```
In [1]:
         include("../Sandpile.jl")
         include("../old/Sandpile64.jl")
         include("../old/SandpileAbstract.jl")
         using .Sandpile
         using .Sandpile64
         using .SandpileAbstract
         using BenchmarkTools
       Need to use a smaller grid and less grains for benchmarking
In [2]:
         x, y = 50, 50; # Dimensions of grid
         N = 1000; # Number of grains to be added
         f_x = 4; # Critical value for sandpile model
       Benchmarking
In [3]:
         @benchmark run sandpileAbstract!(sandpile initAbstract(x, y, "zero"), N)
        BenchmarkTools.Trial: 952 samples with 1 evaluation.
Out[3]:
         Range (min ... max): 3.511 ms ... 26.314 ms
                                                    GC (min ... max): 0.00% ... 70.51%
         Time (median):
                             3.925 ms
                                                      GC (median): 0.00%
         Time (mean \pm \sigma): 5.230 ms \pm 3.364 ms
                                                    GC (mean \pm \sigma): 21.01% \pm 21.81%
                       Histogram: log(frequency) by time
         Memory estimate: 4.67 MiB, allocs estimate: 7007.
In [4]:
         @benchmark run sandpile64!(sandpile init64(x, y, "zero"), N)
        BenchmarkTools.Trial: 1092 samples with 1 evaluation.
Out [4]:
         Range (min ... max): 2.902 ms ... 21.814 ms GC (min ... max): 0.00% ... 82.51%
         Time (median):
                           3.338 ms
                                                     GC (median):
                                                                      0.00%
         Time (mean \pm \sigma): 4.570 ms \pm 3.267 ms | GC (mean \pm \sigma): 23.50% \pm 22.75%
                       Histogram: log(frequency) by time
         Memory estimate: 4.67 MiB, allocs estimate: 7007.
In [5]:
         @benchmark run sandpile!(sandpile init(x, y, "zero"), N)
        BenchmarkTools.Trial: 1105 samples with 1 evaluation.
Out [5]:
         Range (min ... max): 2.918 ms ... 19.102 ms
                                                    GC (min ... max): 0.00% ... 77.52%
         Time (median):
                             3.321 ms
                                                      GC (median): 0.00%
         Time (mean \pm \sigma): 4.510 ms \pm 3.107 ms | GC (mean \pm \sigma): 22.72% \pm 22.65%
          2.92 ms
                       Histogram: log(frequency) by time
                                                                15 ms <
         Memory estimate: 4.65 MiB, allocs estimate: 7006.
In [6]:
         @benchmark run sandpileAbstract!(sandpile initAbstract(x, y, "random"), N)
        BenchmarkTools.Trial: 220 samples with 1 evaluation.
```

```
Time
               (median):
                              20.909 ms
                                                       GC (median):
                                                                       0.00%
         Time (mean \pm \sigma):
                              22.776 \text{ ms} \pm 5.587 \text{ ms}
                                                     GC (mean \pm \sigma): 14.15% \pm 15.70%
                          Histogram: frequency by time
          14.7 ms
                                                                36.6 ms <
         Memory estimate: 11.76 MiB, allocs estimate: 18630.
In [7]:
         @benchmark run sandpile64!(sandpile init64(x, y, "random"), N)
        BenchmarkTools.Trial: 226 samples with 1 evaluation.
Out[7]:
         Range (min ... max): 13.827 ms ... 34.143 ms | GC (min ... max): 0.00% ... 32.62%
         Time (median):
                           20.142 ms
                                                      GC (median):
         Time (mean \pm \sigma): 22.156 ms \pm 4.961 ms | GC (mean \pm \sigma): 14.54% \pm 16.41%
                           Histogram: frequency by time
          13.8 ms
                                                                32.9 ms <
         Memory estimate: 12.41 MiB, allocs estimate: 19731.
In [8]:
         @benchmark run sandpile!(sandpile init(x, y, "random"), N)
        BenchmarkTools.Trial: 224 samples with 1 evaluation.
Out[8]:
         Range (min ... max): 14.419 ms ... 38.888 ms | GC (min ... max): 0.00% ... 32.01%
                              20.152 ms
                                                      GC (median):
         Time (median):
                                                                       0.00%
                             22.330 ms \pm 5.379 ms | GC (mean \pm \sigma): 14.26% \pm 15.80%
         Time (mean \pm \sigma):
                          Histogram: frequency by time
          14.4 ms
                                                                34.6 ms <
         Memory estimate: 12.62 MiB, allocs estimate: 20148.
       Type Stability of Functions
In [9]:
         @code warntype sandpile init(x, y, "zero")
        MethodInstance for Main.Sandpile.sandpile init(::Int64, ::Int64, ::String)
          from sandpile init(x::Int64, y::Int64, setup::String) in Main.Sandpile at /Users/raarome
        ro/sandpile-julia/code/Sandpile.jl:17
        Arguments
          #self#::Core.Const(Main.Sandpile.sandpile init)
          x::Int64
          y::Int64
          setup::String
        Body::Matrix{UInt8}
        1 - %1 = (setup == "random")::Bool
                 goto #3 if not %1
        2 - %3 = Core.apply type(Main.Sandpile.Array, Main.Sandpile.UInt8)::Core.Const(Array{UInt
        8})
            %4 = (0:3) :: Core.Const(0:3)
            %5 = Main.Sandpile.rand(%4, x, y)::Matrix{Int64}
            %6 = Main.Sandpile.convert(%3, %5)::Matrix{UInt8}
                 return %6
        3 - %8 = (setup == "zero")::Bool
                  goto #5 if not %8
        4 - %10 = Main.Sandpile.zeros(Main.Sandpile.UInt8, x, y)::Matrix{UInt8}
                 return %10
```

