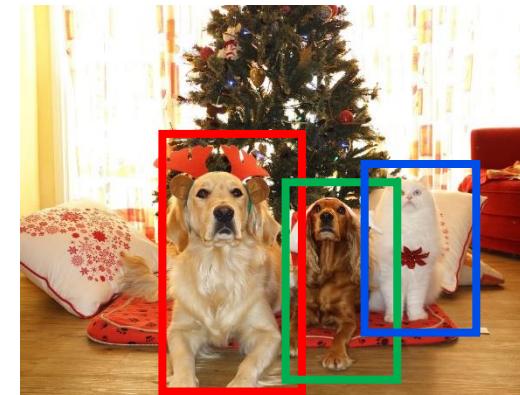


DOG, CAT, BG



Classify each pixel

Instance  
Detection

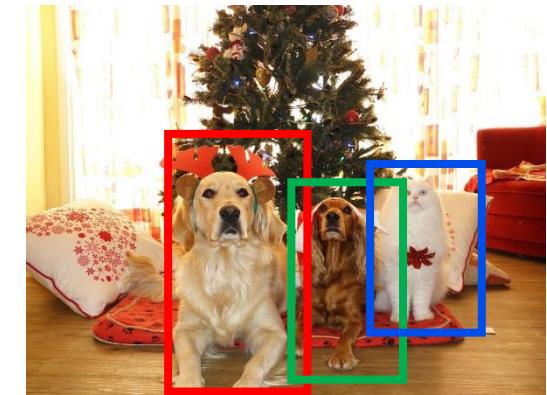


**SMTH, SMTM,  
SMTM**



Detect independent  
instances

Object  
Detection

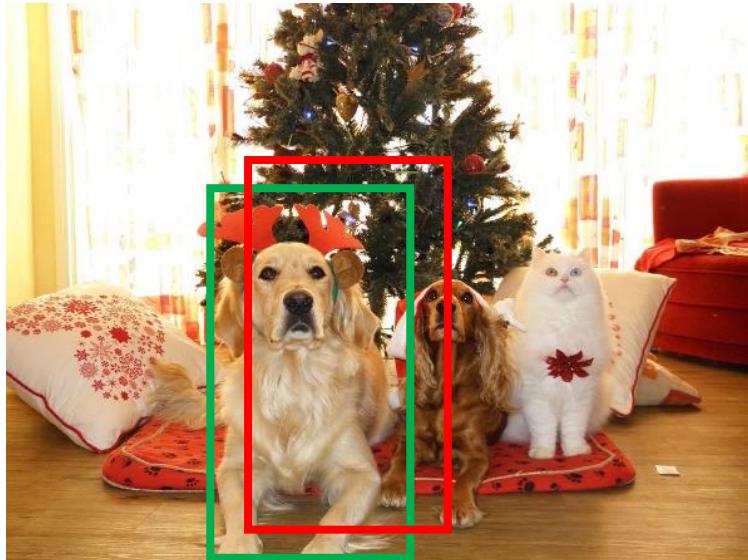


**DOG, DOG, CAT**



Detect & Classify independent  
instances

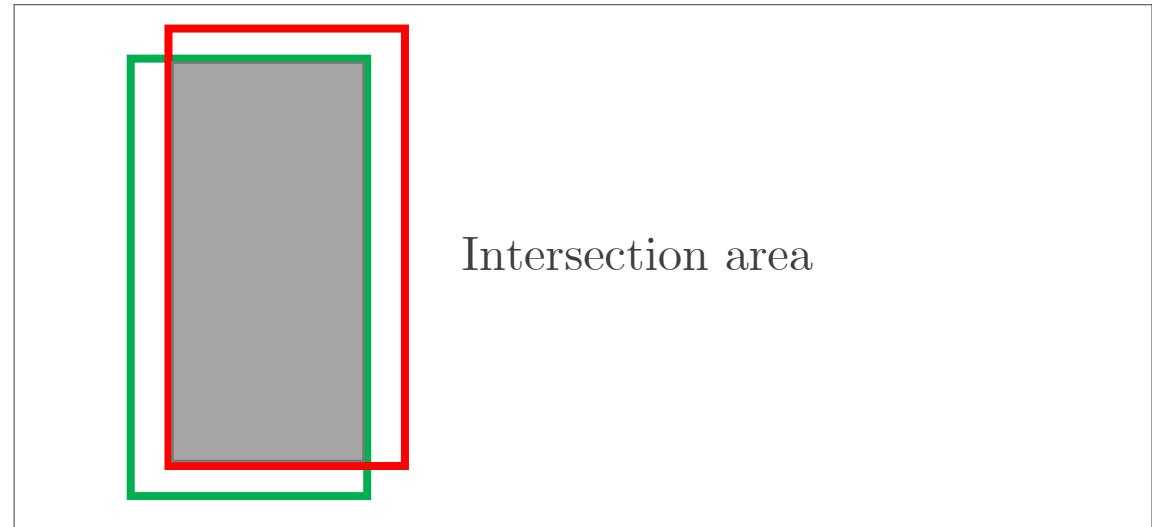
# Object Detection : metrics



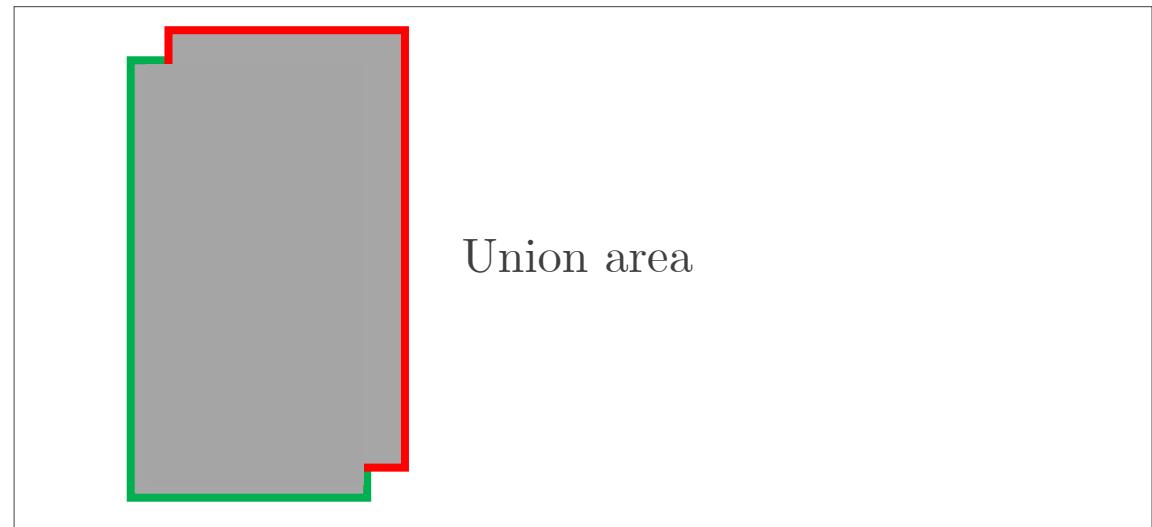
Ground-truth  
bounding box

Predicted  
box

$$IoU = \frac{\text{Intersection}}{\text{Union}}$$

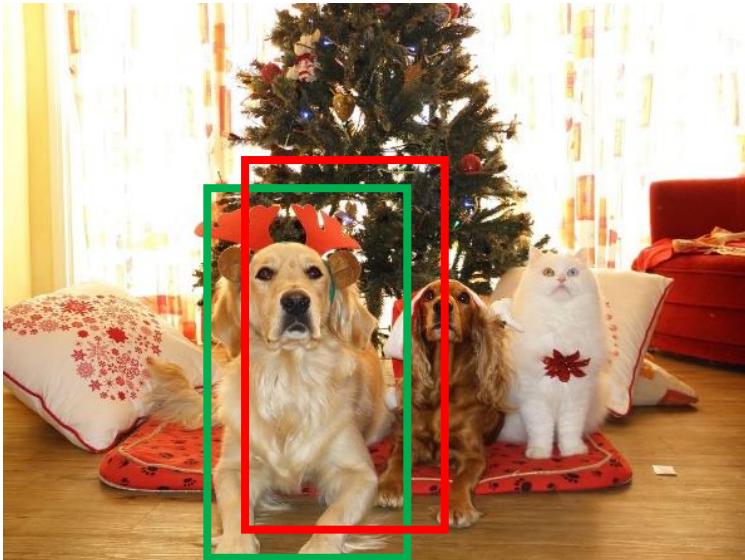


Intersection area



Union area

# Object Detection : metrics



Ground-truth  
bounding box

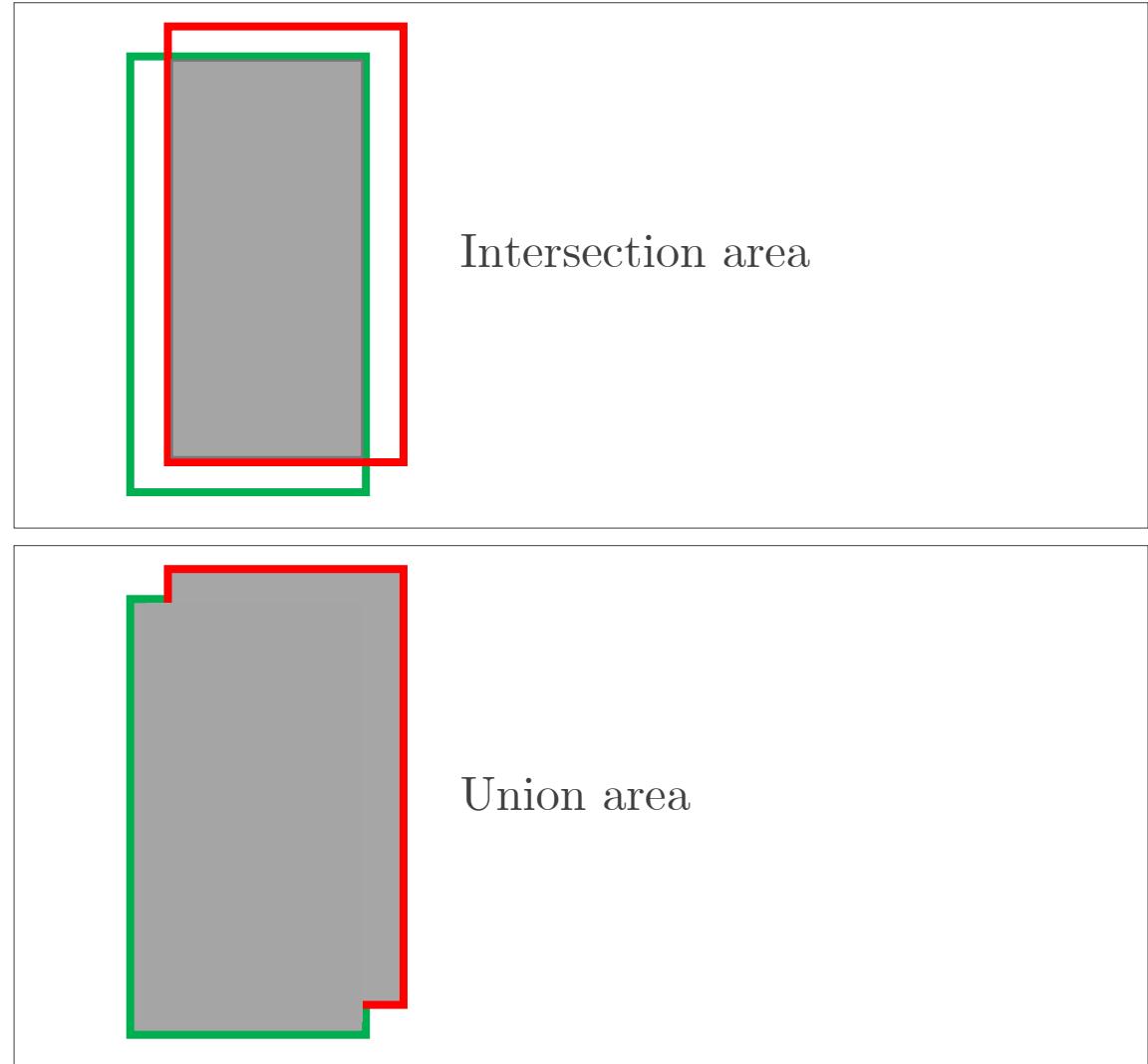
Predicted  
box

$$IoU = \frac{\text{Intersection}}{\text{Union}}$$

A box is correctly detected when  $IoU > t$

$t$  = user-defined threshold

(and when the label associated is correct)



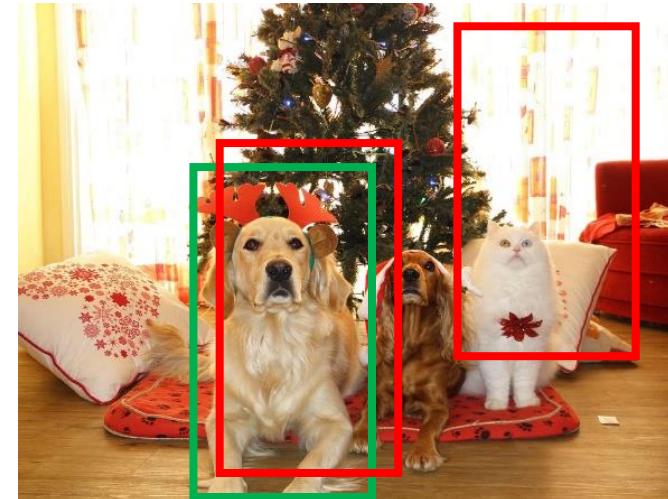
# Object Detection : Precision / Recall



Ground-truth

Prediction

True positive



Ground-truth

Prediction

False positive



Ground-truth

Prediction

False negative

$$\text{Precision: } P = \frac{TP}{TP+FP}$$

# Object Detection : Precision / Recall



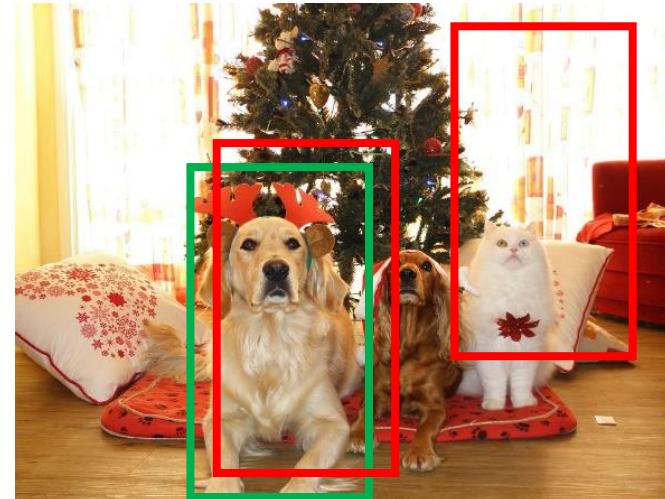
Ground-truth

Prediction

True positive

$$\text{Precision: } P = \frac{TP}{TP+FP}$$

i.e rate of well-detected objects among detected objects



Ground-truth

Prediction

False positive



Ground-truth

Prediction

False negative

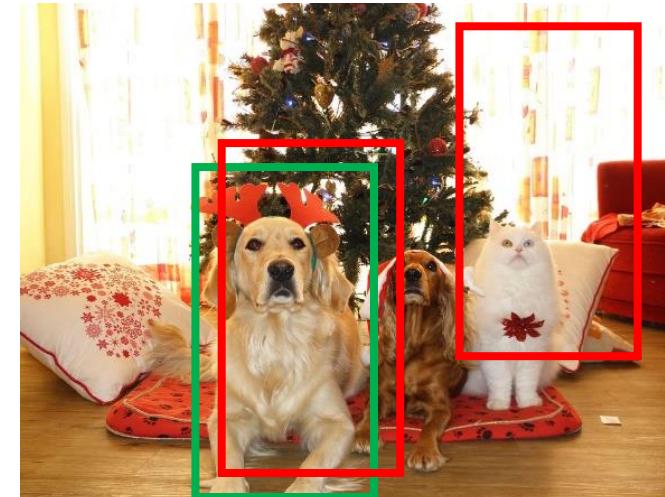
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Ground-truth

Prediction

True positive



