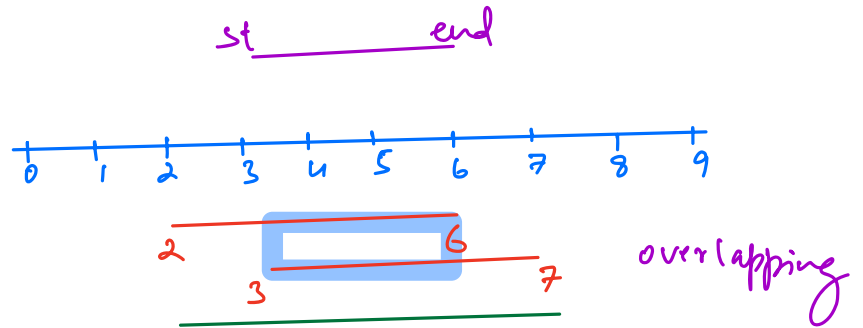


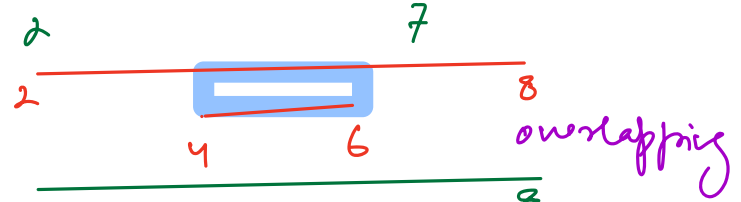
# Array 3 - Interview Problems

## Merge Intervals

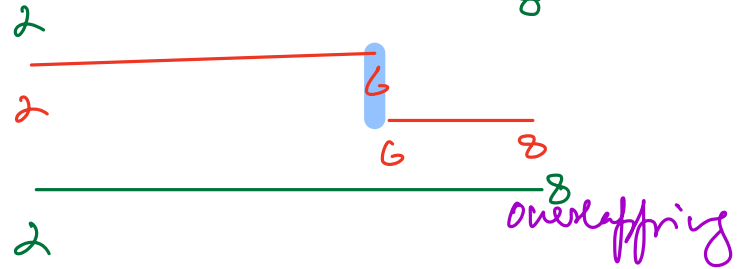
(2,6) (3,7)



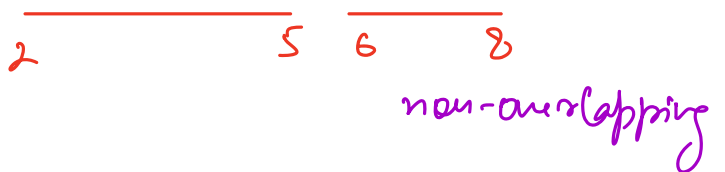
(2,8) (4,6)



(2,6) (6,8)



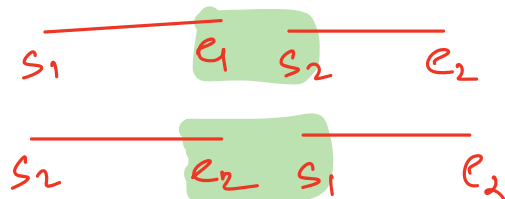
(2,5) (6,8)



