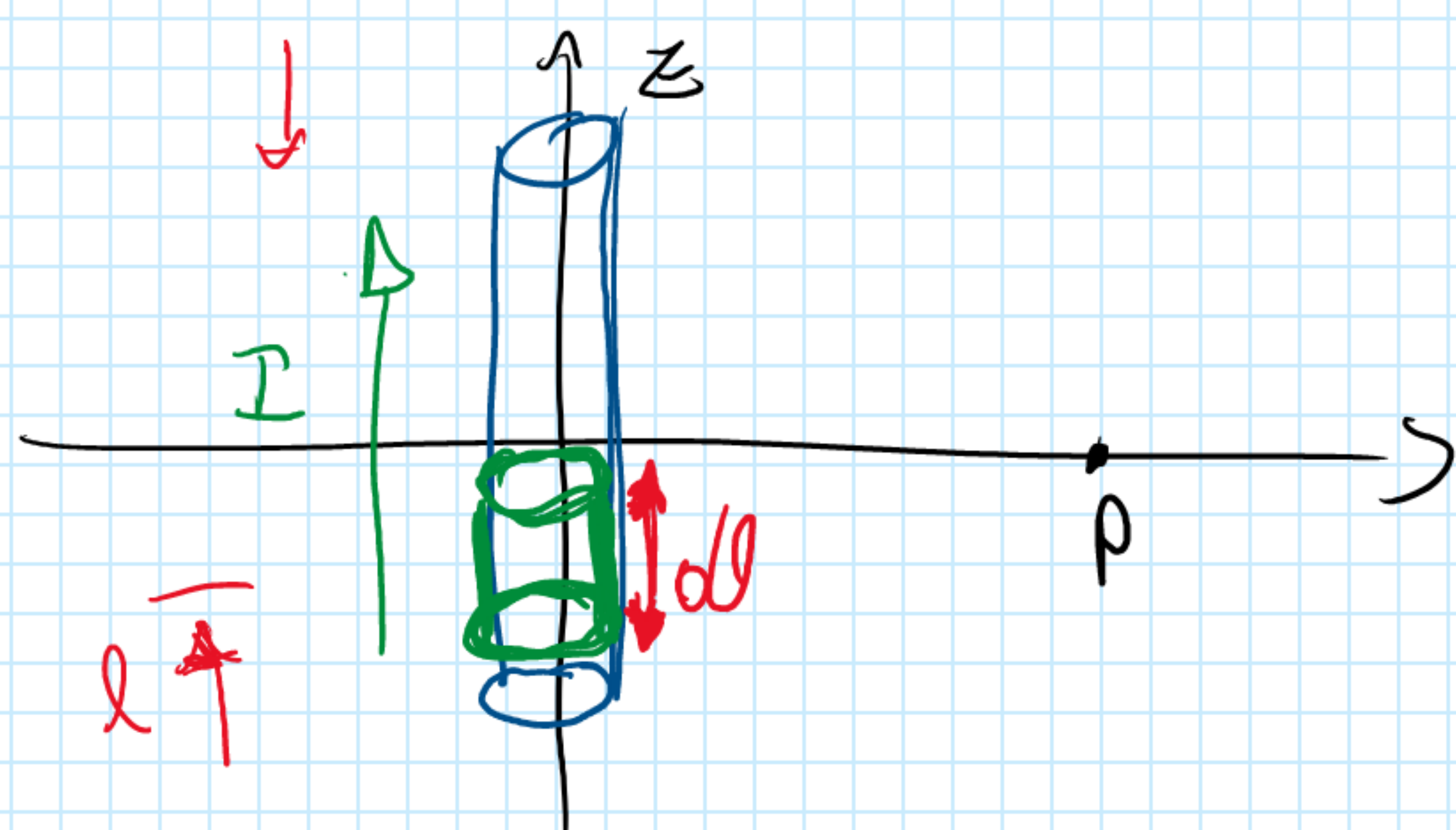


Per ricavare questa legge andiamo a considerare un conduttore

di forma cilindrica



$$\vec{H} = \frac{I}{4\pi} \int \frac{d\vec{l} \times \hat{r}}{r^2}$$

$$d\vec{l} = \hat{z} dz$$

$$d\vec{l} \times \hat{r} = (\hat{z} \times \hat{r}) dz = \phi \sin \theta dz$$

$$\vec{H} = \frac{I}{4\pi} \int_{-\frac{l}{2}}^{\frac{l}{2}} \frac{\phi \sin \theta}{r^2} dz$$

$$r = R \sin \theta \Rightarrow R = \frac{r}{\sin \theta}$$

$$r = -2Tg \theta \Rightarrow z = -\frac{r}{Tg \theta} \Rightarrow dz = \frac{r}{\sin^2 \theta} d\theta$$

