

Comparison of number of decisions in overlapping and non-overlapping sudokus using SAT-solvers.

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Overview

- Introduction & Hypothesis
- Method
- Results
- Discussion and conclusion

Introduction & Hypothesis

- Sat Solvers
- Conjunctive Normal Form (CNF)
- Overlapping sudokus

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 9 | 5 | 6 | 7 | 1 | 4 | 3 | 8 | | | | | | |
| 6 | 1 | 8 | 3 | 4 | 2 | 5 | 7 | 9 | | | | | | |
| 8 | 3 | 6 | 5 | 9 | 4 | 7 | 1 | 2 | | | | | | |
| 9 | 4 | 1 | 7 | 2 | 6 | 8 | 5 | 3 | | | | | | |
| 7 | 5 | 2 | 8 | 1 | 3 | 9 | 6 | 4 | | | | | | |
| 1 | 2 | 3 | 4 | 5 | 9 | 6 | 8 | 7 | 1 | 2 | 3 | 9 | 4 | 5 |
| 4 | 6 | 7 | 1 | 3 | 8 | 2 | 9 | 5 | 6 | 7 | 4 | 8 | 1 | 3 |
| 5 | 8 | 9 | 2 | 6 | 7 | 3 | 4 | 1 | 9 | 8 | 5 | 7 | 6 | 2 |
| | | | | | | 4 | 7 | 9 | 3 | 6 | 1 | 2 | 5 | 8 |
| | | | | | | 1 | 2 | 3 | 4 | 5 | 8 | 6 | 7 | 9 |
| | | | | | | 5 | 6 | 8 | 7 | 9 | 2 | 1 | 3 | 4 |
| | | | | | | 8 | 3 | 4 | 2 | 1 | 6 | 5 | 9 | 7 |
| | | | | | | 9 | 1 | 2 | 5 | 3 | 7 | 4 | 8 | 6 |

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|
| 3 | 6 | 2 | 5 | 9 | 7 | 8 | 4 | 1 | | | | | | |
| 4 | 7 | 1 | 6 | 8 | 3 | 5 | 2 | 9 | | | | | | |
| 8 | 9 | 5 | 1 | 2 | 4 | 6 | 3 | 7 | | | | | | |
| 5 | 4 | 6 | 7 | 1 | 2 | 9 | 8 | 3 | | | | | | |
| 2 | 1 | 3 | 9 | 4 | 8 | 7 | 6 | 5 | 9 | 1 | 2 | 3 | | |
| 7 | 8 | 9 | 3 | 5 | 6 | 2 | 1 | 4 | 3 | 7 | 8 | 9 | | |
| 6 | 5 | 8 | 4 | 3 | 9 | 1 | 7 | 2 | 8 | 4 | 5 | 6 | | |
| 1 | 2 | 4 | 8 | 7 | 5 | 3 | 9 | 6 | 1 | 2 | 4 | 8 | | |
| 9 | 3 | 7 | 2 | 6 | 1 | 4 | 5 | 8 | 2 | 3 | 9 | 7 | | |
| | | | | 9 | 2 | 8 | 4 | 3 | 7 | 5 | 6 | 1 | | |
| | | | | 8 | 3 | 6 | 2 | 1 | 5 | 9 | 7 | 4 | | |
| | | | | 2 | 4 | 9 | 3 | 7 | 6 | 8 | 1 | 5 | | |
| | | | | 1 | 7 | 5 | 8 | 9 | 4 | 6 | 3 | 2 | | |

Introduction & Hypothesis

- The total number of decisions will be lower in one overlapping sudoku, compared to solving two non-overlapping sudokus.

