

# Differentiating Coexisting Phases from Phase Separation regions in Doped Manganites with Spin Waves

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References: Phys. Rev. B59 (1999) 11448  
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## Outline

- I. Continuum Double Exchange Model
- II. Spin Waves in Magnetic ordered configurations
- III. Coexisting Phases vs. Phase Separation

Effective Potential for homogeneous configurations is obtained after integrating out the fermions in the path integral

$$V_{\text{eff}} = J_{AF} N^2 \left[ 2\gamma^2 - 1 - A \left( (\gamma_0 + \gamma)^{5/2} + (\gamma_0 - \gamma)^{5/2} \right) \right]$$

$$A = \frac{2^{3/2}}{15\pi^2} \frac{t}{J_{AF} N^2 a^3}$$

$\gamma \equiv \cos \frac{\Theta}{2} \longrightarrow$  Canting angle

$\gamma_0 \longrightarrow$  Chemical Potential measure

Doping is conjugate of chemical potential

$$x = -a^3 \frac{\partial V_{\text{eff}}}{\partial \mu} = -\frac{a^3}{t} \frac{\partial V_{\text{eff}}}{\partial \gamma_0}$$



$$x = -a^3 \frac{\partial V_{eff}}{\partial \mu} = -\frac{a^3}{t} \frac{\partial V_{eff}}{\partial y_0}$$