Ground-truth

Prediction

False positive



Ground-truth

Prediction

False negative

$$\text{Precision: } P = \frac{TP}{TP+FP}$$

i.e rate of well-detected objects among detected objects

$$\text{Recall: } R = \frac{TP}{TP+FN}$$

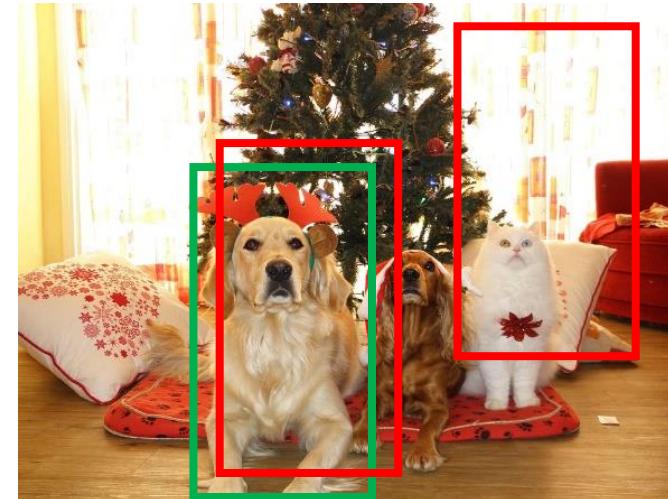
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Ground-truth

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True positive



Ground-truth

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i.e rate of well-detected objects among detected objects

$$\text{Recall: } R = \frac{TP}{TP+FN}$$

i.e rate of well-detected objects among ground-truth objects

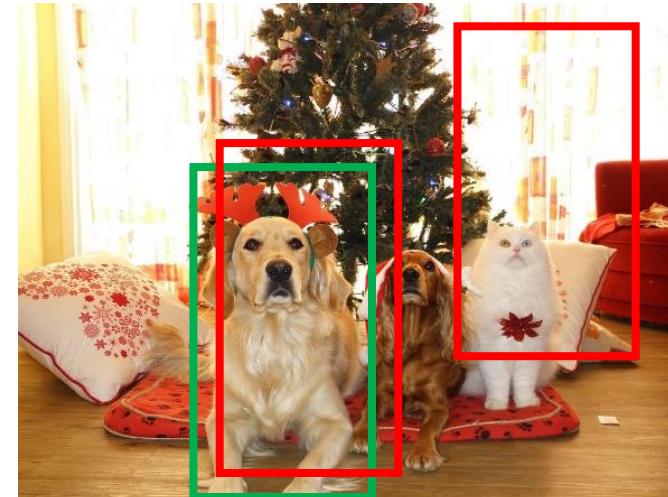
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Prediction

True positive



Ground-truth

Prediction

False positive



Ground-truth

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False negative

$$\text{Precision: } P = \frac{TP}{TP+FP}$$

i.e rate of well-detected objects among detected objects

$$\text{Recall: } R = \frac{TP}{TP+FN}$$

i.e rate of well-detected objects among ground-truth objects

Intuition : if  $\epsilon$  is very low or close to 0, all predictions are considered True Positive, but we increase the number of False Positive (and inversely).

**Precision/Recall trade-off**

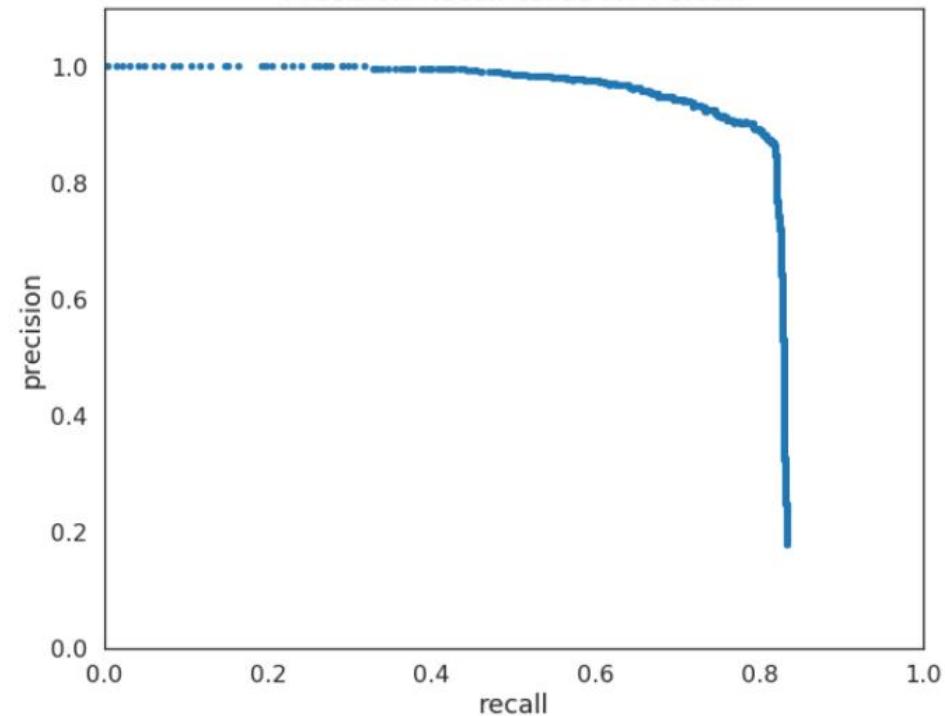
# Object Detection : Precision / Recall curve and mAP

$$\text{Precision: } P = \frac{TP}{TP+FP}$$

$$\text{Recall: } R = \frac{TP}{TP+FN}$$

True Positive if  $IoU > t$

- By varying the confidence threshold  $t$  for the detection, one can obtain so-called precision-recall curve



