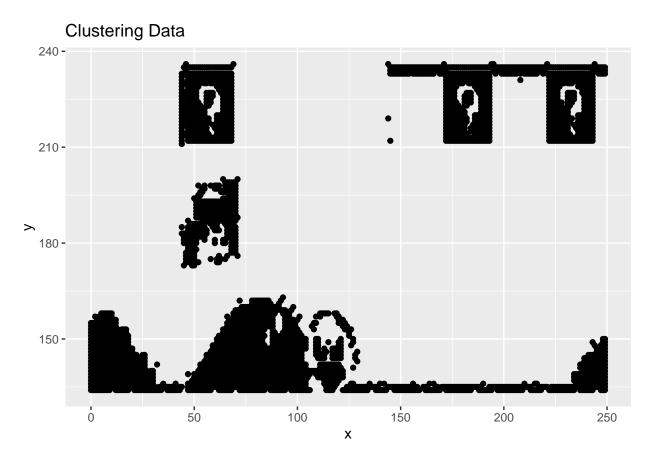
Assignment 8.3: Clustering

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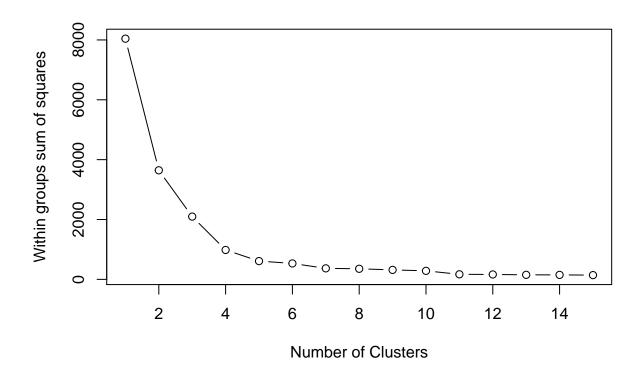
```
clustering_df<-scale(clustering_df)
head(clustering_df)</pre>
```

```
## x y
## [1,] -0.8482235 1.561107
## [2,] -0.5415045 1.561107
## [3,] 0.4586659 1.561107
## [4,] 0.8187273 1.561107
## [5,] 1.1254462 1.561107
## [6,] 1.1387818 1.561107
```

```
library(cluster)
library(factoextra)
```

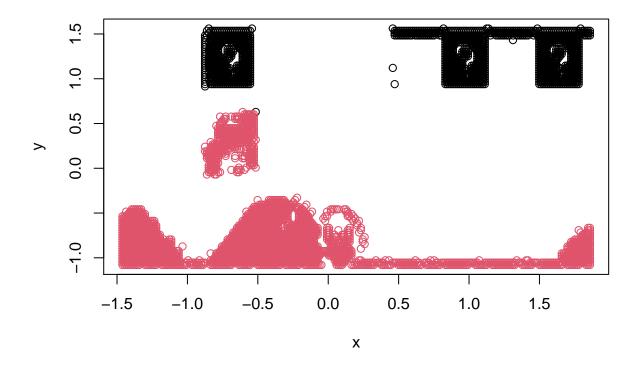
Warning: package 'factoextra' was built under R version 4.0.2

Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

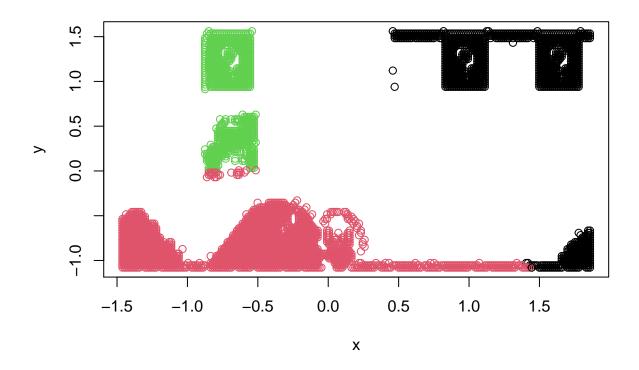


```
## [1] 8042.0000 3644.3577 2097.5918 982.5633 610.6719 532.5799 368.2815
## [8] 353.6523 316.3358 284.9604 168.8087 164.3646 151.6366 149.6875
## [15] 141.9250
```

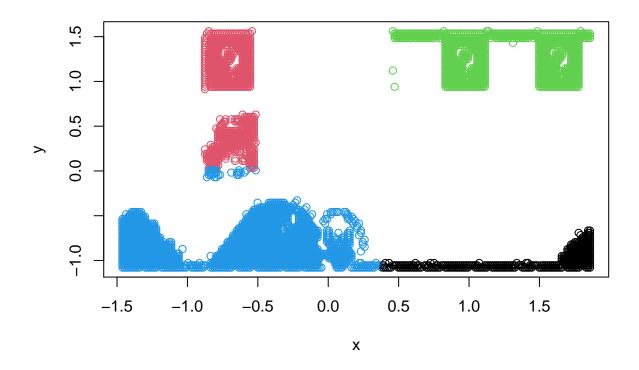
```
cluster_2<-kmeans(clustering_df, 2)
plot(clustering_df, col = cluster_2$cluster)</pre>
```



