
EXTENDS *MQTTBase*

MODULE *Client*

$ReqConnect(self) \triangleq$
 $\wedge pc[self] = \text{"start"}$
 $\wedge \exists m \in msgs :$
 $\wedge m.from = self$
 $\wedge m.to = broker$
 $\wedge m.type = CONNECT$
 $\wedge m.payload.clientId = self$
 $\wedge canSendTo(broker)$
 $\wedge network' = send(m, broker)$
 $\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connecting"}]$
 $\wedge \text{UNCHANGED } active$
 $\wedge \text{UNCHANGED } topic_subscribers$
 $\wedge \text{UNCHANGED } store$
 $\wedge \text{UNCHANGED } used_num$

$RcvConnectRes(self) \triangleq$
 $\wedge pc[self] = \text{"connecting"}$
 $\wedge Len(network[self]) > 0$
 $\wedge \text{LET } m \triangleq Head(network[self]) \text{ IN}$
 $\wedge m.from = broker$
 $\wedge m.to = self$
 $\wedge m.type = CONACK$
 $\wedge network' = rcv(m, self)$
 $\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connected"}]$
 $\wedge \text{UNCHANGED } active$
 $\wedge \text{UNCHANGED } topic_subscribers$
 $\wedge \text{UNCHANGED } store$
 $\wedge \text{UNCHANGED } used_num$

$ReqPing(self) \triangleq$
 $\wedge pc[self] = \text{"connected"}$
 $\wedge \exists m \in msgs :$
 $\wedge m.from = self$
 $\wedge m.to = broker$
 $\wedge m.type = PINGREQ$
 $\wedge canSendTo(broker)$
 $\wedge network' = send(m, broker)$
 $\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"ping"}]$
 $\wedge \text{UNCHANGED } active$
 $\wedge \text{UNCHANGED } topic_subscribers$
 $\wedge \text{UNCHANGED } store$
 $\wedge \text{UNCHANGED } used_num$

$$\begin{aligned}
RcvPingRes(self) &\triangleq \\
&\wedge pc[self] = \text{"ping"} \\
&\wedge Len(network[self]) > 0 \\
&\wedge LET \ m \triangleq Head(network[self]) IN \\
&\quad \wedge m.from = broker \\
&\quad \wedge m.to = self \\
&\quad \wedge m.type = PINGRESP \\
&\quad \wedge network' = rcv(m, self) \\
&\quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connected"}] \\
&\wedge UNCHANGED \ active \\
&\wedge UNCHANGED \ topic_subscribers \\
&\wedge UNCHANGED \ store \\
&\wedge UNCHANGED \ used_num
\end{aligned}$$

$$\begin{aligned}
ReqPublishWithQoS0(self) &\triangleq \\
&\wedge pc[self] = \text{"connected"} \\
&\wedge store[self] \neq \{\} \\
&\wedge \exists m \in msgs : \\
&\quad \wedge m.from = self \\
&\quad \wedge m.to = broker \\
&\quad \wedge m.type = PUBLISH \\
&\quad \wedge m.qos = 0 \\
&\quad \wedge m.packetID \notin used_num \\
&\quad \wedge canSendTo(broker) \\
&\quad \wedge network' = send(m, broker) \\
&\quad \wedge store' = [store \text{ EXCEPT } ![self] = @ \setminus \{m.packetID\}] \\
&\quad \wedge used_num' = used_num \cup \{m.packetID\} \\
&\wedge UNCHANGED \ pc \\
&\wedge UNCHANGED \ active \\
&\wedge UNCHANGED \ topic_subscribers
\end{aligned}$$

