



Article

Explaining Bad Forecasts in Global Time Series Models

Jože Rožanec 1,2,3,*, Elena Trajkova 1,4,0, Klemen Kenda 1,2,3,0, Blaž Fortuna 1,2,0 and Dunja Mladenić 1

- Jožef Stefan Institute, Jamova 39, 1000 Ljubljana, Slovenia; trajkova.elena.00@gmail.com (E.T.); klemen.kenda@ijs.si (K.K.); blaz.fortuna@ijs.si (B.F.); dunja.mladenic@ijs.si (D.M.)
- Qlector d.o.o., Rovšnikova 7, 1000 Ljubljana, Slovenia
- Jožef Stefan International Postgraduate School, Jamova 39, 1000 Ljubljana, Slovenia
- Faculty of Electrical Engineering, University of Ljubljana, Tržaška 25, 1000 Ljubljana, Slovenia
- * Correspondence: joze.rozanec@ijs.si

Featured Application: The outcomes of this work can be applied to understand better when and why global time series forecasting models issue incorrect predictions and iteratively groom the dataset to enhance the models' performance.

Abstract: While increasing empirical evidence suggests that global time series forecasting models can achieve better forecasting performance than local ones, there is a research void regarding when and why the global models fail to provide a good forecast. This paper uses anomaly detection algorithms and explainable artificial intelligence (XAI) to answer when and why a forecast should not be trusted. To address this issue, a dashboard was built to inform the user regarding (i) the relevance of the features for that particular forecast, (ii) which training samples most likely influenced the forecast outcome, (iii) why the forecast is considered an outlier, and (iv) provide a range of counterfactual examples to understand how value changes in the feature vector can lead to a different outcome. Moreover, a modular architecture and a methodology were developed to iteratively remove noisy data instances from the train set, to enhance the overall global time series forecasting model performance. Finally, to test the effectiveness of the proposed approach, it was validated on two publicly available real-world datasets.

Keywords: explainable artificial intelligence; XAI; time series forecasting; global time series models; machine learning; artificial intelligence



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1. Introduction

Time series forecasting is a relevant problem with application in many domains [1], gaining further relevance with the increasing availability of historical data [2]. Historically, much research focused on time series models trained on a single time series [3]. Though global machine learning models issued good results in the past, they gained new attention with the advent of deep learning [4], and recent success on the M4 and M5 time series forecasting competitions [5,6]. Such models can learn patterns shared across multiple time series, enhancing the overall forecasting performance. The usage of multiple time series to train the model can be considered a source of explainability: each forecast can be explained not only through past behavior on a single time series, but similar patterns can be found in other time series, providing a different perspective and complementary insights [7]. The ability to develop global time series models implicates scaling advantages too: it reduces the number of forecasting models, and thus the amount of human supervision required to build them, and fewer deployments, monitoring, and maintenance [8].

While authors have shown that global time series machine learning forecasting models (GTSMLFM) can achieve better performance overall, "understanding when and why global forecasting models work, is arguably the most important open problem currently in time series forecasting" [3]. It is thus crucial to develop Explainable Artificial Intelligence (XAI)

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approaches to answer those questions. The approaches can differ based on the goal they aim to tackle (e.g., increase trust in the model or provide insights that can be used to improve the model), the user profile they target and focus (if the explanations provided are either local or global) [9].

The paper focuses on understanding when and why GTSMLFMs work, providing relevant information to the end-users and the machine learning engineers. The end-users must understand if a particular forecast instance can be relied upon (e.g., detect if it can be considered anomalous) and what features do influence the forecast. If the forecast is anomalous, the user can be interested in getting to know some counterfactual examples. While machine learning engineers will appreciate this information, they can also find which instances from the train set most likely influenced the models' learning to issue an unlikely forecast. To provide such an understanding to the users, we use local features relevance, anomaly detection models, and develop a novel approach to provide counterfactual explanations for regression methods. Furthermore, we integrate the insights into a dashboard that can serve the end-users and the machine learning engineers, to understand better when and why global time series forecasting models work.

This research provides several contributions, with which we address the gap of providing means to answer when and why a GTSMLFM prediction should be considered a bad forecast [3]. First, we make use of anomaly detection algorithms to identify potentially wrong forecasts. Then, we compute the models' feature attribution for those data instances, identify similar data instances in the train set, and create counterfactual examples. Furthermore, we develop a dashboard integrating the insights mentioned above and a line plot showing the time series, with a relevance heatmap overlay to inform the influence of data points on a given forecast. While such relevant heatmaps have been widely applied for deep learning models, they are not frequently used for other time series models. In addition, such a dashboard enables a visual inspection of time series and forecasts—a valuable tool for end-users and machine learning engineers. Finally, based on our experience, we outline an architecture and a methodology that can be followed to enhance the dataset and GTSMLFMs iteratively.

To evaluate our approach, we conduct a series of experiments and perform a quantitative evaluation to measure the impact of the insights are developed when engineering the GTSMLFM. In particular, we measure the Mean Absolute Scaled Error (MASE) [10], the number of outliers observed in the test set, and the number of instances removed from the train set, based on the detected anomalous predictions.

We organized the remainder of this paper as follows. In Section 2, we review related scientific works; in Section 3, we introduce the proposed architecture, while in Section 4, we provide details on the methodology that we followed to treat the dataset and train new GTSMLFMs iteratively. In Section 5, we describe two different time series datasets that we used to test our approach, detailing the preprocessing steps and features that we created. In Section 6, we describe the experiments that we performed, provide a more detailed overview regarding the metrics used to measure the results, and the results we obtained, while in Section 7 we address the limitations of this research. Finally, in Section 8, we conclude by summarizing this research, and outline future work.

2. Review of Related Scientific Works

2.1. Forecasting Time Series: Local vs. Global Approach

For many decades, most research on time series forecasting assumed that the time series are generated by independent processes and can be tackled as a regression problem, creating a single model per time series (local models) [8,11]. Growing empirical evidence suggests that creating a single model to forecast multiple time series (under the assumption of forecasts' independence for different time series) known as global models can outperform local ones. Seminal research on using global models developed decades ago [12], and the concept was further explored by many researchers afterwards [13]. The first approaches towards global models considered pooling similar time series, which improves the overall

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models' accuracy. By having more training data of similar time series, algorithms can better distinguish common data patterns, while also minimizing distortions introduced by outlier data points [14]. On the other side, this approach requires defining some time series grouping criteria, which can lead to suboptimal groupings [15]. Among pooling strategies, we can find model-based clustering [14,16,17], random clustering [8], grouping based on similarity measures [18–20], or expert judgement [21]. Recent research has explored creating global models considering all available time series, regardless of their heterogeneity, obtaining promising results [3,8,22]. Furthermore, it has been demonstrated that, for every dataset, some global model exists that can equal or outperform a local model, regardless of how heterogeneous the data may be [8]. Such models make the strong assumption that some relationship exists between time series, though the forecasts are independent of each other [11].