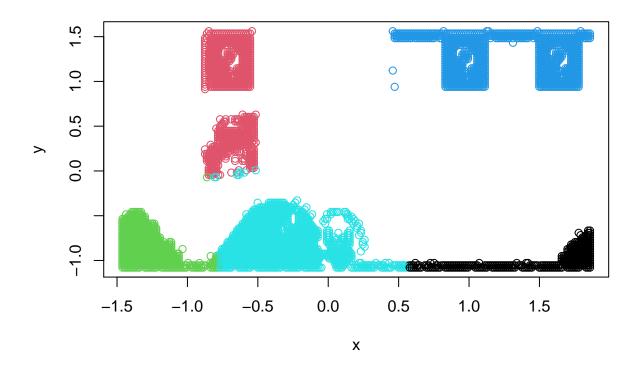
```
cluster_3<-kmeans(clustering_df, 3)
plot(clustering_df, col = cluster_3$cluster)</pre>
```



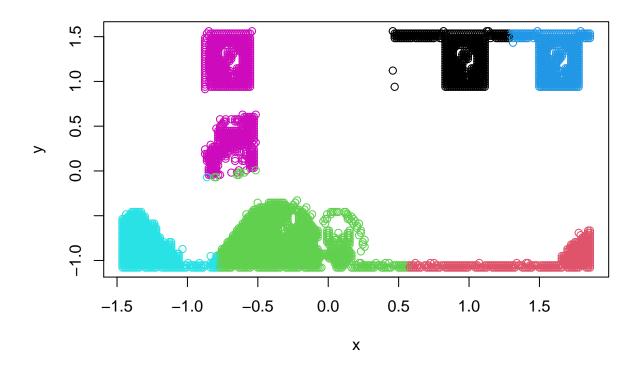
```
cluster_4<-kmeans(clustering_df, 4)
plot(clustering_df, col = cluster_4$cluster)</pre>
```



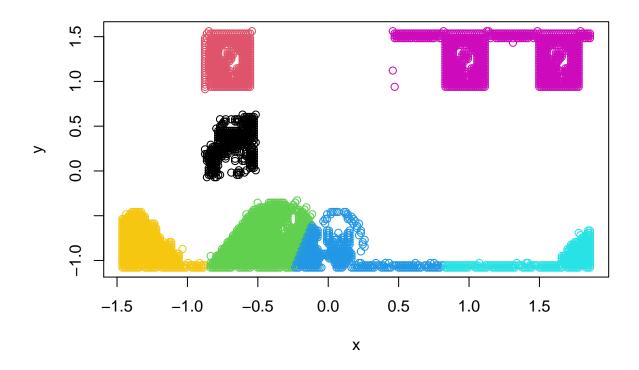
```
cluster_5<-kmeans(clustering_df, 5)
plot(clustering_df, col = cluster_5$cluster)</pre>
```



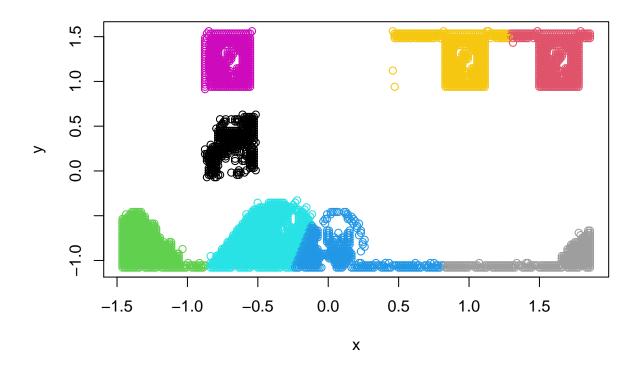
```
cluster_6<-kmeans(clustering_df, 6)
plot(clustering_df, col = cluster_6$cluster)</pre>
```



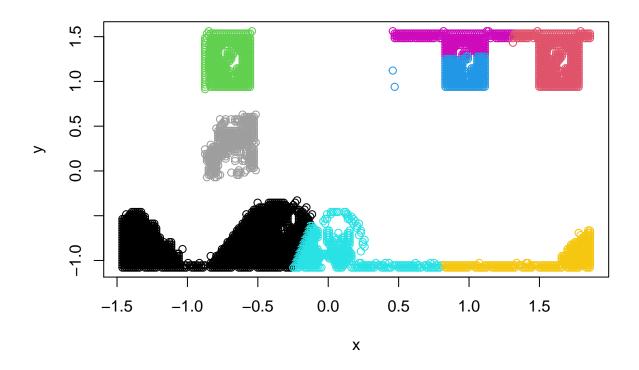
```
cluster_7<-kmeans(clustering_df, 7)
plot(clustering_df, col = cluster_7$cluster)</pre>
```