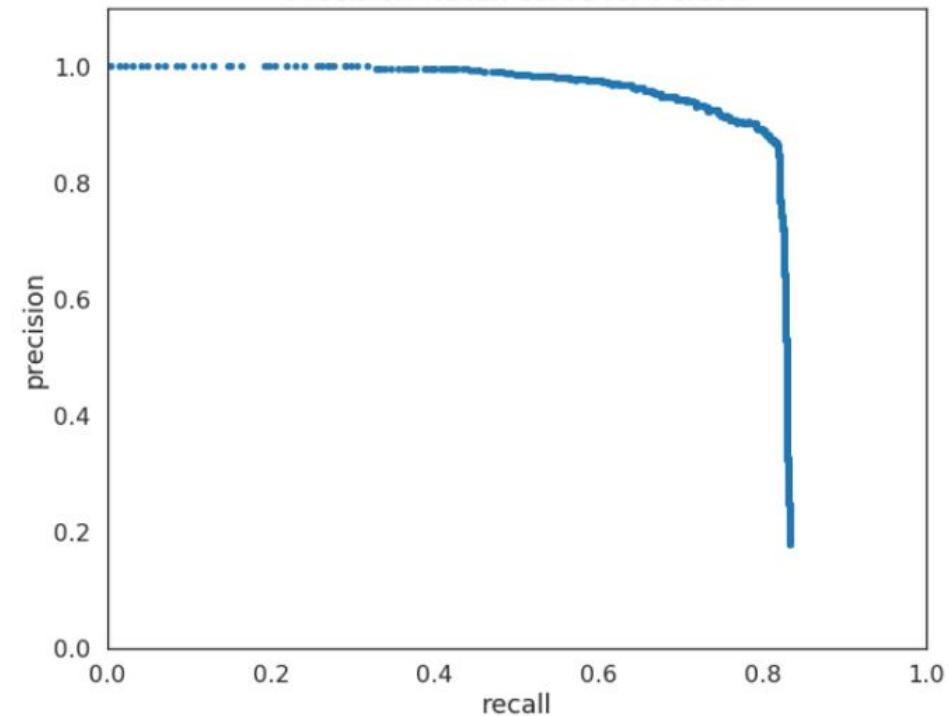
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- The **average precision (AP)** is defined as the area under the curve



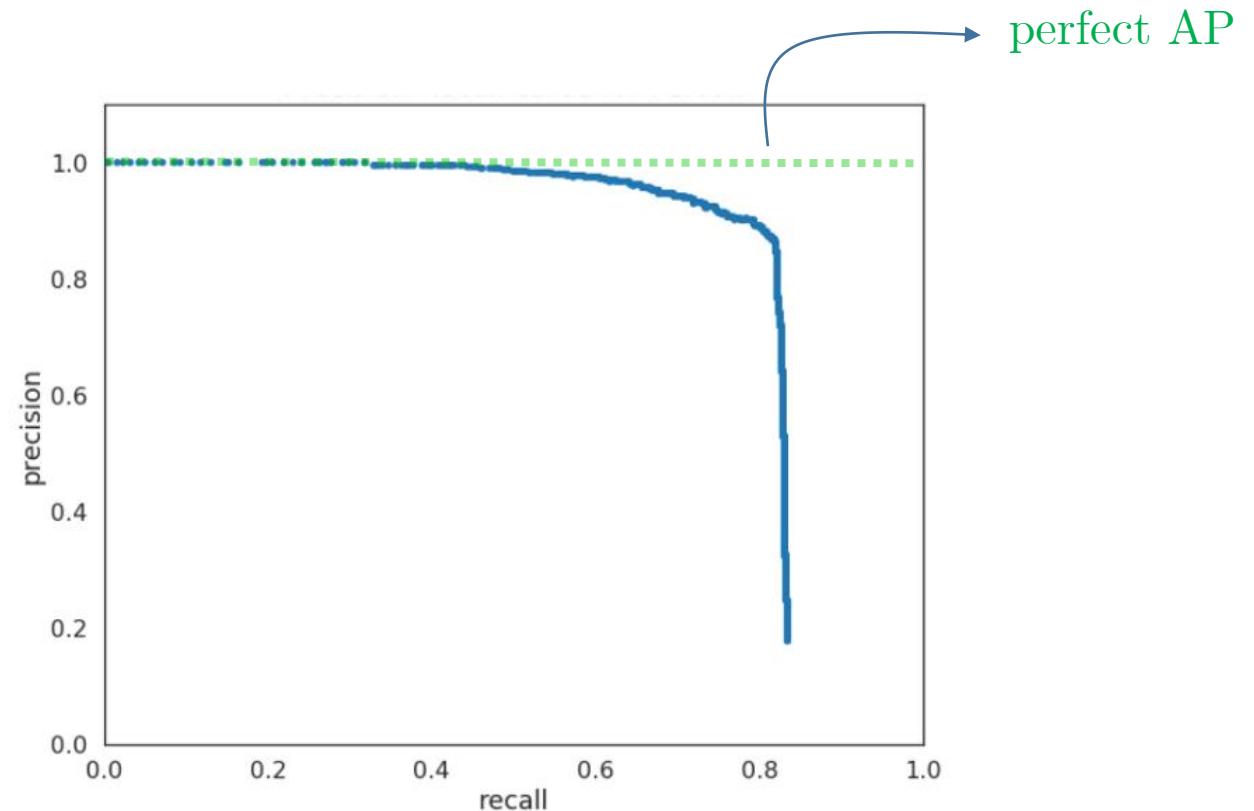
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# Object Detection : Precision / Recall curve and mAP

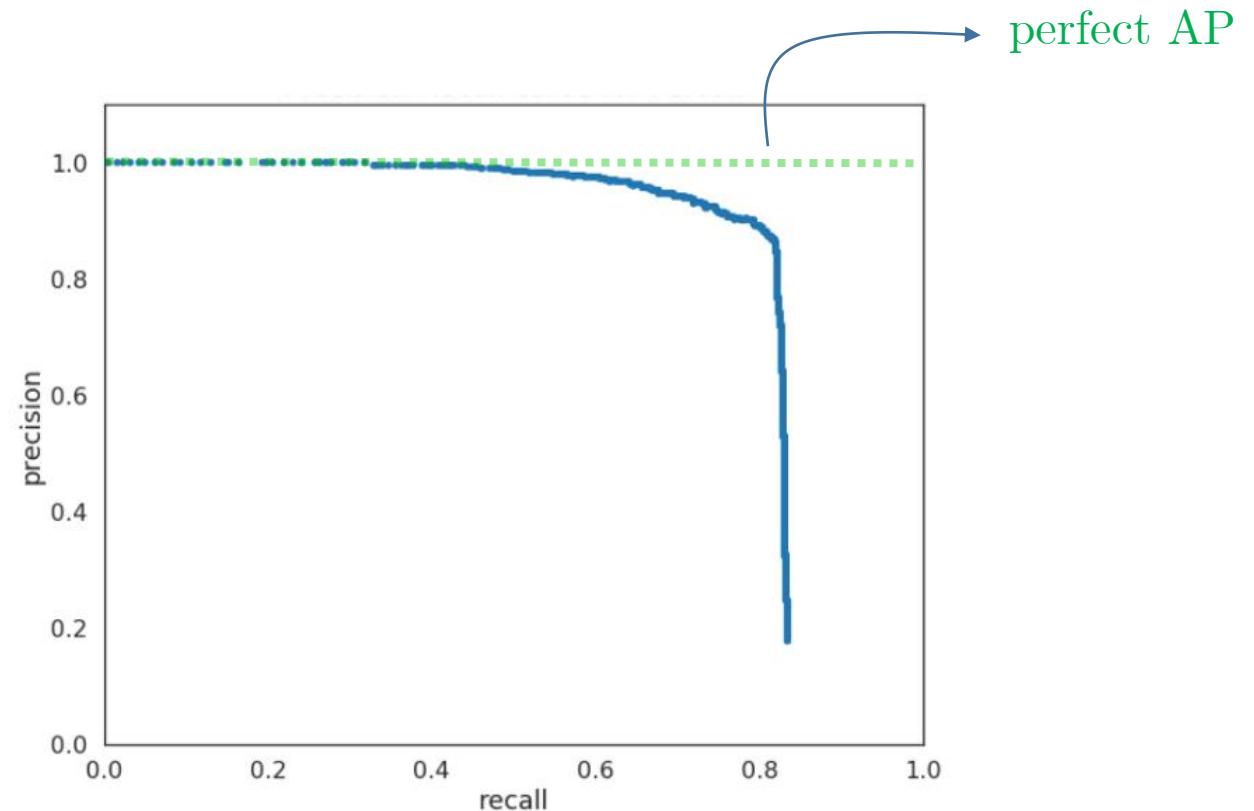
$$\text{Precision: } P = \frac{TP}{TP+FP}$$

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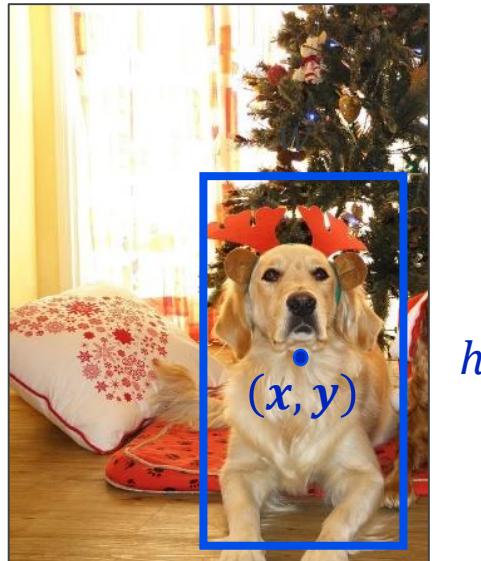
True Positive if  $IoU > t$

- By varying the confidence threshold  $t$  for the detection, one can obtain so-called precision-recall curve
- The **average precision (AP)** is defined as the area under the curve
- We say mean average precision (mAP) because the AP is computed for all object classes

$$\text{mAP} = \text{mean}(AP_{dog}, AP_{cat}, AP_{human})$$



# Object Detection : Box Regression



a box is defined by 4 parameters:

- center  $(x, y)$
- height  $h$
- width  $w$

# Object Detection : Single object

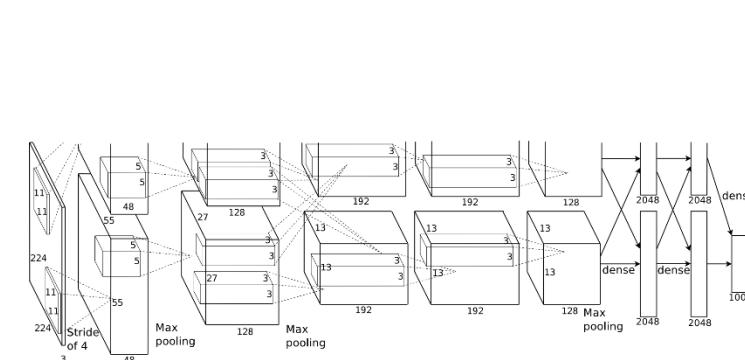


a box is defined by 4 parameters:

