

An Introduction to OCaml

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^{*} Course website: https://www.cs.columbia.edu/ rgu/courses/4115/spring2019

^{**} These slides are borrowed from Prof. Edwards.

An Endorsement?

A PLT student accurately summed up using OCaml:

Never have I spent so much time writing so little that does so much.

I think he was complaining, but I'm not sure.

Other students have said things like

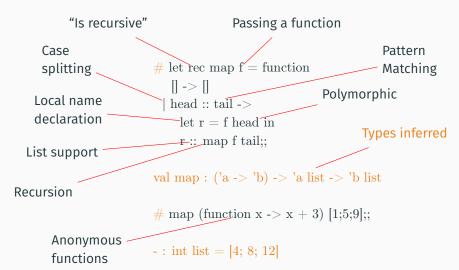
It's hard to get it to compile, but once it compiles, it works.

Why OCaml?

- It's Great for Compilers
 I've written compilers in C++, Python, Java, and OCaml, and it's much easier in OCaml.
- It's Succinct
 Would you prefer to write 10 000 lines of code or 5 000?
- Its Type System Catches Many Bugs
 It catches missing cases, data structure misuse, certain off-by-one errors, etc. Automatic garbage collection and lack of null pointers makes it safer than Java.
- Lots of Libraries and Support
- Lots of Support

OCaml in One Slide

Apply a function to each list element; save results in a list



The Basics

Hello World in OCaml: Interpret or Compile

Create a "hello.ml" file:

```
\verb|print_endline| "Hello World!"|
```

Run it with the interpreter:

```
$ ocaml hello.ml
Hello World!
```

Run it with the bytecode interpreter:

```
$ ocamlc -o hello hello.ml
$ ocamlrun hello
```

Hello World!

On most systems, the bytecode can be run directly:

- \$ ocamlc -o hello hello.ml
- \$./hello

Hello World!

Hello World in OCaml: Interpret or Compile

Compile a native executable and run:

\$ ocamlopt -o hello hello.ml
\$./hello
Hello World!

Use ocamlbuild: built-in compilation rules for OCaml projects handle all the nasty cases; automatic inference of dependencies, parallel compilation, etc.

```
$ ocamlbuild hello.native
$ ./hello.native
Hello World!
```

Hello World in OCaml: REPL

The interactive Read-Eval-Print Loop

```
$ ocaml
      OCaml version 4.02.3

# print_endline "Hello World!";;
Hello World!
-: unit = ()
# #use "hello.ml";;
Hello World!
-: unit = ()
# #quit;;
$
```

Double semicolons ;; mean "I'm done with this expression" #quit terminates the REPL

Other directives enable tracing, modify printing, and display types and values. Use <u>ledit ocaml</u> or <u>utop</u> instead for better line editing (history, etc.)

Comments

OCaml

```
(* This is a multiline comment in OCaml *)

(* Comments
    (* like these *)
    do nest

*)

(* OCaml has no *)
(* single-line comments *)
```

C/C++/Java

```
/* This is a multiline
  comment in C */
/* C comments
    /* do not
    nest
  */
// C++/Java also has
// single-line comments
```

Basic Types and Expressions

```
\# 42 + 17;;
-: int = 59
# 42.0 +. 18.3;;
-: float = 60.3
\# 42 + 60.3;;
Error: This expression has type
float but an expression was
expected of type int
\# 42 + int of float 60.3;;
-: int = 102
# true | (3 > 4) && not false;;
-: bool = true
# "Hello " ^ "World!"::
-: string = "Hello World!"
# String.contains "Hello" 'o';;
-: bool = true
# ();;
-: unit =()
# print endline "Hello World!";;
Hello World!
-: unit =()
```

Integers (31-bit on 32-bit processors)

Floating-point numbers

Floating-point operators must be explicit (e.g., +.)

Only explicit conversions, promotions (e.g., int of float)

Booleans

Strings

The unit type is like "void" in C and Java

Standard Operators and Functions

+ - * / mod	Integer arithmetic
+ *. /. **	Floating-point arithmetic
ceil floor sqrt exp log log10 cos sin tan acos asin atan	Floating-point functions
not &&	Boolean operators
= <> == !=	Structual comparison (polymorphic) Physical comparison (polymorphic)
<>><=>=	Comparisons (polymorphic)

Structural vs. Physical Equality

==, != Physical equality compares pointers

```
# 1 == 3::
-: bool = false
# 1 == 1::
-: bool = true
\# 1.5 == 1.5;;
-: bool = false (* Huh? *)
# let f = 1.5 in f == f;
-: bool = true
# 'a' == 'a'::
-: bool = true
# "a" == "a"::
-: bool = false (* Huh? *)
\# let a = "hello" in a == a;
-: bool = true
```

