# **Heuristic Analysis**

## **Optimal Solutions**

|    | air_cargo_pl        | air_cargo_p2        | air_cargo_p3        |
|----|---------------------|---------------------|---------------------|
| 1  | Load(C1, P1, SF0)   | Load(C1, P1, SF0)   | Load(C1, P1, SF0)   |
| 2  | Fly(P1, SF0, JFK)   | Fly(P1, SF0, JFK)   | Fly(P1, SF0, ATL)   |
| 3  | Unload(C1, P1, JFK) | Unload(C1, P1, JFK) | Load(C3, P1, ATL)   |
| 4  | Load(C2, P2, JFK)   | Load(C2, P2, JFK)   | Fly(P1, ATL, JFK)   |
| 5  | Fly(P2, JFK, SF0)   | Fly(P2, JFK, SF0)   | Unload(C1, P1, JFK) |
| 6  | Unload(C2, P2, SF0) | Unload(C2, P2, SF0) | Unload(C3, P1, JFK) |
| 7  |                     | Load(C3, P3, ATL)   | Load(C2, P2, JFK)   |
| 8  |                     | Fly(P3, ATL, SF0)   | Fly(P2, JFK, ORD)   |
| 9  |                     | Unload(C3, P3, SF0) | Load(C4, P2, ORD)   |
| 10 |                     |                     | Fly(P2, ORD, SF0)   |
| 11 |                     |                     | Unload(C2, P2, SF0) |
| 12 |                     |                     | Unload(C4, P2, SF0) |

### **Uninformed Search**

| breadth_first_search | air_cargo_pl | air_cargo_p2 | air_cargo_p3 |
|----------------------|--------------|--------------|--------------|
| optimality           | <b>~</b>     | V            | V            |
| time elapsed (s)     | 0.24         | 84.01        | 481.47       |
| # expansions         | 43           | 3343         | 14663        |
| # goal tests         | 56           | 4609         | 18098        |
| plan length          | 6            | 9            | 12           |

| depth_first_graph_search | air_cargo_p1 | air_cargo_p2 | air_cargo_p3 |
|--------------------------|--------------|--------------|--------------|
| optimality               | ×            | ×            | ×            |
| time elapsed             | 0.12         | 16.32        | 10.86        |
| # expansions             | 21           | 624          | 408          |
| # goal tests             | 22           | 625          | 409          |
| plan length              | 20           | 619          | 392          |

| depth_limited_search | air_cargo_p1 | air_cargo_p2 | air_cargo_p3 |
|----------------------|--------------|--------------|--------------|
|                      |              |              |              |

| optimality   | ×    | X       | _                 |
|--------------|------|---------|-------------------|
| time elapsed | 0.60 | 5276.41 | (stoped after 3h) |
| # expansions | 101  | 222719  | _                 |
| # goal tests | 271  | 2053741 | _                 |
| plan length  | 50   | 50      | _                 |

Breadth-first search was the only uninformed algorithm that found optimal solutions for all problems, and ran in a reasonable amount of time. Depth-first search took less time and expansions to find a solution, but the plan length was considerably larger, due to the fact that DFS kept adding actions to the solution until the goal was reached (path length is almost as large as the number of expansions). The worst performing algorithm was Depth limited search, searching deep into the state space, but not deep enough as to brute-force the solution (like DFS). The solutions that DLS was able to find both have the length of 50 (the depth limit of the algorithm).

### A\* Search

| h_ignore_preconditions | air_cargo_p1 | air_cargo_p2 | air_cargo_p3 |
|------------------------|--------------|--------------|--------------|
| optimality             | <b>✓</b>     | <b>~</b>     | <b>~</b>     |
| time elapsed           | 0.23         | 32.56        | 124.65       |
| # expansions           | 41           | 1421         | 4589         |
| # goal tests           | 43           | 1423         | 4591         |
| plan length            | 6            | 9            | 12           |

| h_pg_levelsum | air_cargo_p1 | air_cargo_p2 | air_cargo_p3 |
|---------------|--------------|--------------|--------------|
| optimality    | <b>✓</b>     | <b>~</b>     | X            |
| time elapsed  | 2.10         | 186.18       | 744.12       |
| # expansions  | 11           | 79           | 242          |
| # goal tests  | 13           | 81           | 244          |
| plan length   | 6            | 9            | 13           |

The ignore preconditions heuristic (being a relaxed version of the original problem, and thus - admissible) was guaranteed to find the optimal solution for all problems. It was able to find a solution faster than using a planning graph and with levelsum heuristic, which did not find an optimal solution for all problems (the heuristic is not admissible). However, using levelsum resulted in considerably fewer expansions, but the time spent computing the heuristic for each expansion cancels that.

#### **Conclusions**

The heuristic that yielded the best results was <code>ignore preconditions</code>. Compared to non-heuristic search, it expanded less nodes than <code>BFS</code>, but still found optimal solutions for each problem (compared to <code>DFS</code>). While planning graph and with <code>levelsum</code> heuristic solution for the third problem was not optimal, it was very close (1 extra action on solution) while expanding fewer nodes than any other search algorithm.