



# Image Segmentation



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## Segmentation :

- (i) Segmentation subdivides an image into its constituent parts or objects.
- (ii) Segmentation is based on two basic properties of gray level values: **Discontinuity** and **Similarity**

## [ I ] Segmentation using Discontinuity Property:

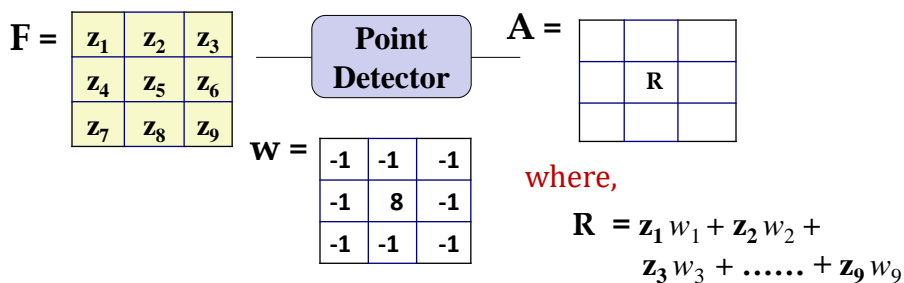
- In this category, image is partitioned into different parts or objects based on abrupt changes in gray level.
- This involves detection of isolated **POINTS** and **LINEs** and **EDGEs** in the image.

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### (1) POINT Detection

Consider a digital subimage F and point detector mask w



For any point P at (x,y) position,

If  $|R| > \text{Threshold}$

Then

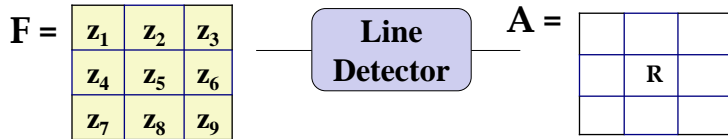
POINT is said to be detected at (x,y) position

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## (2) LINE Detection

Consider a digital subimage F and point detector mask w



Detection of a line can be done using the mask given below

-1	-1	-1
2	2	2
-1	-1	-1

**Horizontal  
Line**

-1	2	-1
-1	2	-1
-1	2	-1

**Vertical  
Line**

2	-1	-1
-1	2	-1
-1	-1	2

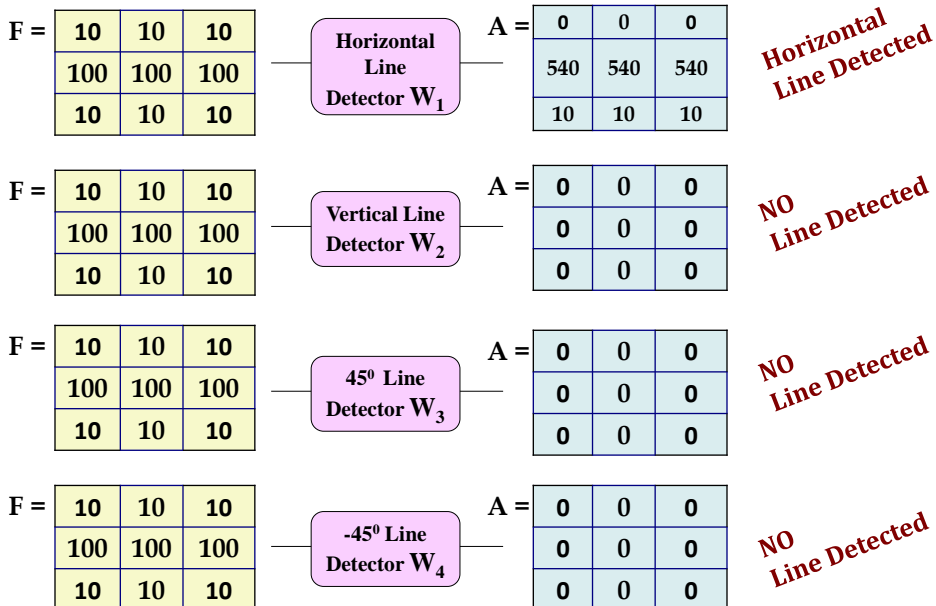
**45° Direction  
Line**

-1	-1	2
-1	2	-1
2	-1	-1

**-45° Direction  
Line**

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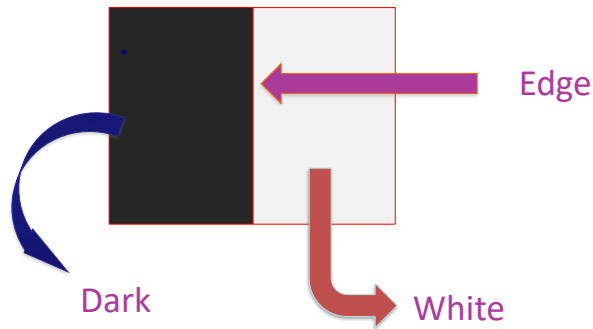


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### (3) EDGE Detection

- Edges are abrupt discontinuities in the Gray Levels
- Edge is defined as rate of change of continuity



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#### [A] Step Edge Detection

(i) Consider a Digital Image

$$F = \begin{bmatrix} 0 & 0 & 200 & 200 & 200 & 200 & 0 & 0 \\ 0 & 0 & 200 & 200 & 200 & 200 & 0 & 0 \\ 0 & 0 & 200 & 200 & 200 & 200 & 0 & 0 \end{bmatrix}$$

(ii) Pixel Values of Row -1 with repeated border values :

$$[ 0 \quad 0 \quad 0 \quad 200 \quad 200 \quad 200 \quad 200 \quad 0 \quad 0 \quad 0 ]$$

(iii) First Order Derivative i.e. Gradient :

$$[ 0 \quad 0 \quad 200 \quad 0 \quad 0 \quad 0 \quad -200 \quad 0 \quad 0 \quad 0 ]$$

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(iv) The Magnitude of First Order Derivative :

$$[ 0 \ 0 \ 200 \ 0 \ 0 \ 0 \ 200 \ 0 \ 0 \ 0 ]$$

(v) The Edge detected image :

F =

0	0	200	0	0	0	200	0	0
0	0	200	0	0	0	200	0	0
0	0	200	0	0	0	200	0	0

Sharp edge
Sharp edge

- Magnitude of First order derivative produces desirable effect. i.e. Sharp Edges.