These insights, the good results obtained by applying global neural network models for time series forecasting [11,23–27], and success of global models at the M4 and M5 competitions [5,6], have renewed the research interest on global models for time series forecasting [3]. In such models, the relationship between time series is not very well understood, and understanding why and when do global time series forecasting models work remains an open research topic [3]. We envision that anomaly detection algorithms can be used to detect when the GTSMLFM provides accurate forecasts or not, and XAI approaches can provide insights to understand better factors affecting the forecasts, and provide prototype (local) explanations [28], and counterfactual examples.

2.2. Time Series Anomaly Detection

One of the open research questions regarding GTSMLFM is, when do such models provide acceptable forecasts [3]? Such response can be obtained from anomaly detection algorithms and models, which can alert on point anomalies. In this section, we provide an overview of anomaly detection techniques, focusing on the ones developed and applied in a time series setting. We use the terms anomaly, outlier, or deviant interchangeably [29], to denote "observations that deviate so much from others as to arouse suspicion that it was generated by another mechanism" [30]. In particular, outliers related to time series data must also consider the behavior across time [31].

Outliers can be characterized into many types. The first characterization of this type can be found in [32], who introduced the concepts of two time series' outlier types: those (a) that affect a single observation (*type I*), and those (b) that affect an observation and the subsequent ones (*type II*). More recently, [31] distinguishes between *point outliers* (single point in the time series, which has an unusual value when compared to the whole time series or the neighboring points) and *subsequence outliers* (points which may not be outliers by themselves, but the sequence arrangement is anomalous). *Subsequence outliers* are further classified into *contextual anomalies* (they are anomalous in the context of the surrounding observations) or *pattern anomalies* (they are anomalous regardless of the surrounding observations) [33]. In this research, we limit ourselves to point outliers.

Anomaly detection techniques are frequently classified into three categories: statistical, distance-based approaches, and model-based approaches [34]. The first anomaly detection techniques were developed in statistics and remained among the most frequently used ones. Non-parametric techniques usually allow fast computations and are adopted where such speed is of primary importance. Among them, we find the histogram-based approaches, which assume feature independence and determine the outliers based on the histogram distribution [35–38]. Other non-parametric approaches are bitmap time series anomaly detectors, which compute the relative frequency of its features to create a bitmap and identify anomalous time series [39,40], and statistical methods that allow estimating outliers based on a kernel density estimation by using a kernel function. Such kernel functions can provide a probability estimate, given that function is a probability density function [34,41–43]. Among the parametric methods, we find the Gaussian methods, such

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as box-plot anomaly detection [44], the Gaussian process [45,46], or regression approaches such as least squares regression [47–49].

Statistical anomaly detection methods cannot be applied on datasets with an unknown distribution [38]. Different approaches were developed to overcome this issue. When considering the distance between data points, we find the k-nearest-neighbors (kNN), which determines the outliers based on the kNN distance. While approaches were developed to determine the best k parameter [50], some techniques attempted to avoid dependence on the k-value. One such method is the local outlier factor (LOF) method, which computes the distance from a point to all other points in the dataset [51]. A similar approach was followed at the outlier detection using indegree number (ODIN), which computes the number of instances that contain a given point in their neighborhood. However, a parameter is required to determine the outlier threshold [52]. A different method was developed by [53], who introduced the multi-granularity deviation factor to identify local density variations that lead to isolated outliers or outlying clusters. Variations to the LOF method were developed to solve some of its shortcomings. For example, the connectivity-based outlier factor (COF) aims to capture better clusters where the data points are distributed in a linear manner [54], while influenced outlierness (INFLO) attempts to better discriminate points nearby two clusters with different densities [55]. Finally, to account for the different feature importance, [56] developed an alternative anomaly detection algorithm, using a weighted kNN.

Model-based techniques can be divided into (i) models that learn and predict whether the value is anomalous and (ii) models that compare the potential outlier with expected values drawn from a generative model or data distribution. Since model-based techniques require labeled data, active learning can be utilized to minimize the labeling effort [57]. Among the models of the first group, we find the SVM-based models, such as the one-class support vector machine (OC-SVM), which was introduced by [58], and later enhanced by many authors [59,60]. Since the regular SVM algorithm can provide poor generalization on an imbalanced dataset, the authors suggested representing the anomalous classes with the high dimensional space origin and mapping anomalous instances close to it. Other SVM variants used for anomaly detection include support vector data description (SVDD) [61], and SVM-SVDD [62]. A different intuition is followed in the Isolation Forest. This treebased model is based on the principle that the fewer instances of anomalies generate a smaller number of partitions, and thus are likely to have short paths in the tree structure [63]. Other models reported in the literature involve the use of random forests [64], gradient boosted machines [65], artificial neural networks [66], or voting ensembles [67]. Models from the second group have multiple configurations, varying the generative methods and outlier detection criteria. Some examples are the use of ARIMA models to predict future time series values and mark incoming readings as anomalies if they exceed a certain threshold when compared with the forecast [68,69]. Other approaches fused statistical methods and ANNs [70], or used ANNs alone [31,71].

Anomaly detection algorithms can identify anomalous forecasts in the context of a particular time series. Based on the algorithm type, insights can be gained on why the point forecast is considered anomalous. Additional insights can be obtained through XAI to understand which features were most influential to such forecast and provide counterfactual examples, highlighting value changes to those features that would produce a better outcome.

2.3. Explainable Artificial Intelligence

The increasing adoption of artificial intelligence demands understanding the logic beneath the forecasts so that a decision can be made as to whether such forecasts can be trusted or not [72]. The sub-field of artificial intelligence devoted to research on obtaining and providing such understanding is called explainable artificial intelligence (XAI). Authors identify two sources of model opacity [73]. The first one is the complexity of the formal structure of the model, which can be beyond human comprehension, or alien to human

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reasoning. When the opacity cannot be removed even by human experts, we speak about deep opacity [74]. The second source of opacity is the intentionally induced opaqueness to avoid revealing sensitive model details (e.g., due to their proprietary nature).

