

# ECE374 SP23 HW3

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## Contributors

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## Problem 1

A *finite-state transducer* (FST) gives an output based on the transition instead of the current state. It is defined by a 5-tuple:

$$(\Sigma, \Gamma, Q, \delta, s)$$

The output alphabet of a  $FST_{AR}$  consists of two signals, namely accept and reject ( $\Gamma = \{A, R\}$ ). We say that  $L(FST_{AR})$  represents the language consisting of all strings that end with an accept (A) output signal.

Prove that  $L(FST_{AR})$  represents the class of regular languages.

## Solution

**Proof.** For the given FST, we construct a DFA  $M'$  such that  $L(M') = L(FST_{AR})$ :

$$M' = (\Sigma, Q', \delta', s', A')$$

where

- $Q' = Q \times \Gamma$
- $\delta'((q, b), a) = \delta(q, a), \forall q \in Q, a \in \Sigma, b \in \Gamma$
- $s' = (s, A)$
- $A' = \{(q, A) \mid q \in Q\}$

Here we assume that in a FST,  $\delta : Q \times \Sigma \rightarrow Q \times \Gamma$

The core idea is to explicitly encode the last output signal in the states. Note that there is a clear boundary between *next-state logic* and *output logic* -- thus, the expression of  $\delta'$  is unrelated to  $b$ .