Week 2: Multiple Regression, Training Exercises

Coursera/Erasmus U., Econometric Methods and Applications

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Training Exercise 2.1

Notes:

- $\bullet\,$ This exercise uses the datafile ${\tt TrainExer21} \\ {\tt and}$ requires a computer.
- The dataset TrainExer21 is available on the website.

Questions

- (a) Use dataset TrainExer21 to regress log-wage on a constant and the gender dummy Female, and check the result presented in Lecture 2.1 that log(Wage) = 4.73 0.25Female + e.
- (b) Let e be the series of residuals of the regression in part (a). Perform two regressions:
 - (i) e on a constant and education;
 - (ii) e on a constant and the part-time job dummy.
- (c) Comment on the outcomes of regressions (i) and (ii) of part (b).

Answers

(a) Use dataset TrainExer21 to regress log-wage on a constant and the gender dummy Female, and check the result presented in Lecture 2.1 that log(Wage) = 4.73 - 0.25Female + e.

We can verify the results from the lecture by quickly running a binary regression on LogWage by Female:

| | Table 1: |
|----------|-----------------------------|
| | Dependent variable: |
| | LogWage |
| Female | -0.251^{***} (0.040) |
| Constant | 4.734*** (0.024) |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |

We can see that the results are the same, with the intercept β_0 (or α if you prefer) term = 4.734 with a Standard Error = 0.024.

Likewise, we can see that the β_1 value = -0.251, with a Standard Error = .040.

(b) Let e be the series of residuals of the regression in part (a). Perform two regressions:

Using the residuals from this regression, we can now run two separate regressions to see if the error terms correlate with other variables in our dataset.

• (i) e on a constant and education;

| Table 2: | |
|----------|-------------------------------|
| | Dependent variable: |
| | $residuals (LogWage_Female)$ |
| Educ | 0.218*** |
| | (0.016) |
| Constant | -0.453^{***} |
| | (0.036) |
| | |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |

• (ii) e on a constant and the part-time job dummy.

| | Table 3: |
|----------|-------------------------------|
| | Dependent variable: |
| | $residuals (LogWage_Female)$ |
| Parttime | 0.099** |
| | (0.043) |
| Constant | -0.028 |
| | (0.023) |
| | |
| Note: | *p<0.1; **p<0.05; ***p<0.01 |

(c) Comment on the outcomes of regressions (i) and (ii) of part (b).

If the residual error from our first regression in part a can be thought of as wage difference between men and women that cannot be explained by our original regressor variable, Female, then the regressions we performed on these error terms in part b hint at what portion of this unexplained wage difference can be explained by other variables.

Specifically, what the first regression we performed in part b says is that an extra level of Education has a 0.218 (22%) effect on the unexplained wage difference between men and women. In other words, higher education levels leads to higher wages.

Similarly, in the second regression, we see that having a Part-timejob has an effect of 0.099 (or 10%) on the unexplained wage difference between men and women. This is unexpected, as we would have expected lower-wages for part-time work.

The results of both of these regressions on our residual error from part a suggest that these additional variables should be added to our model for predicting differences in LogWage.