

# Digital Assignment-0

Course Name: Engineering Physics

Course Code: 5310

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Date of Submission: 8th January 2025

Q1) Length of rope = 5m, weight of rope = 1.45gm  
Frequency = 120 Hz, wavelength = 60 cm =  $1.45 \times 10^{-3}$  Kg  
= 0.6m  
Tension = ??, mass = ??

Ans) We know that,

$$v = f \lambda$$

$$v = 120 \times 0.6 \text{ m/sec}$$

$$v = 72 \text{ m/s}$$

We also know that,

$$\mu = \frac{\text{mass of rope}}{\text{length of rope}} = \frac{1.45 \times 10^{-3}}{5}$$

$$\mu = 2.9 \times 10^{-4} \text{ Kg/m}$$

We know that,

$$v = \sqrt{\frac{F_T}{\mu}}$$

$$v^2 = \frac{F_T}{\mu}$$

$$F_T = v^2 \mu$$

$$F_T = (72)^2 \times (2.9 \times 10^{-4})$$

$$F_T = 1.503 \text{ N}$$

Mass required to produce tension is given by:

$$F_T = mg$$

$$m = \frac{F_T}{g}$$

$$\{g = 9.8 \text{ m/s}^2\}$$

$$m = \frac{1.503}{9.8}$$

$$m = 0.153 \text{ Kg}$$

\* Tension in the rope is 1.503 N.

\* Mass to produce tension is 0.153 Kg.

Q2) Tension in string = 88.2 N, Mass of string = 500 gm  
Length of string = 50 cm = 0.5 m  $= 0.5 \times 10^{-3} \text{ kg}$

a) Wave Speed

b) Fundamental Frequency

c) First & Second overtones

Ans)

Mass density of rope:

$$\mu = \frac{\text{mass of rope}}{\text{length of rope}}$$

$$\mu = \frac{0.5 \times 10^{-3}}{0.5} = 1 \times 10^{-3} \text{ Kg/m}$$

$$\mu = 1 \times 10^{-3} \text{ Kg/m}$$

We know,

$$v = \sqrt{\frac{F_T}{\mu}}$$

$$= \sqrt{\frac{88.2}{10^{-3}}}$$

$$v = 297.153 \text{ m/s}$$

Fundamental Frequency:

$$f_1 = \frac{v}{2L}$$

$$f_1 = \frac{297.153}{2 \times 0.5}$$

$$f_1 = 297.153 \text{ Hz}$$

Overtone

i) First Overtone:

$$f_2 = 2f_1$$

$$f_2 = 594.306 \text{ Hz}$$

ii) Second Overtone:

$$f_3 = 3f_1$$

$$f_3 = 891.459 \text{ Hz}$$

$$2.97 \times 10^3 \text{ Hz} = v$$

Q3) Length of string = 30 cm, Fundamental Frequency = 256 Hz

Length of string = 80 cm, mass = 0.75 g

Tension in string = ?

(ms)

Linear mass density:

$$\mu = \frac{\text{mass}}{\text{length}} = \frac{0.00075}{0.8}$$

$$\mu = 9.375 \times 10^{-4}$$

Wave Speed:

$$v = 2Lf$$

$$v = 2 \times 0.8 \times 256$$

$$v = 153.6 \text{ m/s}$$

We know,

$$v = \sqrt{\frac{F_T}{\mu}}$$

$$v^2 = \frac{F_T}{\mu}$$

$$F_T = v^2 \mu = (153.6)^2 \times 9.375 \times 10^{-4}$$

$$F_T = 22.1 \text{ N}$$

Q4) Fundamental Frequency = 196 Hz  
Where should finger be placed to make it 440 Hz.