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and, we assign a class label  $\underline{c}$  to this box

# Object Detection : Single object



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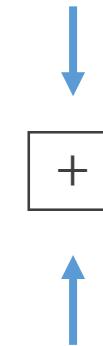
and, we assign a class label  $\underline{c}$  to this box

class vector  $z \in \mathbb{R}^C \rightarrow$  cross-entropy loss



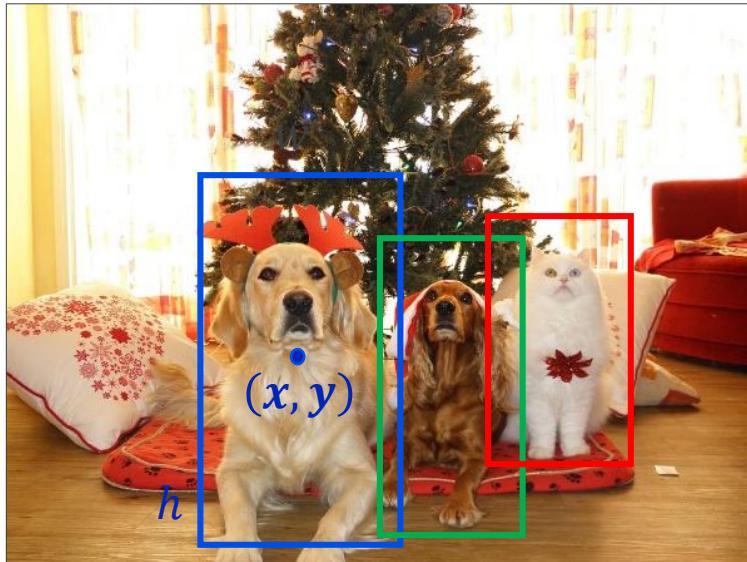
box prediction  
 $(x', y', h', w')$

$\ell_2$  regression loss



Total loss

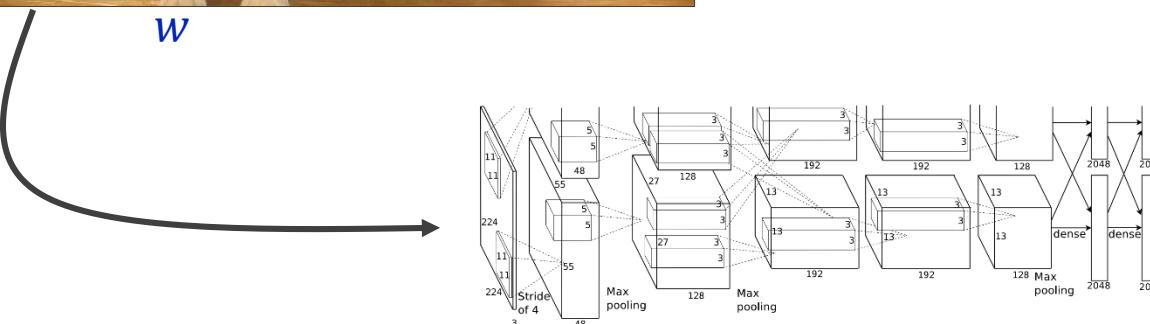
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box prediction  
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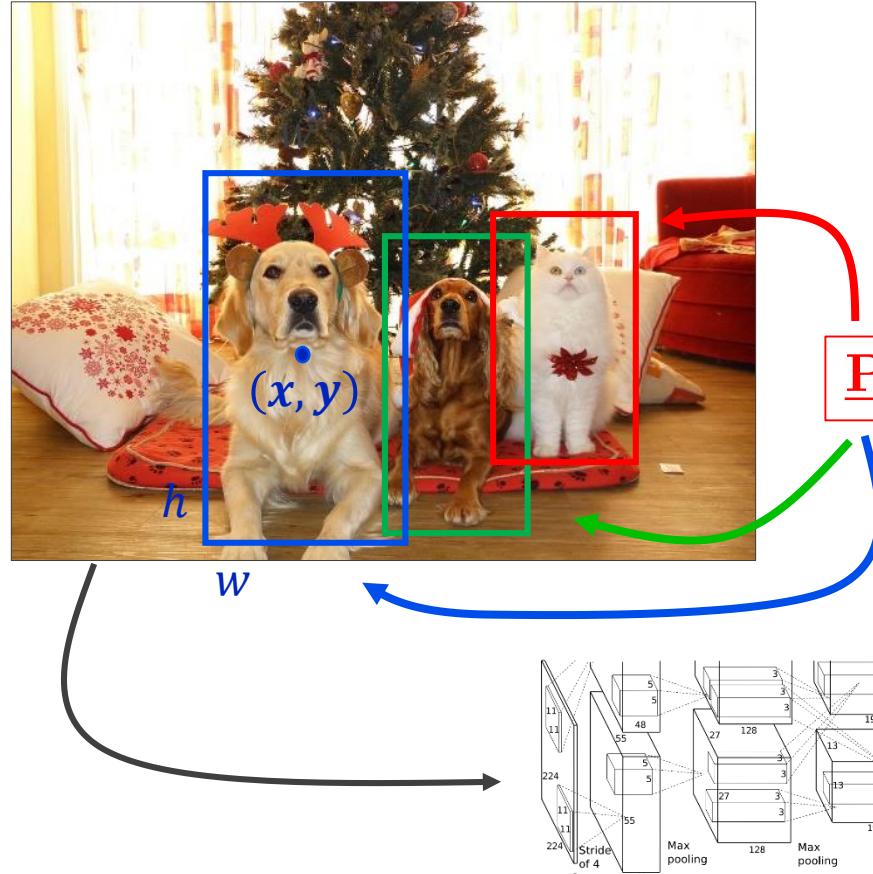
$\ell_2$  regression loss



+

$\rightarrow$  Total loss

# Object Detection : Multi objects

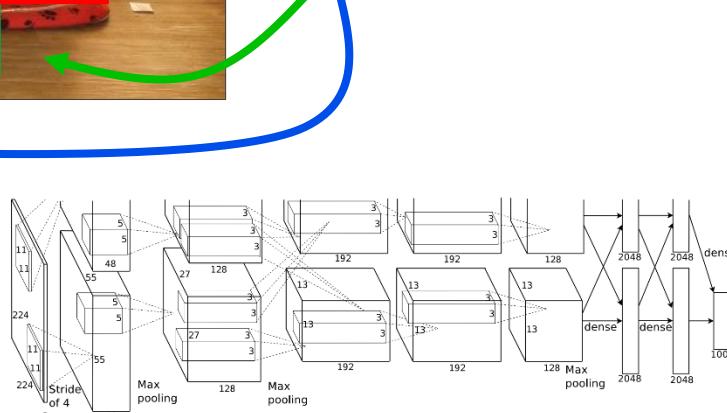


a box is defined by 4 parameters:

- center  $(x, y)$
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- width  $w$

and, we assign a class label  $c$  to this box

**Problem: how to treat a varying number of Objects ??**



class vector  $z \in \mathbb{R}^C \rightarrow$  cross-entropy loss



$\rightarrow$  cross-entropy loss

box prediction  
 $(x', y', h', w')$

$\rightarrow$   $\ell_2$  regression loss



$\rightarrow$  Total loss

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a box is defined by 4 parameters:

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*Naive approach :* sample all possible crops on the image and evaluate the classification/regression network

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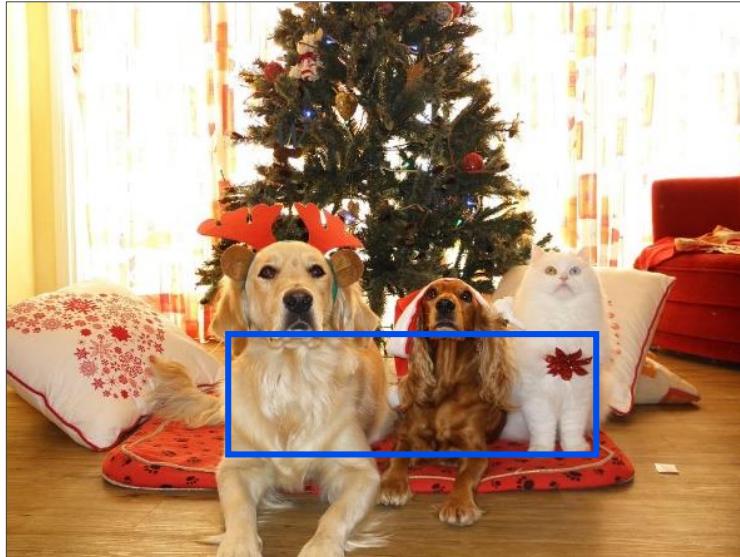
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# Object Detection : Region proposals



a box is defined by 4 parameters:

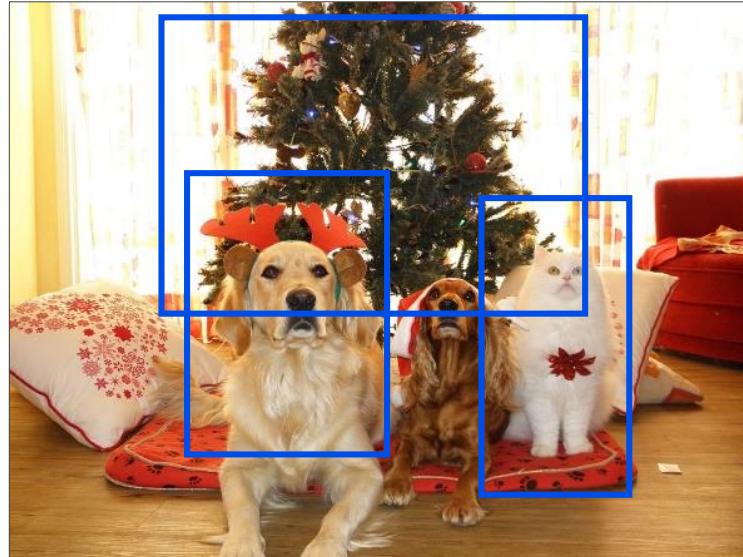
- center  $(x, y)$
- height  $h$
- width  $w$

and, we assign a class label  $\underline{c}$  to this box

*Region of Interest (RoI) proposal approach :* use SOTA algorithms (in 2015) to evaluate objectness of the image and propose a reduced set of patches

2012, Alexe et al, “Measuring the objectness of image windows”  
2013, Uijlings et al, “Selective Search for Object Recognition”  
2014, Zitnick and Dollar, “Edge boxes: Locating object proposals from edges”