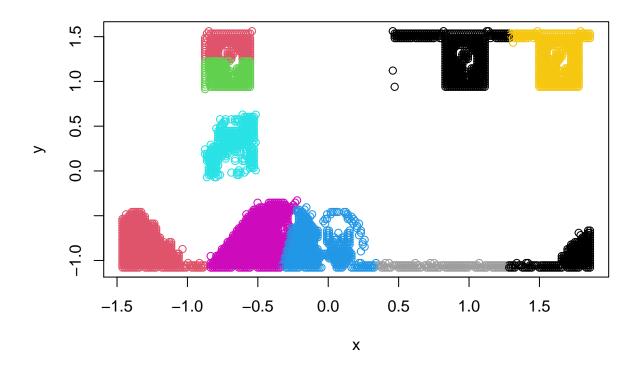
```
cluster_8<-kmeans(clustering_df, 8)
plot(clustering_df, col = cluster_8*cluster)</pre>
```



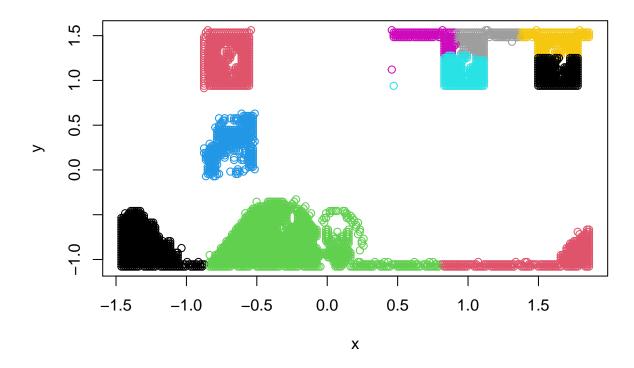
```
cluster_9<-kmeans(clustering_df, 9)
plot(clustering_df, col = cluster_9$cluster)</pre>
```



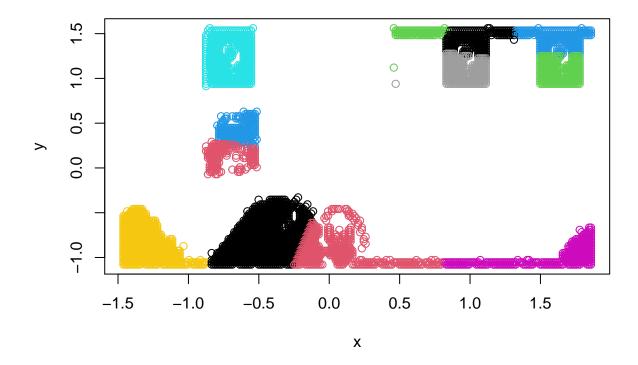
```
cluster_10<-kmeans(clustering_df, 10)
plot(clustering_df, col = cluster_10$cluster)</pre>
```



```
cluster_11<-kmeans(clustering_df, 11)
plot(clustering_df, col = cluster_11$cluster)</pre>
```

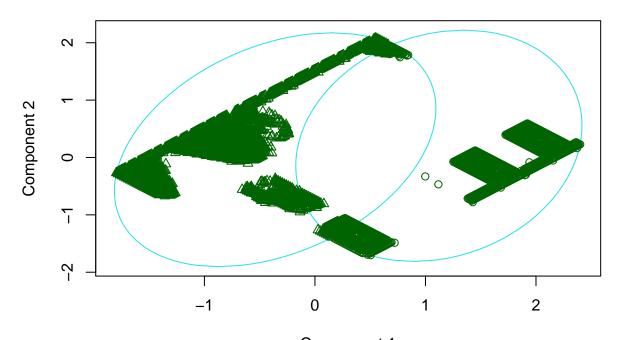


```
cluster_12<-kmeans(clustering_df, 12)
plot(clustering_df, col = cluster_12*cluster)</pre>
```



clusplot(pam(clustering_df, 2))

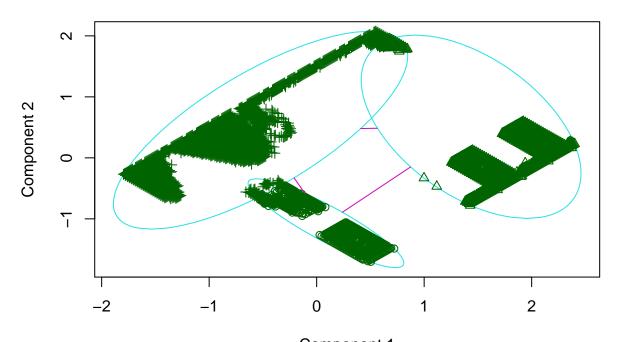
clusplot(pam(x = clustering_df, k = 2))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 3))

