

2nd Year Christmas Test

studyclix

Marking scheme

Question 1

Marking scheme

Q11	Model Solution - 25 marks	Marking Notes
(a) & (b)	(a) $12 - 3(-2)^2$ $= 12 - 3(4)$ $= 0$	Scale 10D (0, 4, 6, 8, 10) Accept correct answer in (a) without work <i>Low Partial Credit:</i> <ul style="list-style-type: none">Work of merit in (a) or (b) for example: -2^2 in (a), $p(m + 3)$ in (b)

Question 2

Marking scheme

Question 3

Marking scheme

Q12	Model Solution – 35 Marks	Marking Notes								
(a)	$(n - 2)(n - 9)$ <p style="text-align: center;">OR</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 5px;">n</td> <td style="padding: 5px;">-9</td> </tr> <tr> <td style="padding: 5px;">n</td> <td style="padding: 5px;">n^2</td> </tr> <tr> <td style="padding: 5px;">-2</td> <td style="padding: 5px;">-2n</td> </tr> <tr> <td style="padding: 5px;"></td> <td style="padding: 5px;">18</td> </tr> </table> <p style="text-align: center;">so $(n - 2)(n - 9)$</p> <p style="text-align: center;">OR</p> $\begin{aligned} & n^2 - 11n + 18 \\ = & n^2 - 9n - 2n + 18 \\ = & n(n - 9) - 2(n - 9) \\ = & (n - 9)(n - 2) \end{aligned}$	n	-9	n	n^2	-2	-2n		18	Scale 5C (0, 2, 3, 5) Accept correct answer without work. <i>Low Partial Credit</i> <ul style="list-style-type: none"> Work of merit, for example: $(n - 2)$ or $(n - 9)$, or any pair of factors of 18, or $n^2 - 9n - 2n + 18$. Some correct substitution into the quadratic formula <i>High Partial Credit</i> <ul style="list-style-type: none"> Factors which multiply to give 2 correct coefficients of the given expression, including the signs, for example: $(n + 2)(n + 9)$, or $(n - 5)(n - 6)$. $n(n - 9) - 2(n - 9)$ Solves $n^2 - 11n + 18 = 0$ (without factorising).
n	-9									
n	n^2									
-2	-2n									
	18									
(b)	$\begin{aligned} & y(w - 1) + 1(w - 1) \\ = & (w - 1)(y + 1) \text{ or } (1 - w)(-y - 1) \end{aligned}$ <p style="text-align: center;">OR</p> $\begin{aligned} & w(y + 1) - 1(y + 1) \\ = & (y + 1)(w - 1) \text{ or } (1 - w)(-y - 1) \end{aligned}$	Scale 5C (0, 2, 3, 5) <i>Low Partial Credit</i> <ul style="list-style-type: none"> Work of merit, for example: a common factor identified from given expression <i>High Partial Credit</i> <ul style="list-style-type: none"> $w(y + 1) - 1(y + 1)$ Correct answer without work 								
(c)	$\begin{aligned} & \frac{5}{3(4)-2} - \frac{7}{6(4)-12} \\ = & \frac{5}{10} - \frac{7}{12} \\ = & -\frac{5}{60} = -\frac{1}{12} \text{ or } -0.083 \dots \end{aligned}$	Scale 10B (0, 5, 10) Accept correct answer without work <i>Partial Credit</i> <ul style="list-style-type: none"> $3(4) - 2$ or $6(4) - 12$ 								

Question 4

Marking scheme

- (a) Multiply out and simplify $(x + 5)(x^2 - 2x + 6)$.

$$\begin{aligned}(x + 5)(x^2 - 2x + 6) &= x^3 - 2x^2 + 6x + 5x^2 - 10x + 30 \\ &= x^3 + 3x^2 - 4x + 30.\end{aligned}$$

OR

	x^2	$-2x$	$+6$
x	x^3	$-2x^2$	$+6x$
$+5$	$+5x^2$	$-10x$	$+30$

$$= x^3 + 3x^2 - 4x + 30$$

Question 5

Marking scheme

$$\begin{aligned}(b)(i) \quad & (5x)^2 - (7n)^2 \\ &= (5x + 7n)(5x - 7n)\end{aligned}$$

OR

$$(-5x - 7n)(7n - 5x)$$

Scale 10C (0, 3, 8, 10)

Accept correct answer without work.