# Object Detection : Region of Interest proposals



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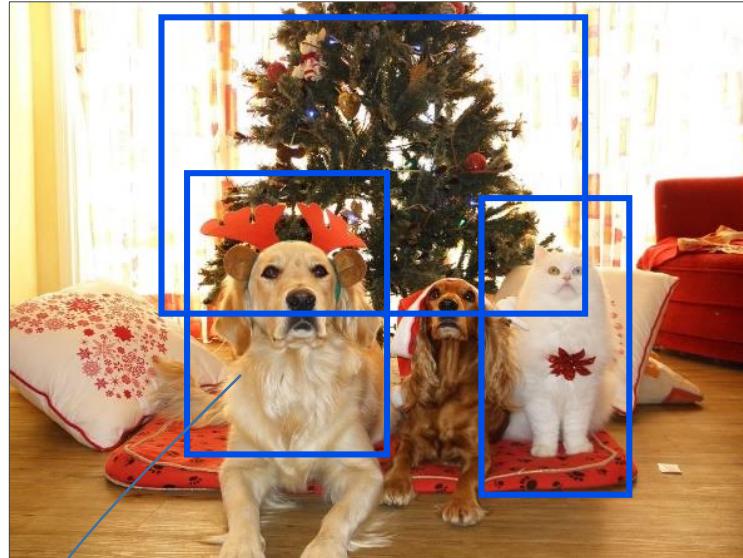
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# Object Detection : Region of Interest proposals

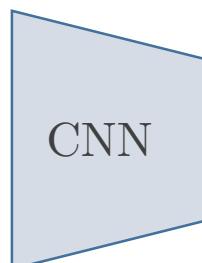


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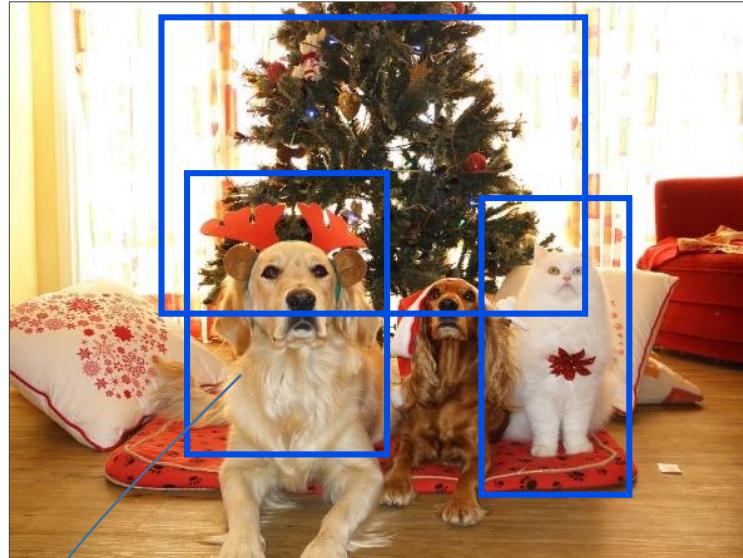


class vector  $z \in \mathbb{R}^c$

box correction  $(x', y', h', w')$

2012, Alexe et al, “Measuring the objectness of image windows”  
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# Object Detection : Region of Interest proposals

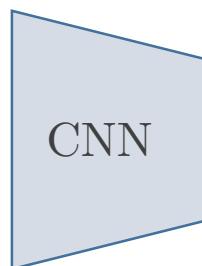


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class vector  $z \in \mathbb{R}^c$

box correction  $(x', y', h', w')$

**Problem: still super slow !**

*Need to run a CNN a few 1000 times per image*

2012, Alexe et al, "Measuring the objectness of image windows"

2013, Uijlings et al, "Selective Search for Object Recognition"

2014, Zitnick and Dollar, "Edge boxes: Locating object proposals from edges"

# Object Detection : From R-CNN to RetinaNet

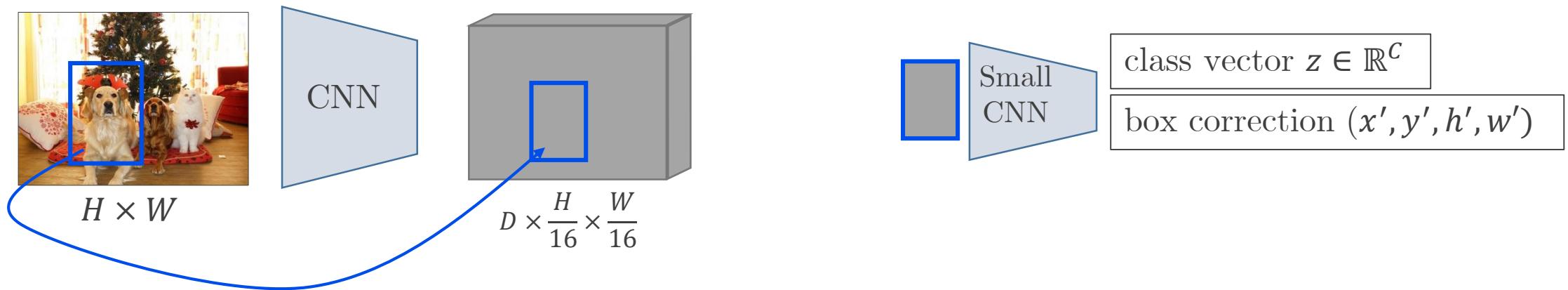
1. R-CNN to Fast R-CNN
2. Fast R-CNN to Faster R-CNN
3. Faster R-CNN to RetinaNet

# Object Detection : RoI pooling

1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression

# Object Detection : From R-CNN to RetinaNet

1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression



Project ROI proposal onto feature map : RoI pooling

# Object Detection : Region Proposal Network

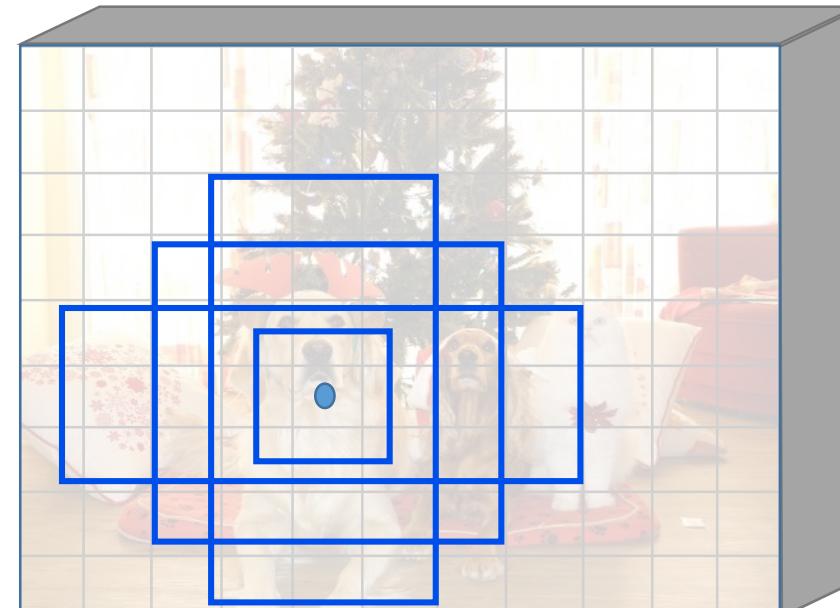
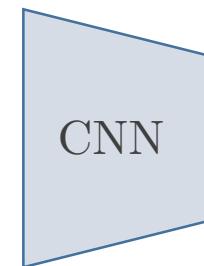
1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression
2. From Fast R-CNN to Faster R-CNN : Use a Region Proposal Network (instead of handcrafted algorithm) to propose RoI

# Object Detection : Anchor-based

1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression
2. From Fast R-CNN to Faster R-CNN : Use a Region Proposal Network (instead of handcrafted algorithm) to propose ROI



$H \times W$



$$D \times \frac{H}{16} \times \frac{W}{16}$$

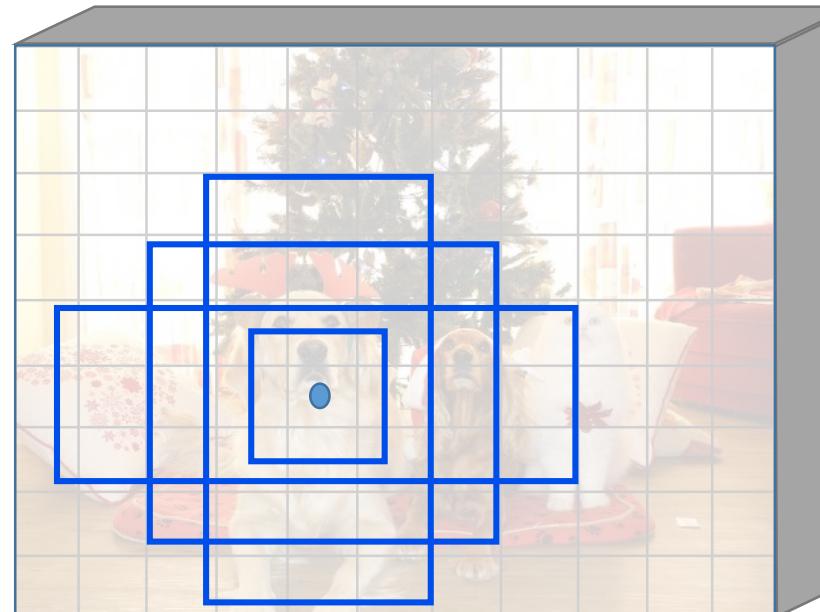
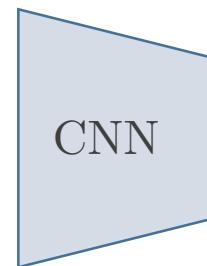
Associate K anchor boxes  
of different size/scale at  
each point

# Object Detection : Anchor-based

1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression
2. From Fast R-CNN to Faster R-CNN : Use a Region Proposal Network (instead of handcrafted algorithm) to propose ROI