Ans) We know that,

$$f \propto \frac{1}{L}$$

$$\frac{f_1}{f_2} = \frac{L_2}{L_1}$$

Ratio of frequency

$$\frac{440}{196} = \frac{L_1}{L_2}$$

$$L_2 = \frac{L_1}{2.2449}$$

Let say total length of string be  $L_1$  & the vibrating portion be  $L_2$

$$d = L_1 - L_2$$

$$d = L_1 - \frac{L_1}{2.2449}$$

$$d = L_1 (1 - 0.4456)$$

$$d = 0.5544 L_1$$

So, the finger should be placed at approx. 55.44% of the string's length from it's original length.

Mass = 2 Kg, Height of mine = 80 m, Mass of shaft = 20 Kg

a) Speed of wave

b) No. of wavelengths if  $f = 2 \text{ Hz}$  &  $L = 80 \text{ m}$ .

Ans)

We know that  $v = \sqrt{\frac{F_T}{\mu}}$

$$\mu = \frac{\text{mass of rope}}{\text{length of rope}} = \frac{2}{80}$$

$$\mu = 0.025 \text{ Kg/m}$$

$$F_T = m \cdot g$$

$$= 20 \times 9.8$$

$$F_T = 196 \text{ N}$$

$$v = \sqrt{\frac{F}{\mu}}$$

$$= \sqrt{\frac{196}{0.025}}$$

$$v = 88.5 \text{ m/s}$$

We know,

$$v = f\lambda$$

$$\lambda = \frac{v}{f} = \frac{88.5}{44.25} = 2 \text{ m}$$

$$n = \frac{2L}{\lambda}$$

$$n = \frac{80 \times 2}{44.25} \approx 3.6$$

So full wavelength is 3

$$y(x, t) = (2.75 \text{ cm}) \cos(0.410 \text{ rad/cm} \cdot x + 6.20 \text{ rad/s} \cdot t)$$

a) Time & Horizontal distance

b) Wave number & no. of waves

c) Wave Speed & max. Speed of cork

$$A = 2.75 \text{ cm} = 2.75 \times 10^{-2} \text{ m}$$

$$k = 0.410, \omega = 6.20$$

$$T = \frac{2\pi}{\omega}$$

$$T = \frac{2\pi}{6.20} = 1.01 \text{ s}$$

$$T = 1.01 \text{ sec}$$

$$v = \frac{\omega}{k}$$

$$v = \frac{6.20}{0.410}$$

$$v = 15.12 \text{ m/s}$$



$$\text{Distance} = v \cdot T$$

$$= 0.151 \cdot 1.01$$

$$\boxed{\text{Distance} = 0.153 \text{ m}}$$

Wave number:

$$k = 0.410 \text{ rad/cm} = 41.0 \text{ rad/m}$$

$$= 41.0 \text{ rad/m}$$

Frequency:

$$f = \frac{1}{T}$$

$$f = \frac{1}{1.01} = 0.99 = \frac{1}{1.01} \text{ Hz}$$

$$\boxed{f = 0.99 \text{ Hz}}$$

Wave speed:

Calculated carrier:

$$\boxed{v = 0.151 \text{ m/s}}$$

Maximum speed of cork

$$v_{\text{max}} = \omega \cdot A$$

$$v_{\text{max}} = 6.28 \times 0.0275$$

$$\boxed{v_{\text{max}} = 0.171 \text{ m/s}}$$

Q7)

Given eq<sup>n</sup>

$$y(x,t) = A \cos \left[ \omega \left( \frac{x}{v} - t \right) \right]$$

We know,

$$\omega = 2\pi f, \quad k = \frac{2\pi}{\lambda}, \quad v = f\lambda, \quad f = \frac{v}{\lambda}$$

$$= \omega \left( \frac{x}{v} - t \right)$$

$$= 2\pi f \left( \frac{x}{v} - t \right)$$

$$= 2\pi \left( \frac{v}{\lambda} \right) \left( \frac{x}{v} - t \right)$$

$$= 2\pi \left( \frac{x}{\lambda} - \frac{vt}{\lambda} \right)$$

$$= 2\pi \frac{x - vt}{\lambda}$$

$$y(x,t) = A \cos\left(2\pi \frac{x-vt}{\lambda}\right)$$

b)

