

Regression model: Housing Price

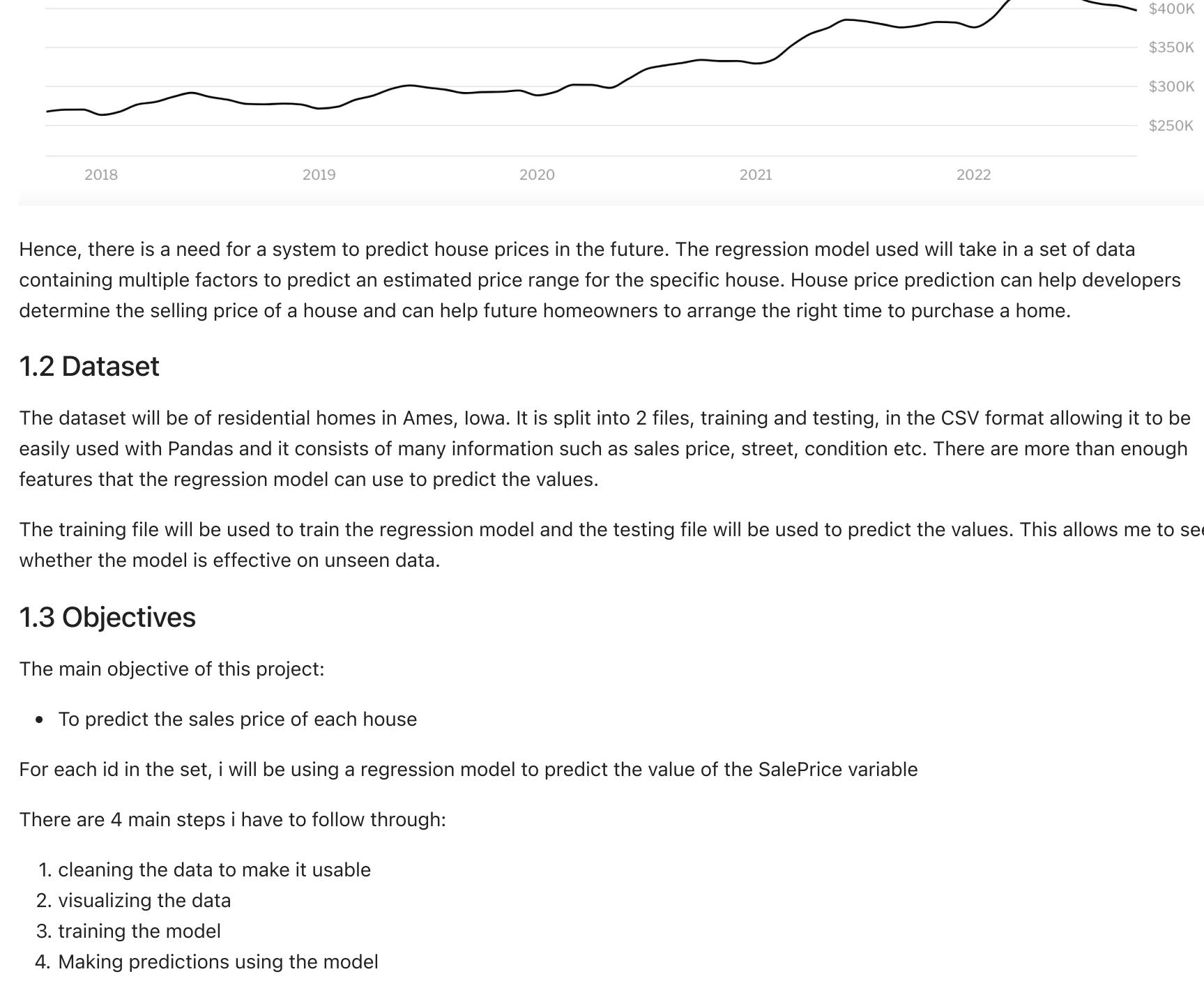
1. Introduction

1.1 Domain specific area

Housing prices increases every year, and with an increasing demand for houses and lack of space, it is easy to see why it is getting more expensive, especially if people are planning to live in the city. Even though some people might choose to live in the suburb or rural areas, prices are still subject to demand and location. According to Redfin, housing prices in the last five years have been slowly increasing at an all-time high in May 2022 at \$430,000.

U.S. Housing Market Overview

What is the housing market like right now?
In October 2022, U.S. home prices were up 5.0% compared to last year, selling for a median price of...