$H \times W$



$D \times \frac{H}{16} \times \frac{W}{16}$



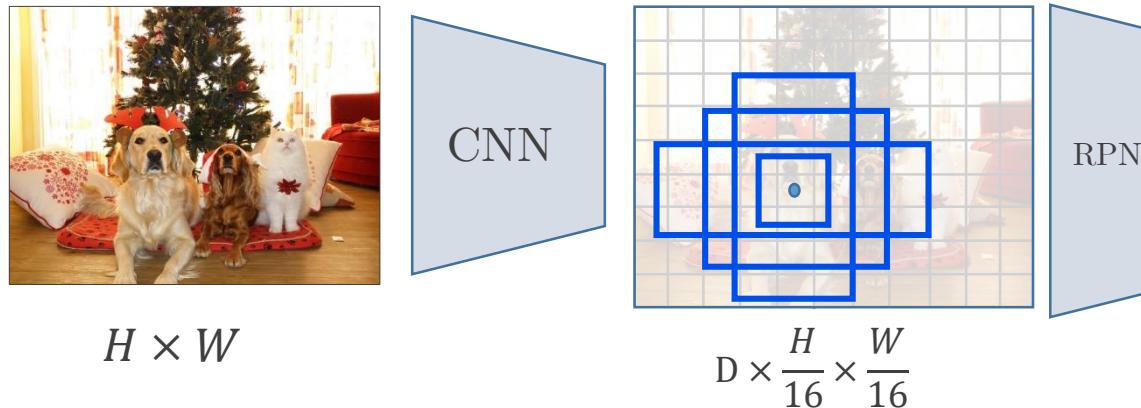
Associate K anchor boxes  
of different size/scale at  
each point

*Objectness ?*  
 $K \times \frac{H}{16} \times \frac{W}{16}$

*Box correction*  
 $4K \times \frac{H}{16} \times \frac{W}{16}$

# Object Detection : Anchor-based RPN

1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression
2. From Fast R-CNN to Faster R-CNN : Use a Region Proposal Network (instead of handcrafted algorithm) to propose RoI



*Objectness ?*

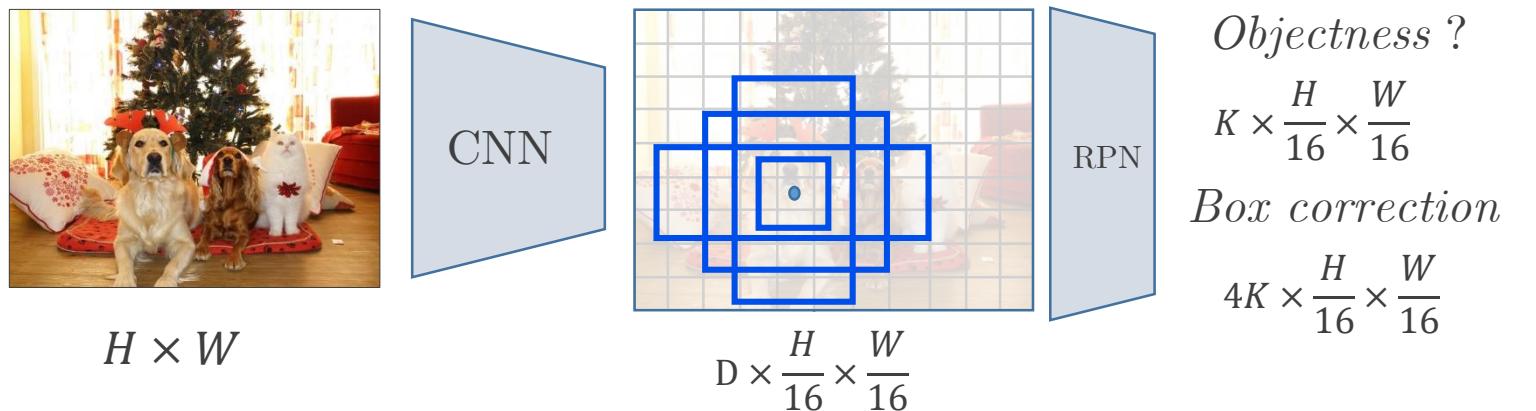
$$K \times \frac{H}{16} \times \frac{W}{16}$$

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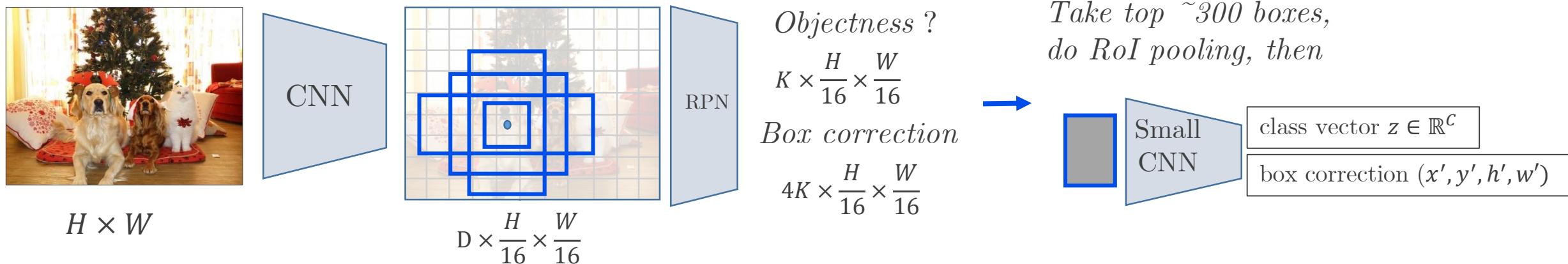
*Box correction*

$$4K \times \frac{H}{16} \times \frac{W}{16}$$

*Take top  $\sim 300$  boxes,  
do ROI pooling, then*

# Object Detection : Anchor-based RPN

1. R-CNN to Fast R-CNN : run a CNN one time on the image, and extract the patches from the feature map not the image. Then small CNN for classification and box regression
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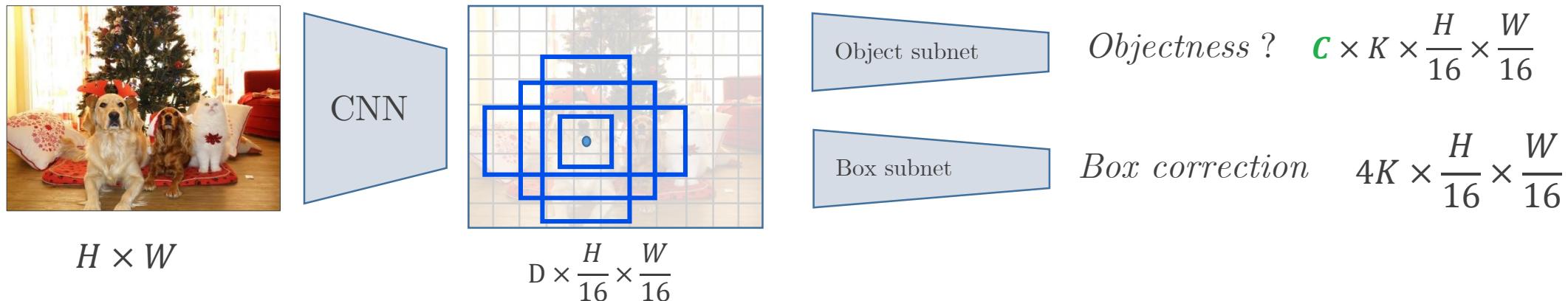


# Object Detection : RetinaNat – One stage detector

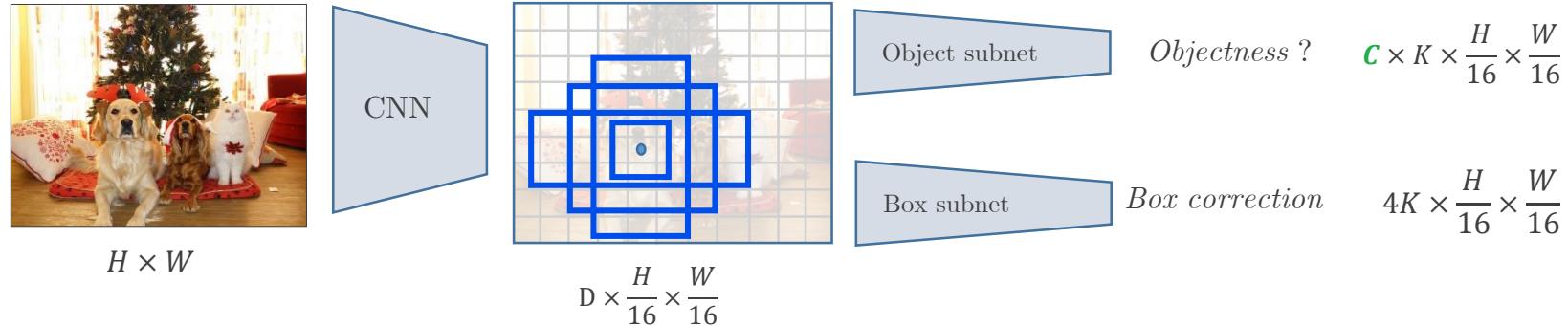
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# Object Detection : RetinaNat – One stage detector

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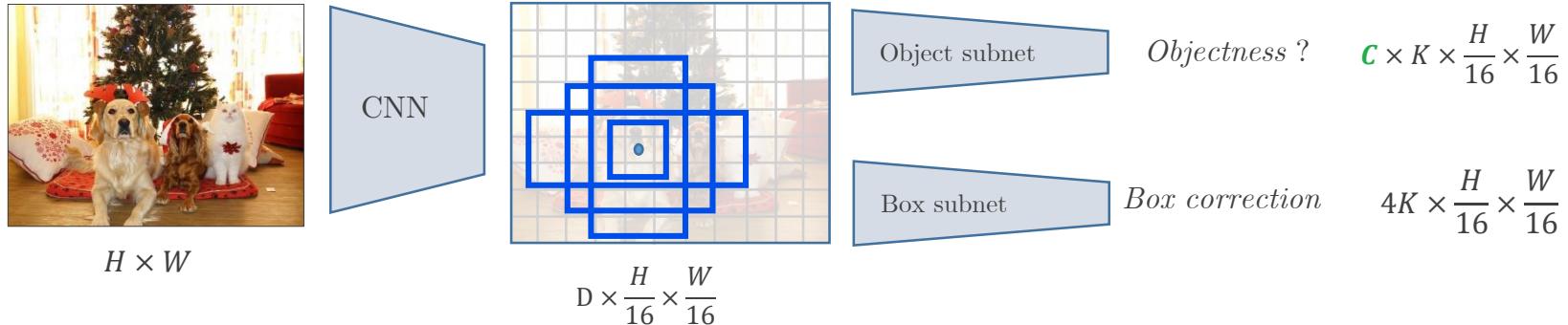
# Object Detection : Non-Maximum Suppresion



Skipped a lot of modelisation details :

- NMS or *non-maximum suppression*

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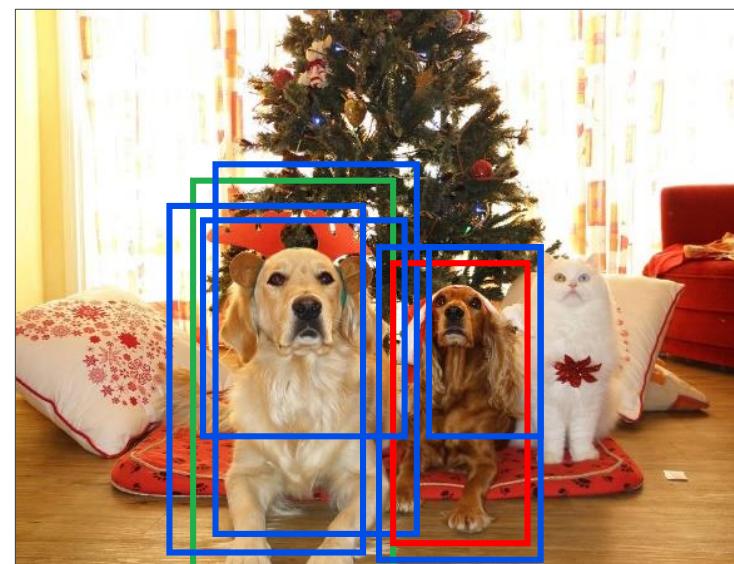
---