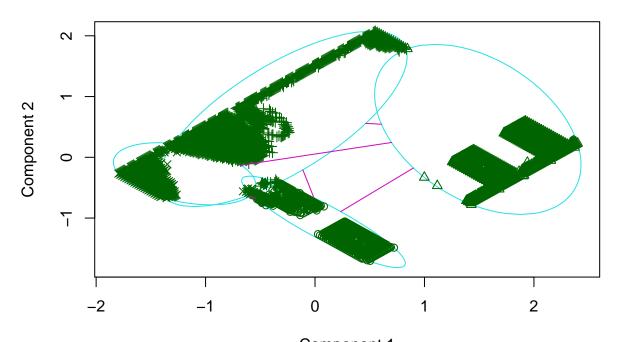
clusplot(pam(x = clustering_df, k = 3))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 4))

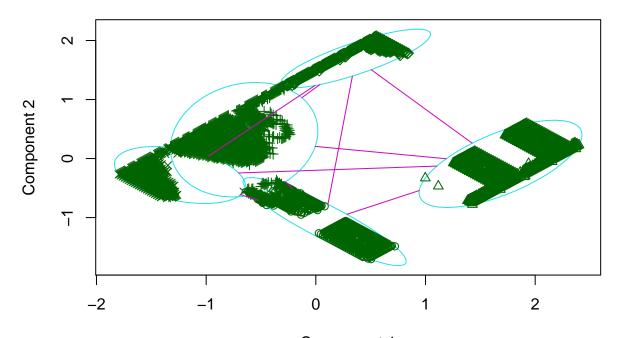
clusplot(pam(x = clustering_df, k = 4))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 5))

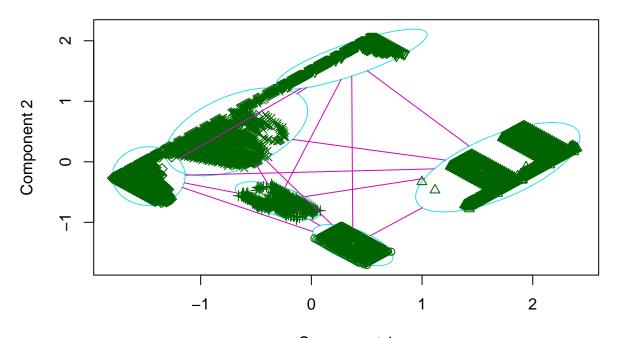
clusplot(pam(x = clustering_df, k = 5))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 6))

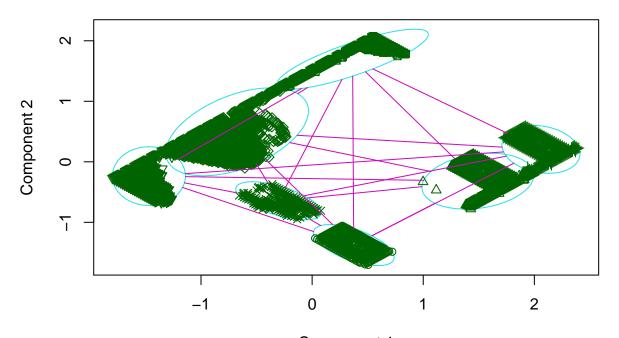
clusplot(pam(x = clustering_df, k = 6))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 7))

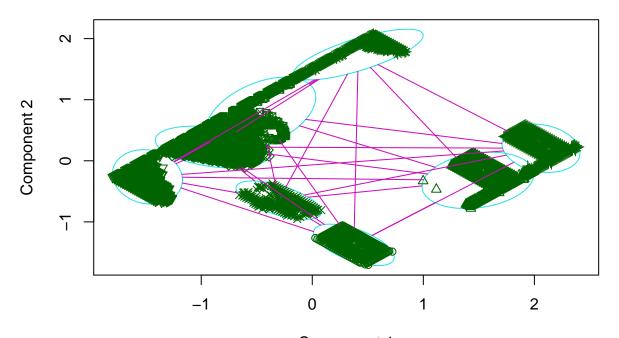
clusplot(pam(x = clustering_df, k = 7))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 8))

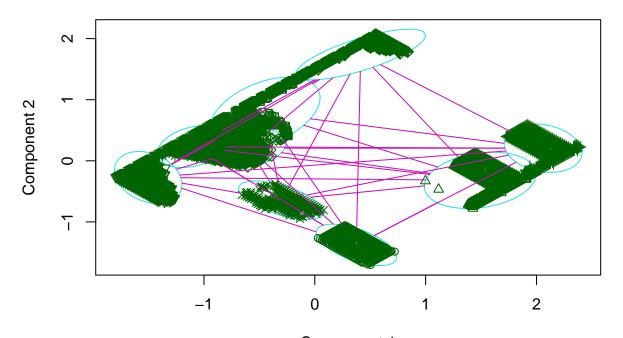
clusplot(pam(x = clustering_df, k = 8))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 9))

