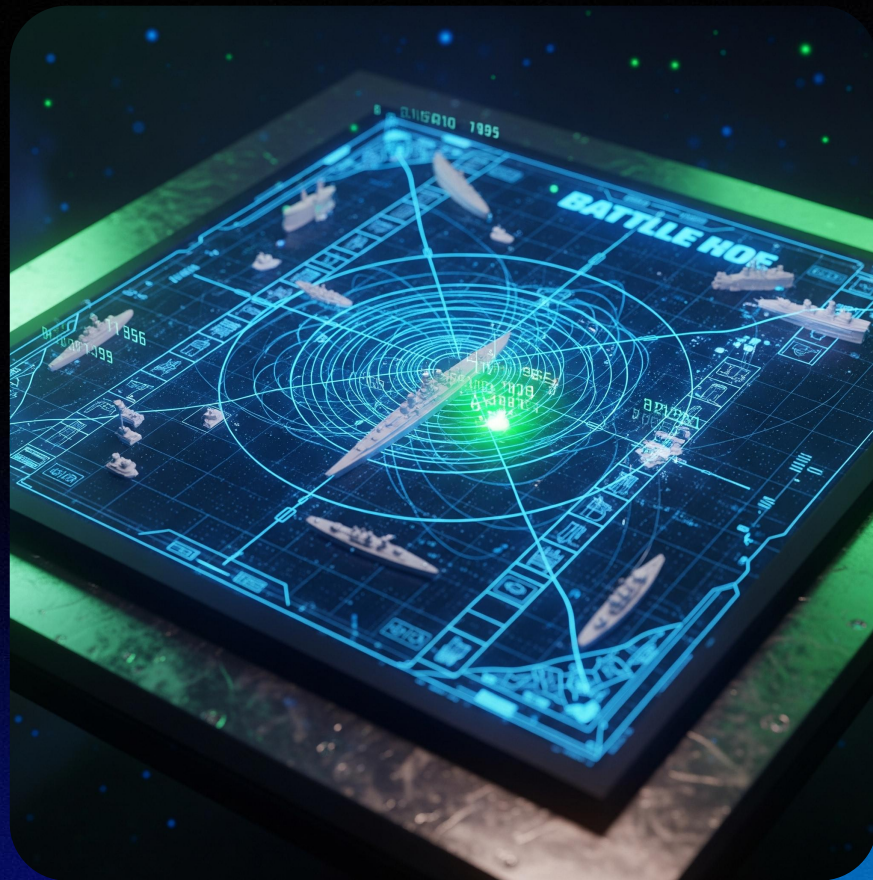


# Quantum Radar: Concept & Problem

- In classical Battleship, you must probe every single square until you find all ships. This is inefficient. A "miss" gives you some information, but a "hit" is the only way to find a ship.
- We use a quantum circuit to perform an "interaction-free" measurement on an entire row or column at once.
- Our "Quantum Guess": Instead of asking, "Is there a ship at (1, 2)?", we ask, "Is there any ship in Row 1?"
- The Goal: Maximize our E.V. (Elitzur-Vaidman) Score, which we define as finding all ships with the fewest number of classical "HITS".



# Quantum Circuit

Our "Quantum Radar" circuit is based on the same principle as Grover's search algorithm, which is a powerful tool for detecting a "marked" item in a list.

## H-Gates (Superposition):

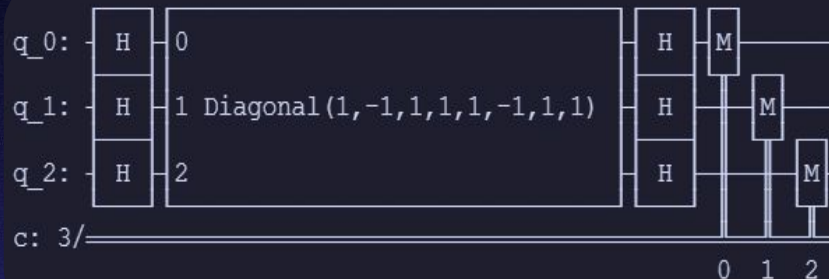
We use Hadamard (H) gates on  $n$  qubits (where  $2^n > \text{row length}$ ) to create a uniform superposition of all  $2^n$  possible squares in that line. Our "quantum light" is now checking all paths simultaneously.

## The Oracle (The "Bomb"):

This is a custom Diagonal gate. It "marks" any state corresponding to a ship's location by flipping its phase (multiplying it by  $-1$ ). This is our "interaction." Crucially, it doesn't measure or collapse the state, it just "tags" it.

## H-Gates (Interference):

We apply H gates again. This causes all the quantum states to interfere. If no ship was present: The Oracle did nothing. The second H gates perfectly reverse the first H gates ( $H \cdot CDOT \cdot H = I$ ). The state returns to  $|00\dots 0\rangle$ . If a ship was present: The phase-flipped state(s) now interfere destructively with the others. The final state will not be  $|00\dots 0\rangle$ .



## The Three Outcomes:

- **Measure  $|00\dots\rangle$  "MISS":** Constructive interference succeeded. We are 100% certain no ship is in that line.
- **Measure anything else "DETECT":** Destructive interference occurred. We are 100% certain a ship is present, but we don't know which square it's in. This is the "interaction-free" detection!
- **"HIT":** This is not an outcome of our quantum circuit. A "HIT" is a classical action we take after the quantum scan, which counts against our E.V. Score.



# Game Strategy & E.V. Score

## Quantum Scanning (No "Hits")

- We run our quantum\_scan\_line circuit on all rows.
- Any row that returns "MISS" is marked as 'O' (safe).
- We then run our quantum\_scan\_line circuit on all columns.
- Any column that returns "MISS" is marked as 'O' (safe).

## Classical Pinpointing (The "Hits")

- After Phase 1, our board is narrowed down. We identify a small list of candidate squares.
- A square (r, c) is a candidate only if Row r returned "DETECT" and Column c returned "DETECT".
- We now loop through only this small candidate list and perform a classical probe (a "HIT").
- Each probe increments our Total Hits then we use  $\text{Total Hits} / \text{Total points} = \text{E.V. Score}$ .

## Result

As the demo shows, for a 8x8 board, we can find all ships with just a few hits (e.g., 16) instead of the 64 (worst-case) or ~32 (average) classical probes. We successfully used quantum interference to find ships without "touching" them.