$$\begin{aligned}
ReqPublishWithQoS1(self) &\triangleq \\
&\wedge pc[self] = \text{"connected"} \\
&\wedge store[self] \neq \{\} \\
&\wedge \exists m \in msgs : \\
&\quad \wedge m.from = self \\
&\quad \wedge m.to = broker \\
&\quad \wedge m.type = PUBLISH \\
&\quad \wedge m.qos = 1 \\
&\quad \wedge m.packetID \notin used_num \\
&\quad \wedge canSendTo(broker) \\
&\quad \wedge network' = send(m, broker) \\
&\quad \wedge used_num' = used_num \cup \{m.packetID\} \\
&\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"publishingwithqos1"}] \\
&\wedge UNCHANGED \ active
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } topic_subscribers \\
RcvPublishWithQoS1Res(self) & \triangleq \\
& \wedge pc[self] = \text{"publishingwithqos1"} \\
& \wedge Len(network[self]) > 0 \\
& \wedge \text{LET } m \triangleq Head(network[self]) \text{IN} \\
& \quad \wedge m.from = broker \\
& \quad \wedge m.to = self \\
& \quad \wedge m.type = PUBACK \\
& \quad \wedge network' = rcv(m, self) \\
& \quad \wedge store' = [store \text{ EXCEPT } ![self] = @ \setminus \{m.packetID\}] \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connected"}] \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \wedge \text{UNCHANGED } used_num \\
ReqPublishWithQoS2(self) & \triangleq \\
& \wedge pc[self] = \text{"connected"} \\
& \wedge store[self] \neq \{\} \\
& \wedge \exists m \in msgs : \\
& \quad \wedge m.from = self \\
& \quad \wedge m.to = broker \\
& \quad \wedge m.type = PUBLISH \\
& \quad \wedge m.qos = 2 \\
& \quad \wedge m.packetID \notin used_num \\
& \quad \wedge canSendTo(broker) \\
& \quad \wedge network' = send(m, broker) \\
& \quad \wedge used_num' = used_num \cup \{m.packetID\} \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"publishingwithqos2"}] \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } topic_subscribers \\
RcvPubrecAndResPubrel(self) & \triangleq \\
& \wedge pc[self] = \text{"publishingwithqos2"} \\
& \wedge Len(network[self]) > 0 \\
& \wedge \text{LET } m \triangleq Head(network[self]) \text{IN} \\
& \quad \wedge m.from = broker \\
& \quad \wedge m.to = self \\
& \quad \wedge m.type = PUBREC \\
& \quad \wedge \exists rmsg \in msgs : \\
& \quad \quad \wedge rmsg.type = PUBREL \\
& \quad \quad \wedge rmsg.from = self \\
& \quad \quad \wedge rmsg.to = broker \\
& \quad \quad \wedge rmsg.packetID = m.packetID
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{canSendTo}(\text{broker}) \\
& \wedge \text{network}' = \text{response}(\text{rmsg}, \text{rmsg.from}, \text{rmsg.to}) \\
\wedge \text{pc}' = [\text{pc} \text{ EXCEPT } ![\text{self}] = \text{"waitingpubcomp"}] \\
& \wedge \text{UNCHANGED } \text{active} \\
& \wedge \text{UNCHANGED } \text{store} \\
& \wedge \text{UNCHANGED } \text{topic_subscribers} \\
& \wedge \text{UNCHANGED } \text{used_num} \\
\\
\text{RcvPubComp}(\text{self}) \triangleq & \\
& \wedge \text{pc}[\text{self}] = \text{"waitingpubcomp"} \\
& \wedge \text{Len}(\text{network}[\text{self}]) > 0 \\
& \wedge \text{LET } m \triangleq \text{Head}(\text{network}[\text{self}]) \text{ IN} \\
& \quad \wedge m.\text{from} = \text{broker} \\
& \quad \wedge m.\text{to} = \text{self} \\
& \quad \wedge m.\text{type} = \text{PUBCOMP} \\
& \quad \wedge \text{network}' = \text{rcv}(m, \text{self}) \\
& \quad \wedge \text{store}' = [\text{store} \text{ EXCEPT } ![\text{self}] = @ \setminus \{m.\text{packetID}\}] \\
& \wedge \text{pc}' = [\text{pc} \text{ EXCEPT } ![\text{self}] = \text{"connected"}] \\
& \wedge \text{UNCHANGED } \text{active} \\
& \wedge \text{UNCHANGED } \text{topic_subscribers} \\
& \wedge \text{UNCHANGED } \text{used_num} \\
\\
\text{ReqSubscribe}(\text{self}) \triangleq & \\
& \wedge \text{pc}[\text{self}] = \text{"connected"} \\
& \wedge \exists m \in \text{msgs} : \\
& \quad \wedge \exists t \in \text{topics} : \\
& \quad \quad \wedge \forall q \in \{QoS0, QoS1, QoS2\} : \\
& \quad \quad \quad \wedge \text{topic_subscribers}[t][q] \cap \{\text{self}\} = \{\} \\
& \quad \quad \quad \wedge m.\text{from} = \text{self} \\
& \quad \quad \quad \wedge m.\text{to} = \text{broker} \\
& \quad \quad \quad \wedge m.\text{type} = \text{SUBSCRIBE} \\
& \quad \quad \quad \wedge m.\text{topic} = t \\
& \quad \quad \quad \wedge \text{canSendTo}(\text{broker}) \\
& \quad \quad \quad \wedge \text{network}' = \text{send}(m, \text{broker}) \\
& \wedge \text{pc}' = [\text{pc} \text{ EXCEPT } ![\text{self}] = \text{"subscribing"}] \\
& \wedge \text{UNCHANGED } \text{active} \\
& \wedge \text{UNCHANGED } \text{topic_subscribers} \\
& \wedge \text{UNCHANGED } \text{store} \\
& \wedge \text{UNCHANGED } \text{used_num} \\
\\
\text{RcvSubscribeRes}(\text{self}) \triangleq & \\
& \wedge \text{pc}[\text{self}] = \text{"subscribing"} \\
& \wedge \text{Len}(\text{network}[\text{self}]) > 0 \\
& \wedge \text{LET } m \triangleq \text{Head}(\text{network}[\text{self}]) \text{ IN}
\end{aligned}$$