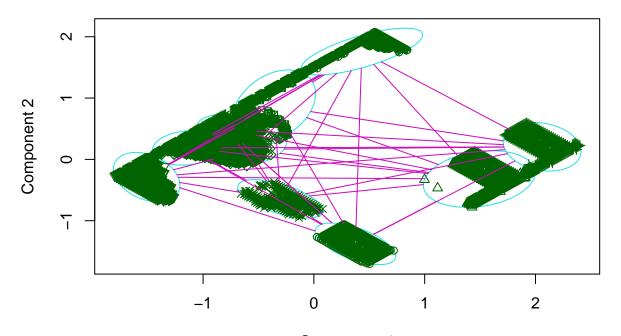
clusplot(pam(x = clustering_df, k = 9))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 10))

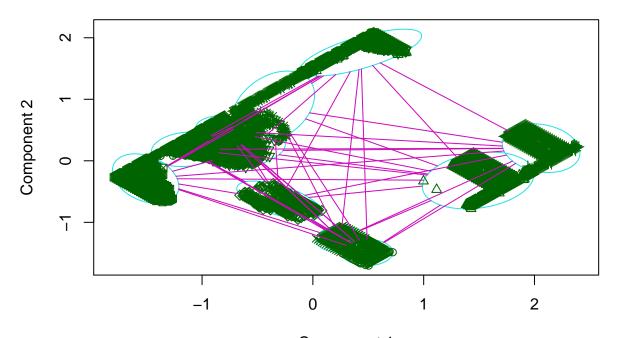
clusplot(pam(x = clustering_df, k = 10))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 11))

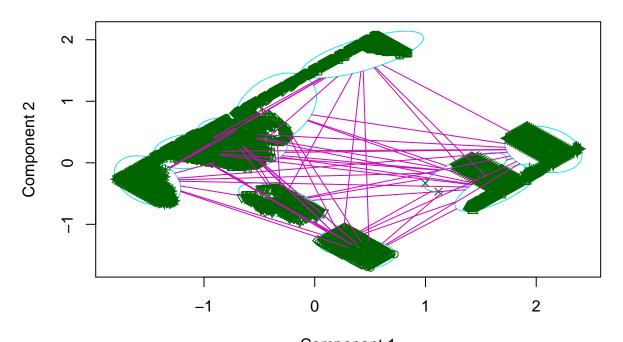
clusplot(pam(x = clustering_df, k = 11))



Component 1
These two components explain 100 % of the point variability.

clusplot(pam(clustering_df, 12))

clusplot(pam(x = clustering_df, k = 12))



Component 1
These two components explain 100 % of the point variability.

```
##install.packages("ggfortify")
library(ggfortify)

## Warning: package 'ggfortify' was built under R version 4.0.2

autoplot(cluster_2, clustering_df, frame = TRUE)

## Warning: 'select_()' is deprecated as of dplyr 0.7.0.

## Please use 'select()' instead.

## This warning is displayed once every 8 hours.

## Call 'lifecycle::last_warnings()' to see where this warning was generated.

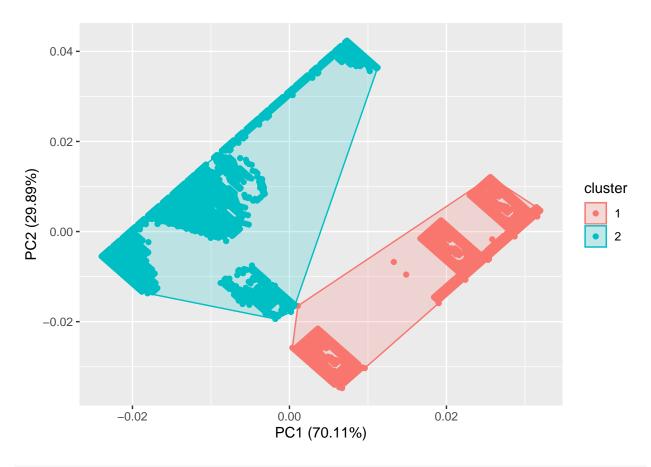
## Warning: 'group_by_()' instead.

## Warning: 'group_by()' instead.

## See vignette('programming') for more help

## This warning is displayed once every 8 hours.

## Call 'lifecycle::last_warnings()' to see where this warning was generated.
```