**Therefore, first derivative mask such as Robert, Prewitt, Sobel and Fri-chen are suitable to detect Step Edges.**

(iii) First Order Derivative i.e. Gradient :

$$[ 0 \ 0 \ 200 \ 0 \ 0 \ 0 \ -200 \ 0 \ 0 \ 0 ]$$

(iv) Second Order Derivative i.e. Laplacian :

$$[ 0 \ 200 \ -200 \ 0 \ 0 \ -200 \ 200 \ 0 \ 0 \ 0 ]$$

(v) Magnitude of Second Order Derivative

$$[ 0 \ 200 \ 200 \ 0 \ 0 \ 200 \ 200 \ 0 \ 0 \ 0 ]$$

(v) The Magnitude of Second Order Derivative :

$$[ 0 \quad 200 \quad 200 \quad 0 \quad 0 \quad 200 \quad 200 \quad 0 \quad 0 ]$$

(vi) The Edge detected image :

F =

0	0	200	200	0	0	200	200	0	0
0	0	200	200	0	0	200	200	0	0
0	0	200	200	0	0	200	200	0	0

Double edges
Double edges

- Magnitude of second order derivative produces double edges which is NOT desirable.

**Therefore, Second order derivative mask such as Laplacian mask is NOT suitable to detect Step Edges.**

## [B] Ramp Edge Detection

(i) Consider a Digital Image

$$F = \begin{bmatrix} 0 & 0 & 80 & 160 & 240 & 240 & 240 & 240 \\ 0 & 0 & 80 & 160 & 240 & 240 & 240 & 240 \\ 0 & 0 & 80 & 160 & 240 & 240 & 240 & 240 \end{bmatrix}$$

(ii) Pixel Values of Row -1 with repeated border Values :

$$[ 0 \quad 0 \quad 0 \quad 80 \quad 160 \quad 240 \quad 240 \quad 240 \quad 240 \quad 240 ]$$

(iii) First Order Derivative i.e. Gradient :

$$[ 0 \quad 0 \quad 80 \quad 80 \quad 80 \quad 0 \quad 0 \quad 0 \quad 0 ]$$

(iv) The Magnitude of First Order Derivative :

[ 0 0 80 80 80 0 0 0 0 ]

(v) The Edge detected image :

F =

0	0	80	80	80	0	0	0
0	0	80	80	80	0	0	0
0	0	80	80	80	0	0	0

Thick edge

- Magnitude of First order derivative produces Thick Edge which is Not desirable
- Therefore, first derivative mask such as Robert, Prewitt, Sobel and Fri-chen are NOT suitable to detect Ramp Edges

(iii) First Order Derivative i.e. Gradient :

[ 0 0 80 80 80 0 0 0 0 ]

(iv) Second Order Derivative i.e. Laplacian :

[ 0 80 0 0 -80 0 0 0 0 ]

(v) Magnitude of Second Order Derivative

[ 0 80 0 0 80 0 0 0 0 ]



(v) The Magnitude of Second Order Derivative :

[ 0 80 0 0 80 0 0 0 0 0 ]

(vi) The Edge detected image :

F =

0	0	80	0	0	80	0	0	0	0
0	0	80	0	0	80	0	0	0	0
0	0	80	0	0	80	0	0	0	0

Sharp edge      Sharp edge

- Second order derivative produces desirable results..i.e. Sharp Edges.

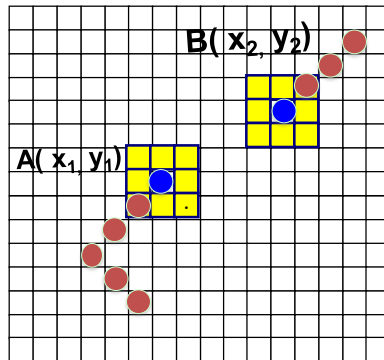
Therefore, Second order derivative mask such as Lapacian mask is the most suitable to detect Ramp Edges.

## Edge Linking and Boundary Detection

- Edge Detection Algorithm is followed by Linking procedures to assemble edge pixels into meaningful edges.
- Edge Linking Methods :
  - (1) Edge Linking using Local Processing
  - (2) Edge Linking using Global Processing Hough Transform Method
  - (3) Edge Linking using Global Processing Graph Theoretic Method

## • Edge Linking using Local Processing

- (i) Consider two edge points  $A(x_1, y_1)$  and  $B(x_2, y_2)$  as shown in figure below



- (ii) Select a small neighbourhood say 3x3.

### Edge Linking using Local Processing . . . .

- (iii) Analyse the characteristics of edge pixels in a small neighbourhood say 3x3.
- (iv) Link all the points that are similar according to a set of predefined criteria
- (v) Two basic properties of pixels are :
- a) Strength of Gradient
  - b) Direction of Gradient

- (v) An edge pixels with co-ordinates  $(x', y')$  is similar in magnitude to the pixel at  $(x, y)$  if the following condition is satisfied

$$\text{If } \left| \nabla f(x, y) - \nabla f(x', y') \right| \leq \text{Magnitude Threshold}$$

Where

$$\nabla f(x, y) = |G_x| + |G_y|$$

- (vi) An edge pixels with co-ordinates  $(x', y')$  is similar in direction to the pixel at  $(x, y)$  if the following condition is satisfied

$$\text{If } \left| \alpha(x, y) - \alpha(x', y') \right| \leq \text{Angle Threshold}$$

Where

$$\alpha(x, y) = \tan^{-1} \left( \frac{G_y}{G_x} \right)$$

That means,

$$\begin{aligned} \text{If } & \left| \nabla f(x, y) - \nabla f(x', y') \right| \leq \text{Magnitude Threshold} \\ \text{AND} \\ & \left| \alpha(x, y) - \alpha(x', y') \right| \leq \text{Angle Threshold} \end{aligned}$$

**Then**

Two pixels at  $(x, y)$  and  $(x', y')$  can be linked.

