

# deep\_learning\_module\_7\_lesson\_2

April 15, 2025

## 0.1 DEEP LEARNING FOR FINANCE

### MODULE 7 | LESSON 2

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## 1 THE WALK FORWARD METHOD: APPLICATION TO BITCOIN

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<b>Reading Time</b>	50 minutes
<b>Prior Knowledge</b>	Neural Networks, Machine Learning
<b>Keywords</b>	Walk forward, Multi-Layer Perceptron, Backtesting

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### 1.1 1. INTRODUCTION

In this notebook, we illustrate the implementation of the Walk Forward method as a backtest procedure for trading strategies based on deep learning models. We will exploit hourly data of Bitcoin prices and train a classification model to predict the direction of Bitcoin's return over 4-hour intervals.

In our previous applications of deep learning to trading strategies, we have always started by splitting the data by time into two parts, training on the first chunk of data and using the second for out-of-sample tests. This procedure is not wrong by itself but employs a very small part of the information to perform backtests. This means that we obtain estimates of the performance of our strategy from relatively few observations compared to the overall sample. Moreover, we are biasing our tests based on the ability of the models to predict out of sample only in the most recent part of the time series. For instance, the test sample may feature a booming period in security prices, and our model may perform well in those periods. However, this may obscure the fact that the model may perform terribly in downturn periods.

A simple way to overcome this—and have a general view of our trading strategies and how the underlying models perform over time—is to opt for a **Walk Forward** backtesting method. To implement a Walk Forward, we generate a sequence of out-of-sample evaluations by periodically re-training the model using a rolling, or expanding, time window.

The figure below illustrates the Walk Forward that we are going to implement below. This is a non-anchored method because we use a fixed rolling window of training data that we are going to shift sequentially so that the training set includes the test set in the previously trained model.

Before proceeding, we load all the required libraries and the data that we will exploit in this notebook. Among other information, the dataset covers hourly Bitcoin prices in 2013–2022. Notice that the earlier data does not include every-hour information due to the lack of transactions. For computational reasons, we will restrict the analysis to post-2020 data.

```
[1]: # %%
import numpy as np
import pandas as pd
import tensorflow as tf

# %%
# =====
name = "Kraken_BTCUSD_60_3Q2022"
df = pd.read_csv(name + ".csv")

df["unix"] = pd.to_numeric(df["unix"])
df["date"] = pd.to_datetime(df["unix"], unit="s")
```

```
2025-04-15 17:42:00.420871: I tensorflow/core/platform/cpu_feature_guard.cc:193]
This TensorFlow binary is optimized with oneAPI Deep Neural Network Library
(oneDNN) to use the following CPU instructions in performance-critical
operations: SSE4.1 SSE4.2 AVX AVX2 AVX512F AVX512_VNNI FMA
To enable them in other operations, rebuild TensorFlow with the appropriate
compiler flags.
2025-04-15 17:42:03.090964: I tensorflow/core/util/util.cc:169] oneDNN custom
operations are on. You may see slightly different numerical results due to
floating-point round-off errors from different computation orders. To turn them
off, set the environment variable `TF_ENABLE_ONEDNN_OPTS=0`.
```

```
[2]: df = df[["date", "close", "volume", "trades"]]
```

```
[3]: df.head()
```

```
[3]:      date   close  volume  trades
0 2013-10-06 21:00:00  122.00  0.1000      1
1 2013-10-07 20:00:00  123.61  0.1000      1
2 2013-10-08 02:00:00  123.90  1.9916      2
3 2013-10-08 05:00:00  124.18  2.0000      2
4 2013-10-09 09:00:00  123.84  2.8230      3
```

```
[4]: df.tail()
```

```
[4]:      date   close  volume  trades
67886 2022-09-30 19:00:00  19497.2  290.023381    1947
67887 2022-09-30 20:00:00  19420.4  759.074836    1648
```

```
67888 2022-09-30 21:00:00 19360.4 564.894247 1245  
67889 2022-09-30 22:00:00 19387.1 90.626135 1978  
67890 2022-09-30 23:00:00 19425.2 57.986112 2466
```

```
[5]: df["Ret"] = df["close"].pct_change()
```

```
[6]: df["year"] = df["date"].dt.year
```

```
[7]: df.tail()
```

```
[7]:
```

