

## Problem set 2

July 14th, 2011  
due July 19th, 2011

### Question 1

Consider changing the units of measurement for observations in a dataset. This is equivalent to multiplying each observation on a given variable by a constant scaling parameter. (Refer to chapter 2.4 for help if needed.)

- Let  $\hat{\beta}_0$  and  $\hat{\beta}_1$  be the intercept and slope coefficient from the regression of  $y_i$  on  $x_i$ . Let  $\tilde{\beta}_0$  and  $\tilde{\beta}_1$  be the intercept and slope coefficient from the regression of  $c_1 y_i$  on  $c_2 x_i$ , where  $c_1$  and  $c_2$  are non-zero constants. Express  $\tilde{\beta}_0$  and  $\tilde{\beta}_1$  as functions of  $\hat{\beta}_0$ ,  $\hat{\beta}_1$ ,  $c_1$  and  $c_2$ .
- Let  $\hat{\alpha}_0$  and  $\hat{\alpha}_1$  be the intercept and slope coefficient from the regression of  $\ln(y_i)$  on  $\ln(x_i)$ . Let  $\tilde{\alpha}_0$  and  $\tilde{\alpha}_1$  be the intercept and slope coefficient from the regression of  $\ln(c_1 y_i)$  on  $\ln(c_2 x_i)$ , where  $c_1$  and  $c_2$  are non-zero constants. Express  $\tilde{\alpha}_0$  and  $\tilde{\alpha}_1$  as functions of  $\hat{\alpha}_0$ ,  $\hat{\alpha}_1$ ,  $c_1$  and  $c_2$ .

### Question 2

Consider the following econometric model relating the birth weight (in ounces) of babies in the US to the cigarettes consumption of the mother:

$$bweight_i = \beta_0 + \beta_1 cigs_i + \epsilon_i$$

To estimate the model, infant birth weight (*bweight*) is regressed on the average number of cigarettes the mother smoked per day during pregnancy (*cigs*). The following estimates are obtained:

$$\hat{\beta}_0 = 119.77$$

$$\hat{\beta}_1 = -0.514$$

- what is the interpretation of  $\hat{\beta}_1$ ?
- what is the interpretation of  $\hat{\beta}_0$ ? Does it make sense in this example?
- if one mom smoked on average 10 cigarettes more per day than the other mom, what would you predict the babies weight difference to be?
- you found out about the babies from the previous point that one baby is 3 ounces heavier than the other. What does this imply for previous point?
- is the ceteris paribus condition satisfied here? what does your answer imply for unbiasedness of applied estimator?

### Question 3

Consider the following simple regression model:

$$y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$

The Zero Conditional Mean assumption holds, and it is known that the error term has a standard normal distribution. The sample size is 100 and the  $x$ 's have variance equal to 16 in the sample. What is the variance of the estimator  $\hat{\beta}_1$ ?

### Question 4

Answer this question using STATA and the data set WAGE1.dta (N=526). The variables of interest are *hourly wage* ( $w_i$ ) and *education* ( $s_i$ ). Attach the Do-File and the output log from your work using Stata. Consider the following equation:

$$w_i = \beta_0 + \beta_1 s_i + \epsilon_i$$

- find the OLS estimates of  $\beta_0$  and  $\beta_1$
- state and verify the first two algebraic properties of the OLS estimator (consult the class notes)
- report the  $R^2$  and comment on the value obtained
- now do the same for the following model:

$$\ln(w_i) = \alpha_0 + \alpha_1 s_i + \epsilon_i$$

compare the estimates of  $\alpha$ 's with the estimates of  $\beta$ 's and comment on the difference.

### Question 5

Sample variances of  $x$  are usually calculated by dividing the sum of  $x$  minus  $\bar{x}$  squared by  $(n-1)$  which "corrects for degrees of freedom". What does this correctness accomplish?