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 9 | 5 | 6 | 7 | 1 | 4 | 3 | 8 | | | | | | |
| 6 | 1 | 8 | 3 | 4 | 2 | 5 | 7 | 9 | | | | | | |
| 8 | 3 | 6 | 5 | 9 | 4 | 7 | 1 | 2 | | | | | | |
| 9 | 4 | 1 | 7 | 2 | 6 | 8 | 5 | 3 | | | | | | |
| 7 | 5 | 2 | 8 | 1 | 3 | 9 | 6 | 4 | | | | | | |
| 1 | 2 | 3 | 4 | 5 | 9 | 6 | 8 | 7 | 1 | 2 | 3 | 9 | 4 | 5 |
| 4 | 6 | 7 | 1 | 3 | 8 | 2 | 9 | 5 | 6 | 7 | 4 | 8 | 1 | 3 |
| 5 | 8 | 9 | 2 | 6 | 7 | 3 | 4 | 1 | 9 | 8 | 5 | 7 | 6 | 2 |
| | | | | | | 4 | 7 | 9 | 3 | 6 | 1 | 2 | 5 | 8 |
| | | | | | | 1 | 2 | 3 | 4 | 5 | 8 | 6 | 7 | 9 |
| | | | | | | 5 | 6 | 8 | 7 | 9 | 2 | 1 | 3 | 4 |
| | | | | | | 8 | 3 | 4 | 2 | 1 | 6 | 5 | 9 | 7 |
| | | | | | | 9 | 1 | 2 | 5 | 3 | 7 | 4 | 8 | 6 |

| | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|--|
| 3 | 6 | 2 | 5 | 9 | 7 | 8 | 4 | 1 | | | | | |
| 4 | 7 | 1 | 6 | 8 | 3 | 5 | 2 | 9 | | | | | |
| 8 | 9 | 5 | 1 | 2 | 4 | 6 | 3 | 7 | | | | | |
| 5 | 4 | 6 | 7 | 1 | 2 | 9 | 8 | 3 | | | | | |
| 2 | 1 | 3 | 9 | 4 | 8 | 7 | 6 | 5 | 9 | 1 | 2 | 3 | |
| 7 | 8 | 9 | 3 | 5 | 6 | 2 | 1 | 4 | 3 | 7 | 8 | 9 | |
| 6 | 5 | 8 | 4 | 3 | 9 | 1 | 7 | 2 | 8 | 4 | 5 | 6 | |
| 1 | 2 | 4 | 8 | 7 | 5 | 3 | 9 | 6 | 1 | 2 | 4 | 8 | |
| 9 | 3 | 7 | 2 | 6 | 1 | 4 | 5 | 8 | 2 | 3 | 9 | 7 | |
| | | | | 9 | 2 | 8 | 4 | 3 | 7 | 5 | 6 | 1 | |
| | | | | 8 | 3 | 6 | 2 | 1 | 5 | 9 | 7 | 4 | |
| | | | | 2 | 4 | 9 | 3 | 7 | 6 | 8 | 1 | 5 | |
| | | | | 1 | 7 | 5 | 8 | 9 | 4 | 6 | 3 | 2 | |