Hence, there is a need for a system to predict house prices in the future. The regression model used will take in a set of data containing multiple factors in order to predict an estimated price range for the specific house. House price prediction can help developers determine the selling price of a house and can help future homeowners to arrange the right time to purchase a home.

1.2 Dataset

The dataset will be of residential homes in Ames, Iowa. It is split into 2 files, training and testing, in the CSV format allowing it to be easily used with Pandas and it consists of many information such as sales price, street, condition etc. There are more than enough features that the regression model can use to predict the values.

The training file will be used to train the regression model and the testing file will be used to predict the values. This allows me to see whether the model is effective on unseen data.

1.3 Objectives

The main objective of this project:

- To predict the sales price of each house

For each id in the set, i will be using a regression model to predict the value of the SalePrice variable

There are 4 main steps i have to follow through:

- cleaning the data to make it usable
- visualizing the data
- training the model
- Making predictions using the model

This regression model will allow us to predict the house prices in the area which is good for developers who want to estimate how much houses will be sold for and homeowners who want to purchase a new house.

1.4 Disclaimer

As this project is used for personal and educational purpose, any conclusions from this project will be based on assumptions after looking at the predicted values and should not be used as a professional analytical judgement.

2. Implementation

Importing necessary Data and libraries

```
In [1]: #Importing necessary libraries
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.linear_model import LinearRegression
from sklearn.metrics import r2_score, mean_squared_error
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import PolynomialFeatures
```

Loading the training data

```
In [2]: df_train = pd.read_csv('data/train.csv')
df_train
```

	Id	MSSubClass	MSZoning	LotFrontage	LotArea	Street	Alley	LotShape	LandContour	Utilities	...	PoolArea	PoolQC	Fea
0	1	60	RL	65.0	8450	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	f
1	2	20	RL	80.0	9600	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	f
2	3	60	RL	68.0	11250	Pave	NaN	IR1	Lvl	AllPub	...	0	NaN	f
3	4	70	RL	60.0	9550	Pave	NaN	IR1	Lvl	AllPub	...	0	NaN	f
4	5	60	RL	84.0	14260	Pave	NaN	IR1	Lvl	AllPub	...	0	NaN	f
...
1455	1456	60	RL	62.0	7917	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	f
1456	1457	20	RL	85.0	13175	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	Mr
1457	1458	70	RL	66.0	9042	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	Gr
1458	1459	20	RL	68.0	9717	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	f
1459	1460	20	RL	75.0	9937	Pave	NaN	Reg	Lvl	AllPub	...	0	NaN	f

1460 rows x 81 columns

2.1 Cleaning the training dataset

Checking the percentage of missing values.

```
In [3]: missingSum = df_train.isna().sum().sort_values(ascending=False)
percentage = (df_train.isna().sum()/df_train.isna().count()) * 100
missingData = df_train[missingSum > 0.1].index(df_train.index)
```

```
Out[3]:
```

	missingSum	percentage
PoolQC	1453	99.520548
MiscFeature	1406	96.301370
Alley	1369	93.767123
Fence	1179	80.734325
FireplaceQu	690	47.260274
LotFrontage	259	17.739726
GarageBlt	81	5.547945
GarageCond	81	5.547945
GarageType	81	5.547945
GarageFinish	81	5.547945

Remove all columns with more than 10% of missing values as there is too many missing data

```
In [4]: #calculates columns with more than 10% of values missing
missingColumn = df_train.isna().sum()
missingColumn = missingColumn[missingColumn > 0.1 * len(df_train.index)]
#removes column
df_train2 = df_train.drop(columns=missingColumn.index)
df_train2
```

```
Out[4]:
```

	Id	MSSubClass	MSZoning	LotArea	Street	LotShape	LandContour	Utilities	LotConfig	LandSlope	...	EnclosedPorch	3S
0	1	60	RL	8450	Pave	Reg	Lvl	AllPub	Inside	Gtl	...	0	0
1	2	20	RL	9600	Pave	Reg	Lvl	AllPub	FR2	Gtl	...	0	0
2	3	60	RL	11250	Pave	IR1	Lvl	AllPub	Inside	Gtl	...	0	0
3	4	70	RL	9550	Pave	IR1	Lvl	AllPub	Corner	Gtl	...	272	0
4	5	60	RL	14260	Pave	IR1	Lvl	AllPub	FR2	Gtl	...	0	0
...
1455	1456	60	RL	7917	Pave	Reg	Lvl	AllPub	Inside	Gtl	...	0	0
1456	1457	20	RL	13175	Pave	Reg	Lvl	AllPub	Inside	Gtl	...	0	0
1457	1458	70	RL	9042	Pave	Reg	Lvl	AllPub	Inside	Gtl	...	0	0
1458	1459	20	RL	9717	Pave	Reg	Lvl	AllPub	Inside	Gtl	...	112	0
1459	1460	20	RL	9937	Pave	Reg	Lvl	AllPub	Inside	Gtl	...	0	0