**Algorithm 1** Non-Max Suppression

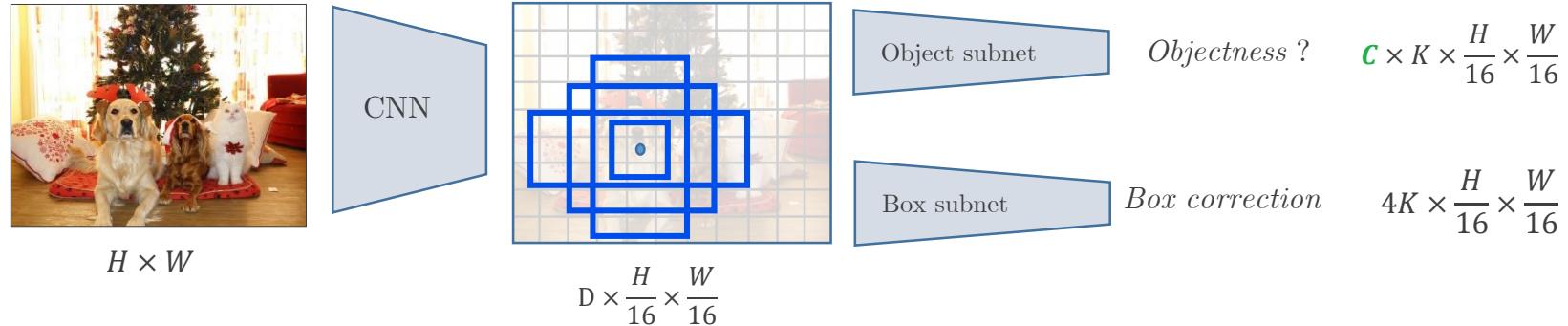
---

```
1: procedure NMS( $B, c$ )
2:    $B_{nms} \leftarrow \emptyset$ 
3:   for  $b_i \in B$  do
4:      $discard \leftarrow \text{False}$ 
5:     for  $b_j \in B$  do
6:       if  $\text{IoU}(b_i, b_j) > \lambda_{nms}$  then
7:         if  $\text{score}(c, b_j) > \text{score}(c, b_i)$  then
8:            $discard \leftarrow \text{True}$ 
9:         if not  $discard$  then
10:           $B_{nms} \leftarrow B_{nms} \cup b_i$ 
11:   return  $B_{nms}$ 
```