## Non-overlapping condition

$s_1 \rightarrow e_1$

$s_2 \rightarrow e_2$



$$e_1 < s_2 \quad || \quad e_2 < s_1$$

## Merge 2 overlapping intervals

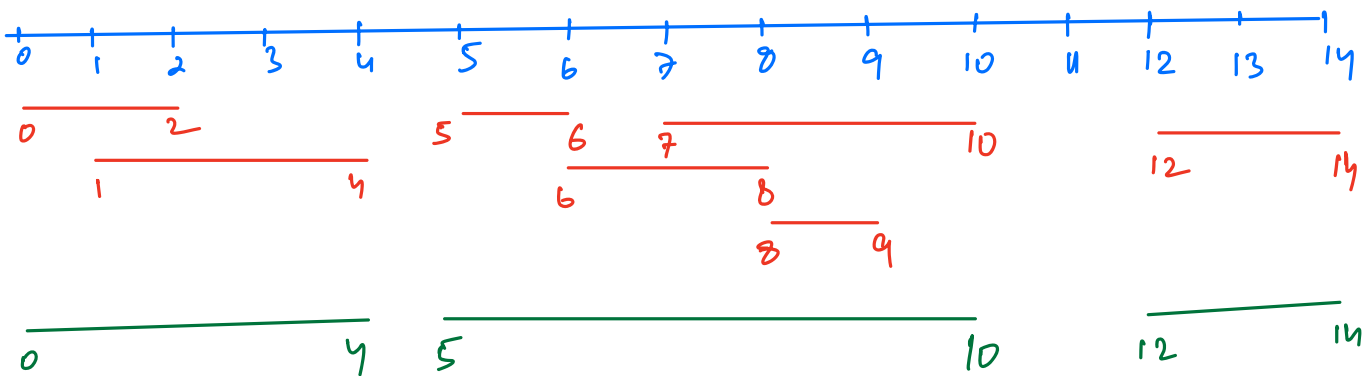
$$\left. \begin{array}{l} s_1 - e_1 \\ s_2 - e_2 \end{array} \right\} \rightarrow \begin{array}{l} st = \min(s_1, s_2) \\ end = \max(e_1, e_2) \end{array}$$

### Question 1

Given a list of intervals, sorted w.r.t Start time.

Merge all overlapping intervals & return the sorted list.

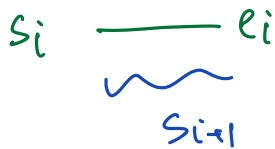
$$\begin{array}{l} st = [0, 5, 12] \\ end = [2, 6, 14] \end{array} \quad \left. \begin{array}{l} \boxed{0, 1} \\ \boxed{5, 8} \\ \boxed{12, 14} \end{array} \right\} \begin{array}{l} S = \emptyset \\ E = \{1, 6, 8, 9, 10, 11, 13\} \end{array}$$



output :

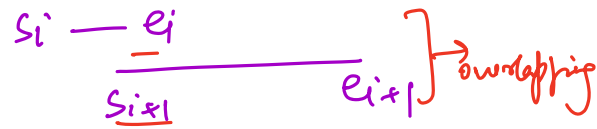
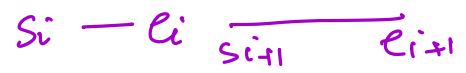
0	4	✓
5	10	✓
12	14	✓

sorted w.r.t start time !?



$$S_i \leq S_{i+1}$$

overlap  $\rightarrow$   $S_{i+1} \leq E_i$



Code

$S = \text{start}[0]$  ,  $E = \text{end}[0]$

for ( $i = 1$  to  $n-1$ ) {

  if ( $\text{start}[i] \leq E$ ) { // overlapping

$E = \max(E, \text{end}[i])$

  }

  else { // not overlapping

    print ( $S, E$ )

$S = \text{start}[i]$  ,  $E = \text{end}[i]$

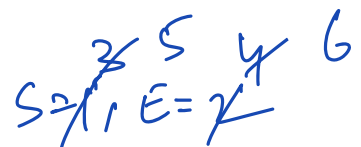
  }

}

print ( $S, E$ )

TC:  $O(N)$

SC:  $O(1)$



(1, 2)

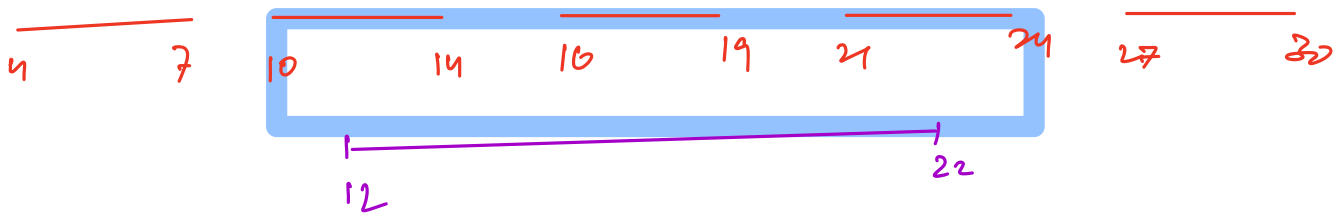
(3, 4)

(5, 6)

## Question 2

Given a list of non-overlapping intervals, sorted w.r.t start time. Insert a new interval in the sorted list s.t. final list is non-overlapping.