1460 rows x 75 columns

Look at the remaining data info

```
In [5]: df_train2.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1460 entries, 0 to 1459
Data columns (total 75 columns):
# Column Non-Null Count Dtype
---
0 Id 1460 non-null int64
1 MSSubClass 1460 non-null object
2 MSZoning 1460 non-null object
3 LotArea 1460 non-null int64
4 Street 1460 non-null object
5 LotShape 1460 non-null object
6 LandContour 1460 non-null object
7 Utilities 1460 non-null object
8 LotConfig 1460 non-null object
9 LandSlope 1460 non-null object
10 Neighborhood 1460 non-null object
11 Condition1 1460 non-null object
12 Condition2 1460 non-null object
13 BldgType 1460 non-null object
14 HouseStyle 1460 non-null object
15 OverallQual 1460 non-null int64
16 OverallCond 1460 non-null int64
17 YearBuilt 1460 non-null int64
18 YearRemodAdd 1460 non-null int64
19 RoofStyle 1460 non-null object
20 RoofMatl 1460 non-null object
21 Exterior1st 1460 non-null object
22 Exterior2nd 1460 non-null object
23 MasVnrType 1452 non-null object
24 MasVnrArea 1452 non-null float64
25 ExterQual 1460 non-null object
26 ExterCond 1460 non-null object
27 Foundation 1460 non-null object
28 BmtQual 1423 non-null object
29 BmtCond 1423 non-null object
30 BmtType 1460 non-null object
31 BmtFinSF1 1460 non-null int64
32 BmtFinSF2 1460 non-null int64
33 BmtUnfSF 1460 non-null int64
34 TotalBsmSF 1460 non-null int64
35 Heating 1460 non-null object
36 HeatingQC 1460 non-null object
37 CentralAir 1460 non-null object
38 Electrical 1459 non-null object
41 JtFltSF 1460 non-null int64
42 2ndFlrSF 1460 non-null int64
43 LowQualFinSF 1460 non-null int64
44 GrLivArea 1460 non-null int64
45 BsmFullBath 1460 non-null int64
46 BsmHalfBath 1460 non-null int64
47 FullBath 1460 non-null int64
48 HalfBath 1460 non-null int64
49 BedroomAbvGr 1460 non-null int64
50 KitchenAbvGr 1460 non-null int64
51 TotRmsAbvGrd 1460 non-null int64
52 Fireplaces 1460 non-null object
53 Functional 1460 non-null object
54 Fireplace 1460 non-null int64
55 GarageType 1379 non-null object
56 GarageYrBlt 1379 non-null float64
57 GarageFinish 1460 non-null object
58 GarageCars 1460 non-null int64
59 GarageArea 1460 non-null int64
60 GarageQual 1379 non-null object
61 GarageCond 1379 non-null object
62 PavedDrive 1460 non-null object
63 WoodDeckSF 1460 non-null int64
64 OpenPorchSF 1460 non-null int64
65 EnclosedPorch 1460 non-null int64
66 3SsnPorch 1460 non-null int64
67 ScreenPorch 1460 non-null int64
68 PoolArea 1460 non-null int64
69 MiscVal 1460 non-null int64
70 MoSold 1460 non-null int64
71 YrSold 1460 non-null int64
72 SaleType 1460 non-null object
73 SaleCondition 1460 non-null object
74 SalePrice 1460 non-null int64
dtypes: float64(2), int64(35), object(38)
memory usage: 422.1+ KB
```

Looking at columns only with int or float

```
In [6]: intorFloat = [x for x in df_train2.columns if df_train2.dtypes[x] != 'object'] #list of columns with int or float
intorFloat
```

```
Out[6]:
```

```
['Id',
'MSSubClass',
'LotArea',
'OverallQual',
'OverallCond',
'YearBuilt',
'YearRemodAdd',
'MasVnrArea',
'BsmFinSF1',
'BsmFinSF2',
'BsmUnfSF',
'TotalBsmSF',
'1stFlrSF',
'2ndFlrSF',
'LowQualFinSF',
'GrLivArea',
'BsmFullBath',
'BsmHalfBath',
'FullBath',
'HalfBath',
'BedroomAbvGr',
'KitchenAbvGr',
'TotRmsAbvGrd',
'Fireplaces',
'GarageYrBlt',
'GarageCars',
'GarageArea',
'WoodDeckSF',
'OpenPorchSF',
'EnclosedPorch',
'3SsnPorch',
'ScreenPorch',
'PoolArea',
'MiscVal',
'MoSold',
'YrSold',
'SalePrice']
```

