

Feature Transformation:

1. Normalization
2. Standardization
3. MaxAbsScaler
4. RobustScaler
5. Log Transformation

See in image

Feature Transformation

Data:

Price
110
105
115
120
110
130
150
100
105

⇒

① Normalization:

$$X_{\text{new}} = \frac{X_i - \min(x)}{\max(x) - \min(x)}$$

if, $X_i = 110$ when

$$\min(x) = 100$$

$$\max(x) = 150$$

$$X_{110} = \frac{110 - 100}{150 - 100}$$

$$= \frac{10}{50}$$

$$= 0.2$$

$$X_{105} = \frac{105 - 100}{150 - 100}$$

$$= \frac{05}{50}$$

$$= 0.1$$

Similarly,

.....

Normal Price
0.2
0.1
0.3
0.4
0.2
0.6
1.0
0.0
0.1

② Standardization:

$$X_{\text{new}} = \frac{X_i - X_{\text{mean}}}{\text{Standard Deviation}(\sigma)}$$

$$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{N}}$$

if, $X_i = 110$,

$$\mu (X_{\text{mean}}) = 116.11$$

$$N = 9 \text{ (Data NO.)}$$

$$\sigma = \sqrt{\frac{\sum (110 - 116.11)^2 + (105 - 116.11)^2 + \dots}{9}}$$

$$= 14.7$$

$$\therefore X_{110} = \frac{110 - 116.11}{14.7} = -0.416$$

Standard Price
-0.416
-0.757
-0.075
-0.264
-0.416
0.946
2.308
-1.097
-0.757

③ MaxAbsScaler:

$$X_{\text{New}} = \frac{X_i}{\text{absolute } X_{\text{max}}}$$

$$X_{110} = \frac{110}{150} \quad \left| \quad X_{105} = \frac{105}{150} \right.$$

$$= 0.73 \quad \quad \quad = 0.7$$

$$X_{115} = \frac{115}{150} = 0.76 \quad \left| \quad X_{120} = \frac{120}{150} \right.$$

$$= 0.8$$

MaxAbs Price
0.733
0.700
0.766
0.800
0.733
0.866
1.000
0.666
0.700

④ RobustScaler:

Price
110
105
115
120
110
130
150
100
105

$$X_{\text{scale}} = \frac{X_i - X_{\text{med}}}{X_{75} - X_{25}}$$

$$\text{IQR} = X_{75} - X_{25}$$

$$= 125 - 110 = 15$$

$$X_{\text{med}} = 110$$

$$X_{\text{New}} = \frac{105 - 110}{15}$$

$$= \frac{-5}{15} = -0.33$$

$$X_{\text{new}} = \frac{115 - 110}{15}$$

$$= \frac{5}{15}$$

$$= 0.33$$

$$X_{\text{New}} = \frac{120 - 110}{15} = \frac{10}{15} = 0.66$$

100
105
105
110
110
115
120
130
150

Robust Scaler
0.00
-0.33
0.33
0.66
0.00
1.33
2.66
-0.66
-0.33