

## Sorting 2: QuickSort & Comparator Problem

Agenda:

1. Sort 0-1 array
2. Pivot partition
3. QuickSort
4. Comparator problem

### Sort 0-1

Given an array of 0s & 1s in random order.

Sort the array [all 0s in left and all 1s in right]

$A = [0 \ 1 \ 0 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0]$

o/p:  $[0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1]$

Idea 1: use in-built sort  $\rightarrow TC = O(n \log n)$

Idea 2: use count sort

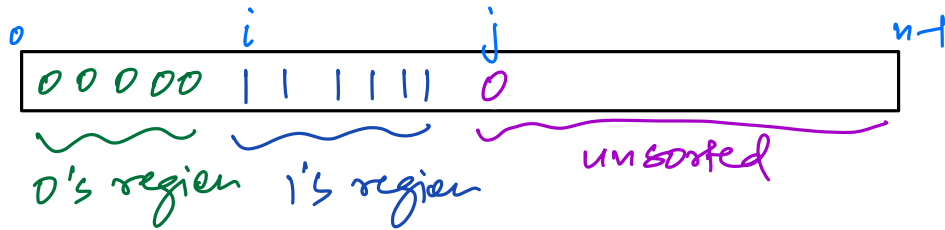
iterating  
2 times

$\rightarrow$  count all 0s & 1s and  
finally populate the array

$TC = O(N)$

$SC = O(1)$

Idea 3 : try to solve in single loop



0 to i-1 is 0's region

i to j-1 is 1's region

j to n-1 is unsorted

initially,  $i=0$   
 $j=0$

$A[j] == 1$	$A[j] == 0$
// increment region of 1 $j++$	// swap 0 in 0's region & increase 0's & 1's region $\text{swap}(A[i], A[j])$ $i++, j++$

Sort 01 (A), n {

$i=0, j=0$

while (j < n) {

if (A[j] == 1) {

$j++$

}

TC =  $O(N)$

SC =  $O(1)$

One iteration

```

    else {
        swap(A[i], A[j])
        i++, j++
    }
}
}

```

$\begin{matrix} j & j & j & j & j & j & j & j \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ i & i & i & i & i & i & & \end{matrix}$

↓

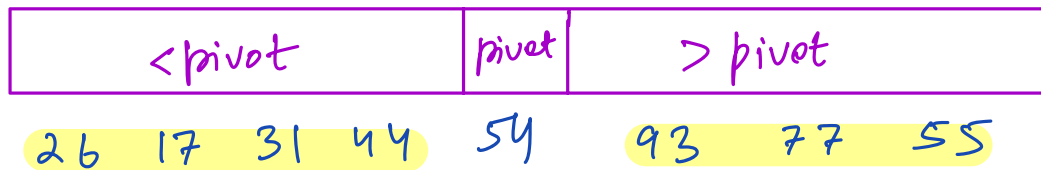
0 0 0 0 0 | 1 1 1 1

HW: sort 0's, 1's & 2's

## Partition

Given an array, consider first element as pivot,  
 rearrange array s.t. all elements  $<$  pivot are  
 on left side of pivot & rest are on right side  
 of pivot.