A new dataframe built using only integer or float values for the regression model.

```
In [7]: df_train3 = df_train2[intorFloat]
df_train3
```

```
Out[7]:
```

	Id	MSSubClass	LotArea	OverallQual	OverallCond	YearBuilt	YearRemodAdd	MasVnrArea	BsmFinSF1	BsmFinSF2	...	Wc
0	1	60	8450	7	5	2003	2003	196.0	706	0	...	0
1	2	20	9600	6	8	1976	1976	0.0	978	0	...	0
2	3	60	11250	7	5	2001	2002	162.0	486	0	...	0
3	4	70	9550	7	5	1915	1970	0.0	216	0	...	0
4	5	60	14260	8	5	2000	2000	350.0	655	0	...	0
...
1455	1456	60	7917	6	5	1999	2000	0.0	0	0	...	0
1456	1457	20	13175	6	6	1978	1988	119.0	790	163	...	0
1457	1458	70	9042	7	9	1941	2006	0.0	275	0	...	0
1458	1459	20	9717	5	6	1950	1996	0.0	49	1029	...	0
1459	1460	20	9937	5	6	1965	1965	0.0	830	290	...	0

1460 rows x 37 columns

there are still some missing values

```
In [8]: missing2 = df_train3.isna().sum()
percentage2 = missing2[missing2 > 0] #columns with missing values
missing2
```

```
Out[8]:
```

```
MasVnrArea      8
GarageBlt       8
dtype: int64
```

Fill missing columns with mean

```
In [9]: #calculates the mean in the column and fills missing value with it
mean = dataframe[column].mean()
dataframe[column].fillna(value=mean, inplace=True)
dataframe
```

```
fillMissing(df_train3, 'MasVnrArea')
fillMissing(df_train3, 'GarageBlt')
```

```
Out[9]:
```

	Id	MSSubClass	LotArea	OverallQual	OverallCond	YearBuilt	YearRemodAdd	MasVnrArea	BsmFinSF1	BsmFinSF2	...	Wc
0	1	60	8450	7	5	2003	2003	196.0	706	0	...	0
1	2	20	9600	6	8	1976	1976	0.0	978	0	...	0
2	3	60	11250	7	5	2001	2002	162.0	486	0	...	0
3	4	70	9550	7	5	1915	1970	0.0	216	0	...	0
4	5	60	14260	8	5	2000	2000	350.0	655	0	...	0
...
1455	1456	60	7917	6	5	1999	2000	0.0	0	0	...	0
1456	1457	20	13175	6	6	1978	1988	119.0	790	163	...	0
1457	1458	70	9042	7	9	1941	2006	0.0	275	0	...	0
1458	1459	20	9717	5	6	1950	1996	0.0	49	1029	...	0
1459	1460	20	9937	5	6	1965	1965	0.0	830	290	...	0

1460 rows x 37 columns

Training dataset after cleaning

```
In [10]: df_train3.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1460 entries, 0 to 1459
Data columns (total 37 columns):
# Column Non-Null Count Dtype
---
0 Id 1460 non-null int64
1 MSSubClass 1460 non-null int64
2 LotArea 1460 non-null int64
3 OverallQual 1460 non-null int64
4 OverallCond 1460 non-null int64
5 YearBuilt 1460 non-null int64
6 YearRemodAdd 1460 non-null int64
7 MasVnrArea 1460 non-null float64
8 BsmFinSF1 1460 non-null int64
9 BsmFinSF2 1460 non-null int64
10 BsmUnfSF 1460 non-null int64
11 TotalBsmSF 1460 non-null int64
12 1stFlrSF 1460 non-null int64
13 2ndFlrSF 1460 non-null int64
14 LowQualFinSF 1460 non-null int64
15 GrLivArea 1460 non-null int64
16 BsmFullBath 1460 non-null int64
17 BsmHalfBath 1460 non-null int64
18 FullBath 1460 non-null int64
19 HalfBath 1460 non-null int64
20 BedroomAbvGr 1460 non-null int64
21 KitchenAbvGr 1460 non-null int64
22 TotRmsAbvGrd 1460 non-null int64
23 Fireplaces 1460 non-null int64
24 GarageYrBlt 1460 non-null float64
25 GarageCars 1460 non-null int64
26 GarageArea 1460 non-null int64
27 WoodDeckSF 1460 non-null int64
28 OpenPorchSF 1460 non-null int64
29 EnclosedPorch 1460 non-null int64
30 3SsnPorch 1460 non-null int64
31 ScreenPorch 1460 non-null int64
32 PoolArea 1460 non-null int64
33 MiscVal 1460 non-null int64
34 MoSold 1460 non-null int64
35 YrSold 1460 non-null int64
36 SalePrice 1460 non-null int64
dtypes: float64(2), int64(35)
memory usage: 422.2 KB
```

```
pd.set_option('max_columns', None) # show all columns
df_train3
```

```
Out[11]:
```

