SMAI-ASSIGNMENT 2

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Abstract. The document is written to answer the following questions

- (1) Prove that the single-sample perceptron algorithm will always converge to a solution if one exists.
- (2) Implement Perceptron-based Linear Discriminant Functions, that is, Singlesample perceptron, Single-sample perceptron with margin, Relaxation algorithm with margin, Widrow-Hoff or Least Mean Squared (LMS) Rule
- (3) Implement a simple supervised, feed-forward, back-propagation network for the problem of optical character recognition for digits 0 and 7.

1. Proof of Convergence of Perceptron

Let the data be Linearly separable and let \hat{a} be solution vector perpendicular to the required plain. So, we know that $\hat{a}^t y_i > 0 \ \forall i$.

```
The Gradient Descent Equation is:,
```

$$a(k+1) = a(k) + y^k$$

We subtracting $\alpha \hat{a}$ from both sides,

$$a(k+1) - \alpha \hat{a} = a(k) - \alpha \hat{a} + y^k$$

Squaring both sides

$$||a(k+1) - \alpha \hat{a}||^2 = ||a(k) - \alpha \hat{a} + y^k||^2$$

$$\begin{aligned} ||a(k+1) - \alpha \hat{a}||^2 &= ||a(k) - \alpha \hat{a} + y^k||^2 \\ ||a(k+1) - \alpha \hat{a}||^2 &= ||a(k) - \alpha \hat{a}||^2 + ||y^k||^2 + 2(a(k) - \alpha \hat{a})^t y^k \end{aligned}$$

$$y^k$$
 was a misclassified point. Hence $\hat{a}^t y^k \leq 0$, so: $||a(k+1) - \alpha \hat{a}||^2 \leq ||a(k) - \alpha \hat{a}||^2 + ||y^k||^2 - 2\alpha \hat{a}^t y^k$

Now, $a^t y^k > 0$. Also,

We define β as the maximum length of the pattern vector. ie. $\beta^2 = max_i||y_i||^2$. As this is a positive value, this is the maximum we can achieve from the second term.

^{2015.}

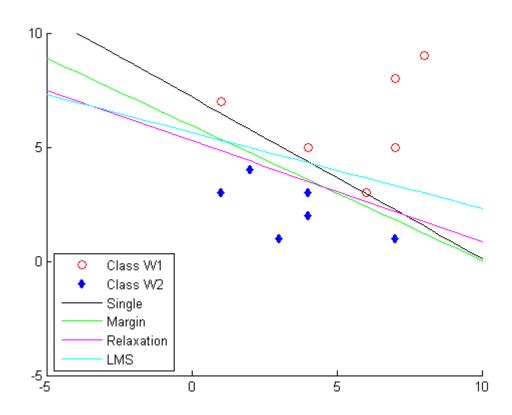
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We define γ as the smaller inner product of the \hat{a} with any pattern vector. ie. $\gamma = min_i[\hat{a}^iy_i]$. This is the minimum we can achieve from the third term which can be subtracted.

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Hence our equation becomes, ||a(k+1) - \alpha \hat{a}||^2 \leq ||a(k) - \alpha \hat{a}||^2 - 2\alpha\gamma + \beta^2 \alpha was a random constant solet \alpha = \beta^2/\gamma. Our equation reduces to, ||a(k+1) - \alpha \hat{a}||^2 \leq ||a(k) - \alpha \hat{a}||^2 - \beta^2 Say that after some k_0 steps, the equation converges, ie. ||a(k_0+1) - \alpha \hat{a}||^2 = 0, hence, 0 \leq ||a(k) - \alpha \hat{a}||^2 - k_0\beta^2 or we can write it as k_0 = ||a(1) - \alpha \hat{a}||^2/\beta^2
```

2. LDF - Gradient Descent Algorithm

2.1. Graph



a1 : For single sample

a2 : For single sample with margin

a3 : For Relaxed a4 : For LMS

Round 1

a = randi(5,[1,size(dataFinal,1)])

a1 =

-2.9500 0.2900 0.4100

Elapsed time is $0.005273 \ \text{seconds}.$

a = randi(5,[1,size(dataFinal,1)])
a2 =

-5.9300 0.5900 1.0000

Elapsed time is 0.013373 seconds.

a = [-1,1,1]; a3 =

-1.2917 0.1083 0.2451

Elapsed time is 0.915025 seconds.

a = [-1,1,1];a4 =

-1.5246 0.0898 0.2704

Elapsed time is 0.433580 seconds.

Round 2

a = randi(5,[1,size(dataFinal,1)])
a1 =

-2.9500 0.2800 0.4600

Elapsed time is 0.006685 seconds.

a = randi(5,[1,size(dataFinal,1)])
a2 =

-5.6500 0.5700 0.9400

Elapsed time is 0.011457 seconds.

a = [-5,1,1]a3 =

-5.0753 0.5898 0.8480

Elapsed time is 0.854140 seconds.

