

# Problem list 5

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**Exercise 1.** Assume that  $\text{char}(K) = p > 0$ ,  $K \subseteq L$  is an algebraic field extension and  $a \in L \setminus K$ . Prove that  $a^{p^l}$  is separable over  $K$  for some  $l \geq 0$ .

We simply want to show that there exists an  $l$  such that  $a^{p^l} \in K$