Low Partial Credit

- Indicates or shows understanding of difference of 2 squares
- $5x$ **or** $7n$ appears
- **5 and 7 appear**

High Partial Credit

- Correct, other than sign errors
- $(5x)^2 - (7n)^2$
- $5x + 7n$ **or** $5x - 7n$

<p>(b)(ii)</p> <p>$(2x + 3)(x - 6)$</p> <p style="text-align: center;">OR</p> <p>Guide Number = $2 \times (-18) = -36$</p> $2x^2 - 12x + 3x - 18$ $= 2x(x - 6) + 3(x - 6)$ $= (2x + 3)(x - 6)$ <p style="text-align: center;">OR</p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td>$2x$</td> <td>$+3$</td> </tr> <tr> <td>x</td> <td>$2x^2$</td> <td>$3x$</td> </tr> <tr> <td>-6</td> <td>$-12x$</td> <td>-18</td> </tr> </table> <p style="text-align: center;">$(2x + 3)(x - 6)$</p>		$2x$	$+3$	x	$2x^2$	$3x$	-6	$-12x$	-18	<p>Scale 5C (0, 2, 4, 5)</p> <p>Accept correct answer without work.</p> <p>No Credit</p> <ul style="list-style-type: none"> • () () <p>Low Partial Credit</p> <ul style="list-style-type: none"> • Some work of merit, e.g. factorises $2x^2$ or 18 or finds / factorises 36 • Any correct substitution into the quadratic formula <p>High Partial Credit</p> <ul style="list-style-type: none"> • $2x(x - 6) + 3(x - 6)$ • $x(2x + 3) - 6(2x + 3)$ • Answer given multiplies out to give two correct terms (including signs) • Solves correctly $2x^2 - 9x - 18 = 0$ (i.e. $x = 6$ and $x = -\frac{3}{2}$)
	$2x$	$+3$								
x	$2x^2$	$3x$								
-6	$-12x$	-18								

Question 6

Marking scheme

<p>(a)</p>	<p style="text-align: center;">10 marks</p>	<p style="text-align: right;">Att 3</p>																						
<p>I</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 30%;">$4 - x$</td> <td style="width: 40%;">$2x - 5$</td> </tr> <tr> <td>$4 + 5$</td> <td>$2x + x$</td> </tr> <tr> <td>9</td> <td>$3x$</td> </tr> <tr> <td>$9 - 3$</td> <td>x</td> </tr> <tr> <td>3</td> <td>x</td> </tr> </table> <p style="text-align: right;">7m</p> <p>II</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 30%;">$4 - x$</td> <td style="width: 40%;">$2x - 5$</td> </tr> <tr> <td>$-x - 2x$</td> <td>$-5 - 4$</td> </tr> <tr> <td>$-3x$</td> <td>-9</td> </tr> <tr> <td>$3x$</td> <td>9</td> </tr> <tr> <td>x</td> <td>$9 \div 3$</td> </tr> <tr> <td>x</td> <td>3</td> </tr> </table> <p style="text-align: right;">7m</p> <p style="text-align: center;">$x \leq 3 \rightarrow \{1,2,3\}$</p> <p style="text-align: right;">7m</p> <p style="text-align: center;">— ● — ● — ● — 1 2 3</p> <p style="text-align: right;">10m</p>			$4 - x$	$2x - 5$	$4 + 5$	$2x + x$	9	$3x$	$9 - 3$	x	3	x	$4 - x$	$2x - 5$	$-x - 2x$	$-5 - 4$	$-3x$	-9	$3x$	9	x	$9 \div 3$	x	3
$4 - x$	$2x - 5$																							
$4 + 5$	$2x + x$																							
9	$3x$																							
$9 - 3$	x																							
3	x																							
$4 - x$	$2x - 5$																							
$-x - 2x$	$-5 - 4$																							
$-3x$	-9																							
$3x$	9																							
x	$9 \div 3$																							
x	3																							