$A = [ \textcircled{54} \ 26 \ 93 \ 17 \ 77 \ 31 \ 44 \ 55 ]$   
 pivot



divide & conquer

Arrange smaller elements on left

index 0 to  $i$  , all elements are smaller than pivot

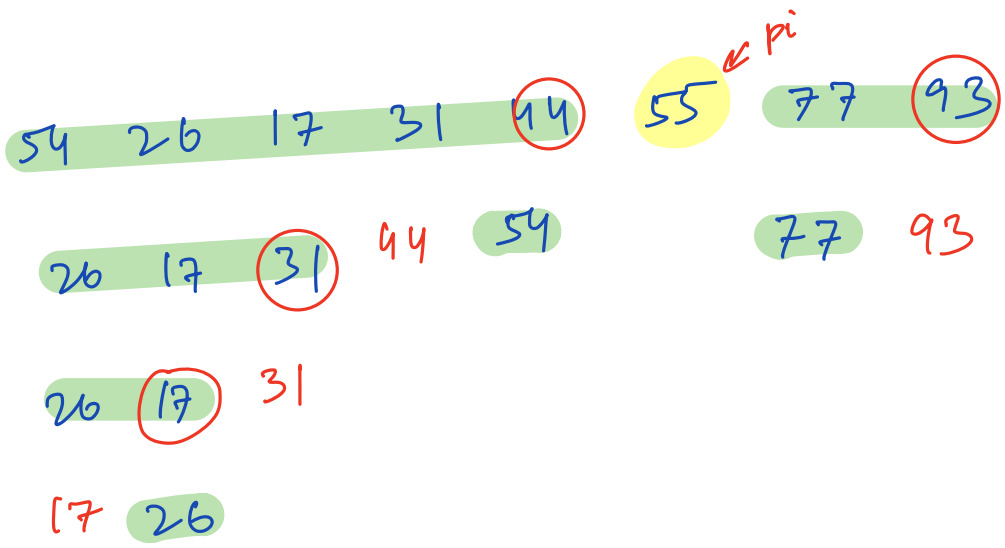
```

int partition (A, l, r) {
    pivot = A[r] // random
    i = l - 1 // 0-i elements < pivot
    for (j = l to (r-1)) {
        if (A[j] < pivot) {
            i++
            swap (A[i], A[j])
        }
    }
    swap (A[i+1], A[r])
    return i+1
}
  
```

$TC = O(N)$

$SC = O(1)$

$A = [54, 26, 93, 17, 77, 31, 55, 44, 77, 93]$   
 $l=0, r=7$   
 $i=7, j=0, i=1, i=2, i=3, i=4$



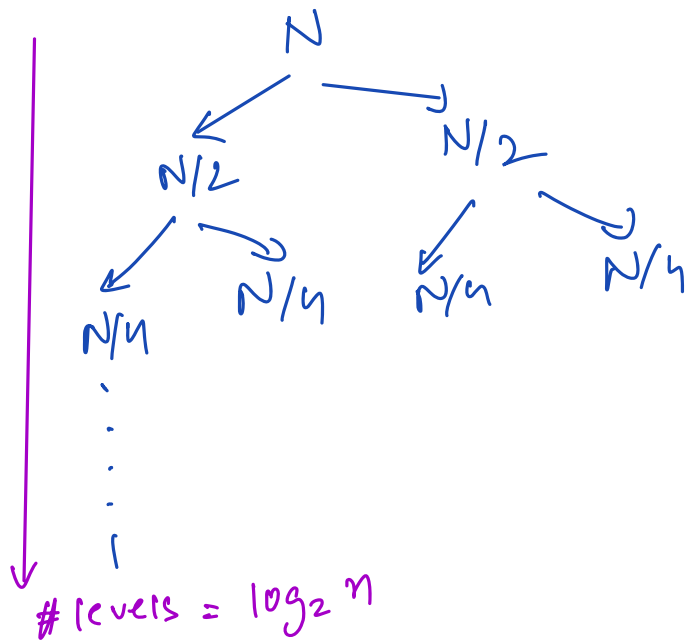
17 26 31 44 54 55 77 77 93 93

```

void quickSort (A, l, r) {
    if (l < r) {
        pi = partition (A, l, r);
        quickSort (A, l, pi-1);
        quickSort (A, pi+1, r);
    }
}
  
```

3 3

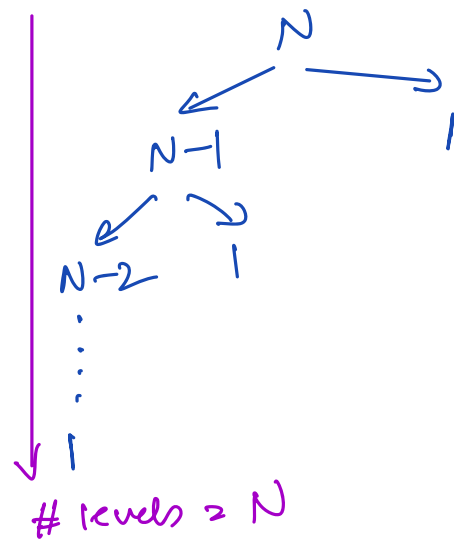
### Best Case



$$TC = O(N \log N)$$

$$SC = O(\log N)$$

### Worst Case



$$TC = O(N^2)$$

$$SC = O(N)$$

### Randomized Quick Sort

Always choose pivot element at random.