=, <> Structural equality compares values

```
# 1 = 3;;
-: bool = false

# 1 = 1;;
-: bool = true

# 1.5 = 1.5;;
-: bool = true

# let f = 1.5 in f = f;;
-: bool = true

# 'a' = 'a';;
-: bool = true

# "a" = "a";;
-: bool = true
```

Use structural equality to avoid headaches

If-then-else

if $expr_1$ then $expr_2$ else $expr_3$

If-then-else in OCaml is an expression. The *else* part is compulsory, $expr_1$ must be Boolean, and the types of $expr_2$ and $expr_3$ must match.

```
# if 3 = 4 then 42 else 17;;
-: int = 17

# if "a" = "a" then 42 else 17;;
-: int = 42

# if true then 42 else "17";;
This expression has type string but is here used with type int
```

Naming Expressions with let

let $name = expr_1$ in $expr_2$ let name = expr Bind name to $expr_1$ in $expr_2$ only Bind name to expr forever after

```
# let x = 38 in x + 4;
 -: int = 42
\# \text{ let } x = (\text{let } y = 2 \text{ in } y + y) * 10 \text{ in } x;;
-: int = 40
\# x + 4;;
Unbound value x
\# \text{ let } x = 38;;
val x : int = 38
\# x + 4;;
-: int = 42
\# \text{ let } x = (\text{let } y = 2) * 10 \text{ in } x;;
Error: Syntax error: operator expected.
\# let x = 10 in let y = x;
Error: Syntax error
```

Let is Not Assignment

Let can be used to bind a succession of values to a name. This is not assignment: the value disappears in the end.

```
# let a = 4 in
let a = a + 2 in
let a = a * 2 in
a;;
-: int = 12

# a;;
Unbound value a
```

This looks like sequencing, but it is really data dependence.

Let is Really Not Assignment

OCaml picks up the values in effect where the function is defined. Global declarations are not like C's global variables.

Functions

Calling Functions

```
C/C++/Java
// This is C/C++/Java code
average (3, 4);
```

```
OCaml
(* This is OCaml code*)
average 3.0 4.0
```

no brackets and no comma between the arguments the syntax average (3.0, 4.0) is meaningful: call the function with ONE argument has the type pair

Defining Functions

```
C/C++/Java
double average (double a, double b)
{
  return (a + b) / 2;
}
```

OCaml

type inference

no implicit casting

no return keyword, the last expression becomes the result

Functions

A function is just another type whose value is an expression.

```
# fun x -> x * x;;
-: int -> int = \langle fun \rangle
# (fun x -> x * x) 5;; (* function application *)
-: int = 25
# fun x -> (fun y -> x + y);;
-: int -> int -> int = < fun>
# fun x y -> x + y;; (* shorthand *)
-: int -> int -> int = < fun>
# let plus = fun x y \rightarrow x + y;
val plus : int \rightarrow int \rightarrow int = \langlefun\rangle
# plus 2;;
-: int -> int = < fun>
# plus 2 3;;
-: int = 5
# let plus x y = x + y; (* shorthand *)
val plus : int -> int =<fun>
```

Let is Like Function Application

$$\det ext{ name} = ext{expr}_1 ext{ in } ext{expr}_2$$
 $(\operatorname{fun } ext{ name } ext{-> } ext{expr}_2) ext{ expr}_1$

Both mean " $expr_2$, with name replaced by $expr_1$ "

```
# let a = 3 in a + 2;;

-: int = 5

# (fun a -> a + 2) 3;;

-: int = 5
```

Semantically equivalent; let is easier to read

Recursive Functions

OCaml

```
\begin{array}{c} \text{let rec gcd a b} = \\ \text{if a} = \text{b then} \\ \text{a} \\ \text{else if a} > \text{b then} \\ \text{gcd (a - b) b} \\ \text{else} \\ \text{gcd a (b - a)} \end{array}
```

C/C++/Java

```
int gcd(int a, int b)
{
  while (a != b) {
    if (a > b)
        a -= b;
    else
        b -= a;
  }
  return a;
}
```

let rec allows for recursion

Use recursion instead of loops

Tail recursion runs efficiently in OCaml

Recursive Functions

By default, a name is not visible in its defining expression.

The rec keyword makes the name visible.

```
\# let rec fac n=if n<2 then 1 else n * fac (n-1);; val fac : int -> int = <fun> \# fac 5;; - : int = 120
```

The and keyword allows for mutual recursion.

```
# let rec fac n = if n < 2 then 1 else n * fac1 n
and fac1 n = fac (n - 1);;
val fac : int -> int = <fun>
val fac1 : int -> int = <fun>
# fac 5;;
- : int = 120
```

First-Class and Higher Order Functions

First-class functions are treated as values: name them, pass them as arguments, return them

```
# let plus5 x = x + 5;;
val plus5 : int -> int = <fun>
# let appadd f n= (f 42) + n;;
val appadd : (int -> int) -> int -> int = <fun>
# appadd plus5;;
- : int -> int = <fun>
# let appadd5 = appadd plus5;;
val appadd5 : int -> int = <fun>
# appadd5 : int -> int = <fun>
```

Higher-order functions: functions that work on other functions

Tuples, Lists, and Pattern Matching

Tuples

Pairs or tuples of different types separated by commas.