	date	close	volume	trades	Ret	year
67886	2022-09-30 19:00:00	19497.2	290.023381	1947	-0.008941	2022
67887	2022-09-30 20:00:00	19420.4	759.074836	1648	-0.003939	2022
67888	2022-09-30 21:00:00	19360.4	564.894247	1245	-0.003090	2022
67889	2022-09-30 22:00:00	19387.1	90.626135	1978	0.001379	2022
67890	2022-09-30 23:00:00	19425.2	57.986112	2466	0.001965	2022

```
[8]: del df["close"]  
df = df.loc[(df["year"] >= 2020)]  
df.head()
```

```
[8]:
```

	date	volume	trades	Ret	year
43802	2020-01-01 00:00:00	70.761775	267	-0.001758	2020
43803	2020-01-01 01:00:00	224.921206	528	0.005408	2020
43804	2020-01-01 02:00:00	138.910528	336	0.003906	2020
43805	2020-01-01 03:00:00	97.687456	240	-0.002908	2020
43806	2020-01-01 04:00:00	25.305555	131	-0.001236	2020

```
[9]: df["Ret"] = df["Ret"].fillna(0)  
df["volume"] = df["volume"].fillna(0)  
df["trades"] = df["trades"].fillna(0)  
df.head()
```

```
[9]:
```

	date	volume	trades	Ret	year
43802	2020-01-01 00:00:00	70.761775	267	-0.001758	2020
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43804	2020-01-01 02:00:00	138.910528	336	0.003906	2020
43805	2020-01-01 03:00:00	97.687456	240	-0.002908	2020
43806	2020-01-01 04:00:00	25.305555	131	-0.001236	2020

```
[10]: df
```

```
[10]:
```

	date	volume	trades	Ret	year
43802	2020-01-01 00:00:00	70.761775	267	-0.001758	2020
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```

43806 2020-01-01 04:00:00    25.305555    131 -0.001236 2020
...
67886 2022-09-30 19:00:00    290.023381   1947 -0.008941 2022
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67890 2022-09-30 23:00:00    57.986112   2466  0.001965 2022

[24089 rows x 5 columns]

```

## 1.2 2. SETTING UP AND TRAINING THE FORECASTING MODEL

To illustrate the workings of Walk Forward, we will resort to a “plain vanilla” MLP architecture where the label to predict is the direction of the cumulative Bitcoin return over the next 4-hour interval. That is, we set up a binary classification problem where the positive class is a positive return and the negative class is a zero or negative return. The input features are the lags of the hourly Bitcoin returns over the previous 15 days, meaning that we have  $24 \times 15 = 360$  features. Our final time series consists of more than 23,000 observations.

```

[11]: df = df.reindex(
    columns=[
        "date",
        "Ret",
        "volume",
        "trades",
        "year",
        "month",
        "day",
        "week",
        "weekday",
        "hour",
    ]
)
df = df[["date", "Ret"]]

n_lags = 24 * 15

for i in range(1, n_lags + 1):
    name = "Ret_" + str(i)
    df[name] = df["Ret"].shift(i)

df["Ret4_i"] = df["Ret"].rolling(4).apply(lambda x: 100 * (np.prod(1 + x / 100) - 1))
df["Ret4"] = df["Ret4_i"].shift(-4)
df["Output"] = df["Ret4"] > 0
df["Output"] = df["Output"].astype(int)
del df["Ret4"]

```

```
del df["Ret4_i"]
```

```
df = df.dropna()
```

```
/tmp/ipykernel_67/604952926.py:21: PerformanceWarning: DataFrame is highly
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    df[name] = df["Ret"].shift(i)  

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/tmp/ipykernel_67/604952926.py:21: PerformanceWarning: DataFrame is highly
```

```
fragmented. This is usually the result of calling `frame.insert` many times,
which has poor performance. Consider joining all columns at once using
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```
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    df[name] = df["Ret"].shift(i)  
/tmp/ipykernel_67/604952926.py:21: PerformanceWarning: DataFrame is highly  
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which has poor performance. Consider joining all columns at once using  
pd.concat(axis=1) instead. To get a de-fragmented frame, use `newframe =  
frame.copy()`  
    df[name] = df["Ret"].shift(i)  
/tmp/ipykernel_67/604952926.py:23: PerformanceWarning: DataFrame is highly  
fragmented. This is usually the result of calling `frame.insert` many times,  
which has poor performance. Consider joining all columns at once using  
pd.concat(axis=1) instead. To get a de-fragmented frame, use `newframe =  
frame.copy()`  
    df["Ret4_i"] = df["Ret"].rolling(4).apply(lambda x: 100 * (np.prod(1 + x /  
100) - 1))
```