- **Edge Linking using Global Processing Hough Transform Method**

**(1) Hough Transform :**

Consider two points  $A(x_1, y_1)$  and  $B(x_2, y_2)$  in  $xy$  plane

The equation of the line passing through AB is then given by,

$$y = m x + c$$

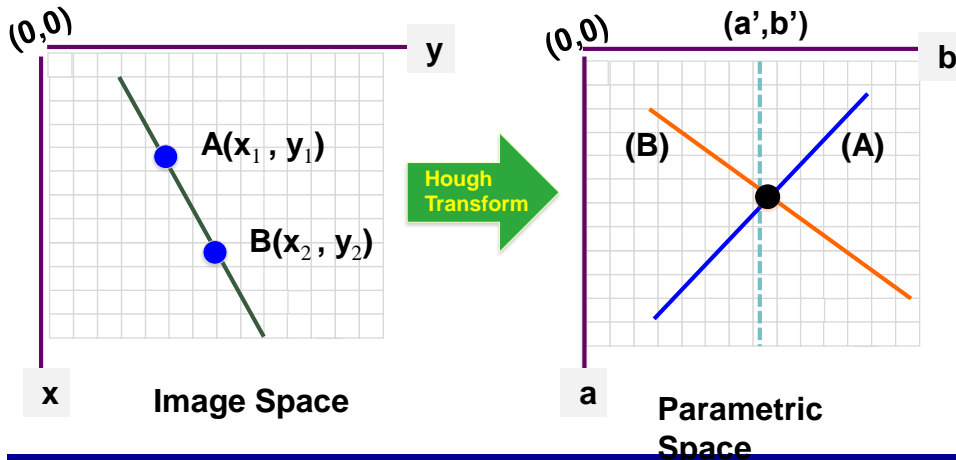
Let  $y = a x + b$  where  $a$  is slope value and  $b$  is y-intercept value

$$b = -a x + y$$

At  $A(x_1, y_1)$ ,  $b = -a x_1 + y_1$

At  $B(x_2, y_2)$ ,  $b = -a x_2 + y_2$

$$b = -a x + y$$



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(i) Hough Transformation is POINT to LINE and LINE to POINT Transformation from xy plane (Image Space) to ab plane (Parametric Space)

(ii) At each intersecting point in ab-plane, we get slope value and y-constant value of line that exist in xy-plane.

(iii) The equation of line is given by,

$$Y = a' x + b' \rightarrow \text{THIS IS LINE AB}$$

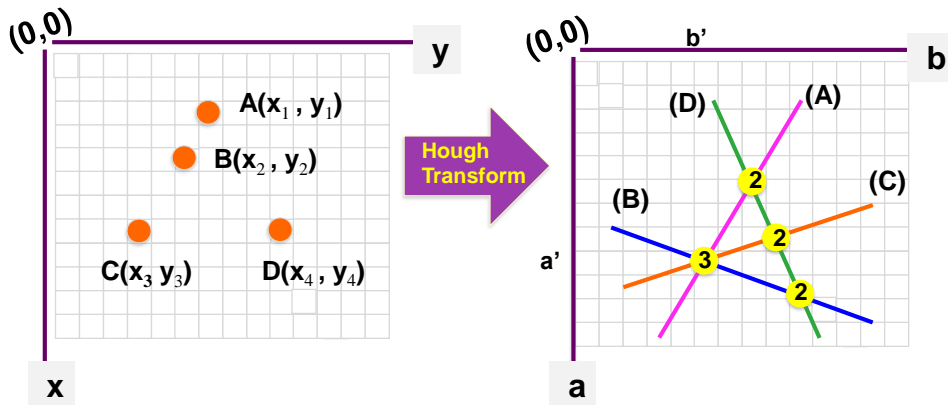
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## (2) Edge Linking using Hough Transform

(I) Map all the input points from xy plane to ab plane using Hough Transform

e.g. Consider 4 input points A, B, C and D as shown in figure.



Edge Linking using Hough Transform . . . .

(II) Count the number of intersecting lines at each point in ab plane.

(III) Select the point with maximum value of count.

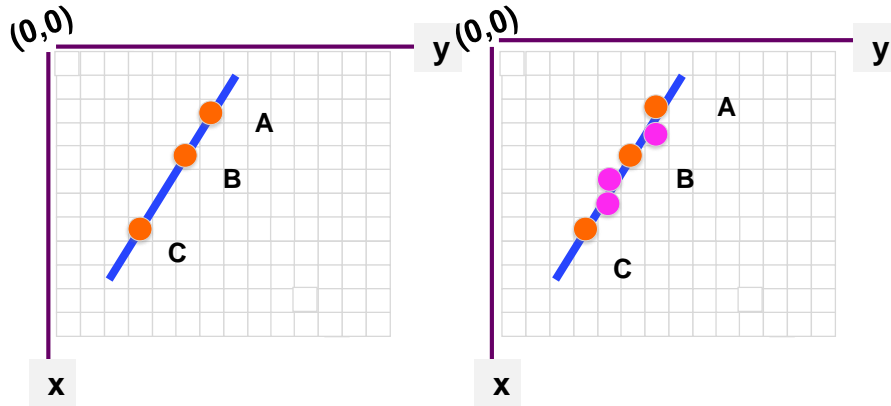
E.g. Max value of count is 3 at point (a',b')

(III) Define line with slope value =  $a'$  and Y-constant value =  $b'$ . The equation of line is  $y = a' x + b'$

(IV) Determine co-linear points..

E.g. Point A, B and C are co-linear points.