Very useful lightweight data type, e.g., for function arguments.

```
# (18, "Adam");;
-: int * string = (18, "Adam")
# (18, "Adam", "CS");;
-: int * string * string = (18, "Adam", "CS")
# let p = (18, "Adam");;
val p: int * string = (18, "Adam")
# fst p;;
-: int = 18
# snd p;;
-: string = "Adam"
# let trip = (18, "Adam", "CS");;
val trip: int * string * string = (18, "Adam", "CS")
# let (age, _, dept) = trip in (age, dept);;
-: int * string = (18, "CS")
```

Records

OCaml supports records much like C's structs.

```
# type stu = {age : int; name : string; dept : string };;
type stu = { age : int; name : string; dept : string; }
# let b0 = {age = 18; name = "Adam"; dept = "CS" };;
val b0 : stu = {age = 18; name = "Adam"; dept = "CS"}
# b0.name;;
- : string = "Adam"
# let b1 = { b0 with name = "Bob" };;
val b1 : stu = {age = 18; name = "Bob"; dept = "CS"}
# let b2 = { b1 with age = 19; name = "Alice" };;
val b2 : stu = {age = 19; name = "Alice"; dept = "CS"}
```

Lists

```
(* Literals *)
[];;
                (* The empty list *)
          (* A singleton list *)
[1];;
[42; 16];; (* A list of two integers *)
(* cons: Put something at the beginning *)
7 :: [5; 3];; (* Gives [7; 5; 3] *)
[1; 2] :: [3; 4];; (* BAD: type error *)
(* concat: Append a list to the end of another *)
[1; 2] @ [3; 4];; (* Gives [1; 2; 3; 4] *)
(* Extract first entry and remainder of a list *)
List.hd [42; 17; 28];; (* = 42 *)
List.tl [42; 17; 28];; (* = [17; 28] *)
```

The elements of a list must all be the same type.

:: is very fast; @ is slower-O(n)

Pattern: create a list with cons, then use List.rev.

Some Useful List Functions

Three great replacements for loops:

```
List.map f[a1; ...; an] = [f a1; ...; f an]
```

Apply a function to each element of a list to produce another list.

```
# List.map (fun a -> a + 10) [42; 17; 128];;
-: int list = [52; 27; 138]
# List.map string_of_int [42; 17; 128];;
-: string list = ["42"; "17"; "128"]
```

```
List.fold\_left\ f\ a\ [b1;\ ...;bn] = f\ (...(f\ (f\ a\ b1)\ b2)...)\ bn
```

Apply a function to a partial result and an element of the list to produce the next partial result.

```
# List.fold_left (fun sum e -> sum + e) 0 [42; 17; 128];; -: int = 187
```

Some Useful List Functions

List.iter f[a1; ...;an] = begin f a1; ...; f an; () end

Apply a function to each element; produce a unit result.

```
# List.iter print_int [42; 17; 128];;
4217128-: unit = ()
# List.iter (fun n -> print_int n; print_newline ())
    [42; 17; 128];;
42
17
128
-: unit = ()
# List.iter print_endline (List.map string_of_int [42; 17; 128]);;
42
17
128
-: unit = ()
```

List.rev [a1; ...; an] = [an; ...; a1]

Reverse the order of the elements of a list.

Example: Enumerating List Elements

To transform a list and pass information between elements, use *List.fold_left* with a tuple:

```
# let (l, _) = List.fold_left
  (fun (l, n) e -> ((e, n)::l, n+1)) ([], 0) [42; 17; 128]
  in List.rev l;;
-: (int * int) list = [(42, 0); (17, 1); (128, 2)]
```

Can do the same with a recursive function.

```
# let rec enum n l = match l with  | [] -> [] \\ | h :: t -> (h, n) :: enum (n + 1) t;;  val enum : int -> 'a list -> ('a * int) list = <fun> # enum 0 [42; 17; 128];; 
-: (int * int) list = [(42, 0); (17, 1); (128, 2)]
```

Example: Enumerating List Elements

Using tail recursion:

Using a helper function:

```
# let enum l =
let rec helper rl n l =
match l with
| [] -> List.rev rl
| h :: t -> helper ((h, n) :: rl) (n + 1) t
in helper [] 0 l;;
val enum : int -> 'a list -> ('a * int) list = <fun>
# enum [42; 17; 128];;
-: (int * int) list = [(42, 0); (17, 1); (128, 2)]
```

Pattern Matching

A powerful variety of multi-way branch that is adept at picking apart data structures. Unlike anything in C/C++/Java.

Pattern Matching

A name in a pattern matches anything and is bound when the pattern matches. Each may appear only once per pattern.

