

fellingdater: a toolkit to estimate, report and combine felling dates derived from historical tree-ring series.

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Summary

Tree-ring dating, or dendrochronology, allows to assign calendar-year dates to growth rings that are observable on a cross-section of a stem or a piece of timber. It involves measuring the width of each growth ring and comparing the measured ring-width pattern to absolutely dated reference chronologies. Once a tree-ring series is securely anchored to a calendar year time-scale, the end date of the outermost ring can be used to determine or estimate the year of death of the parent tree (i.e., the felling of the tree).

The **fellingdater** package aims to offer a suite of functions that can assist dendrochronologists to infer, combine and report felling date estimates from dated tree-ring series of (pre-)historical timbers, based on the presence of partially preserved sapwood or waney edge (Fig. 1).

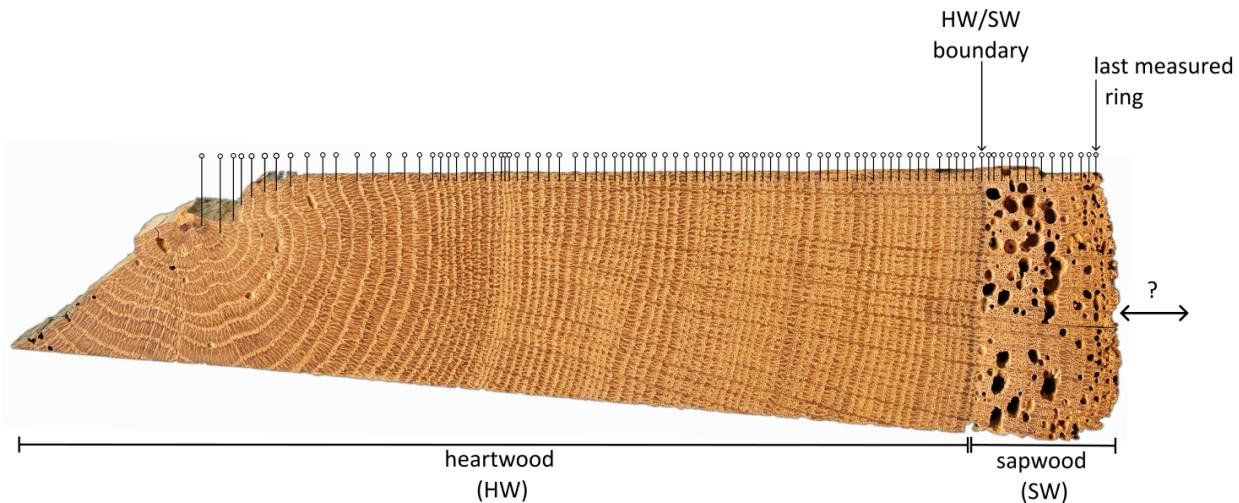


Figure 1: A cross-section of a historical timber from a medieval roof construction. The heartwood and sapwood areas are marked, as well as all ring boundaries. The **fellingdater** package offers a workflow to estimate the number of missing sapwood rings (?) – that have been trimmed-of, powdered by wood-boring insects, or deteriorated by wood-decaying fungi – between the last measured ring and the cambial layer.

Background

Dendrochronology is the most precise chronometric dating technique for (pre-)historical wooden constructions and objects (Baillie 1995). It involves recording the ring-width pattern on a cross-section of the wooden

element under study and matching this pattern to absolutely dated reference chronologies, which allows the recorded tree-ring pattern to be anchored to an absolute time scale. From a dated tree-ring pattern it is known in which growing season each growth ring has been laid down by the parent tree. In archaeological, architectural or art-historical studies, the primary objective of a dendrochronological survey is to ascertain an accurate estimate of the **felling date** (or dying-off) of the parent tree from which the timber originates (Haneca, Cufar, and Beeckman 2009; Tegel et al. 2022). This felling date is the closest related and datable event to the creation of the wooden object or construction under study. These precisely dated events serve as the basis for narratives on various aspects, such as timber selection, craftsmanship, workshop practices, trade, provenance, and historical forest management (Domínguez-Delmás 2020).