```
a = [-5,1,1]
a4 =
   -5.0480
              0.6693
                        0.6749
Elapsed time is 0.003884 seconds.
Round 3
a = randi(5,[1,size(dataFinal,1)])
a1 =
   -3.2000
              0.2200
                        0.6700
Elapsed time is 0.007913 seconds.
a = randi(5,[1,size(dataFinal,1)])
a2 =
              0.5700
   -6.2000
                        1.1200
Elapsed time is 0.011992 seconds.
a = [1,1,1]
a3 =
   -5.0753
              0.5898
                        0.8480
Elapsed time is 0.829555 seconds.
a = [1,1,1]
a4 =
    0.6437
             -0.1371
                        0.0696
```

Elapsed time is 0.019652 seconds. But the answer obtained is not correct.

As one can see the time is almost same for any initial value of A for a1 and a2. The time taken by a3 has a little dependence on A.

The time taken by a 4 varies greatly with the initial value of A. If A is closer to a minimum then it Even though this may lead to wrong output.

ADDING DIFFERENT MARGIN

Round 1

b = 0.5

a2 =

-5.7100 0.5500 1.0000

Elapsed time is 0.013883 seconds.

b = 0.1

a3 =

-1.2917 0.1083 0.2451

Elapsed time is 0.932693 seconds.

Round 2

b = 1.5

a2 =

-14.9100 1.5500 2.3800

Elapsed time is 0.033113 seconds.

b = 1.1

a3 =

-5.8612 0.6099 0.9103

Elapsed time is 1.243246 seconds.

Round 3

b = 0.05

a2 =

-3.1200 0.2100 0.6500

Elapsed time is 0.010261 seconds.

b = 0.01

a3 =

-1.2819 0.0810 0.2800

Elapsed time is 0.809574 seconds.

As one can see the time is greatly dependent on the value of the margin. Higher value of margin usual In almost all the cases a2 is much faster than a3.

2.2. Code

```
1clear;
 2clc;
3data1 = [1,1,7;1,6,3;1,7,8;1,8,9;1,4,5;1,7,5]';
4data2 = -[1,3,1;1,4,3;1,2,4;1,7,1;1,1,3;1,4,2]';
5dataFinal = [data1, data2];
7\, scatter \, (\, data1 \, (\, 2 \, , : ) \,\, , \quad data1 \, (\, 3 \, , : ) \,\, , \, \, 'r \,\, ') \,\, , axis \, (\, [\, -5 \, , 10 \, , -5 \, , 10 \, ]) \,\, , hold \,\, on \, ;
sscatter(-data2(2,:),-data2(3,:),'b','d','filled'), axis([-5,10,-5,10]);
10x = -10:0.5:10;
11tic ,a1 = Single(dataFinal),toc;
12tic, a2 = Margin (dataFinal), toc;
13tic, a3 = Relax(dataFinal), toc;
14 \operatorname{tic}, a4 = \operatorname{LMS}(\operatorname{dataFinal}), \operatorname{toc};
16y1 = (a1(1)+a1(2)*x)/(-a1(3));
17 \operatorname{plot}(x, y1, 'k'), \operatorname{axis}([-5, 10, -5, 10]);
18y2 = (a2(1)+a2(2)*x)/(-a2(3));
19 plot (x, y2, 'g'), axis ([-5, 10, -5, 10]);
20y3 = (a3(1)+a3(2)*x)/(-a3(3));
21 plot (x, y3, 'm'), axis ([-5, 10, -5, 10]);
22y4 = (a4(1)+a4(2)*x)/(-a4(3));
23 plot (x, y4, c), axis ([-5, 10, -5, 10]);
24 legend ('Class W1', 'Class W2', 'Single', 'Margin', 'Relaxation',
       'LMS', 'Location', 'southwest'), hold off;
25
27% In case of linearly classifiable data we asume a model G(x) = A*Y .
28% So for properly classifying the points we need to determine the
       correct
29% value of A. For this we first define an error function J and then
30% minimize it. Now using the technique of Gradiant Decent we update
      the value of A.
32\% A(k+1) = A(k) + (ETA)*J';
```

a's.

% a = randi(5,[1, size(data,1)]);