Case Coverage

The compiler warns you when you miss a case or when one is redundant (they are tested in order):

Wildcards

Underscore (_) is a wildcard that will match anything, useful as a default or when you just don't care.

```
\# let xor p = match p
 with (true, false) | (false, true) -> true
   _ -> false;;
val xor : bool * bool -> bool = <fun>
# xor (true, true);;
- bool = false
# xor (true, false);;
-: bool = true
# let logand p = match p
 with (false, ) -> false
    | (true, x) -> x;;
val logand : bool * bool -> bool = < fun>
# logand (true, false);;
- · bool = false
# logand (true, true);;
-: bool = true
```

Pattern Matching with Lists

```
# let length = function (* let length = fun p -> match p with *)
 | [] -> "empty"
 | [ ] -> "singleton"
 | [ ; ] -> "pair"
 | [ ; ; ] -> "triplet"
 | hd :: tl -> "many";;
val length: 'a list -> string = <fun>
# length [];;
-: string = "empty"
# length [1; 2];;
-: string = "pair"
# length ["foo"; "bar"; "baz"];;
-: string = "triplet"
# length [1; 2; 3; 4];;
-: string = "many"
```

Pattern Matching with when and as

The when keyword lets you add a guard expression:

```
# let tall = function 
| (h, s) when h > 180 -> s ^ " is tall" 
| (_, s) -> s ^ " is short";; 
val tall : int * string -> string = \langle \text{fun} \rangle 
# List.map tall [(183, "Stephen"); (150, "Nina")];; 
- : string list = ["Stephen is tall"; "Nina is short"]
```

The as keyword lets you name parts of a matched structure:

```
# match ([3,9], 4) with
| (3::_ as xx, 4) -> xx
| _ -> [];;
- : int * int = (3, 9)
```

Application: Length of a list

Correct, but not very elegant. With pattern matching,

Elegant, but inefficient because it is not tail-recursive (needs ${\cal O}(n)$ stack space). Common trick: use an argument as an accumulator.

OCaml Can Compile This Efficiently

OCaml source code

```
let length list =
  let rec helper len = function
    [] -> len
    | _::tl -> helper (len + 1) tl
  in helper 0 list
```

- · Arguments in registers
- Pattern matching reduced to a conditional branch
- Tail recursion implemented with jumps
- LSB of an integer always 1

ocamlopt generates this x86 assembly pseudocode

```
camlLength__helper:
.L101:
    cmpl $1, %ebx  # empty?
    je .L100
    movl 4(%ebx), %ebx # get tail
    addl $2, %eax  # len++
    jmp .L101
.L100:
    ret

camlLength__length:
    movl %eax, %ebx
    movl $1, %eax  # len = 0
    jmp camlLength__helper
```

User-Defined Types

Type Declarations

A new type name is defined globally. Unlike *let*, *type* is recursive by default, so the name being defined may appear in the *typedef*.

$$type name = typedef$$

Mutually-recursive types can be defined with and.

```
egin{array}{ll} {
m type} \ {\it name}_1 = {\it typedef}_1 \ {
m and} \ \ {\it name}_2 = {\it typedef}_2 \ & dots \ {
m and} \ \ {\it name}_n = {\it typedef}_n \ \end{array}
```

Records

OCaml supports records much like C's structs.

```
# type base = { x : int; y : int; name : string };;
type base = \{ x : int; y : int; name : string; \}
# let b0 = \{ x = 0; y = 0; name = "home" \};;
val b0 : base = \{x = 0; y = 0; name = "home"\}
# let b1 = { b0 with x = 90; name = "first" };;
val b1 : base = \{x = 90; y = 0; name = "first"\}
# let b2 = \{ b1 \text{ with } v = 90; \text{ name} = "second" \};;
val b2 : base = \{x = 90; y = 90; name = "second"\}
# b0.name::
-: string = "home"
# let dist b1 b2 =
   let hyp x y = sqrt (float of int (x*x + y*y)) in
   hyp (b1.x - b2.x) (b1.y - b2.y);;
val dist: base \rightarrow base \rightarrow float = \langle \text{fun} \rangle
# dist b0 b1;;
-: float = 90.
# dist b0 b2::
-: float = 127.279220613578559
```

Algebraic Types/Tagged Unions/Sum-Product Types

Vaguely like C's unions, enums, or a class hierarchy: objects that can be one of a set of types. In compilers, great for trees and instructions.

```
# type seasons = Winter | Spring | Summer | Fall;;
type seasons = Winter | Spring | Summer | Fall
# let weather = function
 | Winter -> "Too Cold"
  Spring -> "Too Wet"
  Summer -> "Too Hot"
 | Fall -> "Too Short";;
val weather : seasons -> string = <fun>
# weather Spring::
-: string = "Too Wet"
# let year = [Winter; Spring; Summer; Fall] in
 List.map weather year::
-: string list = ["Too Cold"; "Too Wet"; "Too Hot"; "Too Short"]
```

