

SYLABUS – teoria grafów:

1. Basic concepts: graphs, paths and cycles, complete and bipartite graphs
2. Matchings: Hall's Marriage theorem and its variations
3. Forbidden subgraphs: complete bipartite and r -partite subgraphs, chromatic numbers, Turán's theorem, asymptotic behaviour of edge density, Erdős-Stone theorem
4. Hamiltonian cycles (Dirac's Theorem), Eulerian circuits
5. Connectivity: connected and k -connected graphs, Menger's theorem
6. Ramsey theory: edge colourings of graphs, Ramsey's theorem and its variations, asymptotic bounds on Ramsey numbers
7. Planar graphs and colourings: statements of Kuratowski's and Four Colour theorems, proof of Five Colour theorem, graphs on other surfaces and Euler characteristics, chromatic polynomial, edge colourings and Vizing's theorem
8. Random graphs: further asymptotic bounds on Ramsey numbers, Zarankiewicz numbers and their bounds, graphs of large first and high chromatic number, complete subgraphs in random graphs.
9. Algebraic methods: adjacency matrix and its eigenvalues, strongly regular graphs, Moore graphs and their existence.