$$\begin{aligned}
& \wedge m.from = broker \\
& \wedge m.to = self \\
& \wedge m.type = SUBACK \\
& \wedge network' = rcv(m, self) \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connected"}] \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } used_num \\
\\
ReqUnsubscribe(self) & \triangleq \\
& \wedge pc[self] = \text{"connected"} \\
& \wedge Len(network[self]) = 0 \\
& \wedge \exists m \in msgs : \\
& \quad \wedge \exists t \in topics : \\
& \quad \quad \exists q \in \{QoS0, QoS1, QoS2\} : \\
& \quad \quad \quad \wedge topic_subscribers[t][q] \cap \{self\} \neq \{\} \\
& \quad \quad \quad \wedge m.from = self \\
& \quad \quad \quad \wedge m.to = broker \\
& \quad \quad \quad \wedge m.type = UNSUBSCRIBE \\
& \quad \quad \quad \wedge m.topic = t \\
& \quad \quad \quad \wedge canSendTo(broker) \\
& \quad \quad \quad \wedge network' = send(m, broker) \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"unsubscribing"}] \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } used_num \\
\\
RcvUnsubscribeRes(self) & \triangleq \\
& \wedge pc[self] = \text{"unsubscribing"} \\
& \wedge Len(network[self]) > 0 \\
& \wedge \text{LET } m \triangleq Head(network[self]) \text{ IN} \\
& \quad \wedge m.from = broker \\
& \quad \wedge m.to = self \\
& \quad \wedge m.type = UNSUBACK \\
& \quad \wedge network' = rcv(m, self) \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connected"}] \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } used_num \\
\\
GetMsgWithQoS0(self) & \triangleq \\
& \wedge pc[self] = \text{"connected"} \\
& \wedge Len(network[self]) > 0
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{LET } msg \triangleq \text{Head}(\text{network}[self]) \text{IN} \\
& \quad \wedge msg.type = PUBLISH \\
& \quad \wedge msg.qos = 0 \\
& \quad \wedge network' = rcv(msg, self) \\
& \quad \wedge \quad \vee Len(store[self]) = 0 \\
& \quad \quad \vee \quad \wedge Len(store[self]) > 0 \\
& \quad \quad \quad \wedge \exists i \in 1 \dots Len(store[self]) : store[self][i] \neq msg.packetID \\
& \quad \wedge store' = [store \text{ EXCEPT } ![self] = Append(@, msg.packetID)] \\
& \quad \wedge \text{UNCHANGED } pc \\
& \quad \wedge \text{UNCHANGED } active \\
& \quad \wedge \text{UNCHANGED } topic_subscribers \\
& \quad \wedge \text{UNCHANGED } used_num \\
\\
GetMsgWithQoS1AndRes(self) & \triangleq \\
& \quad \wedge pc[self] = \text{"connected"} \\
& \quad \wedge Len(network[self]) > 0 \\
& \quad \wedge \text{LET } msg \triangleq \text{Head}(\text{network}[self]) \text{IN} \\
& \quad \quad \wedge msg.to = self \\
& \quad \quad \wedge msg.type = PUBLISH \\
& \quad \quad \wedge msg.qos = 1 \\
& \quad \quad \wedge \exists m \in msgs : \\
& \quad \quad \quad \wedge m.type = PUBACK \\
& \quad \quad \quad \wedge m.from = msg.to \\
& \quad \quad \quad \wedge m.to = msg.from \\
& \quad \quad \quad \wedge m.packetID = msg.packetID \\
& \quad \quad \quad \wedge \quad \vee Len(store[self]) = 0 \\
& \quad \quad \quad \quad \vee \quad \wedge Len(store[self]) > 0 \\
& \quad \quad \quad \quad \quad \wedge \exists i \in 1 \dots Len(store[self]) : store[self][i] \neq msg.packetID \\
& \quad \quad \quad \wedge network' = response(m, m.from, m.to) \\
& \quad \quad \wedge store' = [store \text{ EXCEPT } ![self] = Append(@, msg.packetID)] \\
& \quad \quad \wedge \text{UNCHANGED } pc \\
& \quad \quad \wedge \text{UNCHANGED } active \\
& \quad \quad \wedge \text{UNCHANGED } topic_subscribers \\
& \quad \quad \wedge \text{UNCHANGED } used_num \\
\\
GetMsgWithQoS2AndRes(self) & \triangleq \\
& \quad \wedge pc[self] = \text{"connected"} \\
& \quad \wedge Len(network[self]) > 0 \\
& \quad \wedge \text{LET } msg \triangleq \text{Head}(\text{network}[self]) \text{IN} \\
& \quad \quad \wedge msg.to = self \\
& \quad \quad \wedge msg.type = PUBLISH \\
& \quad \quad \wedge msg.qos = 2 \\
& \quad \quad \wedge \exists m \in msgs : \\
& \quad \quad \quad \wedge m.type = PUBREC \\
& \quad \quad \quad \wedge m.from = msg.to
\end{aligned}$$

