

## NANENG 512 Applied Digital Control and Drives Fall 2020

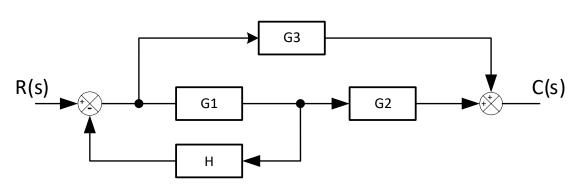
Name: ID#:

Duration: 30 mins.

## Problem 1

Prove that the transfer function of the following system is

$$\frac{C(S)}{R(s)} = \frac{G_1 G_2 + G_3}{1 + G_1 H}$$



Let 
$$G_1 = \frac{1}{s(s+2)}$$
  $G_2 = 3$   $G_3 = \frac{1}{s}$   $H = 5$ 

- 1- Find: Rise time  $t_r$  and maximum overshoot  $M_p$
- 2- Add controller  $G_c$  to the system and consider it a standard feedback system. Design  $G_c$  to decrease the maximum overshoot  $M_p$  to 10% and achieve a settling time  $t_s$  of 2 seconds.
- 3- What is the steady-state error when the input is a unit step after adding  $G_c$ ?

Hint: 
$$t_r = \frac{\pi - \theta}{\omega_n \sqrt{1 - \zeta^2}} \qquad M_p = e^{\frac{-\pi \zeta}{\sqrt{1 - \zeta^2}}} \qquad t_s = \frac{4}{\zeta \omega_n}$$