```

/tmp/ipykernel_67/604952926.py:24: PerformanceWarning: DataFrame is highly
fragmented. This is usually the result of calling `frame.insert` many times,
which has poor performance. Consider joining all columns at once using
pd.concat(axis=1) instead. To get a de-fragmented frame, use `newframe =
frame.copy()`
    df["Ret4"] = df["Ret4_i"].shift(-4)
/tmp/ipykernel_67/604952926.py:25: PerformanceWarning: DataFrame is highly
fragmented. This is usually the result of calling `frame.insert` many times,
which has poor performance. Consider joining all columns at once using
pd.concat(axis=1) instead. To get a de-fragmented frame, use `newframe =
frame.copy()`
    df["Output"] = df["Ret4"] > 0

```

[12]:

```
X, y = df.iloc[:, 2:-1], df.iloc[:, -1]
print(X.shape, y.shape)
```

(23729, 360) (23729,)

The MLP's architecture includes three fully connected hidden layers with, respectively, 85, 55, and 30 hidden units. Each hidden layer features a ReLU activation function and a sigmoid function in the output layer. As regularization tools, we introduce Dropout after all the hidden layers and an early stopping criterion.

[13]:

```
hp_units = 85
hp_units_2 = 55
hp_units_3 = 30
n_dropout = 0.2
act_fun = "relu"
```

Below, we implement the full Walk Forward loop. The size of the training window is 5,000 observations, and the test window has 1,000 observations. Starting at the beginning of our dataset, we are going to train the model using 5,000 observations and test its out-of-sample performance for the following 1,000 observations. After that, we shift the training window 1,000 observations and repeat the process until we reach the end of the full sample. We store in a pandas data frame the prediction results for each test observation.

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QQQQ

[14]:

```
n_train = 5000
n_test = 1000

time_backtest = []
time_backtest = np.array(time_backtest)
time_backtest = time_backtest.astype("datetime64", copy=False)

pred_backtest = []
ret_backtest = []

for i in range(0, len(y) - n_train, n_test):
```

```

X_train, X_test = X[i : i + (n_train)], X[i + n_train : i + n_train + n_test]
y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
test_time = df.iloc[i + (n_train) : i + n_train + n_test, 0:1].values
Ret_vector = df.iloc[i + (n_train) : i + n_train + n_test, 1:2].values
print(
    "ite ",
    i / n_test,
    " -- start test:",
    test_time[0],
    " -- end test",
    test_time[-1],
    " -----",
    X_train.shape,
    y_train.shape,
    X_test.shape,
    y_test.shape,
    test_time.shape,
    Ret_vector.shape,
)
tf.keras.backend.clear_session()
tf.random.set_seed(1234)

model = tf.keras.models.Sequential()
model.add(tf.keras.layers.Dense(units=hp_units, activation=act_fun))
model.add(tf.keras.layers.Dropout(n_dropout))
model.add(tf.keras.layers.Dense(units=hp_units_2, activation=act_fun))
model.add(tf.keras.layers.Dropout(n_dropout))
model.add(tf.keras.layers.Dense(units=hp_units_3, activation=act_fun))
model.add(tf.keras.layers.Dropout(n_dropout))
model.add(tf.keras.layers.Dense(units=1, activation="sigmoid"))

hp_lr = 1e-5

adam = tf.keras.optimizers.Adam(learning_rate=hp_lr)
model.compile(optimizer=adam, loss="binary_crossentropy",
metrics=["accuracy"])

es = tf.keras.callbacks.EarlyStopping(
    monitor="val_accuracy",
    mode="max",
    verbose=0,
    patience=20,
    restore_best_weights=True,
)

```