Given  $N$  elements, probability of random element being minimum =  $1/N$

Again, probability of minimum element =  $1/(N-1)$   
:  
 $1/(N-2)$   
:

$$\frac{1}{N} \times \frac{1}{N-1} \times \frac{1}{N-2} \times \dots = \frac{1}{N!}$$

$$N=10, \quad \frac{1}{10!} = ? \quad 2.7 \times 10^{-7} \approx 0$$

Hence, on average TC of quickSort =  $O(N \log N)$

### Comparator

int compare (first, second) { Java, Py, JS, C#, Ruby

return {  
     → -ive ⇒ first should come before second  
     → 0    ⇒ both are equal  
     → +ive ⇒ first should come after second

}

eg → sort in ascending ⇒ return (first - second)  
       descending ⇒ return (second - first)

bool compare (first, second) { C++

return {  
     → true    ⇒ first should come before second  
     → false   ⇒ first should come after second

}

## Question

Given an integer array, sort the data w.r.t count of factors. If factors are same, sort based on magnitude.

$A = [9, 3, 10, 16, 4]$

#factors  $\rightarrow 3, 2, 4, 5, 3$

sorted  $\rightarrow 3, 4, 9, 10, 16$

## Java

```
Collections.sort(A, new Comparator<Integer>() {
```

```
    @Override
```

```
    public int compare(Integer f, Integer s) {
```

```
        if (factors(f) == factors(s)) {
```

```
            return f - s;
```

```
        }
```

```
        else {
```

```
            return factors(f) - factors(s);
```

```
        }
```

```
    }
```

```
}
```



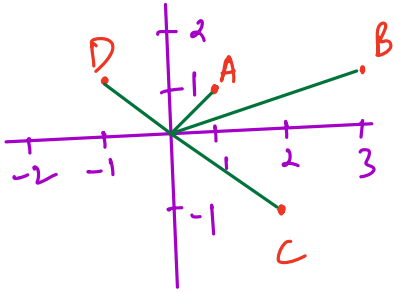
## Question

Given an array of points in 2D-plane,  $p_i = (x_i, y_i)$

Return  $K$  closest points to origin  $(0,0)$ .

$K=2$

o/p  $\rightarrow (1,1) (-1,1)$



compare  $\rightarrow (x_1, y_1) \quad (x_2, y_2)$

distance from origin =  $\sqrt{x^2 + y^2}$

compare  $\rightarrow \sqrt{x_1^2 + y_1^2} \quad \sqrt{x_2^2 + y_2^2}$

compare  $\rightarrow (x_1^2 + y_1^2) \quad (x_2^2 + y_2^2)$

int compare ( f, s ) {

return  $(f.x^2 + f.y^2) - (s.x^2 + s.y^2)$

}

## Question

Given an array of non-negative integers, arrange them so that we get largest no. & return it.

$$A = [2, 5, 7]$$

$$\text{ans} = "752"$$

$$A = [10, 2] \xrightarrow[\text{in desc}]{\text{sort}} "102"$$

$$\text{ans} = "210"$$

$$A = [3, 30, 34, 5, 9] \xrightarrow[\text{in desc}]{\text{sort}} "3430953"$$

$$\text{ans} = "9534330"$$

let's use custom sorting

```
int compare (int f, int s) {
```

```
    s1 = string(f) + string(s)
```

```
    s2 = string(s) + string(f)
```

```
    if (s1 > s2)
```

```
        return -1
```

```
    else return 1
```

3

A = [3, 30, 34, 5, 9]

sorted = [9, 5, 34, 3, 30]

↓ create string

ans = "9534330"

Python

A = sorted(A, key = functools.cmp\_to\_key(compare))

```
def compare(f, s):  
    return f - s
```