Overview

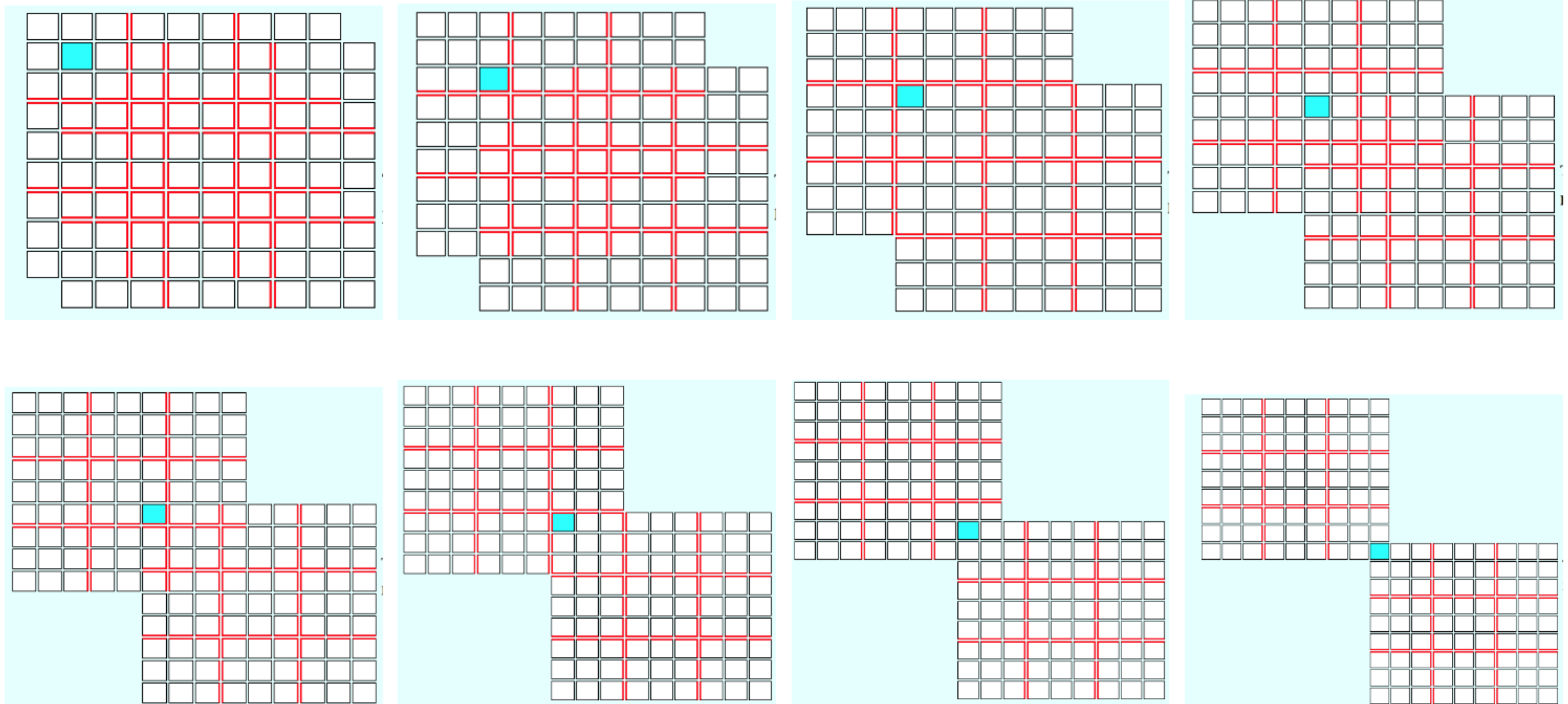
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Method

- What types of overlapping sudokus?
- How do we encode our problem into CNF?
- Which SAT-solver?
- How do we generate data for the sudokus?

Method (cont)

What types of overlapping sudokus?



Method (cont)

How do we encode our problem into CNF?

- DIMACS een format

Method (cont)

Which Sat-solver?

- Zchaff for stastics.
- Pycosat for decoding the sudoku.

Method (cont)

How do we generate data for the sudokus?