```
and ETA is the learning rate.
34% Depending on our choice of J our algorithm changes.
35 function [ a ] = Relax( dataFinal )
36%UNTITLED9 Summary of this function goes here
     Detailed explanation goes here
     a = [-1, 1, 1];
38
     n = 0.1;
                        %learning rate
39
     b = 0.1;
                          %margin
     thres = 100000;
41
     check = zeros(length(dataFinal),1);
     for i = 0:thres
         j = 1+mod(i, length(dataFinal));
         q = a*dataFinal(:,j);
         if q < b
46
             a = a +
     n*(((b-q)^2)/(norm(dataFinal(:,j)')^2))*(dataFinal(:,j)');
             check(j)=0;
49
         else
50
             check(j)=1;
         end
         if sum(check) == length(check)
              break;
         end
     end
56end
58% Till the previous algorithm more weightage was give to outliers.
59% correct this issue it is normalized with norm of the distence.
     Also the
60% concept of relaxation is introduced. If there is under relaxation
61% the learning is slow but if there is over relaxation then it may
62% overshoot.
63% J' is (((AY-B)^2)/(|Y|^2))*Yk;
65% This process was comparitively computationally expensive. But this
66% algorithm also gave correct results and this algorithm has the
     capacity
67% to hendle far off cases.
68 function [ a ] = LMS( dataFinal )
69%UNTITLED8 Summary of this function goes here
70% Detailed explanation goes here
a = [-1, 1, 1];
                     % selected after trying for MANY possible
```

33% J' is the derivate of the error function we are trying to minimize

```
n = 0.0005;
                             %learning rate
      \% b = randi(5,[1, size(data,2)]);
      b = ones(1, size(dataFinal,2));
      thres = 0.000025;
      check = zeros(length(dataFinal),1);
      j = 1;
      i = 0;
79
       while \ norm((n)*dataFinal(:,j) \ '*(a*dataFinal(:,j) \ - \ b(j))) > \ thres 
          j = 1+mod(i, length(dataFinal));
          a = a - (n)*dataFinal(:,j)'*(a*dataFinal(:,j) - b(j));
82
          i = i+1;
83
84
      end
85end
87% Untill now all the algorithms that we saw used misclassified
88% updation purpose. This had a major issue as due to this outliers
      etc
89% had large influence. So to correct this issue this method was
      introduced.
90% In this method all the points are concidered. It is assumed that
      each
91% poiint has a distence bi from the line.
92% But as correct distance cant be estimated error is introduced. So,
93\% e = AY - B;
94% Using this we try and update A to get a favorable vector.
95
96
97% This algorithm give very different results for different
      initallised
98% values. Even then it was not able to correctly identify all the
    points.
99 function [ a ] = Single ( dataFinal )
100%UNTITLED5 Summary of this function goes here
      Detailed explanation goes here
      a = randi(5, [1, size(dataFinal, 1)]);
      n = 0.09;
                           %learning rate
      b = 0;
                            %margin
104
      thres = 50000;
      check = zeros(length(dataFinal),1);
      for i = 0:thres
          j = 1+mod(i, length(dataFinal));
          q = a*dataFinal(:,j);
          if \ q <= b
110
              a = a + n*dataFinal(:,j)';
111
              check(j)=0;
          else
              check(j)=1;
```