Main.Sandpile.error("`setup` must have value of `random` or `zero`")

GC (min ... max): 0.00% ... 23.23%

Range (min ... max): 14.668 ms ... 44.523 ms

Out[6]:

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Core.Const(:(return %12))
In [10]:
          @code warntype add grain!(sandpile init(x, y, "zero"))
         MethodInstance for Main.Sandpile.add grain!(::Matrix{UInt8})
           from add grain!(z::Matrix{UInt8}) in Main.Sandpile at /Users/raaromero/sandpile-julia/co
         de/Sandpile.jl:38
         Arguments
           #self#::Core.Const(Main.Sandpile.add grain!)
           z::Matrix{UInt8}
         Body::Int64
         1 - %1 = Main.Sandpile.size(z)::Tuple{Int64, Int64}
             %2 = Base.getindex(%1, 1)::Int64
             %3 = (1:%2)::Core.PartialStruct(UnitRange{Int64}, Any[Core.Const(1), Int64])
             %4 = Main.Sandpile.rand(%3)::Int64
             %5 = Main.Sandpile.size(z)::Tuple{Int64, Int64}
             %6 = Base.getindex(%5, 2)::Int64
             %7 = (1:%6)::Core.PartialStruct(UnitRange{Int64}, Any[Core.Const(1), Int64])
             %8 = Main.Sandpile.rand(%7)::Int64
             %9 = Base.getindex(z, %4, %8)::UInt8
             %10 = (%9 + 1) :: Int64
                  Base.setindex!(z, %10, %4, %8)
                   return %10
In [11]:
          @code warntype is unstable(sandpile init(x, y, "zero"))
         MethodInstance for Main.Sandpile.is unstable(::Matrix{UInt8})
           from is unstable(z::Matrix{UInt8}) in Main.Sandpile at /Users/raaromero/sandpile-julia/c
         ode/Sandpile.jl:48
         Arguments
           #self#::Core.Const(Main.Sandpile.is unstable)
           z::Matrix{UInt8}
         Body::Bool
         1 - %1 = (\#self\#)(z, 4)::Bool
                  return %1
In [12]:
          @code warntype avalanche!(sandpile init(x, y, "zero"))
         MethodInstance for Main.Sandpile.avalanche!(::Matrix{UInt8})
           from avalanche!(z::Matrix{UInt8}) in Main.Sandpile at /Users/raaromero/sandpile-julia/co
         de/Sandpile.jl:68
         Arguments
           #self#::Core.Const (Main.Sandpile.avalanche!)
           z::Matrix{UInt8}
         Body::UInt8
         1 - %1 = (\#self\#)(z, 4)::UInt8
                  return %1
In [13]:
          @code warntype run sandpile!(sandpile init(x, y, "zero"), 100 000)
         MethodInstance for Main.Sandpile.run sandpile!(::Matrix{UInt8}, ::Int64)
           from run sandpile!(z::Matrix{UInt8}, N::Int64; N crit, f_X) in Main.Sandpile at /Users/ra
         aromero/sandpile-julia/code/Sandpile.jl:102
         Arguments
           #self#::Core.Const(Main.Sandpile.run sandpile!)
           z::Matrix{UInt8}
           N::Int64
         Body:: Vector { Int64 }
         1 - %1 = Main.Sandpile.:(var"#run sandpile!#1")(false, 4, #self#, z, N)::Vector{Int64}
```

In []:			

└─ return %1