Computation Tree Logic

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Motivation and Intuition Motivation Intuition

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Previously on Temporal Logic Week...

Temporal Logic

Motivation and Intuition Motivation

Motivation

Needing of uncertainty;

Motivation

Needing of uncertainty; Different paths of the future;

Motivation and Intuition Motivation

Intuition

Intuition

In Computation Tree Logic (CTL) the model of time is a tree-like structure. This way, we cannot use Linear Temporal Logic (LTL) to express the existence of a certain path of time in which some event occurs.

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Syntax Definition

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$$\mathsf{EF}\phi \mid \mathsf{AG}\phi \mid \mathsf{EG}\phi \mid \mathsf{A}[\phi \mathcal{U}\phi] \mid \mathsf{E}[\phi \mathcal{U}\phi]$$

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With p as a literal (atomic formula), AX, EX, AF, EF, AG e EG unary operators.

Syntax Intuition

content...

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Semanthics