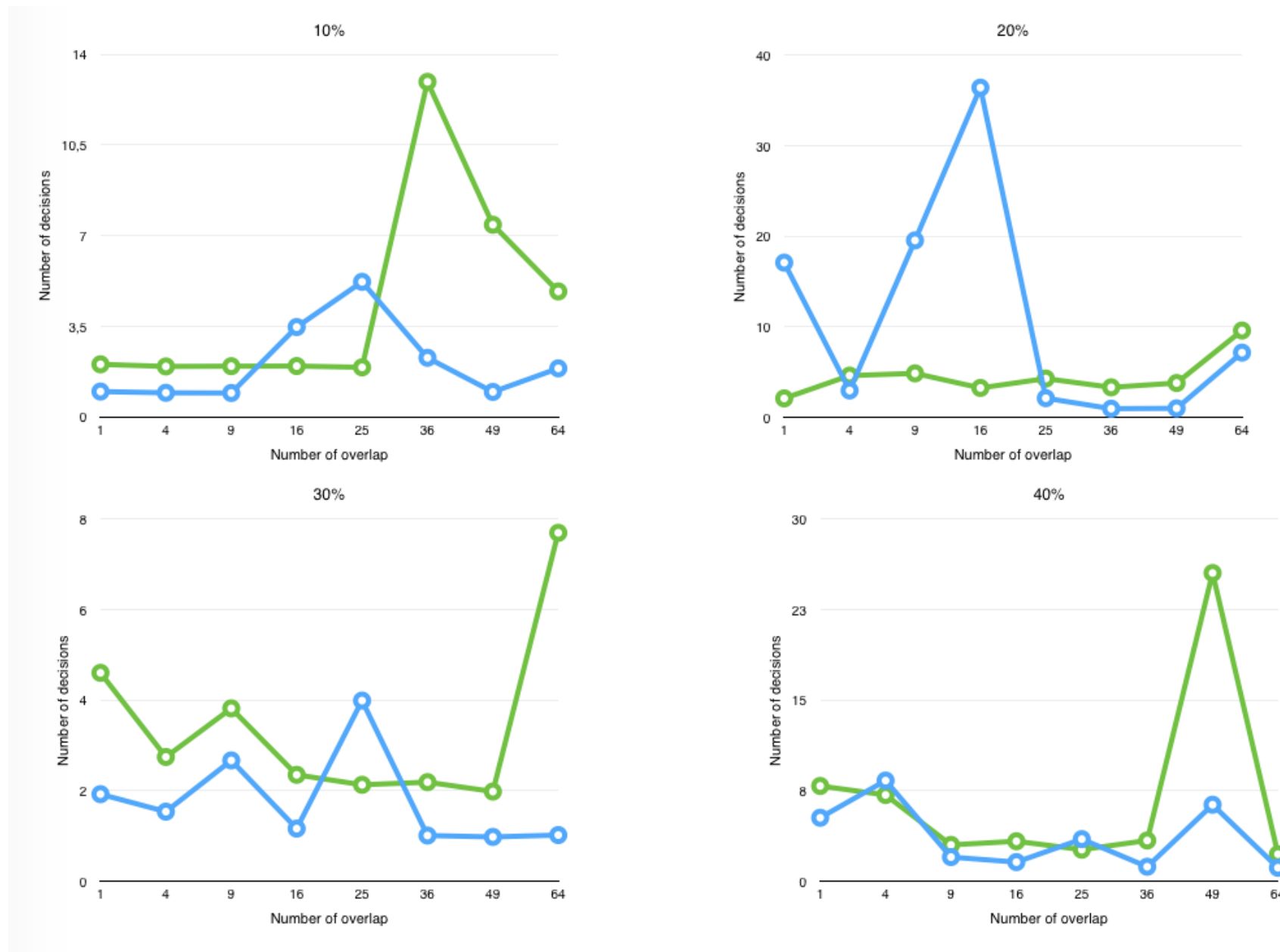
- <http://www.midoku.nl/>
- Tweaked the javascript to generate all the desired shapes.
- Random number assignment
- Punched out method

