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1a. $3x^3 + x^2 \log n + 2x^2 + 3 \log n$

high time complexity = $3x^3$

$$3x^3 + 2x^2 + x^2 \log n + 3 \log n$$

$$3x^3 + 2x^2 + \log n (x^2 + 3) // x^2 + 3 \text{ combine}$$

// $\log n$ combine

$3x^3$ // lower terms removed

$$3x^3 = O(x^3) // \text{constants removed}$$

$$O(x^3)$$

1b. $2x^2 + (\log x)^2 + \log x + 8$

high time complexity = $2x^2$

$$2x^2 + (\log x)^2 + \log x + 8$$

$$2x^2 + \log x (\log x + 1) + 8 // (\log x)^2 \text{ splits}$$

// $(\log x + 1)$ created

$2x^2$ // lower terms removed

$$2x^2 = \Theta(x^2) // \text{constants removed}$$

$$\Theta(x^2)$$