St = 4 10 16 24 27  
end = 7 14 19 24 30 } L = 12  
R = 22



output:

4 7  
10 24  
27 30

st = [ 4    10    16    21    27 ]

L = 25

end = [ 7    14    19    24    30 ]

R = 36

L - R

1. st(i) — end(i)    L - R  $\Rightarrow$  print(st(i), end(i))

2. L - R    st(i) — end(i)  $\Rightarrow$  print(L, R)  
print all  
future intervals

3. overlapping  $\Rightarrow$  merge

code

// L, R

for (i = 0 to n-1) {

if (end(i) < L) {  
    print(st(i), end(i))

}

else if (R < st(i)) {

    print(L, R)

    for (j = i to n-1) { print(st(j), end(j)) }

    return;

}

TC:  $O(N)$

SC:  $O(1)$

~~needed  
loop  $\Rightarrow$   
 $O(N^2)$~~

else {

$L = \min(L, st[i])$

$R = \max(R, end[i])$

}

}

print(L, R)

st = [ 4 ✓ 10 ✓ 16 ✓ 21 ✓ 27 ✓ ]

end = [ 7 14 19 24 30 ]

$L = 25$

$R = 36$

output: 4 7

10 14

16 19

21 24

25 26

27 30

st = [ 4 ✓ 10 ✓ 16 ✓ 21 ✓ 27 ✓ ]

end = [ 7 14 19 24 30 ]

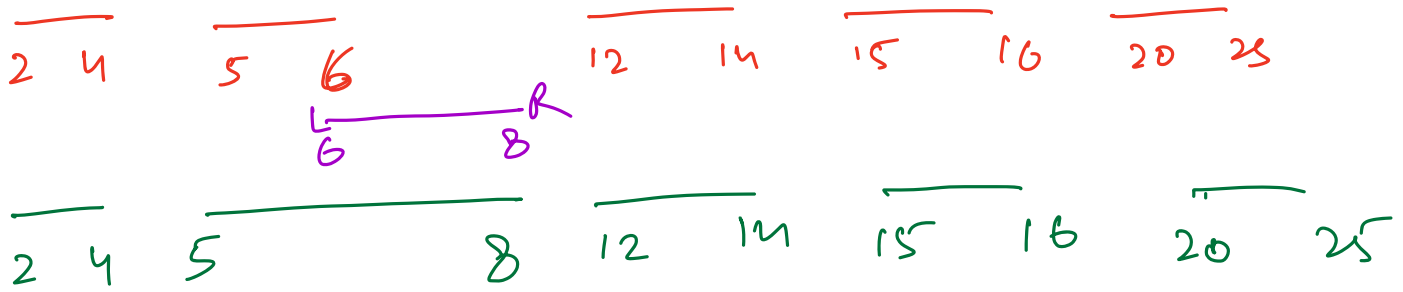
$L = 12$  10

$R = 22$  24

output: 4 7

10 24

27 30



### Question 3

Given an unsorted array of integers, find first missing natural no.  $\boxed{\geq 1}$

$$A = [3 \quad -2 \quad 1 \quad 7 \quad 2] \quad \text{am} = 4$$

$$A = [-8 \quad 7 \quad 2 \quad 5 \quad 3] \quad \text{am} = 1$$

$$A = [4 \quad 1 \quad 3 \quad 2] \quad \text{am} = 5$$

$$\min Am = 1 \quad \Rightarrow \quad 1 \leq am \leq N+1$$

$$\max Am = N+1$$

Brute force  $\rightarrow$  check no. from 1 to  $N+1$  if it is present in array

$$TC: O(N^2)$$

$$SC: O(1)$$

Use hashset  $\rightarrow$  insert all array in hashset & then  
check from 1 to  $N+1$

