ME-172 Computer Programming Language Sessional Assignment No. 03

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Problem 1

Write a program to evaluate the sine series using for loop.

Solution:

The sine series is given by the mathematical formula:

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$$

The following program asks the user to enter the value of x and then it evaluates the sine series by adding up first 10 terms.

```
#include <stdio.h>
#include <math.h>
// Calculates the factorial of a non-negative integer.
long factorial(int n)
{
    long result = 1;
    for(; n > 1; n--)
        result *= n;
    return result;
}
int main(void)
    // Take user input for x
    float x;
    printf("Enter x: ");
    scanf("%f", &x);
    // Represents the sum of sine series up to n terms.
    double sum = 0;
```

```
// Total number of terms from start to add up.
const int n = 10;

// Calculate
for(int i = 0, j = 0; j < n; i+= 2, j++)
{
    sum += pow(-1, j) * pow(x, i + 1) / factorial(i + 1);
}

// Show output
printf("Sum of sine series up to 10th term = %lf\n", sum);
}</pre>
```

Saving the file with name sine.c. Then Compiling the source file with the following command:

```
$ clang -o sine sine.c -lm
```

An executable binary file with name **sine** will be created if everything goes right.

Output

Running the executable with the following command:

```
$ ./sine
Enter x: 2
Sum of sine series up to 10th term = 0.909297
```

Problem 2

Write a program that determines the number of trailing zeros at the end of x! (x factorial), where x is an arbitrary number. For instance, 5! is 120, so it has one trailing zero.

Solution:

The recursive definition of x! is the following.

$$x! = x(x-1)!$$

And the iterative definition is the following. We will be using this definition in our code.

$$x! = x(x-1)(x-2)(x-3)...3.2.1$$

```
#include <stdio.h>
#include <stdbool.h>
// Calculates the factorial of a non-negative integer.
long factorial(int n)
    long result = 1;
    for(; n > 1; n--)
        result *= n;
    return result;
}
int main(void)
{
    // Take user input for \boldsymbol{x}
    int x;
    printf("Enter x: ");
    scanf("%i", &x);
    long x_fact = factorial(x);
    long n = x_fact;
    // Represents the number of trailing zeros
    int count = 0;
    // Calculate
```

Saving the file with name trailingZeros.c. Then compiling the source file with the following command:

```
$ clang -o trailingZeros trailingZeros.c
```

An executable binary file with name trailingZeros will be created if everything goes right.

Output

Running the executable using the following command:

```
$ ./trailingZeros
Enter x: 10
10! = 3628800
Total number of trailing zeros at the end of 10! = 2
```

Problem 3

Draw a Pascal's triangle using C programming (for loop)

Solution:

The binomial theorem is given by the following formula:

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

If we just take the coefficients of $a^{n-k}b^k$ from the above binomial expansion formula and center-align them we get an interesting structure what we call a Pascal's Triangle. From combinatorics, the definition of $\binom{n}{k}$ is given by the following formula:

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

#include <stdio.h>

```
// Calculates the factorial of a non-negative integer.
long factorial(int n)
{
    long result = 1;
    for(; n > 1; n--)
    {
        result *= n;
    }
    return result;
}

// Prints the coefficients of nth row. (counting from 0th row)
void row(int n)
{
    for(int k = 0; k <= n; k++)
    {
        int coe = factorial(n) / (factorial(k) * factorial(n - k));
        printf("\n");
}

printf("\n");
}</pre>
```

```
int main(void)
{
    // Take user input for power of binomial, n.
    int n;
    printf("Enter n: ");
    scanf("%i", &n);

    // Print rows.
    for (int i = 0; i <= n; i++)
    {
        // Print preceding spaces
        for(int j = 0; j < n - i; j++)
        {
            printf(" ");
        }

        // Print row with height i.
        row(i);
    }
}</pre>
```

Saving the file with name pascalsTriangle.c. Then Compiling the source file with the following command:

```
$ clang -o pascalsTriangle pascalsTriangle.c
```

An executable binary file with name pascalsTriangle will be created if everything goes right.

Output

Running the executable with the following command:

```
$ ./pascalsTriangle
Enter n: 4
    1
    1 1
    1 2 1
```

1 3 3 1 1 4 6 4 1

When a binomial raised to a power of n is expanded, we get a total of n+1 terms from the exansion. The first row in our output represents the coefficients of expansion of $(a+b)^0$, which is 1. And if we keep going up to (and including) $(a+b)^4$ we get the coefficients represented by the last row in our output. And there are (4+1) = 5 coefficients (from (4+1) = 5 terms) in the last row, just like we preached.

NOTE: All the programs are written in *Linux* environment. The executable binary files don't have an extension like .exe, .dmg, or .app beacuse in Linux whether a program is executable or not is determined by the permissions on the file, not the extension. And LLVM's *Clang* is used for the compilation of above source files.