Researchers developed multiple approaches to provide black-box explanations of forecasting models. Among the most frequently cited, we find LIME [75] and its variants (e.g., k-LIME [76], DLIME [77], and LIMEtree [78]), Anchors [79], Local Foil Trees [80], or LoRE [81]. These approaches build surrogate models for each prediction sample, learning the reference model's behavior on the particular case of interest by introducing perturbations to the feature vector variables. The Shapley additive explanations take a different approach (SHAP) [82,83], which are grounded in cooperative game theory. The feature relevance is computed based on the approximate computation of Shapley values. Shapley values are also used to explain features relevance in a time series setting. In particular, the TimeSHAP implementation measures which features and past events are most relevant to a recurrent model [84].

Research regarding XAI for time series has focused mainly on explainability for deep learning models. One of the first of such methods was introduced by [85], who computed feature attributions by taking the partial derivative of the output class with respect to the input. This method was later improved in the *Gradient*Input* method, which computes neuron and filter activations for a specific instance by multiplying the input by the partial derivative of a layer with respect to the input [86]. Similar approaches followed, such as the Deep Learning Important FeaTures (DeepLIFT) [87], *integrated gradients* [88], or *Smooth-Grad* [89]. The introduction of attention mechanisms to deep learning models was also envisioned as a source of explainability, since it provides insights regarding which points in time are relevant to the forecast [90]. Such information is frequently presented in heatmaps [91,92], saliency maps [85,93], and custom visualizations [94]. Finally, several feature perturbation methods were developed to measure the features' contribution to the forecasted value when such features are removed [95], or masked [96–98].

Methods such as Shapley values [99] and region partition trees [100] have been successfully applied to explain detected anomalies. More systemic approaches have been developed too, such as Exathlon [101], EXAD [102], and others [103]. While EXAD focuses on explanation discovery for each anomaly, Exathlon crafts the explanations, providing two pieces of information to the user: why the data point was identified as an anomaly and the root causes of such anomaly.

Along with feature relevance, it is sometimes important to know how values should change to achieve a different forecast. Such examples are known as counterfactual explanations. When counterfactual explanations are provided as actionable advice, they are known as directive explanations. Directive explanations can be either directive-specific (suggest a concrete action to change the forecasted value), or directive-generic (suggest a generic action to alter the forecasted value) [104]. While most frequently applied to classification models, counterfactual explanations are also applied to regression models. While such counterfactual explanations most frequently use some threshold [105], other implementations were developed based on potentials [106], or satisfiability modulo theories solvers [107], among others.

While counterfactual examples provide value to understand how to change a certain target state, sometimes it is useful to visualize prototypical instances similar to the feature vector used to issue a prediction. Such examples are known as prototype explanations, and allow us to understand better which instances influenced a certain forecast [108].

As described above, multiple methods exist to obtain relevant information that can explain the underlying reasoning of an artificial intelligence model. Along with them, it is also important to consider how such information is presented to the users. Good explanations should convey meaningful information, resemble a logic explanation [109], target a specific user profile [110], focus on actionability, and if possible, provide some counterfactual examples [111]. An explanation should take into account relevant context, which can be captured in three elements: the target user profile, the explanation goals

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(e.g., improve the model, or enhance trust in the system), and the focus (if the explanations provided are meant at a global or local level).

When developing our architecture and dashboard, we considered different intuitive ways to present the information, ranging from plots and tables to human-readable sentences. When the forecasts are considered anomalous, it is helpful to the user to understand why such a forecast is considered anomalous, which are the most relevant features to that forecast, provide counterfactual examples, and examples from the training set that could have influenced the forecast.

3. The Proposed Architecture

We propose a modular architecture to provide forecast explanations for global time series forecasting models. We combine anomaly detection and explainability methods to enhance the forecasting precision and provide valuable contextual information to the end-users. The anomaly detection module provides a means to identify potentially bad forecasts. In such cases, we can fall back to a local statistical model, or alert the user that a given forecast should not be trusted given past time series' behavior. The feature relevance informs the user on which variables exercised the most influence on the forecast. We use them as an input when computing the counterfactual examples to understand better what value changes on those variables would produce an outcome that is no longer considered an outlier. Finally, we provide insight to the user on which data instances could have influenced the forecasting models to provide such a forecast by identifying them in the train set based on their similarity regarding the forecasted one. We consider that this information helps investigate possible patterns learned by the model and how to engineer a better model learning in the future.

The architecture (see Figure 1) comprises the following components:

- Data Module: provides a dataset to train machine learning GTSMLFMs. The dataset
 comprises time series data, either considering their raw values and derivative features
 or a refined version where specific instances that could cause outlier forecasts were
 treated. The module wraps a set of strategies to find and treat data instances that are
 similar to the ones producing outlier forecasts, identified by the anomaly detection
 module.
- Forecasting Module: comprises a machine learning GTSMLFM, and a set of local statistical models to forecast the time series. The machine learning GTSMLFM is created based on a dataset obtained from the Data Module. The Forecasting Module makes use of the input provided by the Anomaly Detection Module to decide whether the outcome should be the forecast obtained from a GTSMLFM, or a local statistical model.
- Anomaly Detection Module: leverages algorithms and models to analyze the forecast
 in the context of a time series and classify it as an anomaly or not. It interacts with the
 Forecasting Module and the XAI Module, providing feedback on whether a forecast
 can be considered anomalous or not.
- XAI Module: uses various XAI algorithms and models to craft forecast explanations for the user. In particular, we envision that this module (i) indicates if the forecast is anomalous, (ii) crafts a text explanation highlighting most relevant features influencing a specific forecast, (iii) shows a sample of *n* data instances found in the train set that most likely influenced the GTSMLFM towards the given forecast, and (iv) shows a set of counterfactual examples created considering (a) the relevant features to that specific forecast, and (b) past values observed for that particular time series. We consider that this information provides the user a good insight into whether the forecast can be trusted and understand the behavior of the underlying model.
- API: a standard Application Programming Interface (API) endpoint can be used to serve the user as a front-facing interface, masking the structure, complexity, and deployment configuration of each of the modules mentioned above.