Simple Syntax Trees and an Interpreter

```
# type expr =
   Lit of int
  | Plus of expr * expr
   Minus of expr * expr
   Times of expr * expr;;
type expr =
   Lit of int
  | Plus of expr * expr
  | Minus of expr * expr
  | Times of expr * expr
# let rec eval = function
   Lit(x) \rightarrow x
  | Plus(e1, e2) \rightarrow (eval e1) + (eval e2)
  | Minus(e1, e2) -> (eval e1) - (eval e2)
   Times(e1, e2) \rightarrow (eval e1) * (eval e2);;
val eval : expr -> int = < fun>
# eval (Lit(42));;
-: int = 42
# eval (Plus(Lit(17), Lit(25)));;
-: int = 42
```

Algebraic Type Rules

Each tag name must begin with a capital letter

```
# let bad1 = left | right;;
Syntax error
```

Tag names must be globally unique (required for type inference)

```
# type weekend = Sat | Sun;;

type weekend = Sat | Sun

# type days = Sun | Mon | Tue;;

type days = Sun | Mon | Tue

# function Sat -> "sat" | Sun -> "sun";;

This pattern matches values of type days

but is here used to match values of type weekend
```

Algebraic Types and Pattern Matching

The compiler warns about missing cases:

```
# type expr =
   Lit of int
  | Plus of expr * expr
  | Minus of expr * expr
  Times of expr * expr;;
type expr =
   Lit of int
 | Plus of expr * expr
  | Minus of expr * expr
  Times of expr * expr
# let rec eval = function
   Lit(x) \rightarrow x
  \overline{| \text{Plus}(e1, e2)} \rightarrow (\text{eval } e1) + (\text{eval } e2)
 | Minus(e1, e2) -> (eval e1) - (eval e2);;
Warning P: this pattern-matching is not exhaustive.
Here is an example of a value that is not matched:
Times ( , )
val eval : expr -> int = < fun>
```

The Option Type: A Safe Null Pointer

Part of the always-loaded core library:

```
type 'a option = None | Some of 'a
```

This is a polymorphic algebraic type: 'a is any type. *None* is like a null pointer; *Some* is a non-null pointer. The compiler requires *None* to be handled explicitly.

Algebraic Types vs. Classes and Enums

	Algebraic Types	Classes	Enums
Choice of Types Operations	fixed extensible	extensible fixed	fixed extensible
Fields	ordered	named	none
Hidden fields	none	supported	none
Recursive	yes	yes	no
Inheritance	none	supported	none
Case splitting	simple	costly	simple

An algebraic type is best when the set of types rarely change but you often want to add additional functions. Classes are good in exactly the opposite case.

Modules and Compilation

Modules

Each source file is a module and everything is public.

foo.ml

```
(* Module Foo *)  \text{type t} = \left\{ \begin{array}{l} x : \text{int }; \ y : \text{int } \right\} \\ \text{let sum c} = c.x + c.y \end{array} \right\} \left\{ \begin{array}{l} \text{(* The dot notation *)} \\ \text{Foo.x} = 1 ; \\ \text{Foo.y} = 2 \end{array} \right\}
```

To compile and run these,

```
$ ocamlc -c foo.ml
(creates foo.cmi foo.cmo)
$ ocamlc -c bar.ml
(creates bar.cmi bar.cmo)
$ ocamlc -o ex foo.cmo bar.cmo
$ ./ex
333
```

bar.ml

```
(* The dot notation *)
          Foo.y = 2 };;
print int (Foo.sum v)
(* Create a short name *)
module F = Foo;;
print int (F.sum v)
(* Import every name from
   a module with "open" *)
open Foo;;
print int (sum v)
```

Separating Interface and Implementation

stack.mli

```
type 'a t
exception Empty
val create : unit -> 'a t
val push : 'a -> 'a t -> unit
val pop : 'a t -> 'a
val top : 'a t -> 'a
val clear : 'a t -> unit
val copy : 'a t -> 'a t
val is empty: 'a t -> bool
val length: 'a t -> int
val iter : ('a -> unit) ->
                 'a t -> unit
```

stack.ml

```
type 'a t =
 { mutable c : 'a list }
exception Empty
let create () = \{ c = [] \}
let clear s = s.c <-
let copy s = \{c = s.c\}
let push x s = s.c <- x :: s.c
let pop s =
 match s.c with
    hd::tl \rightarrow s.c \leftarrow tl; hd
  | [] -> raise Empty
let top s =
 match s.c with
    hd:: -> hd
  | [] -> raise Empty
let is empty s = (s.c = [])
let length s = List.length s.c
let iter f s = List.iter f s.c
```

Exceptions

Exceptions

```
# 5 / 0;;
{\bf Exception:\ Division\_by\_zero.}
# try
  5 / 0
 with Division_by_zero -> 42;;
-: int = 42
# exception My exception;;
exception My_exception
# try
  if true then
     raise My exception
   else 0
 with My_exception -> 42;;
-: int = 42
```