(V) Link all co-linear points.



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### (3) Limitation of Hough Transform :

- (i) Hough Transform method is not suitable for vertical edges
- (ii) For vertical line, slope value is  $\infty$

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## Paul V. C. Hough

The Hough transform was first proposed by **Paul Hough** in 1962 as a method for detecting lines in images.



It was made popular by Duda and Hart: Duda, R. O. and P. E. Hart, "Use of the Hough Transformation to Detect Lines and Curves in Pictures", 1972.

Ref.

The Hough transform was patented as U.S. Patent 3,069,654 in 1962 and assigned to the U.S. Atomic Energy Commission with the name "Method and Means for Recognizing Complex Patterns". This patent uses a slope-intercept parametrization for straight lines

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## Overview of Hough Transform :

- The Hough transform is a mathematical technique used in computer vision and image analysis to detect simple geometric shapes like lines, circles, and ellipses.
- The basic idea behind the Hough transform is to represent lines or curves in an image as points in a parameter space.
- The Hough transform is a powerful tool for line and curve detection in images, particularly when traditional edge detection techniques fail.
- Its ability to handle broken and incomplete lines makes it a valuable addition to any image processing toolkit

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## Q1. What is Hough Transform?

- The Hough transform in image processing is a technique used to detect simple geometric shapes in images.
- It works by transforming the image space into a parameter space, where the geometric shapes can be detected through the identification of patterns in the parameter space.

## Q2. Why is Hough Transform Needed?

- The Hough transform is needed because traditional image processing techniques like edge detection and thresholding are not always effective at detecting simple geometric shapes in images. These techniques can be particularly ineffective when the shapes are distorted, incomplete, or partially obscured.
- The Hough transform can detect these shapes by transforming the image space into a parameter space where the shapes can be more easily identified.



Input image

Edge detected image

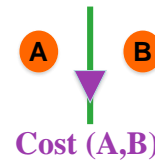
Edge detected image  
processed using  
Hough Transform

## ▪ Edge Linking using Graph Theoretic Method

- (i) In this Method, edge is represented in the form of Graph
- (ii) Edge is also called as Path and Low cost path corresponds to the most significant edge in the image
- (iii) Consider Two pixels A and B
- (iv) The Cost between A and B is given by,

$$\text{Cost (A,B)} = H - |F(A) - F(B)|$$

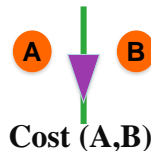
Where H is the max gray value in the image  
F(A) and F(B) are pixel values at point A and at point B respectively



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e.g.

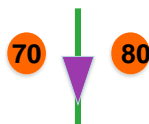


$$\text{Cost (A,B)} = H - |F(A) - F(B)|$$

Assume H = 255

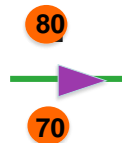
$$\text{Cost (A,B)} = 255 - |F(A) - F(B)|$$

Case-1 :



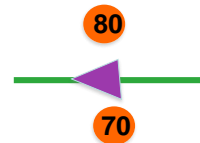
$$\begin{aligned} \text{Cost} &= 255 - |70 - 80| \\ \text{Cost} &= 245 \end{aligned}$$

Case-2 :



$$\begin{aligned} \text{Cost} &= 255 - |70 - 80| \\ \text{Cost} &= 245 \end{aligned}$$

Case-3 :



$$\begin{aligned} \text{Cost} &= 255 - |80 - 70| \\ \text{Cost} &= 245 \end{aligned}$$

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**Example :**

Assume that the edge starts in the first Row and ends in the last row for the following Gray Image.

$$F = \begin{array}{|c|c|c|} \hline 5 & 6 & 1 \\ \hline 6 & 7 & 0 \\ \hline 7 & 1 & 3 \\ \hline \end{array}$$

Sketch all possible paths and determine the edge corresponding to minimum cost path

**Solution :**

The Cost between tow pixels A and B is given by,

$$\text{Cost (A,B)} = H - |F(A) - F(B)|$$

Where  $H = 7$  is the max gray value in the image

$F(A)$  and  $F(B)$  are pixel values at point A and at point B

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**(1) For Edge-1 :**

5		6	1
	↓		
6		7	0
	↓		
7		1	3
	↓		

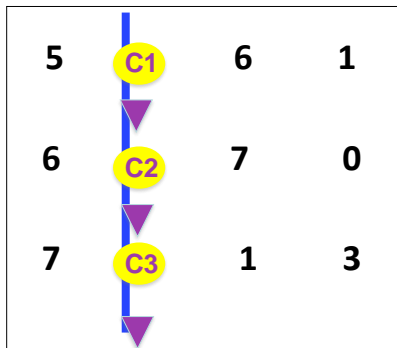
$$\text{Cost (A,B)} = H - |F(A) - F(B)|$$

$$\text{Cost (A,B)} = 7 - |F(A) - F(B)|$$

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(1) For Edge-1 :



$$\begin{aligned}\text{Cost (E1)} &= C1 + C2 + C3 \\ &= 6 + 6 + 1 \\ &= 13\end{aligned}$$

(i) To find C1

$$C1 = 7 - |F(A) - F(B)|$$

$$C1 = 7 - |5 - 6|$$

$$C1 = 6$$

(ii) To find C2

$$C2 = 7 - |F(A) - F(B)|$$

$$C2 = 6$$

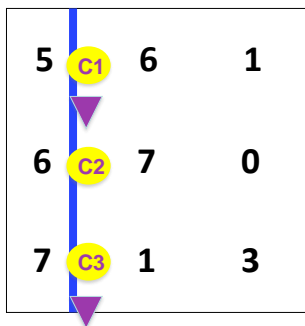
(ii) To find C3

$$C3 = 7 - |F(A) - F(B)|$$

$$C3 = 7 - |7 - 1|$$

$$C3 = 1$$

(1) For Edge-1 :