cluster_2\$centers

```
##
## 1 0.6489063 1.2571500
## 2 -0.3568359 -0.6913114
cluster_k<- list()</pre>
for (i in 2:12) {
 cluster_k[[i]] <- kmeans(clustering_df, i)</pre>
cluster_k
## [[1]]
## NULL
##
\#\# K-means clustering with 2 clusters of sizes 2595, 1427
##
## Cluster means:
## 1 -0.3568359 -0.6913114
## 2 0.6489063 1.2571500
##
## Clustering vector:
```



```
##
## Within cluster sum of squares by cluster:
## [1] 2235.423 1379.822
(between_SS / total_SS = 55.0 %)
## Available components:
##
## [1] "cluster"
   "centers"
     "totss"
        "withinss"
          "tot.withinss"
## [6] "betweenss"
   "size"
     "iter"
        "ifault"
##
## [[3]]
## K-means clustering with 3 clusters of sizes 2255, 1426, 341
## Cluster means:
##
  X
## 1 -0.6241498 -0.6453636
## 2 0.6497223 1.2575905
## 3 1.4104215 -0.9912878
##
## Clustering vector:
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
```

```
##
## Within cluster sum of squares by cluster:
## [1] 898.64282 1378.07217
    76.95713
(between_SS / total_SS = 70.7 %)
## Available components:
## [1] "cluster"
   "centers"
     "totss"
          "tot.withinss"
        "withinss"
## [6] "betweenss"
   "size"
     "iter"
        "ifault"
##
## [[4]]
## K-means clustering with 4 clusters of sizes 1945, 338, 985, 754
## Cluster means:
##
  х
## 1 -0.6150938 -0.8013866
## 2 1.4196187 -0.9906559
## 3 1.2586128 1.2721827
## 4 -0.6939089 0.8493881
##
## Clustering vector:
##
##
##
##
##
##
##
##
```



```
##
## Within cluster sum of squares by cluster:
## [1] 551.86203 73.69142 177.01665 179.99325
##
(between_SS / total_SS = 87.8 %)
##
## Available components:
##
## [1] "cluster"
 "centers"
  "totss"
   "withinss"
    "tot.withinss"
## [6] "betweenss"
 "size"
  "iter"
   "ifault"
##
## [[5]]
```

```
## K-means clustering with 5 clusters of sizes 338, 464, 521, 1945, 754
##
## Cluster means:
##
 х
## 1 1.4196187 -0.9906559
## 2 1.6222263 1.2583422
## 3 0.9347803 1.2845090
## 4 -0.6150938 -0.8013866
## 5 -0.6939089 0.8493881
##
## Clustering vector:
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
## [1111] 2 2 2 2 2 2 2 2 2 2 2 2 2 3 3 3 3 3 3
## [1148] 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 5 5 5 5
```

```
## Within cluster sum of squares by cluster:
## [1] 73.69142 24.58883 36.27618 551.86203 179.99325
(between_SS / total_SS = 89.2 %)
##
## Available components:
##
## [1] "cluster"
    "centers"
       "totss"
          "withinss"
            "tot.withinss"
## [6] "betweenss"
    "size"
       "iter"
         "ifault"
## [[6]]
## K-means clustering with 6 clusters of sizes 287, 453, 748, 569, 985, 980
##
## Cluster means:
##
## 1 1.56663641 -0.9775317
## 2 0.04852981 -0.9013642
## 3 -0.69513141 0.8558284
## 4 -1.28733754 -0.8403549
## 5 1.25861275 1.2721827
## 6 -0.46825394 -0.7410490
##
## Clustering vector:
 ##
##
##
##
##
##
##
##
##
##
```

```
##
## Within cluster sum of squares by cluster:
## [1] 31.53744 38.32528 175.95228 25.87924 177.01665 83.86858
(between_SS / total_SS = 93.4 %)
##
##
## Available components:
## [1] "cluster"
   "centers"
     "totss"
       "withinss"
         "tot.withinss"
## [6] "betweenss"
     "iter"
   "size"
       "ifault"
##
## [[7]]
## K-means clustering with 7 clusters of sizes 441, 569, 985, 341, 286, 984, 416
##
## Cluster means:
##
  Х
## 1 -0.71027100 1.2249978
## 2 -1.28733754 -0.8403549
## 3 1.25861275 1.2721827
```

```
## 4 -0.67716791 0.2920086
## 5 1.56929810 -0.9772649
## 6 -0.45003907 -0.7716581
## 7 0.07433762 -0.9036722
## Clustering vector:
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
##
```

```
##
## Within cluster sum of squares by cluster:
## [1] 19.52538 25.87924 177.01665 13.78287 30.95007 65.95642 35.17087
 (between_SS / total_SS = 95.4 %)
##
## Available components:
##
## [1] "cluster"
      "centers"
          "totss"
                   "tot.withinss"
              "withinss"
## [6] "betweenss"
      "size"
          "iter"
              "ifault"
##
## [[8]]
## K-means clustering with 8 clusters of sizes 550, 281, 341, 560, 526, 985, 441, 338
## Cluster means:
##
## 1 -0.5280962 -0.9280690
## 2 1.5823687 -0.9757179
## 3 -0.6771679 0.2920086
## 4 -1.2934898 -0.8367851
## 5 -0.3244840 -0.6111989
## 6 1.2586128 1.2721827
## 7 -0.7102710 1.2249978
## 8 0.1338769 -0.9414023
##
## Clustering vector:
##
 ##
 ##
 ##
 ##
 ##
 ##
 ##
 ##
 ##
 ##
 ##
##
 ##
 ##
 ##
##
[704] 6 6 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
##
 [778] 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 6 6
```

```
##
##
```

```
##
## Within cluster sum of squares by cluster:
## [1] 21.20268 28.16435 13.78287 24.08252 20.61176 177.01665 19.52538
## [8] 28.63480
## (between_SS / total_SS = 95.9 %)
##
## Available components:
## [1] "cluster"
   "centers"
      "totss"
        "withinss"
           "tot.withinss"
## [6] "betweenss"
      "iter"
   "size"
        "ifault"
##
## K-means clustering with 9 clusters of sizes 441, 341, 521, 464, 281, 560, 526, 550, 338
##
## Cluster means:
 x
## 1 -0.7102710 1.2249978
## 2 -0.6771679 0.2920086
## 3 0.9347803 1.2845090
## 4 1.6222263 1.2583422
## 5 1.5823687 -0.9757179
```

```
## 6 -1.2934898 -0.8367851
## 7 -0.3244840 -0.6111989
## 8 -0.5280962 -0.9280690
## 9 0.1338769 -0.9414023
## Clustering vector:
##
##
##
##
##
##
##
##
##
##
##
##
##
##
[593] 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 1 1 1 1 1 1 1 1 1 1
##
##
##
##
##
##
##
##
##
## [1148] 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 1 1 1 1
## [1185] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 4 4
## [1222] 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 3 3
```

```
##
## Within cluster sum of squares by cluster:
## [1] 19.52538 13.78287 36.27618 24.58883 28.16435 24.08252 20.61176 21.20268
## [9] 28.63480
  (between_SS / total_SS = 97.3 %)
##
##
## Available components:
##
## [1] "cluster"
              "centers"
                        "totss"
                                   "withinss"
                                             "tot.withinss"
## [6] "betweenss"
              "size"
                        "iter"
                                   "ifault"
##
## [[10]]
## K-means clustering with 10 clusters of sizes 441, 984, 425, 286, 247, 341, 416, 163, 569, 150
##
## Cluster means:
##
          X
## 1
   -0.71027100 1.2249978
## 2 -0.45003907 -0.7716581
## 3
    1.64399735 1.2350671
## 4
    1.56929810 -0.9772649
## 5
    0.96525699 1.0930832
## 6
   -0.67716791 0.2920086
## 7
    0.07433762 -0.9036722
## 8
    1.16463492 1.4608797
## 9 -1.28733754 -0.8403549
## 10 0.75187146 1.4672100
##
## Clustering vector:
##
    [1]
      1 1 10 10 8 8 8 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1
##
              ##
   8
                                                   8
##
      8 8
           8
            8
               8
                 8
                   8
                     8
                       8
                         8
                           8
                             8
                               8
                                 8
                                   8
                                     8
                                       8
                                         8
                                           8
                                             8
                                               8
                                                 8
   [73]
                                                     8
                                3
      8 8 8
            8
               8
                 8
                   8
                     8
                       3
                         3
                           3
                             3
                              3
                                  3
                                     3
                                       3
                                         3
                                           3
                                             3
                                               3
##
   [97]
                                                     3
                   3
                     3
                             1 10 10 10 10 10 10 10 10 10 10 10 10
  [121]
      3 3
          3
            3
               3
                 3
                       3
                         3
                           3
  8
                                       8
                                         8
                                           8
##
                                             8
                                               8
                                                 8
                                                     8
##
  Г1697
         8
           8
             8
               8
                 8
                   8
                     8
                       8
                         8
                           8
                             8
                               8
                                 8
                                   8
                                     8
                                       8
                                         3
                                           3
                                             3
                                               3
                                                 3
                                                   3
                                                     3
##
      1
                   1
                                 1
  Г1937
        1
          1
             1
               1
                 1
                     1
                       1
                         1
                           1
                             1
                               1
                                   1
                                     1
                                       1
                                         1
                                           1
                                             1
                                               1
  [241] 10 10 10 10 10 10 10 10
                             8
                               8
                                 8
                                   8
                                     8
                                       8
                                         8
                                           8
                                             8
##
                       8
                         8
                           8
                                               8
                                                 8
                                                   8
                                                     8
                                 8
                                   3
##
  [265]
       8 8
           8
            8
               8
                 8
                   8
                     8
                       8
                         8
                           8
                             8
                               8
                                     3
                                       3
                                         3
                                           3
                                             3
                                               3
                                                 3
                                                   3
                                                     3
       3 3
                   3
                               3
                                 3
##
  [289]
          3
             3
               3
                 3
                     3
                       3
                         3
                           3
                             3
                                   3
                                     3
                                       3
                                         1
                                           1
                                             1
                                     1 10 10 10 10 10 10 10 10
##
  [313]
      1
        1
           1
             1
               1
                 1
                   1
                     1
                       1
                         1
                           1
                             1
                               1
                                 1
                                   1
##
  [337] 10 10
           8
             8
               8
                 8
                   8
                     8
                       8
                         8
                           8
                             8
                               8
                                 8
                                   3
                                     3
                                       3
                                         3
                                           3
                                             3
                                               3
                                                   3
                                                     3
##
       3
        3
           3
            3
               3
                 3
                   3
                     3
                       3
                         3
                           3
                             3
  [361]
                               1
                                 1
                                   1
                                     1
                                       1
                                           1
                                             1
                                               1
                                                 1
                                                   1
                                         1
                                                     1
##
  [385]
       1
        1
          1
             1
               1
                 1
                   1
                     1
                       1 10 10 10 10 10 10 10 10 10
                                           8
                                             8
                                               8
                                                     8
##
  [409]
       8
        8
          8 8
               8
                 8
                   3
                     3
                       3
                         3
                           3
                             3
                               3
                                 3
                                  3
                                     3
                                       3 3
                                           3
                                             3
                                               3
                                                 3
                                                   3
                                                     3
##
  [433]
       3 3 1 1
               1 1
                   1
                     1
                       1 1 1 1 1 1 1 1 1 1
```