Question 7

Marking scheme

Q8	Model Solution – 25 Marks	Marking Notes
(a)	$\begin{aligned}x &= \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(-7)}}{2(1)} \\&= \frac{4 \pm \sqrt{16+28}}{2} \\&= \frac{4 \pm \sqrt{44}}{2} \\&= 5 \cdot 316\dots \text{ or } -1 \cdot 316\dots \\&= 5 \cdot 32 \text{ or } -1 \cdot 32 \quad [2 \text{ D.P.}]\end{aligned}$	<p>Scale 15C (0, 4, 12, 15) Note: If one root is given, award HPC at most Consider the solution as having 3 steps: Step 1: Correct formula Step 2: Full correct substitution into the quadratic formula. Step 3: Evaluates the quadratic formula.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • 1 step correct • Identifies a, or b, or c • Correctly factorised and stops • 1 correct answer without work <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • 2 steps correct • 2 correct answers without work <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> • Apply a * for incorrect rounding, or for answers in surd form: $2 + \sqrt{11}$, $2 - \sqrt{11}$

Question 8

Marking scheme

(c) (i) Solve the simultaneous equations:

$$2x - 3y = 18 \quad \textcircled{1}$$

$$5x + 9y = -10 \quad \textcircled{2}$$

$$\textcircled{1} \times 3: \quad 6x - 9y = 54$$

$$\textcircled{2}: \quad \underline{5x + 9y = -10}$$

$$11x = 44$$

$$\div 11: \quad x = 4$$

Sub in $x = 4$ in $\textcircled{1}$:

$$2(4) - 3y = 18$$

$$8 - 3y = 18$$

$$-3y = 18 - 8$$

$$-3y = 10$$

$$\times (-1): \quad 3y = -10$$

$$\div 3: \quad y = -10 \div 3 = -10/3 \text{ or equivalent}$$

Answer: $x = 4$ and $y = -10/3$.

(ii) Verify your answer to (c)(i).

Note: Only need to check the equation that wasn't used to find the second variable. In this case, we only need use ②.

$$5(4) + 9\left(-\frac{10}{3}\right) = 20 - 30 = -10.$$

Question 9

Marking scheme

Q.10	Model Solution – 15 Marks	Marking Notes
(a)	$\begin{aligned} r &= 4 \text{ cm} \\ C &= 2\pi r \\ C &= 2\pi(4) \\ &= 8\pi \\ &= 25.1 \text{ cm [1 D.P.]} \end{aligned}$	<p>Scale 5C (0, 2, 3, 5) Accept correct answer without work <i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Radius correct Correct relevant formula <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> Fully correct substitution into formula Answer given as 8π Finds area of the circle <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Apply a * for no rounding or incorrect rounding Apply a * for no units or incorrect units
(b), (c)	$\begin{aligned} (\text{b}) \text{ Length} &= 6 \times \text{diameter} + C \\ &= (6 \times 8) + 25.1 \\ &= 48 + 25.1 \\ &= 73.1 \text{ cm} \end{aligned}$ $\begin{aligned} (\text{c}) \text{ Total distance} &= 73.1 \text{ cm} \\ 1 \text{ turn} &= 25.1 \text{ cm} \\ \text{Number of turns} &= \frac{73.1}{25.1} = 2.9 \text{ turns} \\ &\text{2 full turns} \end{aligned}$	<p>Scale 10D (0, 2, 4, 8, 10) <i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Work of merit in one part, for example: adds some relevant measurements <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> One part correct Work of merit in both parts <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> One part correct and work of merit in other part <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> Apply a * for answer given as 2.9 or 3 turns Apply a * for no units or incorrect units in (b)