	Id	MSSubClass	LotArea	OverallQual	OverallCond	YearBuilt	YearRemodAdd	MasVnrArea	BsmFinSF1	BsmFinSF2	BsmUnfSF	TotalBsmSF
0	1	60	8450	7	5	2003	2003	196.0	706	0	0	706
1	2	20	9600	6	8	1976	1976	0.0	978	0	0	978
2	3	60	11250	7	5	2001	2002	162.0	486	0	0	486
3	4	70	9550	7	5	1915	1970	0.0	216	0	0	216
4	5	60	14260	8	5	2000	2000	350.0	655	0	0	655
...
1455	1456	60	7917	6	5	1999	2000	0.0	0	0	0	0
1456	1457	20	13175	6	6	1978	1988	119.0	790	163	0	163
1457	1458	70	9042	7	9	1941	2006	0.0	275	0	0	275
1458	1459	20	9717	5	6	1950	1996	0.0	49	1029	0	1029
1459	1460	20	9937	5	6	1965	1965	0.0	830	290	0	290

1460 rows x 37 columns

pd.set_option('max_columns') #sets max number of columns displayed to default

```
In [12]: df_train3
```

```
Out[12]:
```

	Id	MSSubClass	LotArea	OverallQual	OverallCond	YearBuilt	YearRemodAdd	MasVnrArea	BsmFinSF1	BsmFinSF2	BsmUnfSF	TotalBsmSF
0	1	60	8450	7	5	2003	2003	196.0	706	0	0	706
1	2	20	9600	6	8	1976	1976	0.0	978	0	0	978
2	3	60	11250	7	5	2001	2002	162.0	486	0	0	486
3	4	70	9550	7	5	1915	1970	0.0	216	0	0	216
4	5	60	14260	8	5	2000	2000	350.0	655	0	0	655
...
1455	1456	60	7917	6	5	1999	2000	0.0	0	0	0	0
1456	1457	20	13175									


```
[24]: upperBoundary = df_train.describe().SalePrice[6] + boundary
upperBoundary = 340037.5

creating 2 dataframes to separate SalePrice above the upperBoundary and less than the upperBoundary

In [25]: df_train5 = (df_train[(df_train['SalePrice']>upperBoundary)])

In [26]:

In [27]: df_train6 = df_train[(df_train['SalePrice']>upperBoundary)]

As the features are mostly above the upper boundary, the outlier's value will be changed to the upperBoundary value.

In [28]: df_train6['SalePrice'] = upperBoundary
df_train6
```

OverQual YearBuilt YearRemodAdd TotalBmtSF 1stFlrSF GrLivArea FullBath TotRmsAbvGrd GarageCars GarageArea SalePrice

51	9	1981	2006	1175	1182	2324	3	11	3	736	340037.5
113	9	1985	1987	1842	1842	1842	0	5	3	894	340037.5
58	10	2006	2006	1410	1426	2945	3	10	3	641	340037.5
112	7	2007	2007	1264	1282	2696	2	10	3	792	340037.5
151	8	2007	2008	1710	1710	1710	2	6	3	866	340037.5
...
1268	8	1935	1997	728	1968	3447	3	11	3	1014	340037.5
1353	8	1995	1996	233	2053	3238	2	9	3	666	340037.5
1373	10	2001	2002	2633	2633	2633	2	8	3	804	340037.5
1388	8	2006	2007	1746	1746	1746	2	7	3	758	340037.5
1437	9	2008	2008	1932	1932	1932	2	7	3	774	340037.5