```

class_weight = {0: (np.mean(y_train) / 0.5), 1: 1}
history = model.fit(
    X_train,
    y_train,
    validation_split=0.15,
    epochs=500,
    batch_size=32,
    verbose=0,
    callbacks=[es],
    class_weight=class_weight,
)

y_prob = model.predict(X_test, verbose=0)
y_pred = np.where(y_prob > 0.50, 1, 0)

time_backtest = np.append(time_backtest, test_time.flatten())
pred_backtest = np.append(pred_backtest, y_pred.flatten())
ret_backtest = np.append(ret_backtest, Ret_vector.flatten())

df_predictions = pd.DataFrame(
    {"Date": time_backtest, "Pred": pred_backtest, "Ret": ret_backtest}
)

```

ite 0.0 -- start test: ['2020-08-11T08:00:00.000000000'] -- end test  
['2020-09-21T23:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)  
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel\_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is deprecated. In a future version, this will be treated as \*label-based\* indexing, consistent with e.g. `series[i]` lookups. To retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.

y\_train, y\_test = y[i : i + (n\_train)], y[i + n\_train : i + n\_train + n\_test]  
2025-04-15 17:42:36.616220: I tensorflow/core/platform/cpu\_feature\_guard.cc:193]  
This TensorFlow binary is optimized with oneAPI Deep Neural Network Library  
(oneDNN) to use the following CPU instructions in performance-critical  
operations: SSE4.1 SSE4.2 AVX AVX2 AVX512F AVX512\_VNNI FMA  
To enable them in other operations, rebuild TensorFlow with the appropriate  
compiler flags.

/opt/conda/lib/python3.10/site-packages/keras/engine/data\_adapter.py:1699:  
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is  
deprecated. In a future version, this will be treated as \*label-based\* indexing,  
consistent with e.g. `series[i]` lookups. To retain the old behavior, use  
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.

return t[start:end]

/tmp/ipykernel\_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is deprecated. In a future version, this will be treated as \*label-based\* indexing, consistent with e.g. `series[i]` lookups. To

```

retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
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deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 1.0 -- start test: ['2020-09-22T00:00:00.000000000'] -- end test
['2020-11-02T16:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
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retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
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FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 2.0 -- start test: ['2020-11-02T17:00:00.000000000'] -- end test
['2020-12-14T08:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
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consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 3.0 -- start test: ['2020-12-14T09:00:00.000000000'] -- end test
['2021-01-25T00:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To

```

```

retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
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consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 4.0 -- start test: ['2021-01-25T01:00:00.000000000'] -- end test
['2021-03-07T17:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 5.0 -- start test: ['2021-03-07T18:00:00.000000000'] -- end test
['2021-04-18T09:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 6.0 -- start test: ['2021-04-18T10:00:00.000000000'] -- end test
['2021-05-30T01:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To

```

```

retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 7.0 -- start test: ['2021-05-30T02:00:00.000000000'] -- end test
['2021-07-10T17:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 8.0 -- start test: ['2021-07-10T18:00:00.000000000'] -- end test
['2021-08-21T14:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 9.0 -- start test: ['2021-08-21T15:00:00.000000000'] -- end test
['2021-10-02T06:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To

```

```

retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 10.0 -- start test: ['2021-10-02T07:00:00.000000000'] -- end test
['2021-11-12T22:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 11.0 -- start test: ['2021-11-12T23:00:00.000000000'] -- end test
['2021-12-24T14:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

    y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 12.0 -- start test: ['2021-12-24T15:00:00.000000000'] -- end test
['2022-02-04T06:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To

```

```

retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 13.0 -- start test: ['2022-02-04T07:00:00.000000000'] -- end test
['2022-03-17T22:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 14.0 -- start test: ['2022-03-17T23:00:00.000000000'] -- end test
['2022-04-28T14:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 15.0 -- start test: ['2022-04-28T15:00:00.000000000'] -- end test
['2022-06-09T06:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To

```

```

retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 16.0 -- start test: ['2022-06-09T07:00:00.000000000'] -- end test
['2022-07-20T22:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 17.0 -- start test: ['2022-07-20T23:00:00.000000000'] -- end test
['2022-08-31T14:00:00.000000000'] ----- (5000, 360) (5000,) (1000, 360)
(1000,) (1000, 1) (1000, 1)