$$\begin{aligned}
& \wedge m.to = msg.from \\
& \wedge m.packetID = msg.packetID \\
& \wedge \quad \vee Len(store[self]) = 0 \\
& \quad \vee \quad \wedge Len(store[self]) > 0 \\
& \quad \quad \wedge \exists i \in 1 \dots Len(store[self]) : store[self][i] \neq msg.packetID \\
& \wedge network' = response(m, m.from, m.to) \\
& \wedge store' = [store \text{ EXCEPT } ![self] = Append(@, msg.packetID)] \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"waittingpubrel"}] \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \quad \wedge \text{UNCHANGED } used_num \\
GetMsgWithQoS2PubRelAndRes(self) & \triangleq \\
& \wedge pc[self] = \text{"waittingpubrel"} \\
& \wedge Len(network[self]) > 0 \\
& \wedge \text{LET } msg \triangleq Head(network[self]) \text{ IN} \\
& \quad \wedge msg.to = self \\
& \quad \wedge msg.type = PUBREL \\
& \quad \wedge \exists m \in msgs : \\
& \quad \quad \wedge m.type = PUBCOMP \\
& \quad \quad \wedge m.from = msg.to \\
& \quad \quad \wedge m.to = msg.from \\
& \quad \quad \wedge m.packetID = msg.packetID \\
& \quad \quad \wedge network' = response(m, m.from, m.to) \\
& \quad \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"connected"}] \\
& \quad \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \quad \wedge \text{UNCHANGED } used_num \\
PublisherDone(self) & \triangleq \\
& \wedge pc[self] = \text{"connected"} \\
& \wedge Len(network[self]) = 0 \\
& \wedge Cardinality(used_num) = maxPubNum \\
& \quad \wedge \exists m \in msgs : \\
& \quad \quad \wedge m.from = self \\
& \quad \quad \wedge m.type = DISCONNECT \\
& \quad \quad \wedge m.to = broker \\
& \quad \quad \wedge canSendTo(broker) \\
& \quad \quad \wedge network' = send(m, m.to) \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"closed"}] \\
& \quad \wedge \text{UNCHANGED } store \\
& \wedge \text{UNCHANGED } active \\
& \wedge \text{UNCHANGED } topic_subscribers \\
& \quad \wedge \text{UNCHANGED } used_num
\end{aligned}$$