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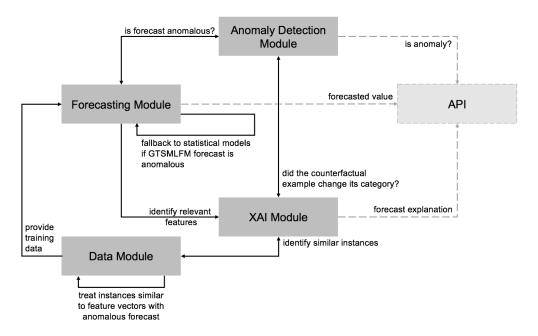


Figure 1. Architecture overview.

The architecture was implemented in a prototype application for the purpose of this paper, and not deployed into production. The backend was built using the Python 3.6 language, and leveraging multiple open-source data processing and machine learning libraries (Numpy [112], Pandas [113], Scikit-Learn [114], Scipy [115], Lime [75], Pyod [116], LightGBM [117]), and exposing relevant data through an HTTP REST API, using the Flask framework [118]. To build the frontend, we used HTML to layout the core of the dashboard, the Bootstrap framework to embellish the user interface, Plotly-js [119] to draw the plot, and jQuery [120] to interface with the HTTP REST API, retrieving the data and serving the content to the web page.

The interaction between the modules embodies the methodology we followed to enhance the GTSMLFM performance iteratively and provide an insight to the user regarding when and why does a GTSMLFM model provides an adequate forecast or not. We detail the methodology in Section 4.

4. Methodology

In this section, we describe how we leveraged the information provided by a prototype application built following the architecture described in Section 3, to enhance a GTSMLFM. To that end, we developed an iterative methodology inspired by work done by several authors, and summarized in Figure 2. Scientific literature on GTSMLFMs agrees that pooling similar time series does provide an advantage over local models [3,4,13,21], while pooling and time series similarity criteria remain an arbitrary choice [15]. Furthermore, some research indicates that GTSMLFMs can be trained over disparate time series and still obtain good forecasting results. We propose training an initial model over all the time series and measuring its performance. We then identify anomalous forecasted values. We consider that these values are a consequence of a subset of train data instances with a similar feature vector but different target values. To identify such instances, we first compute the feature relevance for a particular forecast. Given the N most relevant features to that forecast, we search for similar instances in the train set computing the cosine distance across the feature vectors, considering only the subset of the aforementioned N features. To avoid distortions due to different feature magnitudes, we scaled the features between zero and one. To decide which train instances to remove, we set an arbitrary similarity threshold. It is important to consider that the GTSMLFM performance can be affected by train data instances that lead to learning inaccurate forecasting patterns and

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the amount of data available, which can eventually lead to better predictions. Thus, setting the right threshold requires a compromise between both factors and can be subject to trial and error. To conclude an iteration, we assess the GTSMLFM quality. In particular, we decided to measure it through three metrics (see Section 6): (i) mean absolute scaled error (MASE) [10], (ii) the number of outliers detected in the test set, and (iii) the number of train instances removed from the dataset to train that particular GTSMLFM. Following the Equation (1) [28], we argue that, while local statistical models do not match the overall performance of a good GTSMLFM, they can sometimes provide a better prediction when the GTSMLFM provides an anomalous forecast. To retain the scaling advantages, such as ease of deployment, and avoid dedicating human resources to developing and maintaining such models, simple heuristics such as the näive forecast, simple moving average, or exponential smoothing can be used.

$$Data = Global\ Model + Local\ Models + Noise \tag{1}$$

The equation represents that local models can make better forecasts when the global model fails to predict reasonably. The equation was reproduced from [28].

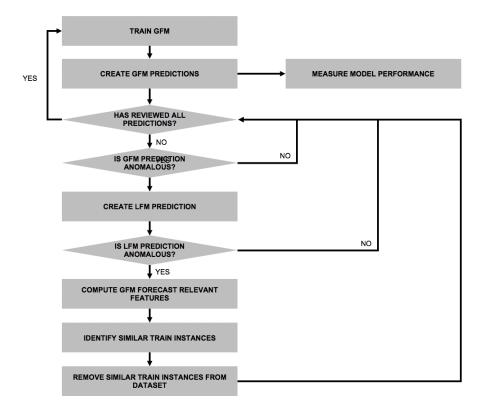


Figure 2. Fluxogram detailing the methodology that we applied to identify anomalous forecasts, most similar instances in the train set, and their treatment to enhance the performance of future GFMs.

Once we finalize an iteration, we start a new one by retraining the GTSMLFM on the new dataset, following the steps mentioned above. Iterative model retraining is based on the RemOve And Retrain (ROAR) method [121], developed to identify features relevance measuring the model performance change between iterations when a feature is nullified. In our case, we do not measure the impact of the features but of a subset of training instances when removed from the dataset. Furthermore, inspiration to look into training instances to understand their impact on a given forecast was obtained from [122], who did so using influence functions.

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5. Case Study

In this research, we considered two open datasets that are widely used in time series forecasting research: M4 competition dataset (M4CD) [5], and the Kaggle Wikipedia Web Traffic forecasting competition dataset (KWWTFCD) [123]. To ensure that the performance of the global models does not depend on the knowledge of a particular domain or characteristics of the time series data, we defined the same set of generic features for both cases. In this section, we describe the characteristics of each dataset, provide details on how we sampled instances from them, and the preprocessing steps we performed before training the GTSMLFM.

The M4CD comprises 100,000 time series selected from the ForeDeCk database, corresponding to multiple business domains, such as industries, government, transport, household, and natural resources. While the dataset includes time series at different frequencies (from hourly to yearly frequency), we focused on those provided monthly, which account for 48,000 time series. When analyzing their metadata and the actual time series length, we found some discrepancies. We clarified them with the authors from [124], who researched how representative it is of the reality. In private correspondence, the authors confirmed that such discrepancies existed, attributing them to the original public sources from which they were obtained. Since such time series represented only a tiny proportion of the total dataset, we ignored them.

The KWWTFCD was provided by Google and introduced in a Kaggle competition in 2017. The dataset comprises time series accounting for the daily views of approximately 145,000 Wikipedia articles, starting from 1 July 2015, until 11 September 2017. The dataset distinguishes between zero and missing values.

We randomly sampled 2000 time series for each dataset and selected only a subsequence to minimize the number of missing values (first 45 values for M4CD and first 56 values for the KWWTFCD). We considered 2000 time series as a big enough sample to evaluate diverse time series and provide meaningful results, while avoiding processing the whole dataset. The need for sampling is grounded in the fact that a feature vector is created per time step for each time series, requiring extensive computational resources and time to train the models.