```
115
          end
          if sum(check) == length(check)
              break;
119
      end
120end
121 function [ a ] = Margin( dataFinal )
122%UNTITLED5 Summary of this function goes here
      Detailed explanation goes here
      a = randi(5, [1, size(dataFinal, 1)]);
      n = 0.09;
                          %learning rate
      b = 0.5;
126
                              %margin
      thres = 50000;
128
      check = zeros(length(dataFinal),1);
129
      for i = 0:thres
          j = 1+mod(i, length(dataFinal));
          q = a*dataFinal(:,j);
131
          if q \le b
132
              a = a + n*dataFinal(:,j);
133
              check(j)=0;
134
135
          else
              check(j)=1;
          if sum(check) == length(check)
               break;
140
          end
141
      end
142end
143
144% This is a little improvement of the previous techique. In this
      algorithm
145% the concept margin is introduced so that the partitioning line is
      not too
146% close to the points. This helps in obtaining a more general line .
147\% So our J is AY – b.
149% This methos also gave very efficient results and was able to
      classify the
150% results correctly in a short time. It is also computationally not
      that
151% expensive. But if the data set was not as good as the one provided
      then
152% this algorithm might not have such results.
153% As a margin was kept it gave pretty good seperation line.
```

3. Neural Network

```
154 clear;
155 clc;
156a = fopen('optdigits-orig.cv');
157i = 1;
158 while ~feof(a)
if mod(i, 33) == 0
           sbl_v(i/33,:)=fgetl(a);
161 else
162
           data_v(i,:)=fgetl(a);
end end
164 i=i+1;
165end
166a = fopen('optdigits-orig.tra');
167i = 1;
168 while ~feof(a)
if mod(i, 33) == 0
           sbl_t(i/33,:)=fgetl(a);
           data_t(i,:)=fgetl(a);
173 end
174 i=i+1;
175end
177 \, s \, b \, l_{-}t = s \, b \, l_{-}t \, (:,2);
178 \, \text{sbl_v} = \text{sbl_v} (:, 2);
180a = data_t = '1';
181 data_t(a) = 255;
182a = data_t = '0';
183 data_t(a) = 0;
184a = data_v = '1';
185 data_v(a) = 255;
186a = data_v = '0';
187 data_v(a) = 0;
188 data_t = double(data_t);
189 data_v = double(data_v);
190
191a = find(sbl_t = '7' | sbl_t = '0');
192 \operatorname{train} = \operatorname{zeros}(8, 9, \operatorname{length}(a));
193 for i = 1: length(a)
if sbl_t(a(i)) = '7
195
           b = 1;
196
    else
           b = 0;
```

```
train(:,1:8,i) =
       imresize(data_t((a(i)-1)*33+1:a(i)*33-1,:),0.25);
       train(:, 9, i) = b;
202a = find(sbl_v = '7' | sbl_v = '0');
203 \text{ validate} = \text{zeros}(8, 9, \text{length}(a));
204 \text{ for } i = 1: \text{length}(a)
       if sbl_v(a(i)) = 7
206
            b = 1;
207
       else
208
            b = 0;
209
       end
       validate(:,1:8,i) =
210
       imresize(data_v((a(i)-1)*33+1:a(i)*33-1,:),0.25);
211
       validate(:, 9, i) = b;
212end
213 clear data_t;
214 clear data_v;
215 clear sbl_t;
216 clear sbl_v;
217 clear a;
218 clear b;
219 clear i;
220 clear;
221 clc;
222 load ./ Q3_data.mat;
223t = train;
224v = validate;
226d = size(t,1)*(size(t,2)-1) +1;
                                                  % because 8X8 + x0;
227nH = 39;
228c = 2;
229n = 0.1;
230 iter = 100;
231 \, \text{thres} = 10;
233Wij = unifrnd(-1/sqrt(d), 1/sqrt(d), d, nH);
234Wjk = unifrnd(-1/sqrt(nH), 1/sqrt(nH), nH, c);
235 \operatorname{netj} = \operatorname{zeros}(nH,1);
236 \operatorname{netk} = \operatorname{zeros}(c, 1);
237 \operatorname{error} = \operatorname{zeros}(1, \operatorname{size}(v,3));
238e = zeros(1, size(v,3));
239
240 \, \text{for j} = 1 : \text{iter}
for i = 1: size(t,3)
    X = 1;
X(2:d) = t(:,1:8,i);
                                                         % 1Xd
                                                         \% 1Xd.dXnH \implies 1XnH
      netj = (X*Wij);
```