Overview

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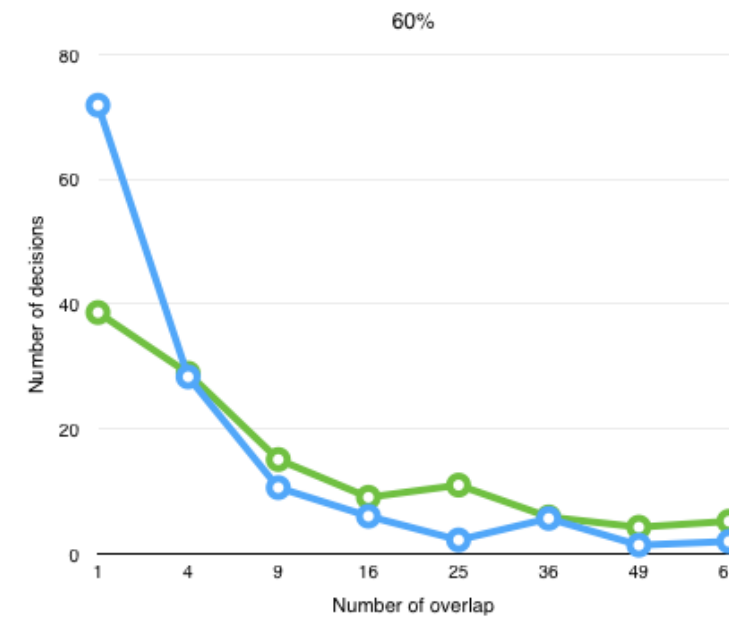
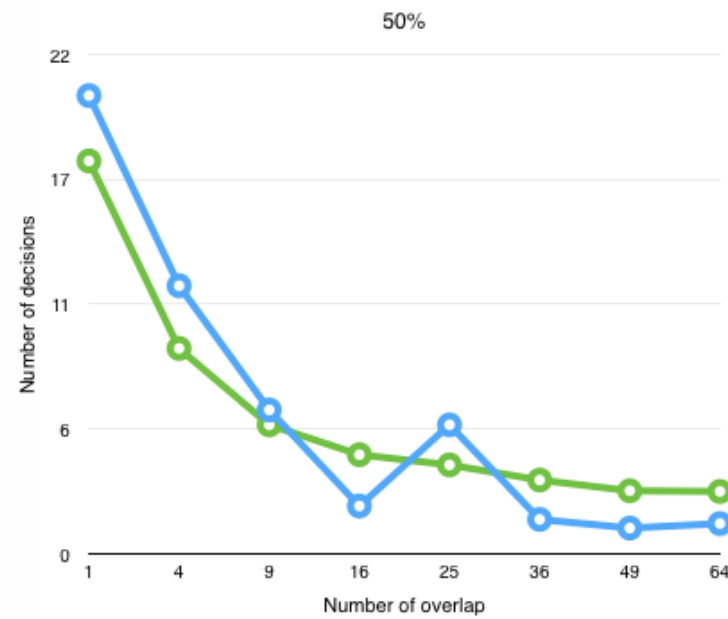
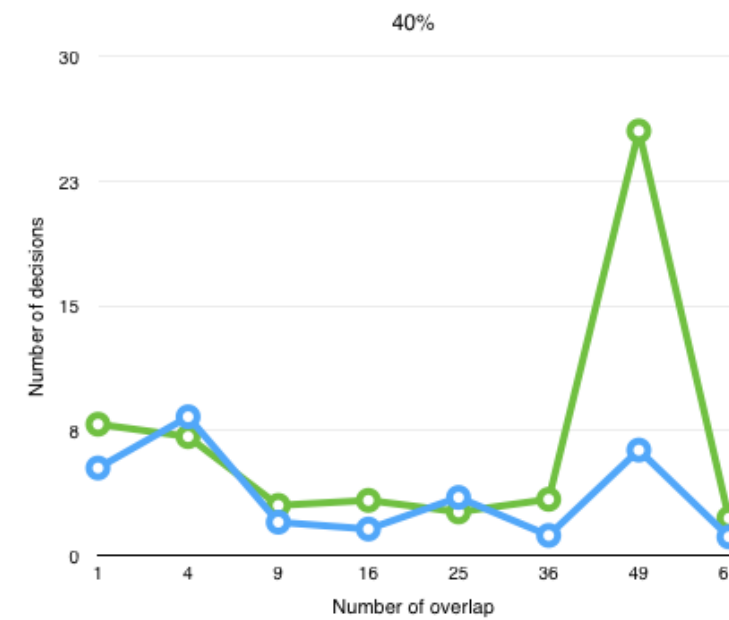
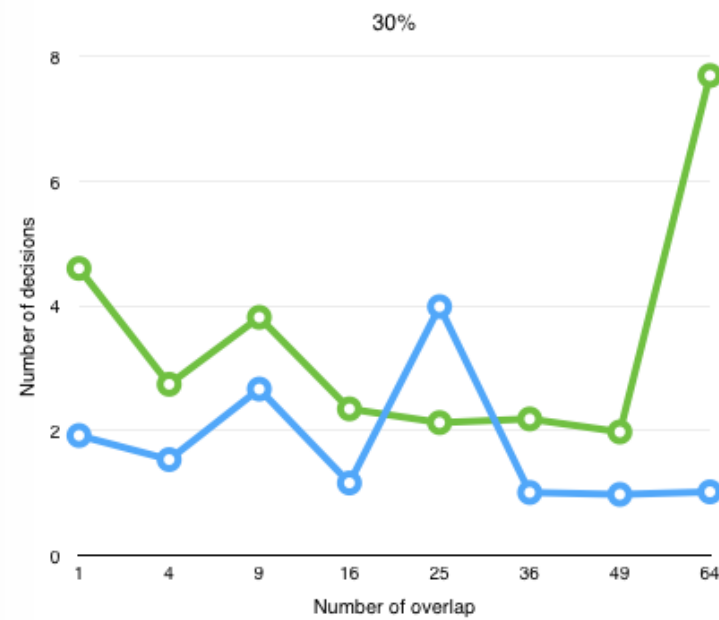
Results