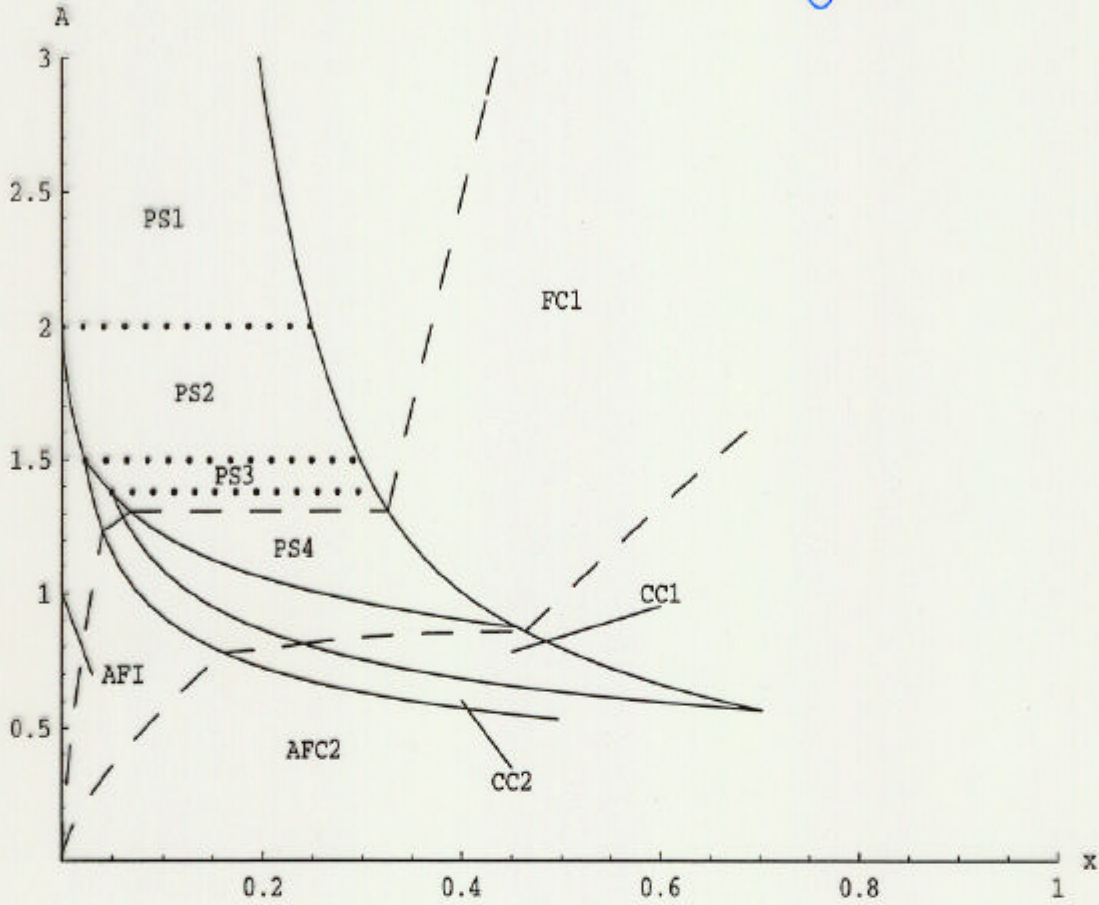


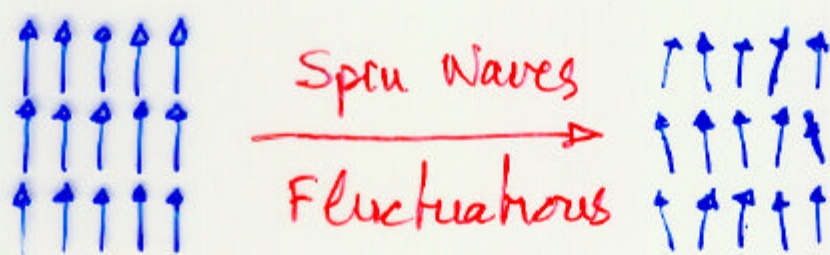
Figure 2: Phase diagram in the  $(x, A)$  plane.  $PSi$  ( $i = 1, 2, 3, 4$ ) indicates the new regions where the phases at their boundary may coexist. The  $x = 0$  axis corresponds to the  $AFI$  phase. The two dashed lines are the boundaries for the reliability of our model for  $z|J_H|M/2(J_{AF}a^3M^2) \sim 50$  and  $z|J_H|M/2(J_{AF}a^3M^2) \sim 200$  respectively. Only the part of the phase diagram to the left of the corresponding dashed line is trustworthy in each case.

$$\frac{t}{J_{AF}a^3M^2} \sim 10-20 \Rightarrow A \sim 1-2$$

## II. Spin Waves in Magnetically Ordered conf.

Magnetic Order  $\Rightarrow$  Spontaneous Symmetry Breaking

Spontaneous Symmetry Breaking  $\Rightarrow$  Goldstone Modes  
(Spin Waves)



$$\Psi_0 = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \longrightarrow$$

$$\Psi(x) = U(x) \Psi_0$$

$$U(x) = e^{i(\pi^1(x) S^1 + \pi^2(x) S^2)}$$

Spin Waves Fields

Symmetry principles allow us to write general effective lagrangians (model independent)



- Ferromagnetic Configuration ( $SU(2) \rightarrow U(1)$ )

$$\mathcal{L} = \pi^- i \partial_t \pi^+ - \frac{1}{2m'} \partial_i \pi^- \partial_i \pi^+$$

Schrödinger eq.: Quadratic dispersion

- Antiferromagnetic Configuration ( $SU(2) \rightarrow U(1)$ )

$$\mathcal{L} = \partial_t \pi^- \partial_t \pi^+ - v^2 \partial_i \pi^- \partial_i \pi^+$$

Wave equation: Linear dispersion

- Gapped Configuration ( $SU(2) \rightarrow 1$ )

$$\mathcal{L} = \pi^- i \partial_t \pi^+ - \frac{1}{2m'} \partial_i \pi^- \partial_i \pi^+ + \frac{1}{2} \partial_t \pi^3 \partial_t \pi^3 - \frac{v^2}{2} \partial_i \pi^3 \partial_i \pi^3$$

$\pi^+(x) \rightarrow$  Quadratic dispersion

$\pi^3(x) \rightarrow$  Linear dispersion.

## Dispersion relations in Manganites

In the CDEN there are two sources of spin waves terms in the Lagrangian

- 1) Heisenberg term
- 2) interaction electron-spin wave

→ After integrating out the electrons in the path integral, a dependence on the doping arises

Different interaction for every configuration (F, AF, C)



Different dependence of the dispersion relations on the doping



## IV. Canted Phases vs. Phase Separation

Phase Separation Region guess:

- Two macroscopic F and AF domains
- The interphase does not modify qualitatively the properties

PS: One F and two AF branches

C: One F and one AF branches

PS: Splitting of the AF branches by a magnetic field

C: No modification of the AF branch by a magnetic field.