Exceptions

```
# exception Foo of string;;
exception Foo of string
# exception Bar of int * string;;
exception Bar of int * string
\# let ex b =
 try
   if b then
    raise (Foo("hello"))
   else
    raise (Bar(42, " answer"))
 with Foo(s) -> "Foo: " ^ s
 | Bar(n, s) -> "Bar: " ^ string of int n ^ s;;
val ex : bool -> unit = < fun>
# ex true;;
-: string = "Foo: hello"
# ex false;;
-: string = "Bar: 42 answer"
```

Standard Library Modules

Maps

Balanced trees for implementing dictionaries. Ask for a map with a specific kind of key; values are polymorphic.

```
# module StringMap = Map.Make(String);;
module StringMap:
 sig
   type key = String.t
   type 'a t = 'a Map.Make(String).t
   val empty: 'a t
   val is empty: 'a t -> bool
   val add : kev -> 'a -> 'a t -> 'a t
   val find : key -> 'a t -> 'a
   val remove : kev -> 'a t -> 'a t
   val mem: kev -> 'a t -> bool
   val iter: (\text{kev} -> \text{'a} -> \text{unit}) -> \text{'a} t -> \text{unit}
   val map: ('a -> 'b) -> 'a t -> 'b t
   val mapi : (key -> 'a -> 'b) -> 'a t -> 'b t
   val fold: (key -> 'a -> 'b -> 'b) -> 'a t -> 'b -> 'b
   val compare: ('a \rightarrow 'a \rightarrow int) \rightarrow 'a t \rightarrow 'a t \rightarrow int)
   val equal : ('a -> 'a -> bool) -> 'a t -> 'a t -> bool
 end
```

Maps

```
# let mymap = StringMap.empty;;
                                       (* Create empty map *)
val mymap: 'a StringMap.t = <abstr>
# let mymap = StringMap.add "Douglas" 42 mymap;; (* Add pair *)
val mymap: int StringMap.t = <abstr>
# StringMap.mem "foo" mymap;;
                                        (* Is "foo" there? *)
- bool = false
# StringMap.mem "Douglas" mymap::
                                     (* Is "Douglas" there? *)
-: bool = true
# StringMap.find "Douglas" mymap;;
                                            (* Get value *)
-: int = 42
# let mymap = StringMap.add "Adams" 17 mymap;;
val mymap: int StringMap.t = <abstr>
# StringMap.find "Adams" mymap;;
-: int = 17
# StringMap.find "Douglas" mymap;;
-: int = 42
# StringMap.find "Slarti" mymap;;
Exception: Not found.
```

- Fully functional: Map.add takes a key, a value, and a map and returns a new map that also includes the given key/value pair.
- Needs a totally ordered key type. Pervasives.compare usually does the job (returns -1, 0, or 1); you may supply your own.

```
module StringMap = Map.Make(struct
  type t = string
  let compare x y = Pervasives.compare x y
end)
```

• Uses balanced trees, so searching and insertion is $O(\log n)$.

Imperative Features

```
(* ": " means sequencing *)
# 0; 42;;
Warning S: this expression should have type unit.
-: int = 42
# ignore 0; 42;; (* ignore is a function: 'a -> unit *)
-: int = 42
# (); 42;; (* () is the literal for the unit type *)
-: int = 42
# print endline "Hello World!";; (* Print; result is unit *)
Hello World!
-: unit =()
# print string "Hello"; print endline "World!";;
Hello World!
-: unit =()
# print int 42; print newline ();;
42
-: unit =()
# print endline ("Hello " ^ string of int 42 ^ " world!");;
Hello 42 world!
-: unit =()
```

Hash Tables

```
# module StringHash = Hashtbl.Make(struct
                                           (* type of keys *)
   type t = string
   let equal x y = x = y (* use structural comparison *)
   let hash = Hashtbl.hash
                                      (* generic hash function *)
 end);;
module StringHash:
 sig
   type key = string
   type 'a t
   val create: int -> 'a t
   val clear: 'a t -> unit
   val copy : 'a t -> 'a t
   val add: 'a t \rightarrow \text{kev} \rightarrow \text{'a} \rightarrow \text{unit}
   val remove: 'a t -> key -> unit
   val find : 'a t \rightarrow \text{kev} \rightarrow 'a
   val find all: 'a t -> key -> 'a list
   val replace: 'a t -> kev -> 'a -> unit
   val mem : 'a t \rightarrow \text{key} \rightarrow \text{bool}
   val iter: (key -> 'a -> unit) -> 'a t -> unit
   val fold: (key -> 'a -> 'b -> 'b) -> 'a t -> 'b -> 'b
   val length: 'a t -> int
 end
```