Punched Out Percentage



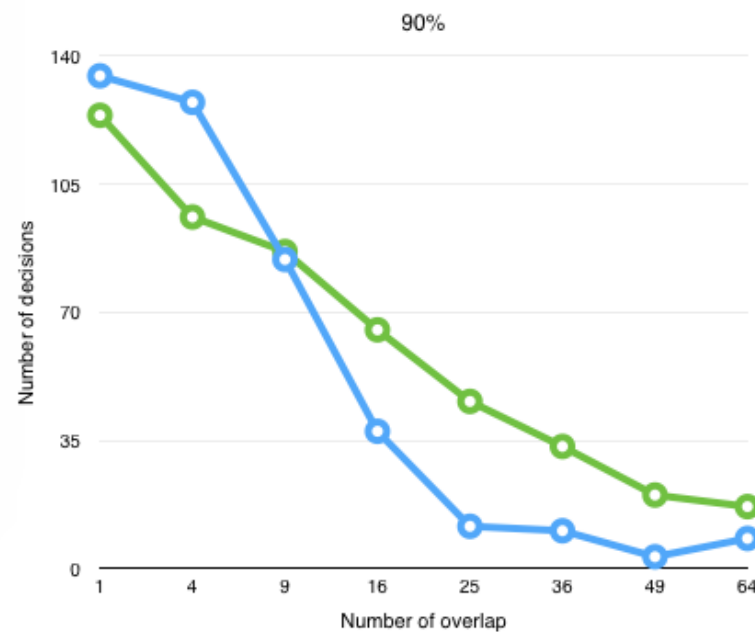
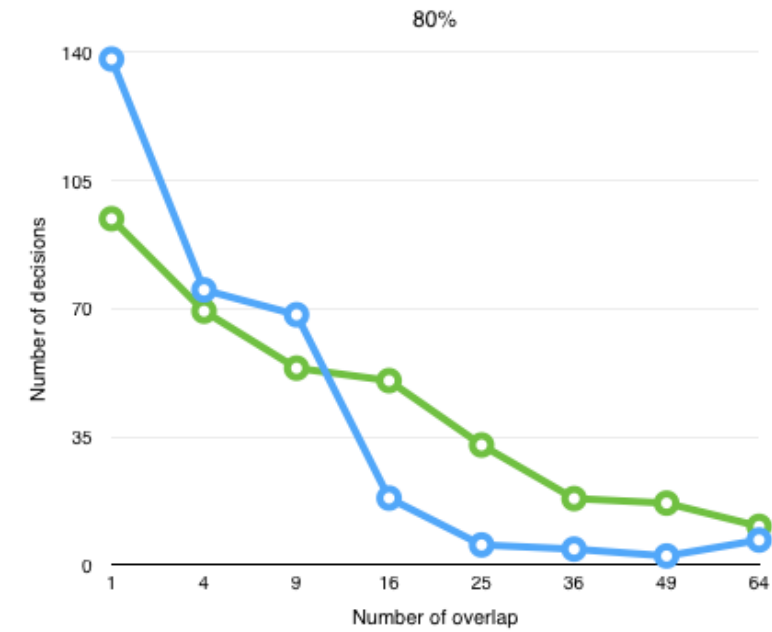
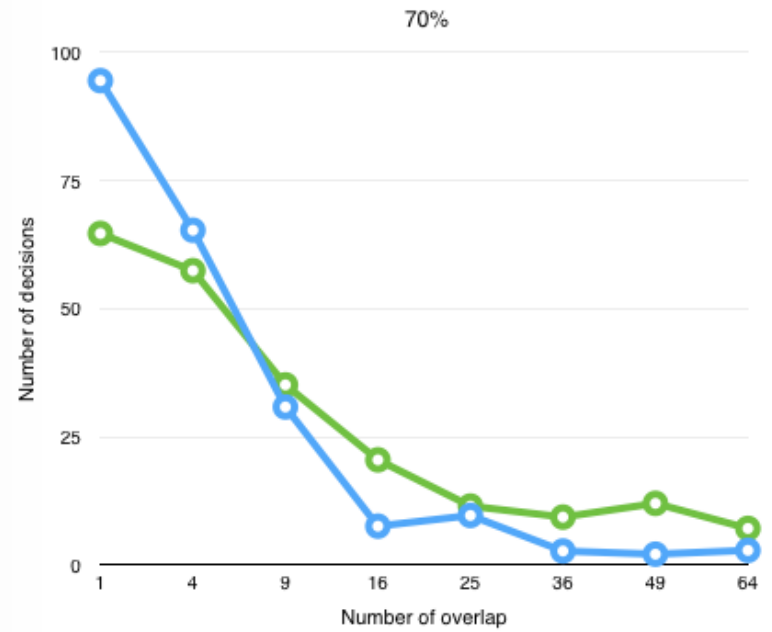
Results (cont)

