
MODULE *MQTTBase*

EXTENDS *TLC, FiniteSets, Sequences, Naturals*

CONSTANTS

CONNECT, CONACK, PUBLISH, PUBACK, PUBREL, PUBREC, PUBCOMP, SUBSCRIBE, SUBACK

CONSTANTS

publishers,
subscribers,
broker,
topics,
maxQueueLen,
maxPubNum

VARIABLES

pc,
*pub2q \ * qos2*
store,
active,
network,
topic_subscribers,
used_num / ID

vars \triangleq $\langle pc, active, network, store, used_num, topic_subscribers \rangle$

agent_vars \triangleq $\langle pc, active, store, used_num, topic_subscribers \rangle$

clients $\triangleq publishers \cup subscribers$

agents $\triangleq clients \cup \{broker\}$

maxSubNum $\triangleq Cardinality(topics)$

PUBLISHERS $\triangleq Permutations(publishers)$

SUBSCRIBERS $\triangleq Permutations(subscribers)$

CLIENTS $\triangleq PUBLISHERS \cup SUBSCRIBERS$

msgs \triangleq

$[from : clients, to : \{broker\}, type : \{CONNECT\}, payload : [clientId : clients]]$
 $\cup [from : clients, to : \{broker\}, type : \{PINGREQ\}]$
 $\cup [from : \{broker\}, to : clients, type : \{CONACK, PINGRESP\}, qos : \{NULL\}, topics : \{NULL\}, packetID : 1 \dots maxPubNum]$
 $\cup [from : publishers, to : \{broker\}, type : \{PUBLISH\}, qos : \{0, 1, 2\}, topic : topics, packetID : 1 \dots maxPubNum]$
 $\cup [from : publishers, to : \{broker\}, type : \{PUBREL\}, packetID : 1 \dots maxPubNum]$
 $\cup [from : subscribers, to : \{broker\}, type : \{UNSUBSCRIBE\}, topic : topics]$
 $\cup [from : subscribers, to : \{broker\}, type : \{SUBSCRIBE\}, qos : \{0, 1, 2\}, topic : topics, packetID : 1 \dots maxPubNum]$
 $\cup [from : \{broker\}, to : publishers, type : \{PUBACK, PUBREC, PUBCOMP\}, packetID : 1 \dots maxPubNum]$
 $\cup [from : \{broker\}, to : subscribers, type : \{SUBACK\}, qos : \{0, 1, 2\}, topic : topics, packetID : 1 \dots maxPubNum]$
 $\cup [from : \{broker\}, to : subscribers, type : \{UNSUBACK\}, topic : topics]$
 $\cup [from : \{broker\}, to : subscribers, type : \{PUBLISH\}, qos : \{0, 1, 2\}, topic : topics, packetID : maxPubNum + 1 \dots maxPubNum * 2]$
 $\cup [from : subscribers, to : \{broker\}, type : \{PUBREL\}, packetID : maxPubNum + 1 \dots maxPubNum * 2]$
 $\cup [from : subscribers, to : \{broker\}, type : \{PUBACK, PUBREC, PUBCOMP\}, packetID : maxPubNum + 1 \dots maxPubNum * 2]$

$$\begin{aligned}
& \cup [from : clients, to : \{broker\}, type : \{DISCONNECT\}] \\
canSendTo(chan) & \triangleq Len(network[chan]) < maxQueueLen \\
send(msg, chan) & \triangleq [network \text{ EXCEPT } ![chan] = Append(@, msg)] \\
rcv(msg, chan) & \triangleq [network \text{ EXCEPT } ![chan] = Tail(@)] \\
response(msg, from, to) & \triangleq [network \text{ EXCEPT } ![to] = Append(@, msg), ![from] = Tail(@)]
\end{aligned}$$