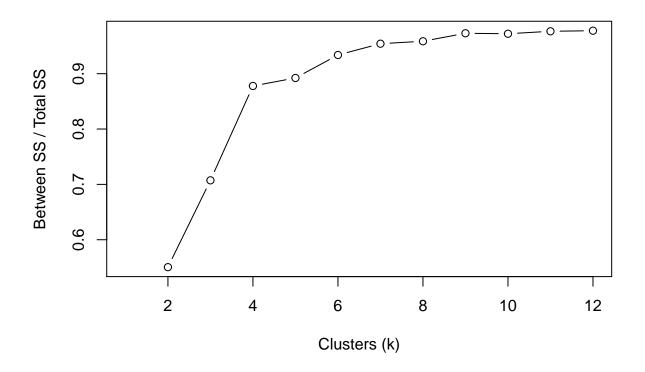
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##
## Within cluster sum of squares by cluster:
##
    [1] 19.525379 65.956422 19.316793 30.950073 4.903574 13.782873 35.170870
##
          4.404013 25.879236 4.039289
     (between_SS / total_SS = 97.2 %)
##
##
##
   Available components:
##
##
   [1] "cluster"
                            "centers"
                                              "totss"
                                                                  "withinss"
                                                                                    "tot.withinss"
##
   [6] "betweenss"
                            "size"
                                              "iter"
                                                                 "ifault"
##
## [[11]]
## K-means clustering with 11 clusters of sizes 241, 244, 504, 341, 237, 332, 516, 559, 328, 441, 279
```