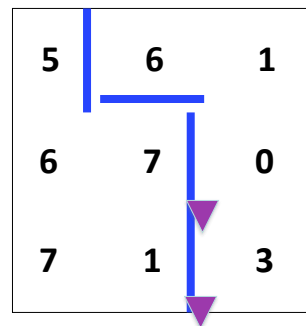


$$\text{Cost (E1)} = C1 + C2 + C3$$

$$\text{Cost (E1)} = 6 + 6 + 1$$

$$\text{Cost (E1)} == 13$$

(2) For Edge-2 :

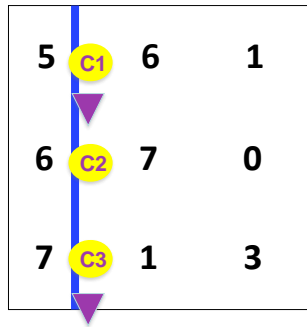


$$\text{Cost (E1)} = C1 + C2 + C3 + C4$$

$$\text{Cost(E2)} = 6 + 6 + 0 + 5$$

$$\text{Cost (E2)} == 13$$

(1) For Edge-1 :

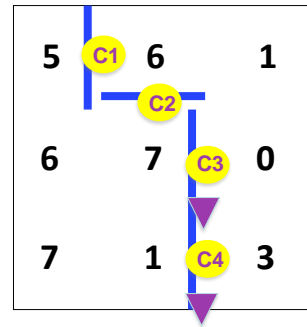


$$\text{Cost (E1)} = C1 + C2 + C3$$

$$\text{Cost (E1)} = 6 + 6 + 1$$

$$\text{Cost (E1)} == 13$$

(2) For Edge-2 :



$$\text{Cost (E1)} = C1 + C2 + C3 + C4$$

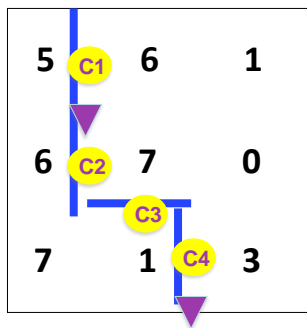
$$\text{Cost(E2)} = 6 + 6 + 0 + 5$$

$$\text{Cost (E2)} == 13$$

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(3) For Edge-3 :

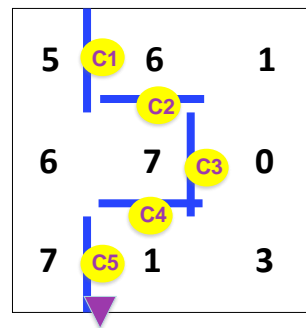


$$\text{Cost (E3)} = C1 + C2 + C3 + C4$$

$$\text{Cost (E3)} = 6 + 6 + 1 + 5$$

$$\text{Cost (E3)} == 18$$

(4) For Edge-4 :



$$\text{Cost (E4)} = C1 + C2 + C3 + C4 + C5$$

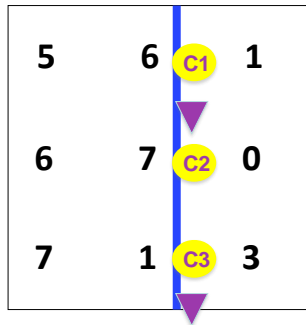
$$\text{Cost(E4)} = 6 + 6 + 0 + 1 + 1$$

$$\text{Cost (E4)} == 14$$

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(5) For Edge-5 :

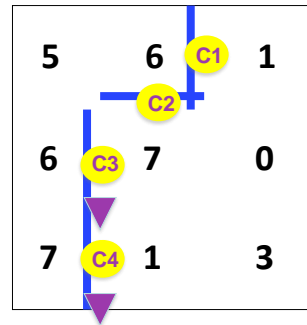


$$\text{Cost (E5)} = C1 + C2 + C3$$

$$\text{Cost (E5)} = 2 + 0 + 5$$

$$\text{Cost (E5)} == 13$$

(6) For Edge-6 :



$$\text{Cost (E6)} = C1 + C2 + C3 + C4$$

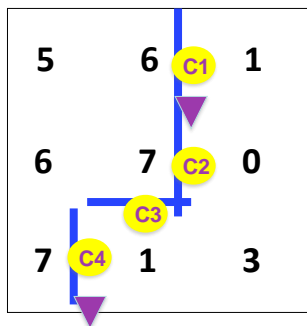
$$\text{Cost(E6)} = 2 + 6 + 6 + 1$$

$$\text{Cost (E6)} == 15$$

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(7) For Edge-7 :

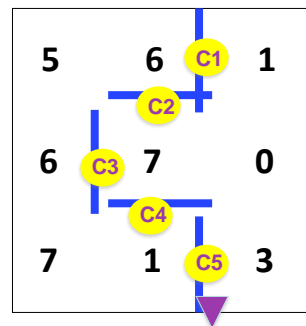


$$\text{Cost (E7)} = C1 + C2 + C3 + C4$$

$$\text{Cost (E7)} = 2 + 0 + 1 + 1$$

$$\text{Cost (E7)} == 4$$

(8) For Edge-8 :



$$\text{Cost (E8)} = C1 + C2 + C3 + C4 + C5$$

$$\text{Cost(E8)} = 2 + 6 + 6 + 1 + 5$$

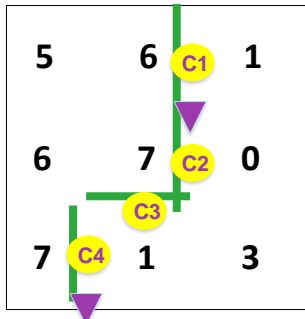
$$\text{Cost (E8)} == 20$$

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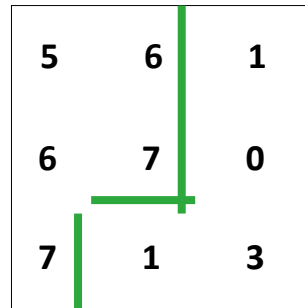
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Edge-7 has the minimum value of Cost.  
Therefore, Edge-7 is the most significant edge in the image