Punched Out Percentage



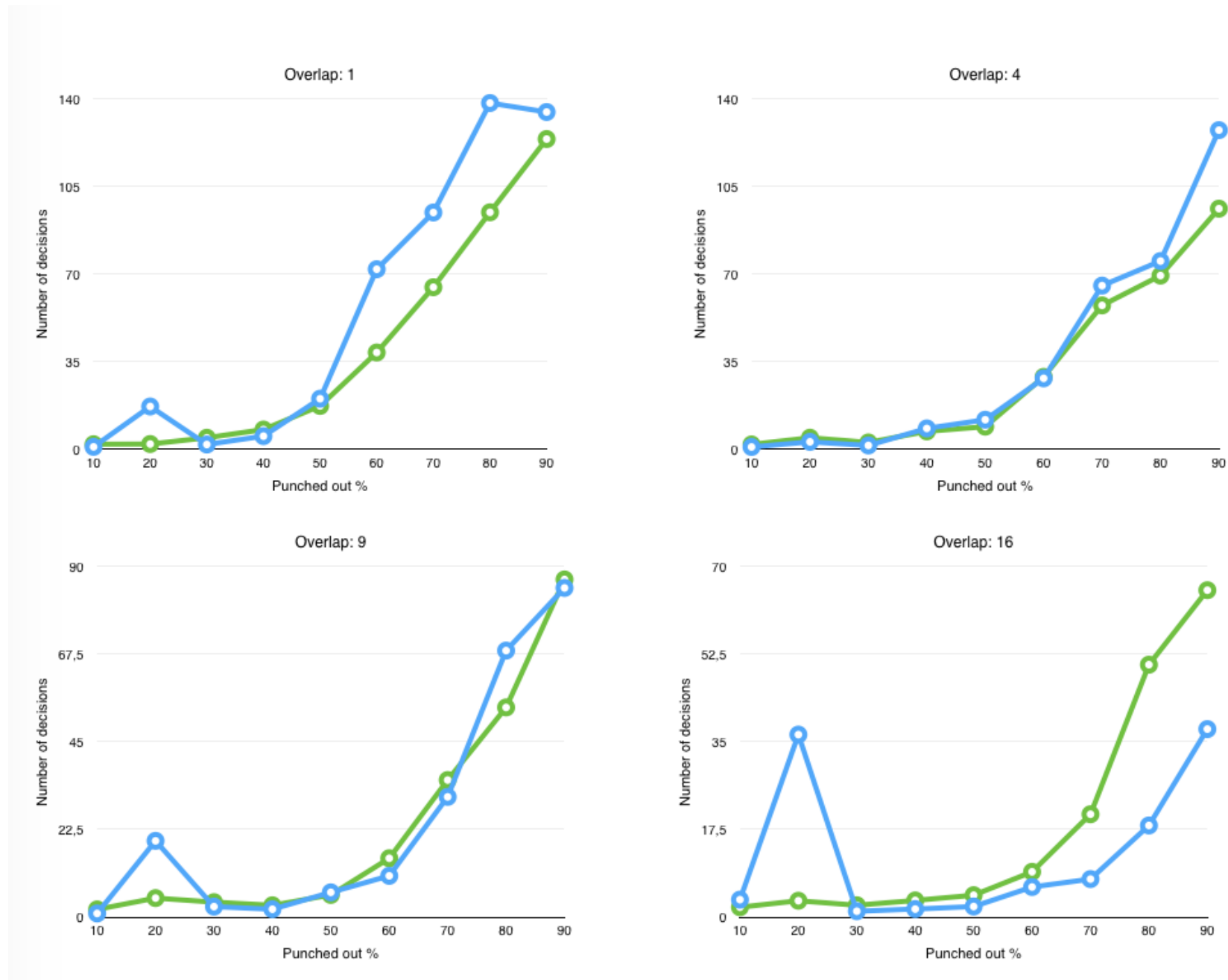
Results (cont)