```
##
## Cluster means:
##
     -1.3539251 -0.6696803
## 1
## 2
      1.5814256
                  1.4427949
## 3
      0.9240098
                 1.2768745
     -0.6771679
                  0.2920086
## 5
      1.6378261
                 1.0865538
## 6
      0.1459620 -0.9417097
## 7
     -0.3237155 -0.6072366
     -0.5142130 -0.9243509
## 9
     -1.2384119 -0.9657591
## 10 -0.7102710 1.2249978
## 11 1.5875561 -0.9750650
##
##
   Clustering vector:
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## [3961]
       ##
## Within cluster sum of squares by cluster:
  [1] 3.755767 7.983527 33.568586 13.782873 4.248952 28.809384 20.108509
  [8] 21.077980 8.091273 19.525379 27.092500
##
  (between_SS / total_SS = 97.7 %)
##
## Available components:
##
## [1] "cluster"
                "centers"
                            "totss"
                                       "withinss"
                                                  "tot.withinss"
## [6] "betweenss"
                "size"
                            "iter"
                                       "ifault"
##
## [[12]]
## K-means clustering with 12 clusters of sizes 338, 242, 281, 526, 148, 235, 560, 206, 550, 461, 282,
## Cluster means:
##
           Х
     0.1338769 -0.9414023
## 1
## 2
     0.9663558 1.0880137
    1.5823687 -0.9757179
## 3
## 4
   -0.3244840 -0.6111989
## 5
    -0.7266712 0.1288981
## 6 -0.7131082 1.0725995
## 7 -1.2934898 -0.8367851
    -0.7070343 1.3988502
## 8
## 9 -0.5280962 -0.9280690
## 10 1.6243020 1.2565966
## 11 0.9116036 1.4557079
## 12 -0.6392068 0.4170881
##
## Clustering vector:
##
    ##
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##
##
## Within cluster sum of squares by cluster:
   [1] 28.634796 4.928350 28.164346 20.611761 3.220997
                                                       4.163265 24.082517
       3.673850 21.202680 24.063776 13.929891 2.964061
##
##
    (between_SS / total_SS = 97.8 %)
##
## Available components:
##
## [1] "cluster"
                                   "totss"
                                                               "tot.withinss"
                     "centers"
                                                 "withinss"
## [6] "betweenss"
                    "size"
                                  "iter"
                                                 "ifault"
betweenss_totss <- list()</pre>
for (i in 1:12) {
  }
plot(1:12, betweenss_totss, type = "b", ylab = "Between SS / Total SS", xlab = "Clusters (k)")
```



Based on the elbow and shoulder plots, it appears that the correct cluster is around 4. Based on the kmeans plot, it looks like 6 makes the most sense.