---

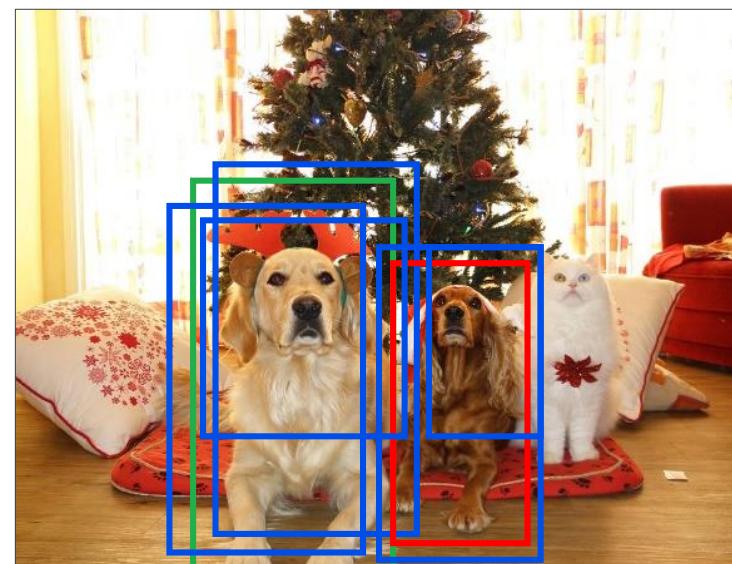


# Object Detection : Non-Maximum Suppresion

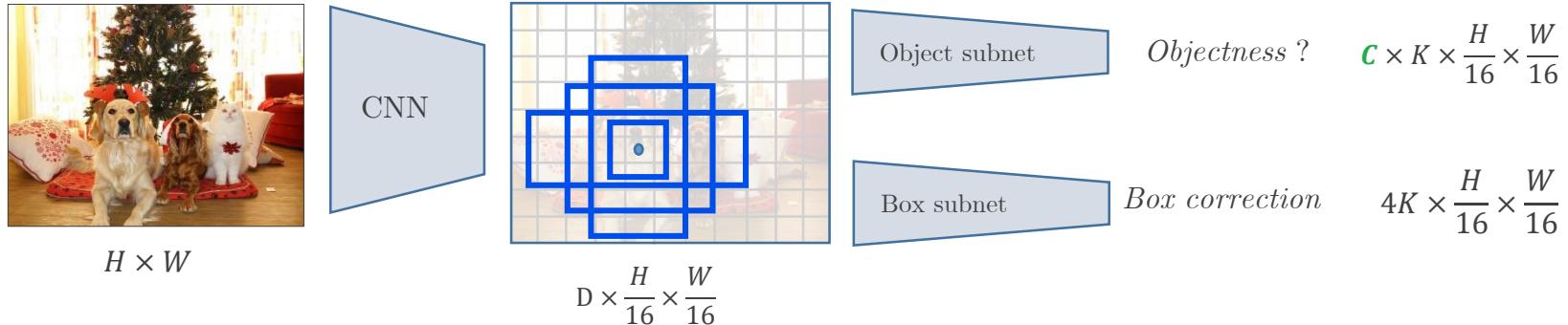


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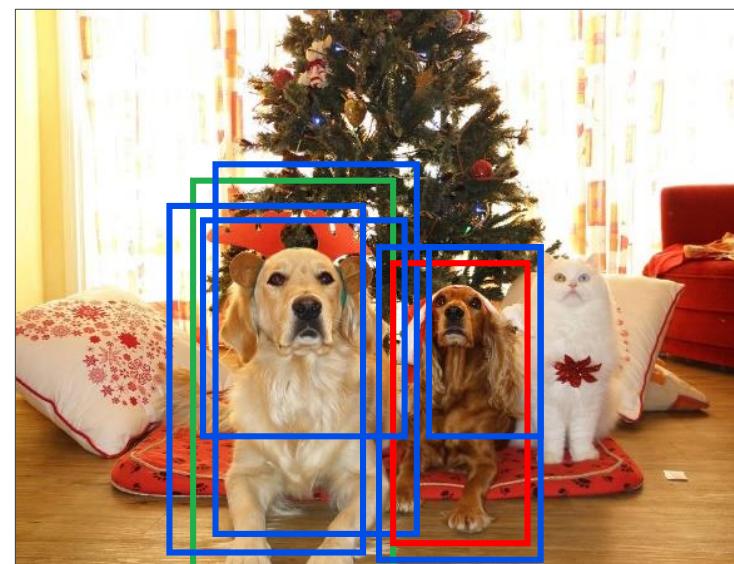
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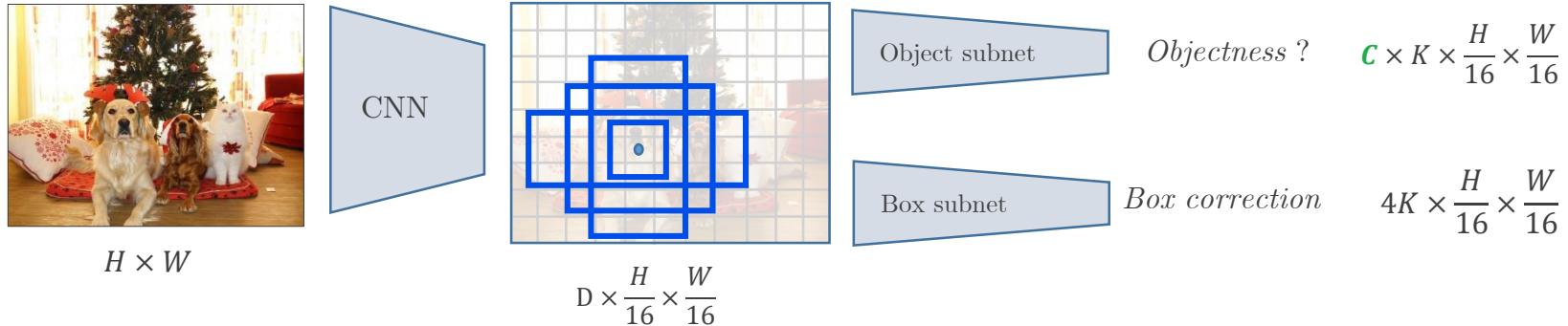
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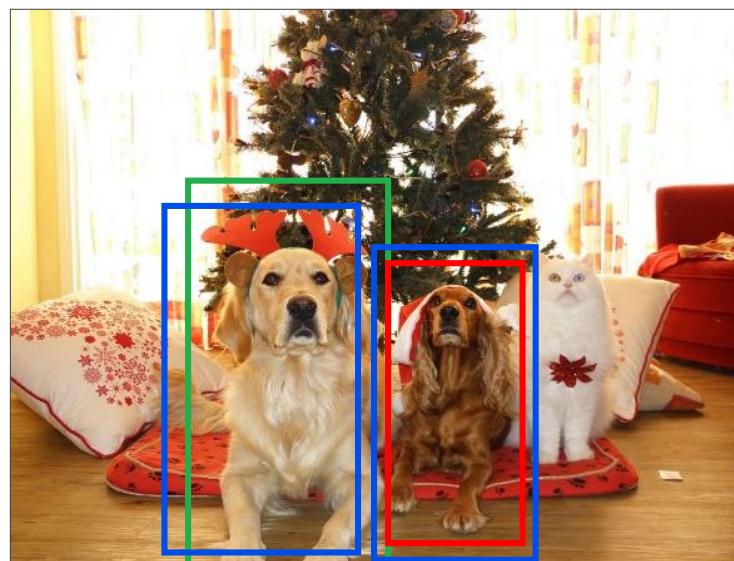
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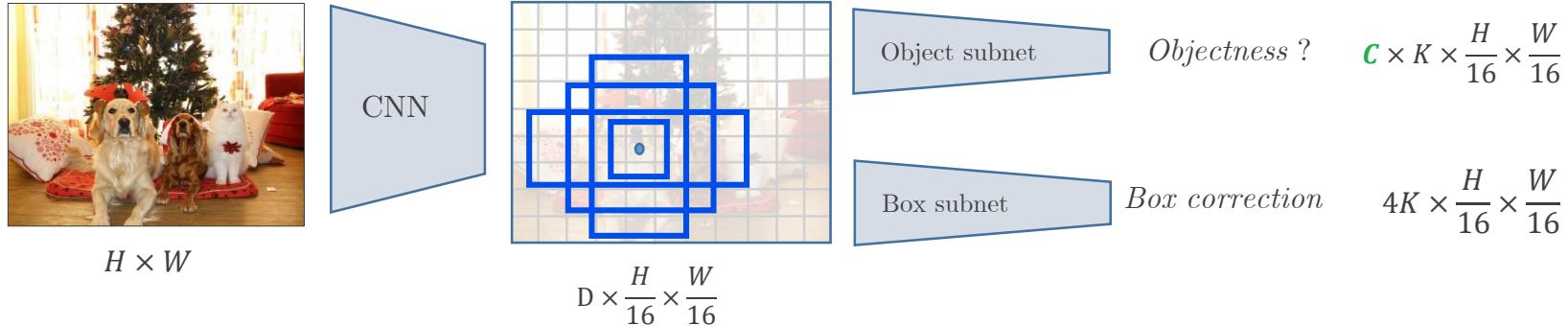
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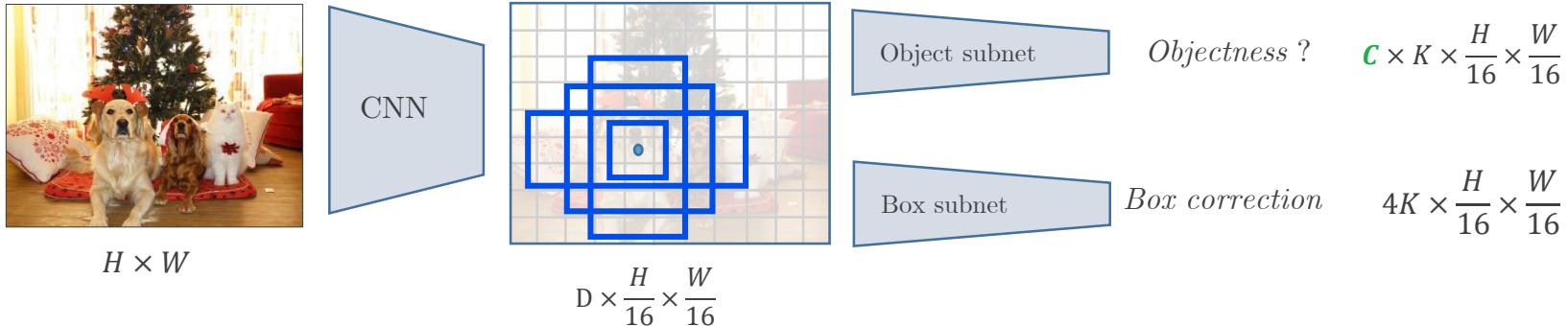
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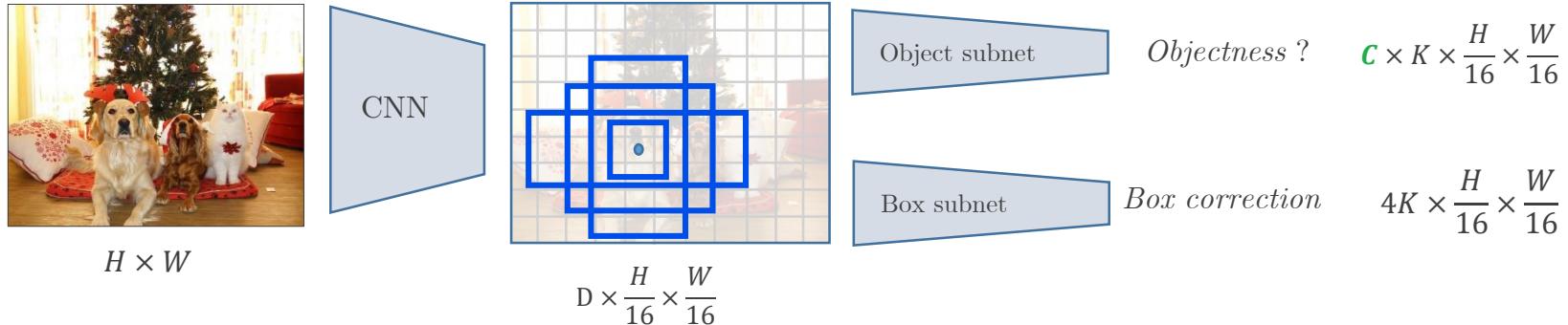
# Object Detection : Non-Maximum Suppresion



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- Solve *imbalance* between negative and positive anchors,  
*i.e* among  $K \sim 50000$  anchors most of them do not bind  
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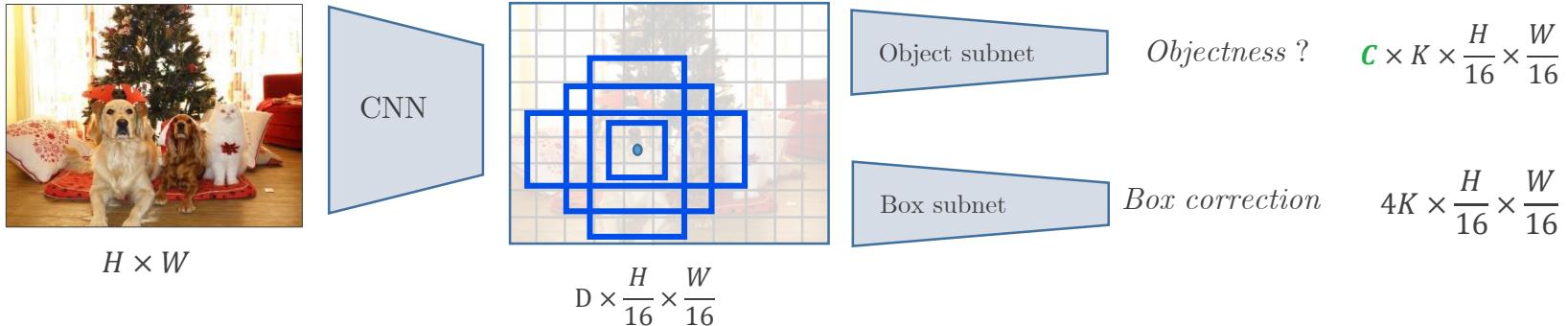
# Object Detection : Foreground-Background imbalance



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  - Sampling heuristics: fixed foreground-background  
ratio of anchors, online hard example mining

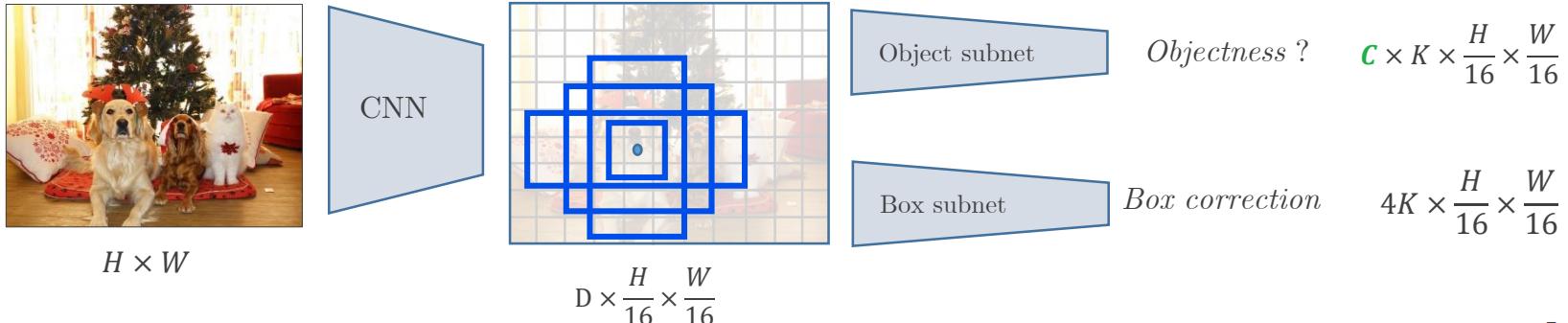
# Object Detection : Focal loss



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# Object Detection : Focal loss



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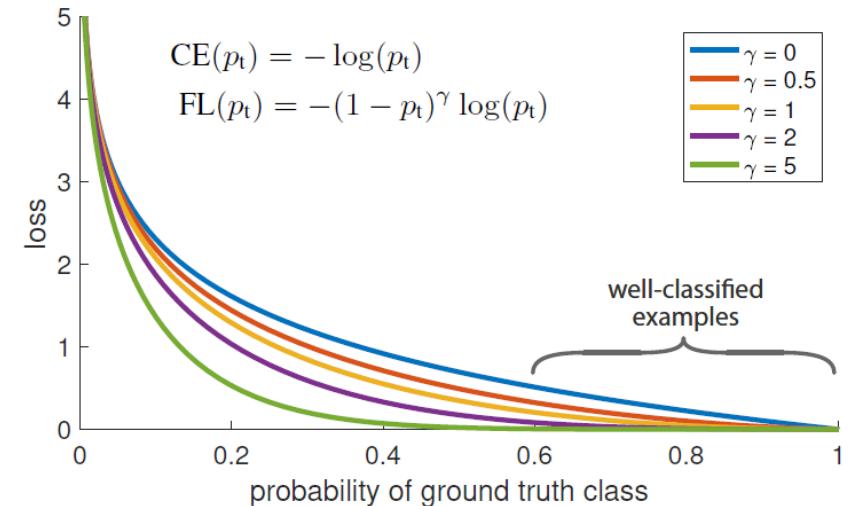


Figure 1. We propose a novel loss we term the *Focal Loss* that adds a factor  $(1 - p_t)^\gamma$  to the standard cross entropy criterion. Setting  $\gamma > 0$  reduces the relative loss for well-classified examples ( $p_t > .5$ ), putting more focus on hard, misclassified examples. As our experiments will demonstrate, the proposed focal loss enables training highly accurate dense object detectors in the presence of vast numbers of easy background examples.

# Object Detection : Other architectures

Subsequent anchor-based methods:

- 2017, He et al, Mask R-CNN → perform instance and semantic segmentation
- 2020, Bochkovskiy et al, YOLOv4: Optimal Speed and Accuracy of Object Detection
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Anchor-Free detectors : avoid cumbersome modelisation, NMS, etc..

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## Transformers-based:

- 2020, Carion et al, DETR: End-to-End Object Detection with Transformers
- 2023, Zong et al, DETRs with Collaborative Hybrid Assignments Training

Thank you for your  
attention



\*slides adapted from [CS231n](#)