When designing the experiment, we considered that a global model is more likely to produce anomalous forecasts if trained over a dataset that contains two types of time series: (i) the ones whose values remain in the same order of magnitude, and (ii) the ones whose values comprehend different orders of magnitude (TSDM). We thus analyzed the proportion of time series with such properties in each dataset and ensured that the sampling respected those proportions. The new datasets comprised 903 of type (i) and 1097 of type (ii) time series for the M4CD, and 512 type (i) and 1488 type (ii) time series for the KWWTFCD. We provide further details on the original and reduced dataset in Table 1, and describe the target values distribution in Figure 3.

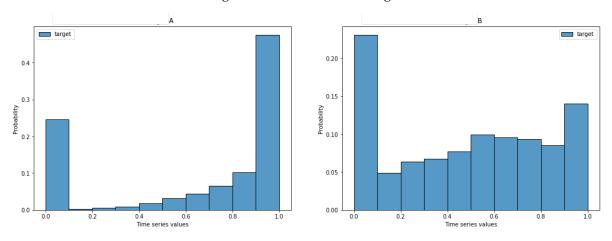


Figure 3. Target values distribution. (A) describes values for M4CD, while (B) describes values for KWWTFCD.

Table 1. Descriptive data for the M4CD and KWWTFCD datasets. TSDM is used as an abbreviation for time series with
values of different orders of magnitude, while TS abbreviates time series.

Dataset	Original				Test Window				
	# TS	% TSDM	#TS	# TSDM	TS Datapoints	# Instances	Mean (Target)	Std (Target)	rest willdow
M4CD	47,983	55	2000	1097	45	90,000	0.6598	0.4036	12
KWWTFCD	145,063	74	2000	1488	56	112,000	0.4782	0.3442	14

To describe the time series, we created a set of features, presented in Table 2. We considered three types of features: (i) the features that describe the values observed for a given time series (e.g., minimum, mean, median values, along with the standard deviation), (ii) the features that describe the time series shape (e.g., skew, kurtosis, the number of peaks we observed, and the number of values above the mean), and (iii) the features that describe the context close to the forecasted value (e.g., last observed value—which can be used as a näive forecast). We compute thirty-three features for each dataset. For the global models, we do not perform feature selection, given that in all cases, we observe the number of features satisfies the Equation (2), as suggested in [125]. For the local machine learning models, we perform feature selection selecting top K features based on their mutual information [126].

$$k \le \sqrt{N} \tag{2}$$

k represents the maximum number of features used to train a model to avoid overfitting. *N* represents the number of data instances available in the train set. The equation is based on research done by [125].

Several kinds of preprocessing have been tried for GTSMLFMs in the scientific literature. Smyl [127] applied on the fly preprocessing to remove level and seasonality components. Rabanser et al. [128] found that binning proved to be useful in almost all the cases they analyzed. Duncan et al. [13] understands that differences in magnitudes and variances can be removed, either by standardizing the time series or using dimensionless dependent variables. Hewamalage et al. [129] describe applying a local normalization, deseasonalization, and log transformation to the features. Finally, Salinas et al. [27] describes scaling the features by their average value. In our case, we opted to scale the values of a feature vector between zero and one by dividing the entries by the maximum value observed in the period of interest. Such scaling forced most feature values to a standard interval between zero and one, helping the model learn similar patterns, regardless of the original time series magnitudes. To further ease the learning process to the model, we scaled the target values too.

Table 2. Description of features we created for each dataset. We used n = 3, 5, 7, 12.

Feature	Data Type	Description
min_n	Double	Minimum value in rolling window of last <i>n</i> observations.
mean_n	Double	Mean of values in rolling window of last <i>n</i> observations.
std_n	Double	Standard deviation for values in rolling window of last <i>n</i> observations.
median_n	Double	Median value in rolling window of last <i>n</i> observations.
skew_n	Double	Skew value in rolling window of last <i>n</i> observations.
kurt_n	Double	Kurtosis value in rolling window of last <i>n</i> observations.
peaks_n	Integer	Count the number of peaks for a rolling window of last <i>n</i> observations.
above_mean_ <i>n</i> Double Count the number of datapoints above the mean, for a rolling The value is normalized by windows length.		Count the number of datapoints above the mean, for a rolling window of last n observations. The value is normalized by windows length.
n-1	Double	Last observed target value, normalized by maximum value observed in time window $n = 12$.

Outlier detection was performed considering a time series comprised of the original time series data points up to the start of the forecasting horizon and then adding the forecasted value, since we only performed one step ahead forecasts (see Figure 4). Doing so enables us to use multiple anomaly detection approaches to evaluate aspects under which a particular value can be considered an outlier within the time series.

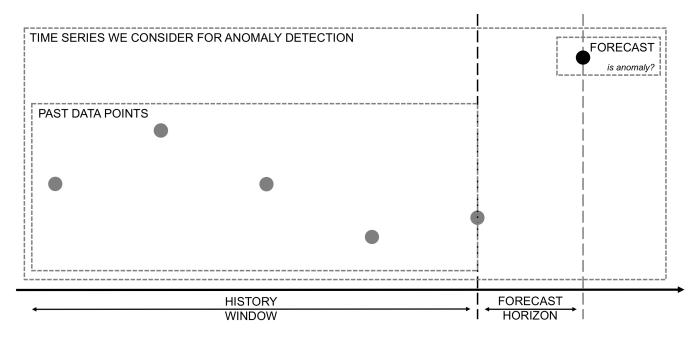


Figure 4. Diagram describing the data that we provide to build the time series context for anomaly detection.

6. Experiments, Results, and Analysis

To validate the architecture and methodology described in Sections 3 and 4, we conducted a series of experiments (summarized in Table 3) comparing four models (described in Table 4) on the reduced version of two open datasets presented in Section 5. We built our local and global forecasting model with a gradient boosted machine regressor (GBMR) [117], considering that all but one of the top five solutions of the M5 forecasting competition were based on it [6]. We configured the GBMR model to be deterministic, have a maximum depth of five, and at most a hundred estimators. All GBMR models were instantiated with the same random seed (using the value 744) and an L2 loss. For every time series, we also created two simple local statistical models: a simple moving average, based on the last three points of data, and a näive forecast, providing a forecast based on the last observed value. On top of the models we described, we built an additional model, which considered the predictions issued by the GM(GBMR) model, and used the nive model to issue fallback predictions when detecting an anomalous prediction was given by the global model. We opted to use a näive model as fallback, since it is considered a baseline model in most of timeseries literature. In addition, the näive model is cheap to compute, and requires no previous knowledge regarding specific timeseries, making it a more scalable solution. We evaluated the models performing a nested cross-validation [130] over the last twelve data points (a year of data monthly) for M4CD and the last fourteen data points (two weeks of data daily) for KWWTFCD.