/tmp/ipykernel_67/2457061983.py:13: FutureWarning: The behavior of `series[i:j]`
with an integer-dtype index is deprecated. In a future version, this will be
treated as *label-based* indexing, consistent with e.g. `series[i]` lookups. To
retain the old behavior, use `series.iloc[i:j]`. To get the future behavior, use
`series.loc[i:j]`.

y_train, y_test = y[i : i + (n_train)], y[i + n_train : i + n_train + n_test]
/opt/conda/lib/python3.10/site-packages/keras/engine/data_adapter.py:1699:
FutureWarning: The behavior of `series[i:j]` with an integer-dtype index is
deprecated. In a future version, this will be treated as *label-based* indexing,
consistent with e.g. `series[i]` lookups. To retain the old behavior, use
`series.iloc[i:j]`. To get the future behavior, use `series.loc[i:j]`.
    return t[start:end]

ite 18.0 -- start test: ['2022-08-31T15:00:00.000000000'] -- end test
['2022-09-30T23:00:00.000000000'] ----- (5000, 360) (5000,) (729, 360)
(729,) (729, 1) (729, 1)

```

[15]: df\_predictions.Date = pd.to\_datetime(df\_predictions.Date,   
`format="%YYYY-%mm-%dd")`

```
df_res = df_predictions
df_res.tail()
```

[15]:

	Date	Pred	Ret
18724	2022-09-30 19:00:00	1.0	-0.008941
18725	2022-09-30 20:00:00	1.0	-0.003939
18726	2022-09-30 21:00:00	1.0	-0.003090
18727	2022-09-30 22:00:00	0.0	0.001379
18728	2022-09-30 23:00:00	1.0	0.001965

### 1.3 3. RESULTS

Using the predictions of the trained models over all the test samples, we can now perform our backtest and obtain estimates of the returns of the underlying trading strategy. We will compare the cumulative returns of three different strategies:

1. A buy-and-hold strategy that is long on Bitcoin as of the beginning of the sample period.
2. A Long-Short strategy that arises from the predictions of the MLP: The position is long one unit when the predicted probability of a positive return over 4 hours is greater than 0.5 and the position is short one unit otherwise.
3. A Long-only strategy that arises from the predictions of the MLP. The position is long one unit when the predicted probability of a positive return over 4 hours is greater than 0.5 and the position is zero otherwise.

Below, we report the cumulative returns and display the evolution of returns of these three strategies. Note that while we have fixed some seeds for the random number generators, there is some additional randomness involved and the results may vary each time you run the code.

[16]:

```
df_res["Positions"] = np.where(df_res["Pred"] > 0.5, 1, -1)
df_res["Positions_shift"] = df_res["Positions"].shift(1)
df_res["Strat_ret"] = df_res["Positions"].shift(1) * df_res["Ret"]
df_res["Positions_L"] = df_res["Positions"].shift(1)
df_res["Positions_L"][df_res["Positions_L"] == -1] = 0
df_res["Strat_ret_L"] = df_res["Positions_L"] * df_res["Ret"]
df_res["CumRet"] = df_res["Strat_ret"].expanding().apply(lambda x: np.prod(1 + x) - 1)
df_res["CumRet_L"] = (
    df_res["Strat_ret_L"].expanding().apply(lambda x: np.prod(1 + x) - 1)
)
df_res["bhRet"] = df_res["Ret"].expanding().apply(lambda x: np.prod(1 + x) - 1)

Final_Return_L = np.prod(1 + df_res["Strat_ret_L"]) - 1
Final_Return = np.prod(1 + df_res["Strat_ret"]) - 1
Buy_Return = np.prod(1 + df_res["Ret"]) - 1

print("Strat Return Long Only =", Final_Return_L * 100, "%")
print("Strat Return =", Final_Return * 100, "%")
print("Buy and Hold Return =", Buy_Return * 100, "%")
```

```
/tmp/ipykernel_67/529454916.py:5: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame

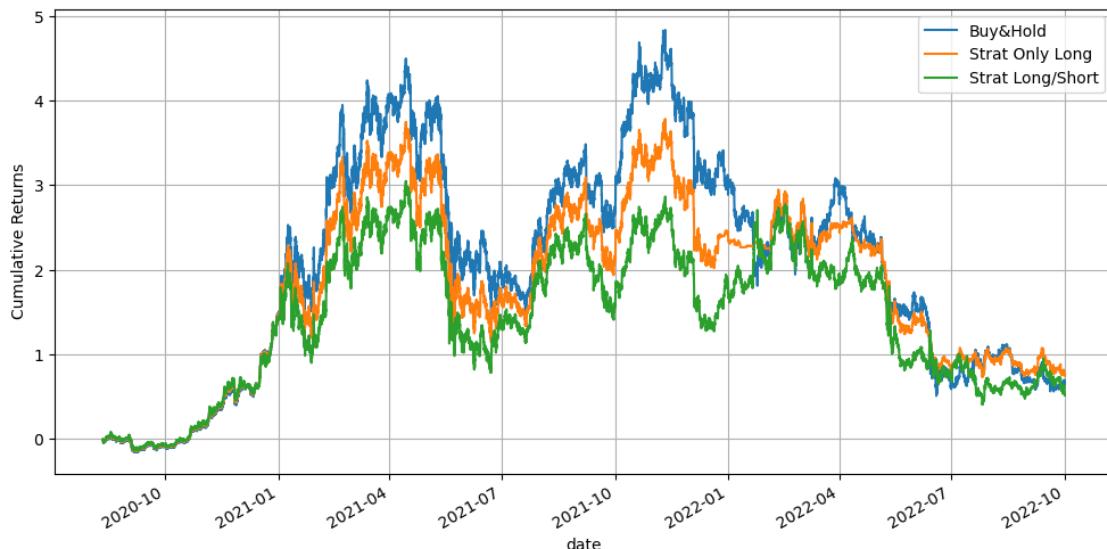
See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
    df_res["Positions_L"][df_res["Positions_L"] == -1] = 0

Strat Return Long Only = 75.02921313824528 %
Strat Return = 52.06406243287236 %
Buy and Hold Return = 65.15499328334393 %
```

```
[17]: import matplotlib.pyplot as plt

fig = plt.figure(figsize=(12, 6))
ax = plt.gca()
df_res.plot(x="Date", y="bhRet", label="Buy&Hold", ax=ax)
df_res.plot(x="Date", y="CumRet_L", label="Strat Only Long", ax=ax)
df_res.plot(x="Date", y="CumRet", label="Strat Long/Short", ax=ax)
plt.xlabel("date")
plt.ylabel("Cumulative Returns")
plt.grid()
plt.show()

df_res["trade_bin"] = df_res["Positions"].diff().abs()
df_res["trade_bin"] = df_res["trade_bin"] / 2
df_res.describe()
```



	Pred	Ret	Positions	Positions_shift	\
count	18729.000000	18729.000000	18729.000000	18728.000000	

mean	0.815527	0.000060	0.631053	0.631034		
std	0.387880	0.008154	0.775760	0.775776		
min	0.000000	-0.121059	-1.000000	-1.000000		
25%	1.000000	-0.003351	1.000000	1.000000		
50%	1.000000	0.000090	1.000000	1.000000		
75%	1.000000	0.003556	1.000000	1.000000		
max	1.000000	0.124064	1.000000	1.000000		
	Strat_ret	Positions_L	Strat_ret_L	CumRet	CumRet_L	\
count	18728.000000	18728.000000	18728.000000	18728.000000	18728.000000	
mean	0.000056	0.815517	0.000058	1.442544	1.786733	
std	0.008154	0.387888	0.007491	0.829507	1.025505	
min	-0.121059	0.000000	-0.121059	-0.133223	-0.142172	
25%	-0.003349	1.000000	-0.002415	0.741244	0.930585	
50%	0.000091	1.000000	-0.000000	1.472824	1.983144	
75%	0.003573	1.000000	0.002667	2.133715	2.554529	
max	0.124064	1.000000	0.124064	3.047122	3.781394	
	bhRet	trade_bin				
count	18729.000000	18728.000000				
mean	2.053200	0.150363				
std	1.292641	0.357437				
min	-0.154755	0.000000				
25%	0.821464	0.000000				
50%	2.209577	0.000000				
75%	3.033303	0.000000				
max	4.832441	1.000000				

## 1.4 4. CONCLUSION

In this notebook, we have outlined and implemented the Walk Forward method to increase the robustness of our backtests for strategies based on Deep Learning methods.

In Lesson 3, we will describe a more advanced method to robustify our backtests: the Combinatorial Purged Cross-Validation.

See you there!