HW #1

1. Prove that  $\sqrt{3}$  is irrational.

Bonus (not required): prove that for all primes  $p \ge 2$ ,  $\sqrt{p}$  is irrational (among other things, this shows us that there exist an infinite number of irrational numbers, due to the infinitude of primes)

2. Recall that the power set of a set  $\Lambda$  is the set of all subsets (not necessarily proper) of  $\Lambda$ .

Prove using induction, that for any finite set A with |A| = n,  $|P(A)| = 2^n \forall n \ge 1$ , where P(A) denotes the power set of A.

First:

Son care: 
$$N=0$$

A. [i],  $P(A) = [0] = 2^{\circ} - 1$ 

Ind Step:  $pron P(K) \rightarrow P(K^{H})$ 

Assum  $P(K) + 2^{K} = 2^{K} = 2^{K}$ 
 $= 2 \cdot 2^{K}$ 
 $= 2 \cdot 2^{K}$