```
Module Spec
EXTENDS TLC, Broker, Client
Init \triangleq
     \land \ pc = [c \in \mathit{clients} \mapsto \mathit{``start"}]
          \land active = \{\}
     \land network = [a \in agents \mapsto \langle \rangle]
          \land topic\_subscribers = [t \in topics \mapsto [qos \in \{QoS0, QoS1, QoS2\} \mapsto \{\}]]
          \land used\_num = \{\}
     \land store =
                            a \in \mathit{agents} \mapsto \mathit{CASE}\ a \in \mathit{publishers} \to 1 \ldots \mathit{maxPubNum}
                            \Box a = broker \rightarrow [t \in topics \mapsto [qos \in \{QoS0, QoS1, QoS2\} \mapsto \langle \rangle]]
                            \Box a \in subscribers \rightarrow \langle \rangle
Next \triangleq
          \vee PublisherAction
          \vee SubscriberAction
           \vee BrokerAction
     \lor ClientsDone
Liveness \triangleq
     \land \forall p \in publishers:
          \wedge \operatorname{SF}_{vars}(ReqConnect(p))
          \land SF<sub>vars</sub>(ReqPublishWithQoS0(p) \lor ReqPublishWithQoS1(p) \lor ReqPublishWithQoS2(p))
          \wedge WF_{vars}(PublisherDone(p))
     \land \forall s \in subscribers:
          \wedge \operatorname{SF}_{vars}(ReqConnect(s))
          \wedge SF_{vars}(ReqSubscribe(s))
          \land SF<sub>vars</sub>(GetMsgWithQoS0(s) \lor GetMsgWithQoS1AndRes(s) \lor GetMsgWithQoS2AndRes(s))
          \wedge SF_{vars}(RegUnsubscribe(s))
          \wedge WF_{vars}(SubscriberDone(s))
     \wedge SF_{vars}(HandleConnectReq)
     \wedge SF_{vars}(HandleSubscribeReq)
     \wedge SF_{vars}(HandleUnsubscribeReq)
     \wedge SF_{vars}(HandlePublishWithQoS0Req)
     \wedge SF_{vars}(HandlePublishWithQoS1Req)
     \wedge SF_{vars}(HandlePublishWithQoS2Req)
     \wedge SF_{vars}(HandlePubrelReq)
     \wedge SF_{vars}(HandlePushQoS1Res)
     \wedge SF_{vars}(HandlePushQoS2Res)
     \wedge SF_{vars}(HandlePubCompRes)
     \wedge SF_{vars}(PushMsgsWithQoS0)
     \wedge SF_{vars}(PushMsgsWithQoS1)
     \wedge SF_{vars}(PushMsgsWithQoS2)
```

 $Spec \stackrel{\Delta}{=} Init \wedge \Box [Next]_{vars} \wedge Liveness$