$$g(\mathbf{R}) = \bigcup_{i=1}^{4} g_i^* \left(\mathbf{R} \cap \mathbf{S_i} \right)$$