```
245
            Y = (1+\exp(-netj)).\hat{}(-1);
                                                            \% 1XnH
            netk = (Y*Wjk);
                                                        \% 1XnH.nHXc \implies 1Xc
            Z = (1+exp(-netk)).^{(-1)};
249
            if t(1, end, i) = 1
250
                 tc = [1, 1];
251
252
            else
                 tc = [0, 0];
254
            end
255
            if (norm(Z) > 0.4 \& t(1,end,i) == 1) | (norm(Z) <= 0.4 \&
       t(1,end,i) == 0)
                 e(i) = 0;
256
257
            else
                 e(i) = 1;
            \quad \text{end} \quad
            Dk = ((tc-Z).*(Z.*(1-Z)));
            Wjk = Wjk + n*Y'*Dk;
            Dj = ((Dk*Wjk').*(Y.*(1-Y)));
            Wij = Wij + n*X'*Dj;
263
264
       end
       if sum(e) < thres
            break;
267
       end
268end
269
270 \, \text{for i} = 1: \text{size}(v,3)
       X = 1;
       X(2:d) = v(:,1:8,i);
                                                   % 1Xd
       netj = (X*Wij);
                                                   \% 1Xd.dXnH \implies 1XnH
274
                                                       % 1XnH
       Y = (1+exp(-netj)).^{(-1)};
275
       \mathtt{netk} \; = \; (Y{*}W\mathtt{jk}) \; ;
                                                   \% 1XnH.nHXc \Longrightarrow 1Xc
276
277
       Z = (1+\exp(-netk)).^{(-1)};
       if (norm(Z) > 0.5 \& v(1,end,i) == 1) | (norm(Z) <= 0.5 \&
       v(1, end, i) == 0
            error(i) = 0;
280
281
       else
282
            error(i) = 1;
283
       end
284end
285q = find(error == 1);
286 fprintf('Number of misclassified "7": %d n', sum(v(1,end,q)));
287 fprintf ('Total misclassified samples: %d\n', length (q));
288 fprintf (': %d\n', length (q));
```

For the purpose of recognizing letters '0' and '7' Since the number of training samples was 390 I decided to use 39 hidden states.

Wij is 65X39:

```
0.00852377110196400 0.0168167108194295 0.0906906995135764 -0.0341521508520852
0.00915446012818496 \ -0.0768488757602270 \ 0.0502128894586879 \ 0.0279794871327043
0.0621662893305959 0.0759595787983735 0.105897485065351 0.0225581981968135
0.117390193773649 \ 0.0214895782727926 \ -0.102615639285905 \ -0.0620640004927365
-0.0754294689332468 \ -0.0178795726500848 \ -0.0110213735800909 \ 0.0727804090855225
-0.0439326189495888 0.00715505421676795 -0.0875192492853352 -0.0310464378044200
0.109104246623387 \ 0.0316997788661457 \ -0.0117638930064226 \ 0.0371779579678653
-0.0980467288909962 0.0637766875999936 -0.00738271533583162 0.102774214462131
0.0867514018326965 \ -0.0982989098190917 \ 0.0850625005994987 \ 0.0588708982926175
0.0776162569032200 0.123112547436863 -0.0543850089758245
0.0595261495178468 \ 0.00714056952943048 \ 0.0811628260928037 \ -0.0543772358575069
0.0604521855394331 - 0.00463698755753382 \ 0.0149190270129171 - 0.00962944054533800
0.0348426394699797 0.105751071978376 -0.00130163968318400 -0.0932268375130779
0.0605169515811133 \ 0.113086409361776 \ -0.105243020771068 \ -0.0918293699951344
0.0633270255349999 \ 0.0276696150246281 \ 0.0551462743085977 \ 0.0609341949144762
0.0309797976289314 \ 0.122647670708964 \ -0.0962274418719907 \ -0.0644266090832099
-0.0869059280930350 \ -0.0830993920358655 \ 0.0315682349228637 \ -0.0687050112872726
-0.0788778677112658 \ -0.0894439736089960 \ -0.0555879414724181 \ 0.111940823629141
-0.102190073481889 0.115545801728561 0.0729077843414233 0.0529256065176578
-0.0688455307960449 0.101037817289172 -0.0965540374183246
-0.109830646143318 \ 0.0643703207794488 \ -0.0510154309450226 \ -0.111173648015054
-0.104774750720731 \ -0.0512938753621463 \ -0.0830650986088040 \ -0.120837949145864
-0.0633115424174788 0.0630578449510213 0.0577851075628820 0.0501532617037082
-0.123415622604114 -0.0284690187788827 0.111677824945701 -0.109004834976096
-0.0303006290010616 \ -0.0721013123039012 \ 0.0441962771640571 \ -0.00625855068888152
-0.0296402637734693 \ 0.00543342804006497 \ 0.0366871065203631 \ -0.0827904583583095
0.0916374172128980 \ -0.00170096551716990 \ 0.0908825317463318 \ -0.0264418823150248
0.0484401807211761 \ \ 0.0687638588174358 \ \ -0.0529297910571880 \ \ -0.0207345205815580
0.0774297023751123 -0.0674558460383876 0.0288951106614635
-0.0775996271336807 \; -0.0354858986491108 \; 0.0629885797464172 \; 0.00329630169952517 \\
0.00366246233055242 \ \ 0.0927470099417445 \ \ 0.0246810386538579 \ \ 0.0397235116995779
-0.108078142634465 \ -0.121952161062692 \ -0.0100547123556675 \ 0.111037991501745
0.0464084145353480 \ 0.0967093501366771 \ -0.00670515450603525 \ 0.101880141465277
0.00630307902247911 \ -0.0832242425839677 \ 0.0336513946901884 \ -0.0340988001202030
0.0246847402122981 0.0270451310606321 -0.106392477300683 0.0737746673311120
0.0444435754981999 \ 0.0470601757378302 \ -0.127280448215099 \ 0.108799655935066
0.0189361108794941 \ 0.0979002756323457 \ 0.0566501830871377 \ 0.123363766078253
-0.0211705114952527 \ -0.0158793591601205 \ 0.0195125379740267 \ 0.0807670769482862
0.124674283331374\ 0.0745102561387080\ 0.0601811156435985
0.000771526493604177 \ \ 0.0630723614547452 \ \ 0.0674020062402522 \ \ -0.0444395094839052
-0.107461400179258 \ -0.120991075915206 \ -0.0903457458305285 \ -0.0292480171837627
-0.0328254138786684 \ -0.0679071115991325 \ -0.0554740791000339 \ -0.120848877603020
```