61 rows x 11 columns

Combine the 2 dataframes with outliers adjusted.

```
In [29]: df_train7 = pd.concat((df_train5, df_train6))

Ensuring that the outliers have been adjusted by checking the max value of 'SalePrice'

In [30]: df_train7['SalePrice'].describe()

Out[30]: count    1460.000000
mean    17331.226370
std      67203.835925
min      34900.000000
25%     129975.000000
50%     163000.000000
75%     214000.000000
max     340037.500000
Name: SalePrice, dtype: float64

as seen from the max price of SalePrice the upper boundary has been set properly

In [31]: df_train7.info()

<class 'pandas.core.frame.DataFrame'>
Int64Index: 1460 entries, 0 to 1437
Data columns (total 11 columns):
#   Column      Non-Null Count  Dtype
---  --
0   OverallQual  1460 non-null    int64
1   YearBuilt    1460 non-null    int64
2   YearRemodAdd 1460 non-null    int64
3   TotalBmtSF   1460 non-null    float64
4   1stFlrSF     1460 non-null    int64
5   GrLivArea    1460 non-null    float64
6   FullBath     1460 non-null    int64
7   TotRmsAbvGrd 1460 non-null    int64
8   GarageCars   1460 non-null    int64
9   GarageArea   1460 non-null    float64
10  SalePrice    1460 non-null    float64
dtypes: float64(1), int64(10)
memory usage: 136.9 KB

In [ ]:
```

Model training

with the training data modified, we can now split the data into training set and testing set.

```
In [32]: x = df_train.drop('SalePrice', axis=1) # removing the 'SalePrice' as that is what i am training the model on
y = df_train['SalePrice']

# splitting data into train and test data set
x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.3, random_state=0)
```

using polynomial regression and linear regression to train the model to predict y.

```
In [33]: polyReg = PolynomialFeatures(degree = 2) # train using a high degree to prevent overfitting
x_poly = polyReg.fit_transform(x_train) # adding x^2 to the feature set
regression = LinearRegression()
regression.fit(x_poly, y_train) # train x_poly because we have additional information

x_test_polyReg = polyReg.fit_transform(x_test)
y_pred = regression.predict(x_test_polyReg)
```

array([119430.0429084, 198401.83800896, 183031.28304756, 251839.77867655, 256749.84624462, 100923.34086749, 276431.34142883, 114082.46793201, 191252.62517434, 198151.9429883, 95010.66045409, 189008.70705185, 178580.28292495, 140074.83916397, 147375.05401192, 103738.88117345, 198747.49441399, 178877.89923728, 207644.82935289, 222800.06578013, 102574.32572919, 146715.94021172, 136791.14975238, 246348.54393633, 75856.08930946, 85422.50241484, 135035.82809152, 219339.61530983, 298169.41160077, 178986.84748774, 173361.31929329, 177641.04041121, 268574.02518588, 285738.00151856, 210474.9946175, 137971.64473948, 287004.66824406, 204780.52074055, 121346.67124245, 182729.05899037, 99061.82246649, 218235.3513316, 194548.4142074, 191324.76039823, 98373.61235796, 143795.86257744, 137405.84597463, 129350.9892957, 242292.02849521, 108631.67690599, 311997.37161289, 153024.91072173, 300649.21150989, 217818.63344025, 223439.97127965, 121145.69653734, 177083.14508997, 93887.72989715, 268637.36414641, 171345.63843792, 97289.77353268, 122592.07031027, 119848.60780076, 268081.85262359, 71221.60267329, 137931.74303716, 274036.60786788, 252431.8147119, 122427.94857917, 268648.8514615, 158020.12322452, 182451.7920736, 56305.242738, 193329.4489251, 197123.6832372, 99529.71759549, 174639.23064338, 132774.50696462, 123484.53789776, 151694.3064381, 255428.79349952, 132899.25161337, 166295.57088984, 151217.06451398, 225337.60940243, 188958.80041828, 214828.67177732, 110666.60843318, 188064.14264608, 191977.89172225, 121420.61347022, 224441.90303949, 239673.62743678, 167790.1430672, 152691.64546878, 142550.60667324, 153537.45743287, 192083.04045409, 139324.07403774, 112038.65948231, 192107.10738917, 179315.36703343, 279088.07239868, 121145.69653734, 189596.47547415, 101538.36806684, 167514.17044519, 140186.66069536, 126485.12123279, 196983.80128986, 175858.41957342, 78641.84940202, 258363.91287023, 166839.68841778, 209900.96430061, 122862.35381681, 208297.55926473, 152012.08664444, 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