Test

1) M=[-6,0) U{ 1 (m ell, m7/1) B) a) M - Enchisa (=) M = M M=MOM' M'=[-6,0] pt. & XEM, Fo vicinitate pt. fiecale x a.c. si contina o infinitate de proste pt- punctele de folma { In EN, n 71 } me exista meio recinatale de acest fel pt. {0} pot alege vice recinatale interest la larga lu re garere o infinitale de puncle => M'2 [-6,0] M Z MUM' Z MUGOY M + M (=) M nu e multime inchis

B) M = (-6,0)Pp. pin reducere la absurd cà $M = \{-6\} \cup \{\frac{1}{m+1} \mid n \in \mathbb{N}, m \neq 1\}$ $Z = S + X \in M$, $\exists 1, 0 = 0$ a.c. $(X - 1, X + 1) \in M$ Fals pt. cà un interval de forma (X - 1) non poote fi

inclus intro multipline de punete. $\exists M = (-6,0)$

C) M'=[-6,0]

Pp. prin reducere la abouted ce M'={m+1 (m+N, m71)}

Lyther, Flyo a.c.

(x-1, x+1) si ailie o infinitate de elem. din M

Fals pt. cei txeM' mu are an mu pot sie ian vec

recinatate care sa contine prinche din M

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d) Fie A = IR mult deschisa =) A = A

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compata

2)
$$f:(-5,5) \to \mathbb{R}$$

 $f(x) = \int_{x-c}^{x^2-1} \int_{x-c}^{x} x \in (-5,0)$

Verfice cont. In
$$x=0$$

$$f(c) = \lim_{x \to 0} x^{2} - \frac{1}{5} = -\frac{1}{5} \left(\frac{1}{5} \right) = \frac{1}{5} \left(\frac{1}{5$$

$$f'(x) = \begin{cases} 2x, x \in (-5, 0] \\ -\frac{1}{(x-5)^2} + 1, x \in (0, 5) \end{cases}$$

 $= \lim_{\substack{x \to 0 \\ x > 0}} \frac{1+x^2-5x}{x-5} + \frac{1}{5} = \lim_{\substack{x \to 0 \\ x > 0}} \frac{5x^2-25x+5+x-5}{5x^2-25x} = \frac{1}{5}$ $= \lim_{\substack{x \to 0 \\ x \to 0}} \frac{5x^2 - 24x}{5x^2 - 25x} \lim_{\substack{x \to 0 \\ x \to 0}} \frac{5x - 24}{5x - 25} = 4\frac{24}{25}$ 2'3(0) + f'd(0) => f deirabete pe (-5, 5) 160 y of derivabile pe (-5,0) f deviable pe (-5,0)

{1 (x) = 2x => £1(x) ∈ (-10,0) marginit (->) £ unif. cont. pe(-5,0) & deivable pe (0,5) £((x)=-1 +1 -15-12 co (+1 = 0 6 2 6 6 61 2'(b) 6(9,1) marginitar (7 f este lipschito pe (5,0)

f dwalder pe (9,5)

s f unif. cont. pe (0,5) => fe wif-cont-pe (5,0) U(0,5)