Punched Out Percentage



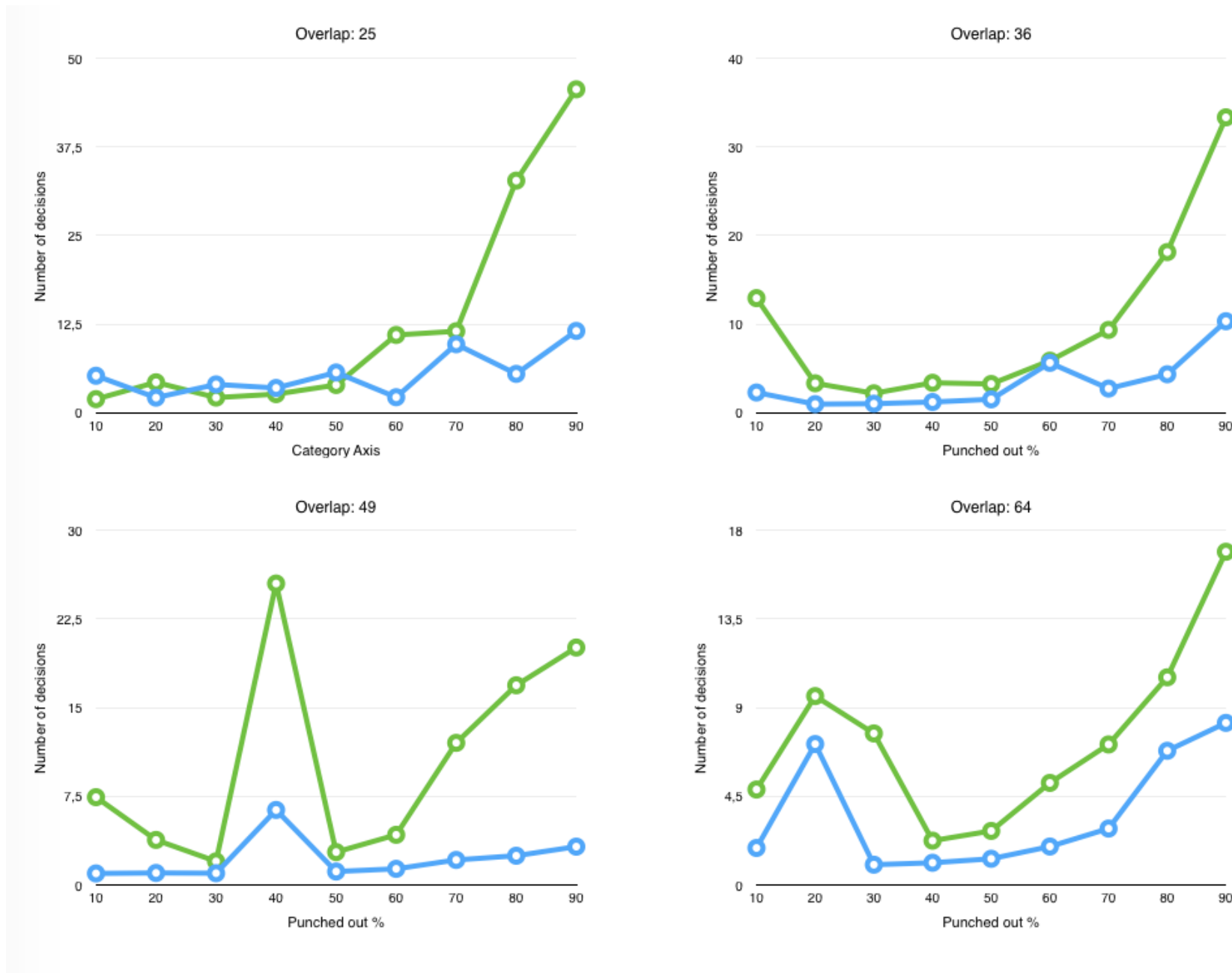
Results (cont)

Overlap



Results (cont)

Overlap



Overview

- Introduction & Hypothesis
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Discussion and Conclusion

- Different shapes
- Multiple sudokus

Discussion and **Conclusion**

- Hypothesis is partially true