For Edge-7, Let  $F(A) = 7$  and  $F(B) = 0$  and  $F(\text{other}) = 0$



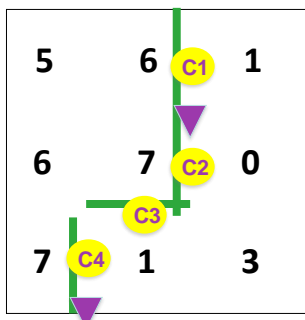
Input Image



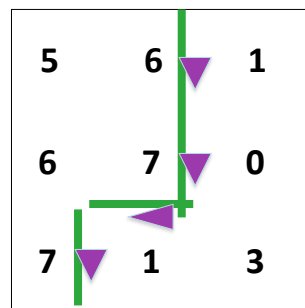
Output Image

Edge-7 has the minimum value of Cost.  
Therefore, Edge-7 is the most significant edge in the image

For Edge-7, Let  $F(A) = 7$  and  $F(B) = 0$  and  $F(\text{other}) = 0$



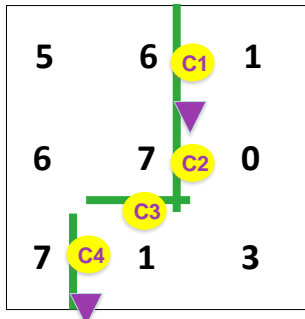
Input Image



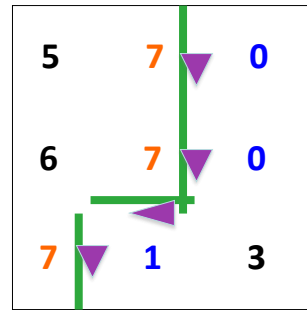
Output Image

Edge-7 has the minimum value of Cost.  
Therefore, Edge-7 is the most significant edge in the image

For Edge-7, Let  $F(A) = 7$  and  $F(B) = 0$  and  $F(\text{other}) = 0$



Input Image



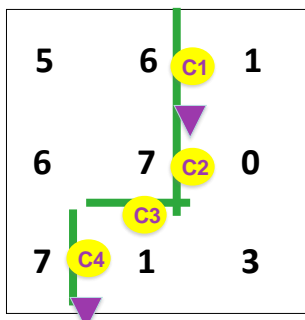
Output Image

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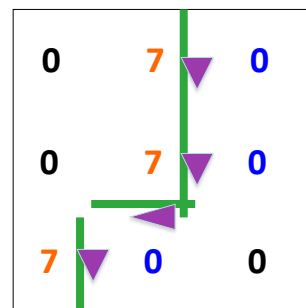
47

Edge-7 has the minimum value of Cost.  
Therefore, Edge-7 is the most significant edge in the image

For Edge-7, Let  $F(A) = 7$  and  $F(B) = 0$  and  $F(\text{other}) = 0$



Input Image



Output Image

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Edge-7 has the minimum value of Cost.  
Therefore, Edge-7 is the most significant edge in the image

For Edge-7, Let  $F(A) = 7$  and  $F(B) = 0$  and  $F(\text{other}) = 0$

5	6	1
6	7	0
7	1	3

Input Image

0	7	0
0	7	0
7	0	0

Output Image

## [II] Segmentation using Similarity property:

- In this category, Image is partitioned into regions based on Similarity in gray level.
- This involves detection of region.
- Let  $R$  represents the entire image and  $R_1, R_2, \dots, R_N$  are segmented regions such that,
  - (i)  $\bigcup_{i=1} R_i = R$
  - (ii)  $R_i$  is connected Region
  - (iii)  $R_i \cap R_j = \text{Null}$  for all  $i$  and  $j$
  - (iv) Predicate ( $R_i$ ) = TRUE for all  $i$

## (A) Region Growing by Pixel Aggregation :-

- (i) Region growing is a procedure that groups pixels into larger regions.
- (ii) Pixel aggregation procedure starts with a seed point AND Neighbouring pixels that have similar values are appended

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Example-1 :

F =

0	1	2	3
0	1	2	3
0	4	5	6
4	5	6	7

Predicate :

If  $F(x,y) = \{ 0, 1, 2, 3 \}$

Then  $F(x,y) = \text{Red}$

Else  $F(x,y) = \text{Yellow}$

F =

0	1	2	3
0	1	2	3
0	4	5	6
4	5	6	7

F =

0	1	2	3
0	1	2	3
0	4	5	6
4	5	6	7

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Ex-2: Segment the following given image using Region Growing by Pixel Aggregation.

Assume Threshold=2.

Predicate :

Let Seed Point be  $S(x',y')$

If  $|F(x,y) - S(x',y')| \leq T$

Then  $F(x,y) =$  Intensity of  
Segmented  
Region

	0	1	2	3	4	5	6	7
0	3	3	2	3	2	1	4	3
1	1	5	3	2	7	5	6	4
2	2	1	2	6	4	7	3	5
3	4	5	6	7	7	6	2	0
4	4	5	6	7	4	0	3	2
5	7	7	6	5	2	3	3	1
6	1	1	0	0	3	1	2	1
7	2	3	4	3	3	4	3	2

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(I) Let Seed Point  $S_1(4,1) = 5$  and  $T = 2$

Predicate :

If  $|F(x,y) - S_1(4,1)| \leq T$

i.e.  $|F(x,y) - 5| \leq 2$

i.e.  $F(x,y) = \{ 3, 4, 5, 6, 7 \}$

Then  $F(x,y) = A$

Segmented Region :  $R_1 = \{ A \}$

	0	1	2	3	4	5	6	7
0	3	3	2	3	2	1	A	A
1	1	5	3	2	A	A	A	A
2	2	1	2	A	A	A	A	A
3	A	A	A	A	A	A	2	0
4	A	A	A	A	A	0	3	2
5	A	A	A	A	2	3	3	1
6	1	1	0	0	3	1	2	1
7	2	3	4	3	3	4	3	2