To evaluate the experiments, we considered three groups of metrics. First, we used MASE [10] to measure the model's performance. The MASE metric provides a magnitude agnostic estimate of the forecasting precision achieved by the model, comparing the model's performance against a nïve forecast. We measured the MASE values for the MA(3), GM(GBMR), GM(GBMR)+näive, and LM(GBMR) models. Second, we assessed the anomalies detected in the test set. We measured (i) how many GM(GBMR) predictions were considered anomalous when the target values were not (GM(GBMR) vs. Target

discrepancy column in Table 5); (ii) how many target values were identified as anomalous (Target column in Table 5); (iii) how many GM(GBMR) predictions were identified as anomalous, and their overlap regarding the GM(GBMR) column under Anomalies in test in Table 5); and (iv) how many GM(GBMR)+näive predictions were identified as anomalous, and their overlap regarding the GM(GBMR)+näive column under Anomalies in test in Table 5). Finally, we measured how many instances were erased from the train set based on their similarity to feature vectors producing anomalous forecasts. Through these sets of metrics, we could assess the model's performance when changing the experimental conditions, understand if the detected outliers correspond to true or false positives, and how successfully does the global model behave in such cases, and if there is any correlation between the number of train instances removed and the global model's performance.

Table 3. Description of the experiments that we performed.

Experiment	Description
Experiment 1	Compare the performance of GFM and LFM.
Experiment 2	Remove instances similar to the cases where the forecast was considered anomalous. The similarity of the train instances is measured on relevant features of the forecast feature vector.
Experiment 3	Remove only instances similar to the cases where the fallback was considered anomalous. The similarity of the train instances is measured on relevant features of the forecast feature vector.
Experiment 4	Remove instances similar to the cases where the forecast was considered anomalous. The similarity of the train instances is measured on relevant features of the forecast feature vector and target value.
Experiment 5	Remove only instances similar to the cases where the fallback was considered anomalous. The similarity of the train instances is measured on relevant features of the forecast feature vector and target value.

Table 4. Description of the models we evaluated through the experiments that we performed.

Model name	Description
MA(3)	Moving average over last three time steps.
näive	Last time step actual is used as the forecast value.
GM(GBMR)	Global model built with GBMR.
LM(GBMR)	Local model built with GBMR.
GM(GBMR)+näive	Forecasts are issued from GM(GBMR), except when the forecasted value is considered anomalous. In such cases, it falls back to a näive forecast.

Table 5. Results obtained for the experiments. For columns GM(GBMR) and GM(GBMR)+näive under anomalies in test, we use the following convention to present the results: A/B (C), where A denotes the number of datapoints considered anomalies both, in the prediction and effective target value; B denotes the number of forecasts issued by the model that were considered anomalous; and C provides the ratio between A and B. ETI is used as an abbreviation for erased train instances. TD is used as an abbreviation for target discrepancy.

Experiment	Dataset	MASE				Anomalies in Test					ETI	
		MA(3)	GM(GBMR)	GM(GBMR)+näive	LM(GBMR)	GM(GBMR) vs. TD	Target	GM(GBMR)	GM(GBMR)+näive	# ETI	Ratio ETI	
Experiment 1	M4CD	1.8473	0.7387	0.7644	4.3261	304	4337	1553/1857 (0.84)	1555/2249 (0.69)	NA	NA	
	KWWTFCD	1.4871	0.6828	0.7216	1.0360	407	2750	991/1398 (0.71)	924/1916 (0.48)	NA	NA	
Experiment 2	M4CD	1.8473	0.7392	3.0213	4.3261	290	4337	1567/1857 (0.84)	1555/2249 (0.69)	1857	0.0281	
	KWWTFCD	1.4871	0.6832	1.5915	1.0360	374	2714	919/1293 (0.71)	869/1808 (0.48)	1293	0.0154	
Experiment 3	M4CD	1.8473	0.7361	3.0228	4.3261	283	4337	1588/1871 (0.85)	1555/2249 (0.69)	1365	0.0207	
	KWWTFCD	1.4871	0.6829	1.5912	1.0360	375	2714	925/1300 (0.71)	869/1808 (0.48)	813	0.0097	
Experiment 4	M4CD	1.8473	0.7392	3.0213	4.3261	290	4337	1567/1857 (0.84)	1555/2249 (0.69)	1857	0.0281	
	KWWTFCD	1.4871	0.6832	1.5915	1.0360	374	2714	919/1293 (0.71)	869/1808 (0.48)	1293	0.0154	
Experiment 5	M4CD	1.8473	0.7361	3.0229	4.3261	283	4337	1588/1871 (0.85)	1555/2249 (0.69)	1365	0.0207	
	KWWTFCD	1.4871	0.6828	1.5911	1.0360	374	2714	925/1299 (0.71)	869/1808 (0.48)	813	0.0097	

6.1. Premise Validation (Experiment 1)

We devoted the first experiment to validate the premise of this work: that the global model outperformed the local ones (GM(GBMR) vs. MA(3) and LM(GBMR) in Experiment 1), and even the GM(GBMR)+näive, showing that the fallback to the näive forecast did not provide the expected performance improvements. This was confirmed

in the rest of the experiments. Our intuition behind the result is that fallback forecasts replacing the original prediction in false positives issued by the anomaly detector (for which the GM(GBMR) model would have a better prediction) degrade the overall performance and lead to suboptimal results. We then performed four additional experiments to understand if removing instances from the train set similar to the reference vector generating an anomalous forecast could improve the performance of the global model.

It must be noted that the anomaly detection is run on forecasted values. Thus, while anomalies can be subjective, we consider that objective criteria can be established to identify suspicious data points (or forecasts) that meet those criteria, and are most likely to be considered outliers (or anomalous).

6.2. Dealing with Anomalous GTSMLFM Forecasts (Experiment 2 and Experiment 4)

Once the GTSMLFM was trained, we proceeded to identify outliers produced by the GTSMLFM using an ensemble of time series anomaly detectors (COPOD [131], ABOD [132], and KNN [133]), and considering a given forecast anomalous only when all the detectors agreed it should be considered as such. Next, we used the LIME [75] to compute features relevance for each anomalous forecast.