Hash Tables

```
# let hash = StringHash.create 17;; (* initial size estimate *)
val hash: ' a StringHash.t = <abstr>
# StringHash.add hash "Douglas" 42;; (* modify the hash table *)
-: unit =()
# StringHash.mem hash "foo";;
                               (* is "foo" there? *)
- bool = false
# StringHash.mem hash "Douglas";; (* is "Douglas" there? *)
-: bool = true
# StringHash.find hash "Douglas";;
                                             (* Get value *)
-: int = 42
# StringHash.add hash "Adams" 17;; (* Add another key/value *)
-: unit =()
# StringHash.find hash "Adams";;
-: int = 17
# StringHash.find hash "Douglas";;
-: int = 42
# StringHash.find hash "Slarti";;
Exception: Not found.
```

Arrays

```
\# let a = [|42; 17; 19|];
                                      (* Array literal *)
val a : int array = [|42; 17; 19|]
# let aa = Array.make 5 0;;
                                       (* Fill a new array *)
val aa : int array = [0; 0; 0; 0; 0]
\# a.(0);;
                                    (* Random access *)
-: int = 42
# a.(2);;
-: int = 19
# a.(3);;
Exception: Invalid argument "index out of bounds".
                                 (* Arrays are mutable! *)
# a.(2) <- 20;;
-: unit =()
# a;;
-: int array = [|42; 17; 20|]
# let l = [24; 32; 17];
val l: int list = [24; 32; 17]
# let b = Array.of list l;;
                           (* Array from a list *)
val b : int array = [|24; 32; 17|]
# let c = Array.append a b;;
                                         (* Concatenation *)
val c: int array = [|42; 17; 20; 24; 32; 17|]
```

Arrays vs. Lists

	Arrays	Lists
Random access	O(1)	O(n)
Appending	O(n)	O(1)
Mutable	Yes	No

Useful pattern: first collect data of unknown length in a list then convert it to an array with *Array.of_list* for random queries.

Slides

A Complete Interpreter in Three

The Scanner and AST

scanner.mll

ast.mli

The Parser

parser.mly

```
%{\text{open Ast }%}
%token PLUS MINUS TIMES DIVIDE EOF
%token <int> LITERAL
%left PLUS MINUS
%left TIMES DIVIDE
%start expr
%type <Ast.expr> expr
expr:
  expr PLUS expr { Binop($1, Add, $3) }
  expr MINUS expr { Binop($1, Sub, $3) }
  expr TIMES expr { Binop($1, Mul, $3) }
  expr DIVIDE expr
                   { Binop($1, Div, $3) }
  LITERAL
                      Lit($1) }
```

The Interpeter

calc.ml

```
open Ast
let rec eval = function
    Lit(x) \rightarrow x
    Binop (e1, op, e2) \rightarrow
      let v1 = eval e1 and v2 = eval e2 in
      match op with
        Add \rightarrow v1 + v2
       Sub \rightarrow v1 - v2
       | Mul -> v1 * v2
        Div \rightarrow v1 / v2
let =
  let lexbuf = Lexing.from channel stdin in
  let expr = Parser.expr Scanner.token lexbuf in
  let result = eval expr in
  print endline (string of int result)
```

Compiling the Interpreter

```
$ ocamllex scanner.mll # create scanner.ml
8 states, 267 transitions, table size 1116 bytes
$ ocamlyacc parser.mly # create parser.ml and parser.mli
$ ocamle -c ast.mli # compile AST types
$ ocamle -c parser.mli # compile parser types
$ ocamle -c scanner.ml # compile the scanner
$ ocamle -c parser.ml # compile the parser
$ ocamle -c calc.ml # compile the interpreter
$ ocamle -o cale parser.cmo scanner.cmo cale.cmo
$./calc
2*3+4*5
26
```

Compiling with ocamlbuild

```
$ 1s
ast.mli calc.ml parser.mly scanner.mll
$ ocambuild calc.native # Build everything
Finished, 15 targets (0 cached) in 00:00:00.
$ 1s
ast.mli build calc.ml calc.native parser.mly scanner.mll
$./calc.native
2*3+4*5
Ctrl-D
26
ocambuild -clean # Remove build and all .native
```

Directed Graphs

Application: Directed Graphs

```
let edges = [
 ("a", "b"); ("a", "c");
 ("a", "d"); ("b", "e");
 ("c", "f"); ("d", "e");
  ("e", "f"); ("e", "g") ]
let rec successors n = function
 (s, t) :: edges ->
     if s = n then
        t :: successors n edges
      else
         successors n edges
```

```
a \rightarrow c \rightarrow f \rightarrow g
```

```
# successors "a" edges;;
-: string list = ["b"; "c"; "d"]

# successors "b" edges;;
-: string list = ["e"]
```

More Functional Successors

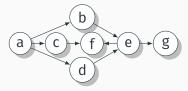
Our first example is imperative: performs "search a list," which is more precisely expressed using the library function List.filter:

```
let successors n edges = let matching (s, \_) = s = n in List.map snd (List.filter matching edges)
```