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(II) Let Seed Point  $S_2(0,0) = 3$  and  $T = 2$

Predicate :

If  $|F(x,y) - S_2(0,0)| \leq T$

i.e.  $|F(x,y) - 3| \leq 2$

**i.e.  $F(x,y) = \{ 1, 2, 3, 4, 5 \}$**

Then  $F(x,y) = B$

**Segmented Region :  $R_2 = \{ B \}$**

	0	1	2	3	4	5	6	7
0	B	B	B	B	B	B	A	A
1	B	B	B	B	A	A	A	A
2	B	B	B	A	A	A	A	A
3	A	A	A	A	A	A	2	0
4	A	A	A	A	A	0	3	2
5	A	A	A	A	2	3	3	1
6	1	1	0	0	3	1	2	1
7	2	3	4	3	3	4	3	2

(III) Let Seed Point  $S_3(6,1) = 2$  and  $T = 2$

Predicate :

If  $|F(x,y) - S_3(6,1)| \leq T$

i.e.  $|F(x,y) - 2| \leq 2$

**i.e.  $F(x,y) = \{ 0, 1, 2, 3, 4 \}$**

Then  $F(x,y) = C$

**Segmented Region :  $R_3 = \{ C \}$**

	0	1	2	3	4	5	6	7
0	B	B	B	B	B	B	A	A
1	B	B	B	B	A	A	A	A
2	B	B	B	A	A	A	A	A
3	A	A	A	A	A	A	C	C
4	A	A	A	A	A	C	C	C
5	A	A	A	A	C	C	C	C
6	C	C	C	C	C	C	C	C
7	C	C	C	C	C	C	C	C

**No of Segmented Regions : 3**

**$R = R_1 \cup R_2 \cup R_3$**

## (B) Region Splitting & Merging :-

In this method,

- First an image is **subdivided** into a set of regions and
- Then subdivided adjacent regions are **merged** to form a new region.

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Ex-1 :

10	10	80	80
10	10	80	80
50	50	80	80
50	50	80	80

**Predicate** : All the pixels in the image must have same intensity value.

By Splitting :

10	10	80	80
10	10	80	80
50	50	80	80
50	50	80	80

By Merging :

10	10	80	80
10	10	80	80
50	50	80	80
50	50	80	80

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Ex-2 : Segment the following given image such that the difference between the Maximum intensity value and the minimum intensity value in the segmented region is less than 8 using Region Splitting & Merging Technique

10	9	30	4
7	6	33	37
50	52	54	53
55	52	56	58

**Predicate** for Splitting:

For Any Region R ;

IF  $|\text{Max Intensity Value} - \text{Min Intensity Value}| \geq 8$

Then Split the region into 4 parts

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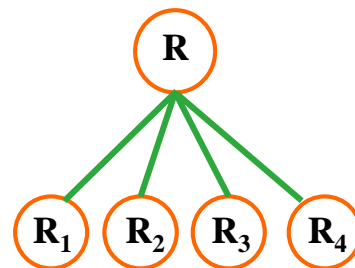
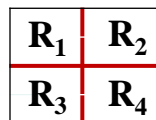
### Step-1 : Region Splitting

**Predicate** for Splitting:

For Any Region R ;

IF  $|\text{Max Intensity Value} - \text{Min Intensity Value}| \geq 8$

Then Split the region into 4 parts



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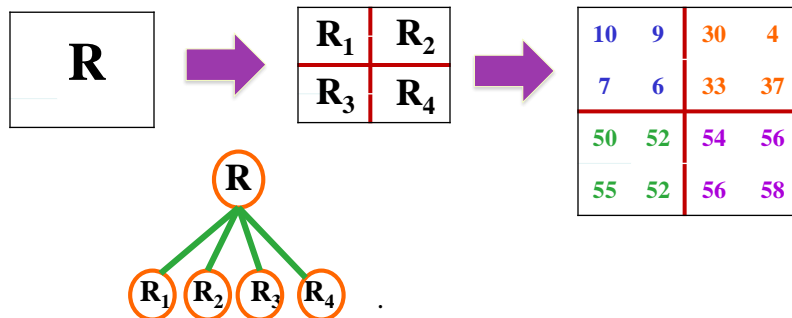
60

### (1) For Input Image R

$I_{\max} = 58$      $I_{\min} = 4$   
 $I_{\max} - I_{\min} = 54 \geq 8$   
 Predicate (R) = **TRUE**

10	9	30	4
7	6	33	37
50	52	54	53
55	52	56	58

So, Split the region R into 4 parts



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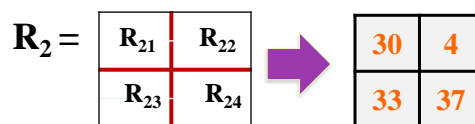
### (2) For Region R1

$I_{\max} = 10$      $I_{\min} = 6$   
 $I_{\max} - I_{\min} = 4$   
 Predicate (R) = **FALSE**

### (3) For Region R2

$I_{\max} = 37$      $I_{min} = 4$   
 $I_{\max} - I_{\min} = 33$   
 Predicate (R) = **TRUE**

So, Split the region **R<sub>2</sub>** into 4 parts



<b>R<sub>1</sub></b>	<b>R<sub>2</sub></b>	10	9	30	4
<b>R<sub>3</sub></b>	<b>R<sub>4</sub></b>	7	6	33	37
		50	52	54	56
		55	52	56	58


<b>R<sub>1</sub></b>	<b>R<sub>2</sub></b>	10	9	30	4
<b>R<sub>3</sub></b>	<b>R<sub>4</sub></b>	7	6	33	37
		50	52	54	56
		55	52	56	58