Velocity of wave:

$$v_y = \frac{dy}{dt}$$

$$\frac{d}{dt} \left( A \cos\left(\frac{2\pi}{\lambda} x - \omega t\right) \right)$$

$$v_y = -A \omega \sin\left(\frac{2\pi}{\lambda} x - \omega t\right)$$

$$v_y = A \omega \sin\left(\frac{2\pi}{\lambda} x - \omega t\right)$$

c)

Maximum speed of a particle:

$$v_{\max} = A \omega$$

$$v = \frac{\omega}{k}, \quad k = \frac{2\pi}{\lambda}$$

$$A \omega = \frac{\omega \lambda}{2\pi}$$

$$A = \frac{\lambda}{2\pi}$$

Here,

we can conclude that

$$A \propto \lambda$$

If

$A \uparrow$  so,  $\lambda \uparrow$

When  $v_{\max}$  is less than  $v$

$$A \omega < \frac{\omega}{k}$$

$$A < \frac{1}{k} = \frac{\lambda}{2\pi}$$

$$A < \frac{\lambda}{2\pi}$$

So,  $v_{\max}$  is less than  $v$  when  $A < \frac{\lambda}{2\pi}$

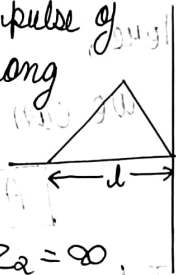
Similarly,

Yes it can exceed when

$v_{\max}$  is greater than  $v$  when  $A > \frac{\lambda}{2\pi}$

08)

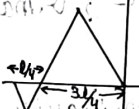
Consider a triangle pulse of length  $l$  traveling along a string at a fixed end, with a reflection coefficient  $Z_2 = \infty$ .



Some points that can be drawn are:

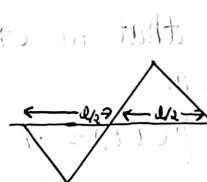
- 1) Wave moves in a triangular shape towards the fixed end.
- 2) It has reflection coefficient  $Z_2 = \infty$ , which means that the wave ~~is~~ will be reflected completely.
- a)  $1/4$  of the pulse is reflected

This means that  $1/4$  of the wave is inverted & the rest  $3/4$  is still moving without being inverted



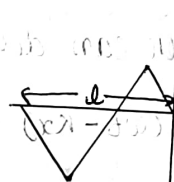
b)  $1/2$  of pulse is reflected

Half of the wave is reflected backwards while the other half still moves towards the fixed end.

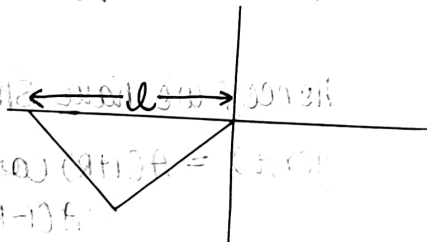


c)  $3/4$  of pulse is reflected

This means that  $3/4$  of the wave is reflected backwards while the other  $1/4$  still moves towards the fixed end



d) when entire pulse is reflected  
The entire pulse is inverted or reflected backwards.





Q9) Displacement of a wave is given as

$$y(x,t) = A \cos(\omega t - kx) + R A \cos(\omega t)$$

1) Show that it can be expressed in the form

$$y(x,t) = A(1+R) \cos \omega t \cos kx + A(1-R) \sin \omega t \sin kx$$

We know that,

$$\cos(a+b) = \cos a \cos b - \sin a \sin b$$

$$\cos(a-b) = \cos a \cos b + \sin a \sin b$$

So, we can derive that,

$$= A \cos(\omega t - kx) = A(\cos \omega t \cos kx) + A(\sin \omega t \sin kx)$$

$$= AR(\cos \omega t \cos kx) - AR(\sin \omega t \sin kx)$$

$$= (\cos \omega t \cos kx)(A(1+R)) + (\sin \omega t \sin kx)(A(1-R))$$

Hence, we have shown that,

$$y(x,t) = A(1+R) \cos \omega t \cos kx + A(1-R) \sin \omega t \sin kx$$

2) Verify that it satisfies the wave equation:

$$\frac{\partial^2 y}{\partial t^2} = v^2 \frac{\partial^2 y}{\partial x^2}$$

Given,

$$y(x,t) = A(1+R) \cos \omega t \cos kx + A(1-R) \sin \omega t \sin kx$$

$$y(x,t) = A(1+R) \cos \omega t \cos kx + A(1-R) \sin \omega t \sin kx$$

$$\frac{\partial y}{\partial t} = -A(1+R) \omega \sin \omega t \cos kx + A(1-R) \omega \cos \omega t \sin kx$$

$$\frac{\partial^2 y}{\partial t^2} = -A(1+R) \omega^2 \cos \omega t \cos kx - A(1-R) \omega^2 \sin \omega t \sin kx$$

$$\frac{\partial^2 y}{\partial t^2} = -\omega^2 [A(1+R) \cos(\omega t) \cos(kx) + A(1-R) \sin(\omega t) \sin(kx)]$$

$$y(x,t) = A(1+R) \cos \omega t \cos kx + A(1-R) \sin \omega t \sin kx$$

$$\frac{\partial y}{\partial x} = -A(1+R) k \cos \omega t \sin kx + A(1-R) k \sin \omega t \cos kx$$

$$\frac{\partial^2 y}{\partial x^2} = -A(1+R) k^2 \cos(\omega t) \cos(kx) - A(1-R) k^2 \sin(\omega t) \sin(kx)$$

$$\frac{\partial^2 y}{\partial x^2} = -k^2 [A(1+R) \cos \omega t \cos kx + A(1-R) \sin \omega t \sin kx]$$

$$\frac{\partial^2 y}{\partial t^2} = \frac{+ \omega^2}{+ k^2} \frac{\partial^2 y}{\partial x^2}$$

$$\boxed{\frac{\partial^2 y}{\partial t^2} = v^2 \frac{\partial^2 y}{\partial x^2}}$$

Hence, the wave equation is satisfied.

Q10) Given there are two strings connected to one another. The density of string 2 is 4 times that of string 1.

Given,

$$y_{\text{incident}} = A_i \cos(k_1 x - \omega t)$$

$$y_{\text{reflected}} = A_r \cos(-k_1 x - \omega t)$$

$$y_{\text{ref}} = A_r \cos(k_1 x + \omega t)$$

Given,

$$y_{\text{trans}} = A_t \cos(k_2 x - \omega t)$$

where,

$$k_2 = \frac{\omega_1}{v_2}, v_2 = \sqrt{\frac{T}{\mu_2}}$$

Given,

$$\mu_2 = 4\mu_1 \Rightarrow v_2 = \frac{v_1}{2}, k_2 = 2k_1$$

$$\boxed{y_{\text{transmitted}} = A_t \cos(2k_1 x - \omega t)}$$

Reflection & Transmission Co-efficients

We know,

$$y_{\text{incident}} + y_{\text{reflected}} = y_{\text{transmitted}}$$

$$R = \frac{A_r}{A_i}$$

$$T = \frac{A_t}{A_i}$$

We know that,

$$1 + R = T$$

$$\phi \quad 1 - R = \frac{T}{2}$$

Solving:

$$R = \frac{1-2}{1+2} = -\frac{1}{3}, T = \frac{2}{3}$$

Also,

$$R = -\frac{1}{3}$$

$$T = \frac{2}{3}$$

Here, we can conclude that,

- Since,  $R = -\frac{1}{3}$  indicates that the reflected wave has an inverted amplitude due to denser medium in string 2.
- Since,  $T = \frac{2}{3}$  means that two-thirds of the wave's amplitude is transmitted into string 2. The reduction occurs for the energy sharing b/w reflected & transmitted waves.

$$\frac{T}{R} = 2 - 1$$

: parallel

$$\frac{2}{3} = T \quad \frac{1}{3} = \frac{2-1}{2+1} = \frac{1}{3}$$