Different behaviour of the mass and velocity with the doping

PS: Figure  $A = 2.20$

C: Figure  $A = 0.80$

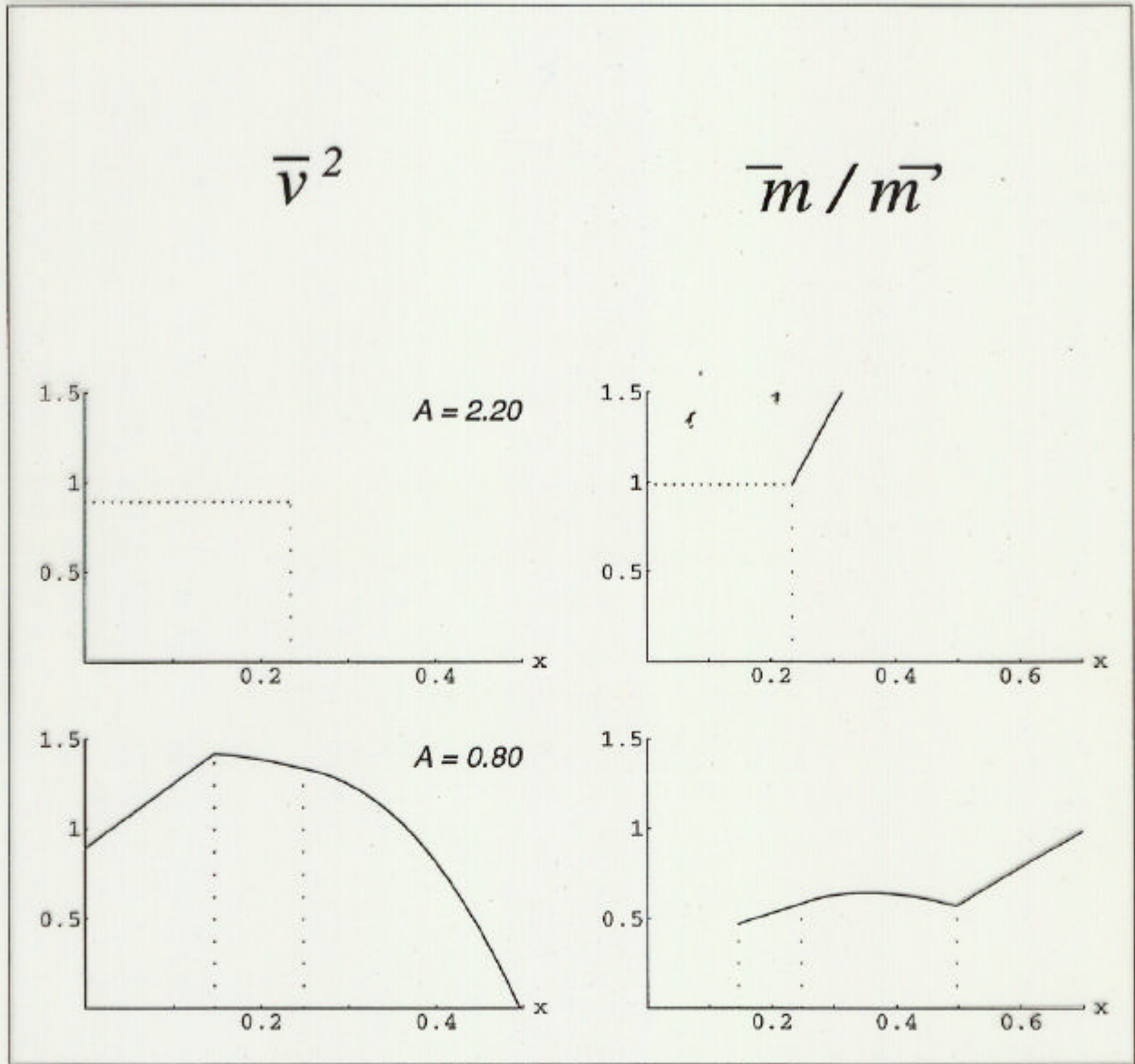


Figure 1: The dependence of the velocities and the masses on the doping for the  $F - AF$  phase separation region and the canted phase.  $\bar{v}^2 = (15\pi^2 A) 2mzv^2 / 6z^{3/2} (J_{AF} a^3 M^2)$  and  $\bar{m}/\bar{m}' = (15\pi^2 A) m / z^{3/2} m'$ . The horizontal dotted lines correspond to the phase separation regions, and the vertical dotted lines correspond to the phase transitions.



## Conclusions

- A simple continuum model describes the low energy and long distance properties for manganites systems
- Phase Diagram: AF, F, Canted and Phase Sep.
- The effective lag. for spin waves in the low energy and momentum presents:
  - F: One quadratic branch
  - AF: Two linear branches
  - C: One quadratic and one linear.
- We presented the the spin waves dispersion relations in the manganites (dependence on the doping)
- Three distinctive characteristic of the spin waves differentiate the canted phases from the phase separation regions.