#### (4) For Region R3

$I_{\max} = 55$   $I_{\min} = 50$

$I_{\max} - I_{\min} = 5$

Predicate (R) = **FALSE**

$R_1$	$R_2$	
$R_3$	$R_4$	

10	9	30	4
7	6	33	37
50	52	54	56
55	52	56	58


#### (5) For Region R4

$I_{\max} = 58$   $I_{\min} = 54$

$I_{\max} - I_{\min} = 4$

Predicate (R) = **FALSE**

$R_1$	$R_2$
$R_3$	$R_4$

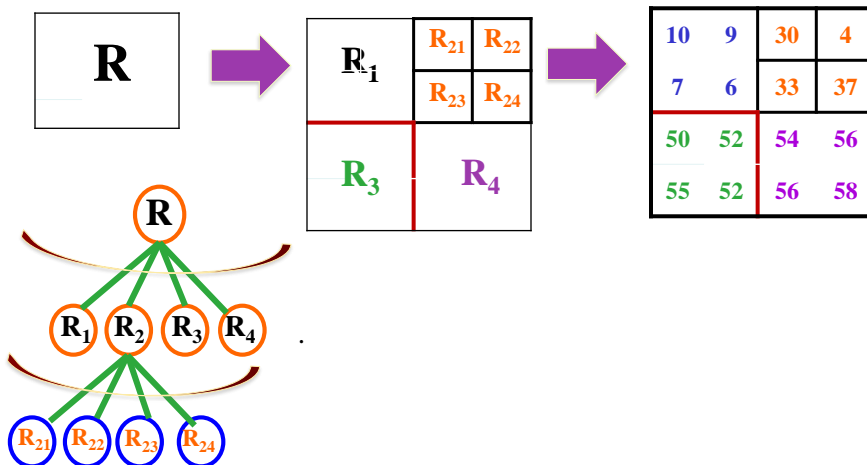


10	9	30	4
7	6	33	37
50	52	54	56
55	52	56	58

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### Result of Splitting



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## Step-1 : Region Merging

Predicate for Merging

For adjacent Regions  $R_A$  and  $R_B$

IF  $| \text{Max Intensity Value} - \text{Min Intensity Value} | < 8$

Then Merge the regions :

Let  $M_{AB} = R_A \cup R_B$

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(I) For adjacent Regions

$R_{21}$   $R_{22}$   $R_{23}$  and  $R_{24}$

1. For  $\{ R_{21} \cup R_{23} \}$

$I_{\max} = 33$   $I_{\min} = 30$

$I_{\max} - I_{\min} = 3 < 8$

Predicate = **TRUE**

Merge the regions

Let  $M_1 = \{ R_{21} \cup R_{23} \}$

$R_1$	$R_{21}$	$R_{22}$	10	9	30	4
	$R_{23}$	$R_{24}$				
$R_3$	$R_4$		7	6	33	37
			50	52	54	56
			55	52	56	58

$R_1$	$M_1$	$R_2$	10	9	30	4
		$R_2$				
$R_3$	$R_4$		7	6	33	37
			50	52	54	56
			55	52	56	58

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2. For  $\{M_1 \cup R_{24}\}$

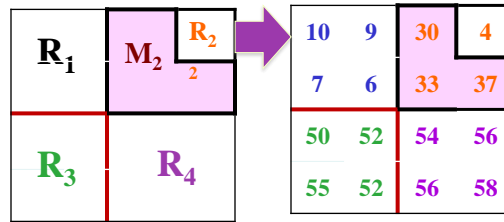
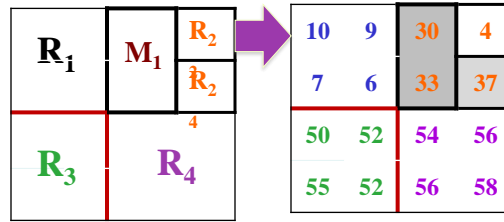
$I_{\max} = 37$   $I_{\min} = 30$

$I_{\max} - I_{\min} = 7 < 8$

Predicate = **TRUE**

Merge the regions

Let  $M_2 = \{M_1 \cup R_{24}\}$



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3. For  $\{R_3 \cup R_4\}$

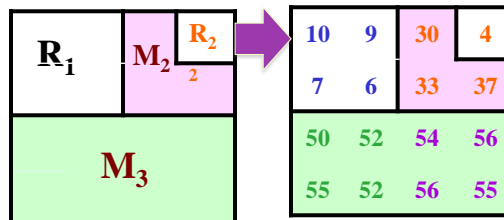
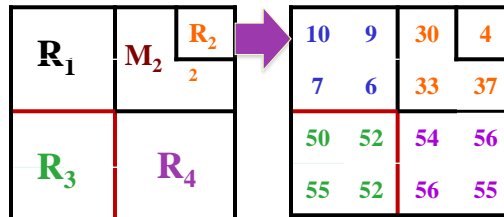
$I_{\max} = 56$   $I_{\min} = 50$

$I_{\max} - I_{\min} = 6 < 8$

Predicate = **TRUE**

Merge the regions

Let  $M_3 = \{R_3 \cup R_4\}$



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## Result of Segmentation :

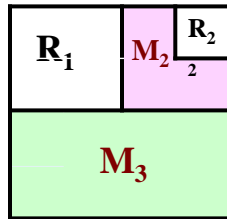
1) No of Segmented Regions = 4

Such that  $R = R_1 \cup R_{22} \cup M_2 \cup M_3$

2) Let  $R_1 = \{ A \}$ ,  $R_{22} = \{ B \}$ ,  $M_2 = \{ C \}$  and  $M_3 = \{ D \}$

10	9	30	4
7	6	33	37
50	52	54	53
55	52	56	55

Input IMAGE



A	A	C	B
A	A	C	C
D	D	D	D
D	D	D	D

Segmented IMAGE

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- He is a Treasurer of IEEE Bombay Section and Mentor for Startup Incubation & Intellectual Asset Creation.
- He received incentives for excellent performance in academics and research from Management of S.P.I.T. in 2008-09. He is a recipient of P.R. Bapat IEEE Bombay Section Outstanding Volunteer Award 2019.