$TC: O(N)$

$SC: O(N)$

Sorting  $\rightarrow$   $TC: (N \log N) \times$

check if an element  $(x)$  is present in array?

$$1 \leq x \leq N+1$$

let  $x_i, a_i) = -ive$

$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 \\ 3 & 10 & 1 & 7 & 2 \\ \checkmark & \checkmark & \checkmark & \checkmark & \checkmark \\ -3 & -10 & -1 & & \end{bmatrix}$

$am = 4$

$am$  index

$1 \rightarrow 0$

$2 \rightarrow 1$

$\vdots$

$4 \rightarrow 3$

$\vdots$

$N \rightarrow N-1$

$N+1 \rightarrow$  not needed

if  $a_i) = -ive$

$\Rightarrow (i+1)$  is present in array

$A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ -1 & -2 & -3 \end{bmatrix}$



$$A = \begin{bmatrix} 1 & 3 & 10 & 1 \\ -3 & & & -1 \end{bmatrix}$$

$$ans = 2$$

$$A = [11, 12, 13, 17]$$

$$ans = 1$$

Code

```
for (i = 0 to n-1) {
    if (a[i] <= 0) ans = N+2
}
for (i = 0 to n-1) {
```

```
    x = abs(a[i])
```

```
    if (1 <= x && x <= n) {
```

```
        idx = x - 1
```

```
        if (a[idx] > 0)
```

```
            a[idx] *= -1
```

```
    }
```

```
}
```

```
for (i = 0 to n-1) {
```

```
    if (a[i] > 0)
```

```
        return i+1
```

```
}
```

```
return n+1
```

TC:  $O(N)$

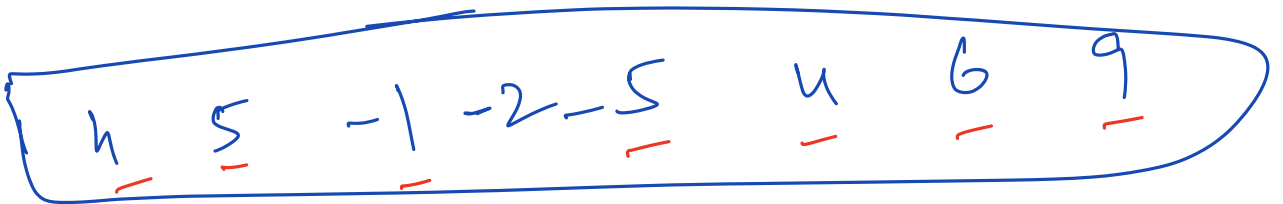
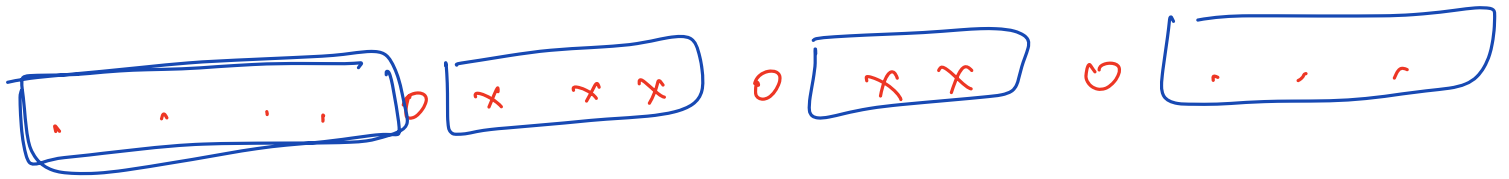
SL:  $O(1)$

if  $a[i] \leq 0 \Rightarrow a[i] = N+2$

$$a = [1 \quad -100^6 \quad 3 \quad 4]$$

$$N=4$$

Proof



$$8 \quad 7 \quad -2 \quad 5 \quad 6 \quad -2 \quad 7 \quad -5 \quad 10^5$$