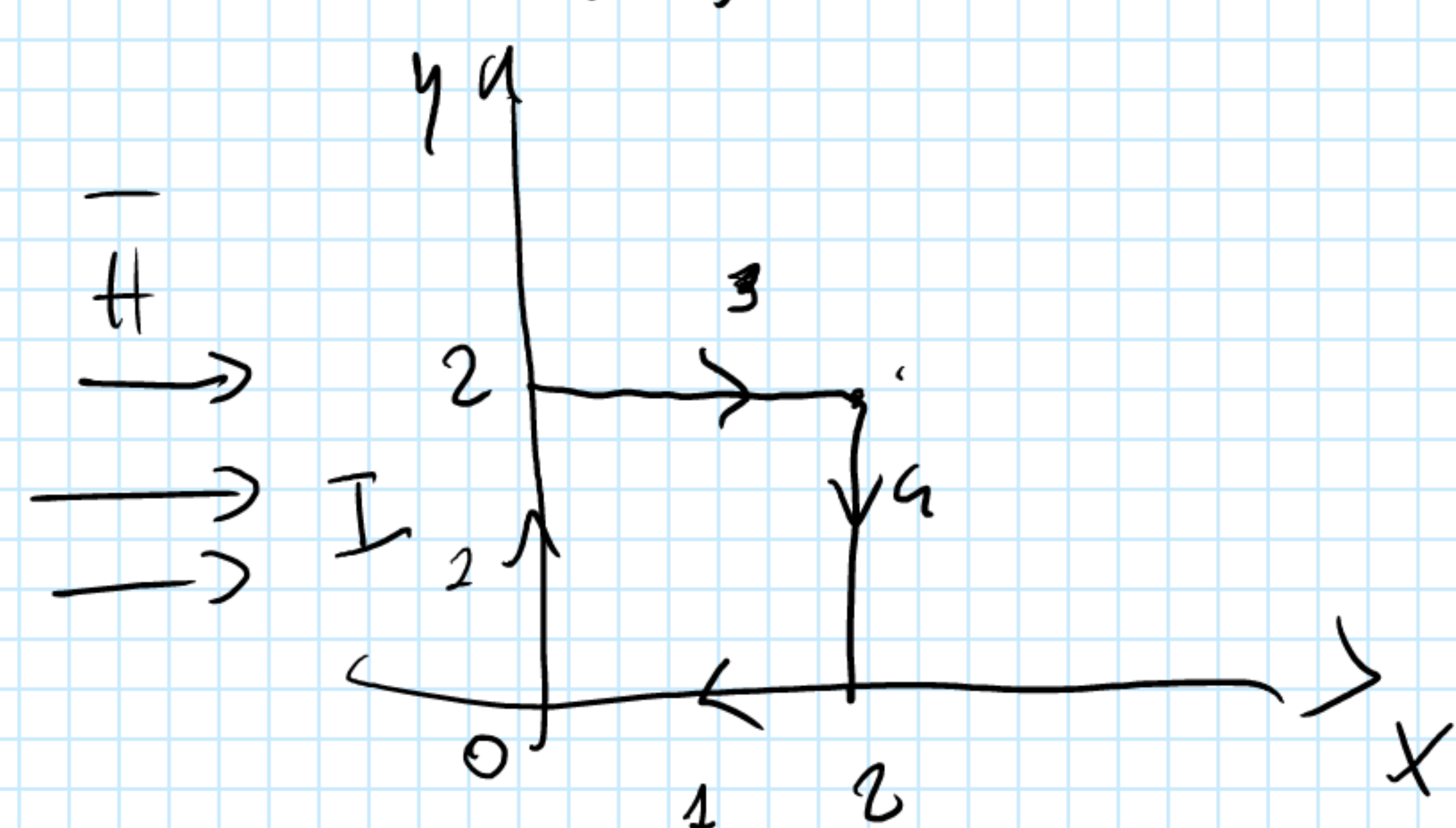
$$\vec{H} = \phi \frac{I}{4\pi R} \int_{\theta_1}^{\theta_2} \frac{\sin \theta}{\pi^2} \cdot \frac{r}{\sin^2 \theta} d\theta \Rightarrow \vec{H} = \phi \frac{I}{4\pi R} \int_{\theta_1}^{\theta_2} \sin \theta d\theta$$

$$= \phi \frac{I}{4\pi R} (\cos \theta_1 - \cos \theta_2) = \phi \frac{I}{2\pi R} = I = |\vec{H}| \cdot 2\pi R \Rightarrow I = \oint \vec{H} \cdot d\vec{l}$$

LEGGE DI AMPERE

### ESERCIZIO

ASSIGNATO  $\vec{H} = \hat{x} 3y^2$  CALCOLARE LA CORRENTE CHE ATTRAVERSA LA SPIRA QUADRATA.



$$I = \int \vec{H} \cdot d\vec{l} \Rightarrow$$

$$\Rightarrow \int_0^2 \hat{x} 3y^2 \cdot (-\hat{x} dx) = -6 \cdot 0 = 0$$

$\nwarrow y=0$

$$\int_0^2 \hat{x} 3y^2 \cdot \hat{y} dy = 0$$

$$2 \int_0^2 \hat{x} 3y^2 \cdot \hat{y} dy = 0$$

$$I = 24$$

$$3 \int_0^2 \hat{x} 3y^2 \cdot \hat{x} dx = 3 \cdot 2^2 \cdot 2 = 24$$

$\nwarrow$

### ESERCIZIO

UN CONDUTTORE CILINDRICO DI RAGGIO  $r = 10^{-2} m$  È SOTTOPOSTO ALL'AZIONE DI UN CAMPO MAGNETICO  $\vec{H} = (4,77 \cdot 10^4) \left( \frac{\pi}{2} - \frac{\pi^2}{3 \cdot 10^{-2}} \right) \hat{\phi}$   
 $I = ?$

$$I = \int \vec{H} \cdot d\vec{l} \Rightarrow \int_0^{2\pi} (4,77 \cdot 10^4) \left( \frac{\pi}{2} - \frac{\pi^2}{3 \cdot 10^{-2}} \right) \hat{\phi} \cdot \hat{\phi} r d\phi \Rightarrow$$

$$d\vec{l} = \hat{\phi} r d\phi$$

$$\Rightarrow (4,77 \cdot 10^4) \frac{10^{-2}}{2} - \frac{10}{(3 \cdot 10^{-2})} 10^{-2} \cdot 2\pi = 4,92 (A)$$