$$\begin{aligned}
& \text{SubscriberDone}(self) \triangleq \\
& \quad \wedge pc[self] = \text{"connected"} \\
& \quad \wedge \text{Len}(\text{network}[self]) = 0 \\
& \quad \quad \wedge \exists m \in \text{msgs} : \\
& \quad \quad \quad \wedge m.from = self \\
& \quad \quad \quad \wedge m.type = \text{DISCONNECT} \\
& \quad \quad \quad \wedge m.to = broker \\
& \quad \quad \quad \wedge \text{canSendTo}(broker) \\
& \quad \quad \quad \wedge \text{network}' = \text{send}(m, m.to) \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"closed"}] \\
& \quad \quad \wedge \text{UNCHANGED } store \\
& \quad \wedge \text{UNCHANGED } active \\
& \quad \wedge \text{UNCHANGED } topic_subscribers \\
& \quad \quad \wedge \text{UNCHANGED } used_num \\
\\
& \text{SubscriberAction} \triangleq \\
& \quad \exists self \in subscribers : \\
& \quad \quad \vee \text{ReqConnect}(self) \\
& \quad \quad \vee \text{RcvConnectRes}(self) \\
& \quad \quad \vee \text{ReqSubscribe}(self) \\
& \quad \quad \vee \text{RcvSubscribeRes}(self) \\
& \quad \quad \vee \text{ReqUnsubscribe}(self) \\
& \quad \quad \vee \text{RcvUnsubscribeRes}(self) \\
& \quad \quad \vee \text{GetMsgWithQoS0}(self) \\
& \quad \quad \vee \text{GetMsgWithQoS1AndRes}(self) \\
& \quad \quad \vee \text{GetMsgWithQoS2AndRes}(self) \\
& \quad \quad \vee \text{GetMsgWithQoS2PubRelAndRes}(self) \\
& \quad \vee \text{SubscriberDone}(self) \\
\\
& \text{PublisherAction} \triangleq \\
& \quad \exists self \in publishers : \\
& \quad \quad \vee \text{ReqConnect}(self) \\
& \quad \quad \vee \text{RcvConnectRes}(self) \\
& \quad \quad \vee \text{ReqPublishWithQoS0}(self) \\
& \quad \quad \vee \text{ReqPublishWithQoS1}(self) \\
& \quad \quad \vee \text{RcvPublishWithQoS1Res}(self) \\
& \quad \quad \vee \text{ReqPublishWithQoS2}(self) \\
& \quad \quad \vee \text{RcvPubrecAndResPubrel}(self) \\
& \quad \quad \vee \text{RcvPubComp}(self) \\
& \quad \vee \text{PublisherDone}(self) \\
\\
& \text{ClientsDone} \triangleq \text{whenall clients disconnected} \\
& \quad \wedge \forall c \in clients : \\
& \quad \quad \wedge pc[c] = \text{"closed"} \\
& \quad \quad \wedge \text{Len}(\text{network}[c]) = 0 \\
& \quad \wedge \text{UNCHANGED } vars
\end{aligned}$$