The most similar instances between the feature vector generating an anomalous prediction and data available in the training set were obtained, computing the cosine distance over a subset of the five most relevant features to each prediction. In Experiment 2 and Experiment 4, we computed such similarity against the data instances in the train set for all GTSMLFM anomalous forecasts. For Experiment 2, we considered a vector built with the most relevant features to a specific forecast, while in Experiment 4, we enlarged that vector with the target value for the train set instances and the predicted value for the reference vector. The intuition behind including such value in the vector is that instances most likely influence the model with similar input values and teach a target value close to the observed prediction.

While we experimented with multiple similarity thresholds, we finally adopted a threshold of 0.9999999, for which, in most cases, just a handful of train instances were identified as similar to the feature vectors producing anomalous forecasts. However, due to some exceptional cases resulting in a relatively high number of similar instances despite the tight threshold, we decided to provide an additional bounding criterion, collecting, at most, ten top train instances for each anomalous forecast. This limit was established considering the relationship between the size of the test set, the number of anomalies, and an upper bound to the number of instances to be removed. While such a procedure helped us identify and remove instances that distorted the GTSMLFM's training, future work will develop a better procedure to determine the parameters and identify such instances.

When analyzing the results, we observed, in both cases, that the model's performance decayed (MASE measurements for GM(GBMR) and GM(GBMR)+näive), while the discrepancy between GM(GBMR) predictions and target values that were considered anomalous reduced, indicating a better adjustment to the real data behavior for unexpected values. While the MASE improvement was slight, it must be noted that such improvement was consistent and thus is improbable that it could be attributed to models' variance. Furthermore, we expect that the forecast improvements are minor in terms of MASE: reducing the number of anomalies across a test set of 24,000 records for dataset M4CD, and 28,000 for dataset KWWTFCD, should not have a substantial impact on the overall MASE. While the MASE is indicative of the overall models' forecast adjustment, the improvement regarding anomalous forecasts should be considered in terms of a reduction of the target discrepancy (the model better adjusts to the observed target values in the test set). We observe that the number of anomalous forecasts is reduced in both cases, showing that the new model better adjusts to the time series behavior.

6.3. Dealing with Anomalous Fallback Forecasts (Experiment 3 and Experiment 5)

Assuming that more data is beneficial to global model performance and that the näive forecast can provide a reasonable estimate when the GM(GBMR) issues an anomalous forecast, we conducted two additional experiments (Experiment 3 and Experiment 5), removing only the train instances that were similar to feature vectors for which both, the GM(GBMR) and the näive forecast provided an anomalous forecast. For Experiment 5, we enlarged the reference vector with the predicted value (or the target value for the vectors in the train set). In both experiments, we observed an improved MASE score regarding Experiment 2 and Experiment 4 and a reduced discrepancy between values considered anomalous for GM(GBMR) predictions and target values. In particular, we found that the best results for all metrics in both datasets were obtained for Experiment 5, reducing outliers discrepancy regarding the original model for at least seven percent in both datasets.

From the results that we obtained, we consider the vector structure used to measure the similarity between the instances (using the most relevant features either with the target (or predicted) value or not), did not influence the results. We confirmed that improving the global model performance is possible by removing particular data instances from the train set. When searching for such instances, it is crucial to ensure that the least possible data is removed. Since the M4CD dataset comprises a wide variety of time series and the same architecture and methodology were used to replicate the findings on the KWWTFCD dataset, we expect that they can be generalized to other domains. Moreover, though the research was applied to time series datasets, we consider that the findings can be ported to regression problems in general, due to how we formulated the forecasting problem.

6.4. Dashboard

To inform the user when and why a given forecast should be trusted, we built a dashboard (see Figure 5). The dashboard has six sections, each of which provides specific information to the user. At the top of the dashboard (Figure 5A), we provide information regarding the time series identifier, the dataset they belong to, the forecast date and value, if considered an outlier, and the most relevant features to that particular forecast. We then created a line plot of the time series, where the last value corresponds to the forecast (Figure 5B). We use a gray dashed vertical line (see the Figure 5(B2) arrow) to indicate the start of the forecasting horizon, and a red dashed vertical line (see the Figure 5(B3) arrow) to highlight the occurrence of an anomalous forecast. We provide a short explanation regarding the criteria applied to the forecast to determine if it is anomalous or not (Figure 5C).

Given that the machine learning models that we consider assume manually crafted features, insights regarding the time dimension can be conveyed only through the features and their metadata. Inspired by related work [91,93], we map features metadata regarding the time dimension and compute how strongly that the referenced time windows and points-in-time are from the most relevant features to a particular forecast overlay. Based on that information and the values of the time series data points within each range considered, we overlayed a heatmap to the time series line plot, showing how influential those data points are to the forecast. In particular, in Figure 5(B1), we show a heatmap with a heat scale ranging from yellow (low relevance) to red (high relevance). The relevance heatmap's area is determined by the time windows of the relevant features and the values of the data points that fall within the aforementioned time window.

In Figure 5D, we display a set of training instances that probably influenced the forecast (prototype local explanations), followed by two counterfactual examples: a set of instances that would result in a non-anomalous forecast (Figure 5E). We created our utility code to compute the counterfactual examples (see algorithm's pseudocode in Listing 1). To compute them, we restricted the values search to the most significant features identified by LIME and ensured that the values were plausible. To decide whether there was a significant change in the forecasted value when computing counterfactual examples, we created a feature vector with the mean values of all the features, except for the meaningful

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> ones identified through LIME, which received values of their own by ninety thousand values from a normal distribution. The normal distribution was parameterized with a mean equal to the mean of past time series values, and a standard deviation equal to three times the standard deviation measured in the past for that same time series. We then used the GTSMLFM to issue a forecast and the anomaly detector to determine if the proposed sample instance qualified as an outlier or not, and randomly selected a subset of them to show them to the user.