```
-0.00398370138512121 \ \ 0.125916167422714 \ \ 0.0511030084448825 \ \ -0.120662612974428
0.119034558869075 - 0.0640480667925480 \ 0.108543865352031 - 0.0121778929587795
-0.0550411125496900 \; -0.00121992069175365 \; \; 0.0805420814576100 \; \; 0.0865317399464556
-0.0300564171047141 -0.0371411208113495 0.0773612724774837 -0.0146339639866768
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 $-0.000202193588980811 \ -0.0551173638116757 \ -0.135393421393931 \ 0.0475030407642223$ 0.0186806184072189 - 0.0201011646784361 0.113656725660994 $0.0836362134873772 \ 0.00984815653387767 \ 0.0497672918808433 \ 0.0114636933124908$ $0.0292131938373349 \ -0.101858315653476 \ 0.0190255965884177 \ -0.0596841037154334$ $0.120172394362308 \ -0.0296473339978907 \ 0.117466489908532 \ 0.0904075905056672$ $0.111384748928521 \ -0.0647638548212813 \ -0.00882732341395094 \ 0.0899959334906892$ $0.0539919136695452 \;\; -0.0148274674357357 \;\; 0.0651624301432882 \;\; -0.106387916302696$ 0.0173701545937486 0.0174672586236107 0.0368935338563719 0.07434944252072210.0546144184627391 0.0771951652077632 0.0451415765007281 0.0795345459604575 0.0530021595078960 0.116236584082299 0.0103340379531966 0.0309774391122167 $-0.0646373522356078 \ \, 0.0291072931791787 \ \, 0.0756122631022866 \ \, 0.0754364589706667$ $-0.113260567513677 \quad -0.0594809496467407 \quad 0.00774161828472708$ $0.00365516579923664 \ -0.0217548843370082 \ -0.0855968124693114 \ 0.0612497021527259$ -0.110446922753585 -0.0984428543546035 0.0624914496438473 0.1100862941112690.0352498351970032 -0.0158278220687346 0.0252725487884273 0.0678191015937083 $-0.109425163348491 \ -0.0418791930314000 \ -0.00130794065824217 \ 0.106581566198199$ $-0.0105612075917460 \ 0.117450848532430 \ -0.0834578256098664 \ 0.00200891627837784$ $0.117615274323557 \ 0.0330723218948563 \ -0.00999106135364955 \ 0.0333303352026631$ $-0.0635760921193727 \ -0.0978864728459570 \ 0.0101471996563584 \ -0.0474548145191703$ $0.115505280367130 \ 0.0279115395751556 \ -0.0681286515712746 \ -0.122396914926808$ $-0.0838928533126141 \ -0.0611582817121180 \ 0.133252353881465 \ -0.0777834326546494$ $0.0388675847331945 \ -0.0316788163313181 \ -0.0148897460359126$

Wjk is 39X2

-0.0337095227918965 -0.284363502208470 -0.103657890117210 0.00312369271914147 0.501239722921204 0.625476000336401 -0.0426668886667314 -0.0525941174672867-0.0334568496565777 -0.126361050595986 0.0896866334133813 -0.0160944446480960 -0.210973311495875 -0.122085487579645 -0.147061961169505 -0.0746243029369546 -0.0503097915793686 -0.100564284358652 -0.151165323903561 -0.0889024191193843 -0.229136248113805 -0.138731487953058 -0.236710569068868 -0.212650018876514 0.343371415819075 0.414764880852649 0.212782275176833 0.141969721374065 -0.268575687554513 -0.349562596003312 -0.217228513293514 0.0130162776785750 -0.356383758478093 -0.356588273402812 0.485236343008666 0.487386311145658 0.159260075540558 -0.0601767371625775

- $0.708315927142868 \ 0.736238354017106$
- -0.157801606859383 0.0542462297658544
- -0.224767942996655 -0.0579619552322774
- -0.123241894940539 -0.139556317196560
- -0.0922370552104423 -0.227582701085438
- -0.186614403282785 -0.383488794045763
- -0.129809179241090 -0.152096621040679
- -0.806980019203608 -0.806400588510975
- -0.105235157001332 -0.132815156838359
- -0.553212222608577 -0.459859473671445
- -0.0206310872695532 -0.109650362628761
- 0.0466861829217910 0.267926669798453
- 0.0342671703470048 -0.0776845544853902
- -0.00751575114146142 -0.162914801690849
- 3.22867989716808 3.19405164699631
- 0.993456860048897 0.964476818167372
- -0.227809423900753 -0.0417678994597344
- 0.0302554524437047 -0.0226765214035136
- -0.134499084961815 -0.185985486148993
- 0.487463939772401 0.258201209972127

With the help of these weights I was able to get ZERO error in most of the cases(Weights are initial)

Procedure followed:

- -First the data was extracted from the files taken from the online resouce.
- -Then it was normalized and converted into favourable format.
- -After some testing and using m/10 (m = # test cases) 39 was chosen as nH.
- -Some random initial weights were picjed and then used for forward mapping.
- -Using the training data and back propagation technique some weights were learned.
- -They helped in classifying the incoming test cases.

3.1. Diagram