This uses the built-in snd function, which is defined as

```
let snd (\_,x) = x
```

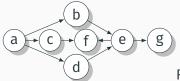
Depth-First Search



```
let rec dfs edges visited = function
[]     -> List.rev visited
| n::nodes ->
    if List.mem n visited then
        dfs edges visited nodes
else
        dfs edges (n::visited) ((successors n edges) @ nodes)
```

```
# dfs edges [] ["a"];;
-: string list = ["a"; "b"; "e"; "f"; "g"; "c"; "d"]
# dfs edges [] ["e"];;
-: string list = ["e"; "f"; "g"]
# dfs edges [] ["d"];;
-: string list = ["d"; "e"; "f"; "g"]
```

Topological Sort



Remember the visitor at the end.

```
# tsort edges [] ["a"];;
-: string list = ["a"; "d"; "c"; "b"; "e"; "g"; "f"]
# let cycle = [ ("a", "b"); ("b", "c"); ("c", "a") ];;
val cycle : (string * string) list = [("a", "b"); ...]
# tsort cycle [] ["a"];;
Stack overflow during evaluation (looping recursion?).
```

Better Topological Sort

Exception: Cyclic "a".

```
exception Cyclic of string
let tsort edges seed =
  let rec sort path visited = function
         -> visited
     n::nodes \rightarrow
      if List.mem n path then raise (Cyclic n) else
      let v' = if List.mem n visited then visited else
                n :: sort (n::path) visited (successors n edge
      in sort path v' nodes
  in
  sort [] [] [seed]
# tsort edges "a";;
-: string list = ["a"; "d"; "c"; "b"; "e"; "g"; "f"]
# tsort edges "d";;
- : string list = ["d"; "e"; "g"; "f"]
# tsort cycle "a";;
```

Depth-First Search Revisited

Previous version

```
let rec dfs edges visited = function
[]          -> List.rev visited
| n::nodes ->
    if List.mem n visited then
        dfs edges visited nodes
else
    dfs edges (n::visited) ((successors n edges) @ nodes)
```

was not very efficient, but good enough for small graphs.

Would like faster visited test and successors query.

Depth-First Search Revisited

Second version:

- use a Map to hold a list of successors for each node
- use a Set (valueless Map) to remember of visited nodes

```
module StringMap = Map.Make(String)
module StringSet = Set.Make(String)
```

Depth-First Search Revisited

```
let top_sort_map edges =
 (* Create an empty successor list for each node *)
 let succs = List.fold_left
      (fun map (s,d) \rightarrow
        StringMap.add d [] (StringMap.add s [] map)
     ) StringMap.empty edges
 in (* Build the successor list for each source node *)
  let succs = List.fold left
      (\text{fun succs (s. d)}^-)
        let ss = StringMap.find s succs
        in StringMap.add s (d::ss) succs) succs edges
  in
  (* Visit recursively, storing each node after visiting successors*)
  let rec visit (order, visited) n =
    if StringSet.mem n visited then
      (order, visited)
    else let (order, visited) = List.fold left
              visit (order, StringSet.add n visited)
              (StringMap.find n succs)
          in (n::order, visited)
  in (* Visit the source of each edge *)
  fst (List.fold left visit ([], StringSet.empty)
                             (List.map fst edges))
```

DFS with Arrays

Second version used a lot of *mem*, *find*, and *add* calls on the string map, each $O(\log n)$. Can we do better?

Solution: use arrays to hold adjacency lists and track visiting information.

Basic idea: number the nodes, build adjacency lists with numbers, use an array for tracking visits, then transform back to list of node names.

DFS with Arrays 1/2

```
let top_sort array edges =
  (* Assign a number to each node *)
  let map, nodecount =
    List.fold left
      (fun nodemap (s, d) ->
        let addnode node (map, n) =
          if StringMap.mem node map then (map, n)
          else (StringMap.add node n map, n+1)
        in
        addnode d (addnode s nodemap)
      ) (StringMap.empty, 0) edges
 in
  let successors = Array.make nodecount [] in
  let name = Array.make nodecount "" in
  (* Build adjacency lists and remember the name of each node *)
  List. iter
    (fun (s, d) ->
      let ss = StringMap.find s map in
      let dd = StringMap.find d map in
      successors.(ss) <- dd :: successors.(ss);
      name.(ss) < -s;
      name.(dd) < -d:
    ) edges;
```

DFS with Arrays 2/2

```
(* Visited flags for each node *)
let visited = Array.make nodecount false in
(* Visit each of our successors if we haven't done so yet *)
(* then record the node *)
let rec visit order n =
 if visited.(n) then order
  else (
   visited.(n) <- true;
   n :: (List.fold left visit order successors.(n))
in
(* Compute the topological order *)
let order = visit [] 0 in
(* Map node numbers back to node names *)
List.map (fun n -> name.(n)) order
```