Listing 1: Algorithm used to compute counterfactual examples.

```
# X_train: dataset train instances
# feature_vector: feature vector used to issue the forecast
# relevant_features: list of relevant features to the given forecast
# model: forecasting model
# anomaly_detector: some anomaly detector
# n_samples: number of samples to draw from the Normal distribution
given X_train, feature_vector, relevant_features, model, anomaly_detector
synthetic_samples = new dictionary()
for each feature in relevant_features:
   feature_mean = mean(X_train[feature])
   feature_std = standard_deviation(X_train[feature])
   feature_perturbed_values = normal(feature_mean, 3*feature_std, n_samples)
   synthetic_samples[feature]=feature_perturbed_values
# create new dataset, merging data from non relevant features, and perturbed ones
new_dataset = create_dataset(X_train, synthetic_samples)
counterfactual_examples = new list()
for each feature_vector in new_dataset:
   y_pred = model.predict(feature_vector)
   if not anomaly_detector.is_anomaly(y_pred):
       counterfactual_examples.append(feature_vector)
return counterfactual_examples
```

The last dashboard square is devoted to providing a set of values expected to make a better forecast (Figure 5F). To obtain them, we drew ten thousand values following a normal distribution, with a mean equal to the mean of past time series values and a standard deviation equal to three times the standard deviation measured in the past for that same time series. The values were then filtered by performing the same anomaly detection procedure as for the GTSMLFM forecasts, keeping only those not considered anomalous. Figure 5F displays just a subset of them: the minimum, median, and maximum values, and additional four random samples drawn from them.

In this work, we used a particular selection of models and algorithms to create the forecasts, detect anomalies, and craft the explanations. However, given the architecture's modular structure, these can be replaced as black boxes, impacting the quality of the content displayed in the dashboard.

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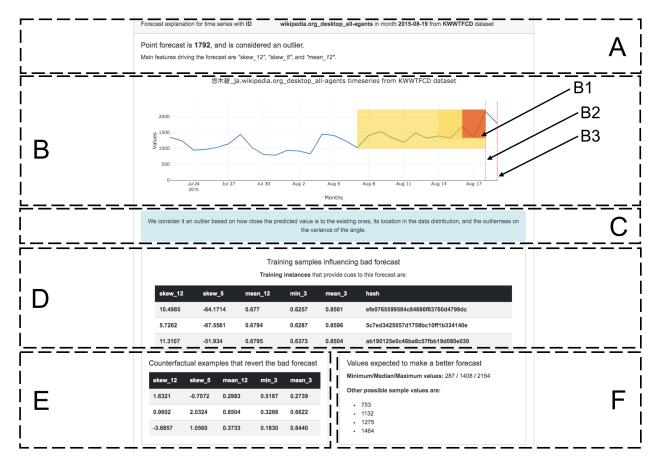


Figure 5. Dashboard screenshot. We highlight different areas devoted to explaining a given forecast, providing a context within the time series, indicating the most relevant features to the forecast, train instances that most likely influenced the forecast, counterfactual examples, and alternative values expected to make a good forecast.

7. Limitations and Improvement Opportunities

We identify two significant limitations of the research described above. It must first be noted that, while the methodology and dashboard that we developed are generic, they target global time series models constrained to machine learning algorithms whose input features are intelligible to the human. Furthermore, many of the explanations assume the features convey a particular meaning to the user—which is, in our view, a criterion that handcrafted features can only meet. Due to this limitation, we consider this approach is not suitable for deep learning models. In addition, given how the features are framed for such machine learning models, insights regarding the time dimension can be conveyed through the features and their metadata. Second, the current approach to selecting train data instances similar to the data instances creating the anomalous forecast requires some tuning to find an appropriate instances' similarity threshold and set proper constraints towards the maximum number of instances to consider for each case. While this could be replaced by an automatic procedure searching for the best similarity measure, threshold, and instances' limit, such a procedure would come at a high cost, since it would require computing the similarities across all instances for each run. Further research is required to understand better alternative procedures to identify similar train data instances that drive the forecast towards an anomalous value.

From experience that we obtained through the experiments and results described above, we identified improvement opportunities. Following research done by [122], finding the most influential instances in the train set for an anomalous forecast can be done using influence functions. Other possible enhancements would be to use a more stable model to estimate feature relevance for each prediction. In particular, we could replace LIME for DLIME, since LIME is not deterministic, and changes in feature ranking computations can

affect the instance selection based on the similarity to the detected anomalous forecasts. Another improvement can be made regarding the anomaly detection module. Reducing the number of false positives correlates to the number of instances removed from the train set. Furthermore, removing only instances similar to the ones where the global model and fallback provide anomalous forecasts has been shown to improve the performance of the model trained without such instances. Following this intuition, we can use our current anomaly detector for unsupervised anomalies labeling. By labeling instances as anomalous only when the current anomaly detector predicts the actual value is not anomalous when the forecast was, we can later train more precise supervised machine learning models to detect outliers.

8. Conclusions

In this work, we developed a modular architecture, a methodology, and a dashboard, that provide insights when a GTSMLFM forecast can be trusted or not and the reasons behind anomalous forecasts. The architecture, methodology, and dashboard support the development and engineering of GTSMLFMs, providing means to enhance their performance. We evaluated our approach through a series of experiments conducted on a reduced version of two publicly available datasets and measuring the performance improvements of the GTSMLFM when following the methodology described in Section 4. Our research confirmed that removing particular instances from the train set can lead to a better GTSMLFM performance and compared several approaches to achieve the best outcome.

As future work, we envision extending the current application to support explainable anomaly detection algorithms and include a semantic model to enrich the explainability of any anomaly detection model. Such a semantic model can provide additional insights based on domain knowledge regarding the inner workings of the anomaly detection model and the data of a particular time series and forecast. Finally, we would like to explore different policies to deal with problematic train instances. In particular, we are interested in studying if replacing the values of a subset of features of interest with some imputation criteria can be an effective alternative to removing such data instances. Such a technique would retain the advantages of keeping all the data to train a global model, while removing patterns that create outlier forecasts. Moreover, to avoid losing valuable information in the noisy instances, we could leverage generative adversarial sampling to enrich the dataset with synthetic train instances that resemble noisy ones. Such enrichment could help the model better learn the decision boundaries, increasing the overall model's performance.

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Abbreviations

The following abbreviations are used in this manuscript:

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AF Anomalous Forecast

COF Connectivity based Outlier Factor

ETI Erased Train Instances

GBMR Gradient Boosted Machine Regressor

GFM Global Forecasting Model

GTSMLFM Global Time Series Machine Learning Forecasting Model

INFLO Influenced Outlierness kNN n-Nearest Neighbor

KWWTFCD Kaggle Wikipedia Web Traffic Forecasting Competition Dataset

LFM Local Forecasting Model
LOF Local Outlier Factor
M4CD M4 Competition Dataset
MASE Mean Absolute Scaled Error

ODIN Outlier Detection using Indegree Number

ROAR RemOve And Retrain TD Target Discrepancy

TS Time Series

TSDM Time Series with Different Magnitude values

XAI Explainable Artificial Intelligence

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