The exact felling date can be inferred from the calendar year assigned to the most recently formed tree ring prior to the felling or death of the tree. Achieving this requires the presence of the last-formed ring on the object or timber under study, enabling tree-ring dating to achieve (sub-)annual chronological resolution. Unfortunately, this prerequisite is often not fulfilled. The wood of the felled tree may have undergone processing, trimming, or biological deterioration leading to the irreversible loss of wood tissue. When the outermost portion of the timber no longer includes the cambial zone (as illustrated in Fig. 1), the timing of the felling date can only be estimated. The most challenging situation is when neither sapwood, nor the transition between heartwood and sapwood, remains on the object or timber under study (Fig. 1, HW/SW boundary). **Sapwood** comprises the outermost wood tissues of the xylem in a living tree, representing the physiologically active outer portion of the stem or a branch. It is situated between the cambial zone and the (dead) heartwood, and includes several growth rings. If none of the sapwood is retained, an untraceable amount of wood and growth layers has been removed. In such cases, the last measured and dated ring then only provides an earliest possible felling date or *terminus post quem*.

To refine estimates of felling dates, since the early development of tree-ring dating, datasets have been published with counts of sapwood rings on historical timbers and from living trees, providing a framework for estimating the number of missing rings on tree-ring dated wooden elements with partially preserved sapwood. These sapwood datasets, their transformation into a probabilistic model and the confidence intervals they provide are key elements to obtain a reliable estimate of the felling date of a tree-ring dated piece of timber.

The **fellingdateR** package aims to facilitate this process by providing functions to infer, combine and report felling date estimates from dated tree-ring series, based on the presence of (partially) preserved sapwood or waney edge.

Statement of need

Many descriptive statistics and statistical models have been published to establish accurate estimates of the expected number of sapwood ring (Edvardsson et al. 2022; Bleicher et al. 2020; Rybnicek, Vavrik, and Hubeny 2006; Pilcher 1987; Hollstein 1965, 1980; Wazny 1990; Miles 1997; Sohar, Vitas, and Läänelaid 2012; Bräthen 1982; Haneca, Cufar, and Beeckman 2009; Hughes, Milsom, and Leggett 1981; Jevšenak et al. 2019; Hillam, Morgan, and Tyers 1987; Gjerdrum 2013; Shindo et al. 2024). These models often rely on log-transformation of the original counts of sapwood numbers from living and historical timbers, or use regression models that include additional variables such as mean ring width, the cambial age of the tree or a combination of both. These statistical procedures report the expected minimal and maximal number of sapwood rings, usually within 95% a confidence interval, but have also been presented in a wide variety of ways and differ among laboratories and dendrochronologists. This variety in methodology and reporting comes even more to the surface when tree-ring dates of multiple elements from a single object, construction or building phase are combined into a single felling date for the whole ensemble. The goal of such a mutual interpretation of the individual felling dates is to refine the range of the felling date, but also to check or test whether these dated tree-ring series/wooden elements could indeed represent one single event (i.e. the felling of trees).

A Bayesian method to improve the procedures to model sapwood data, compute lower and upper limits for the felling date based upon the selected sapwood model and a given credible interval have been introduced by Millard (2002). This procedure was then further refined by Miles (2006), and critically reviewed with real-life

examples by Tyers (2008). Furthermore, these routines have been incorporated in OxCal, the routine software for calibration and analysis of radiocarbon dates and related archaeological and chronological information (Bronk Ramsey 2009: <https://c14.arch.ox.ac.uk/oxcalhelp/Sapwood.html>). Tree-ring analyses, on the other hand, rely on a growing set of R-packages, with the ‘*Dendrochronology Program Library in R*’ (Bunn 2008, 2010; Bunn et al. 2022), the *dplR*-package, at its core (see opendendro.org; (Bunn, Anchukaitis, and Swetnam 2022)). Yet, the Bayesian methodology to establish sapwood estimates and felling dates was so far not available as a suite of functions in R (R Core Team 2022).

In order to facilitate and standardize the reporting, interpretation and combination of felling dates from historical timbers and objects, the *fellingdateR* R-package was devised . The package allows to fully document the methodology to establish a felling date – for a single timber or a group of timbers – making the whole procedure reproducible and assists in building standardized workflows when applied to large datasets of historical tree-ring series originating from geographically distinct regions. An example of the latter, with an analysis of a large dataset of historical tree-ring series from medieval roof constructions, can be found in (Haneca, Debonne, and Hoffsummer 2020). The package is designed to offer several functions that are related to each step in the (generalized) workflow when analysing tree-ring series from (pre-)historical objects or constructions (Fig. 2).

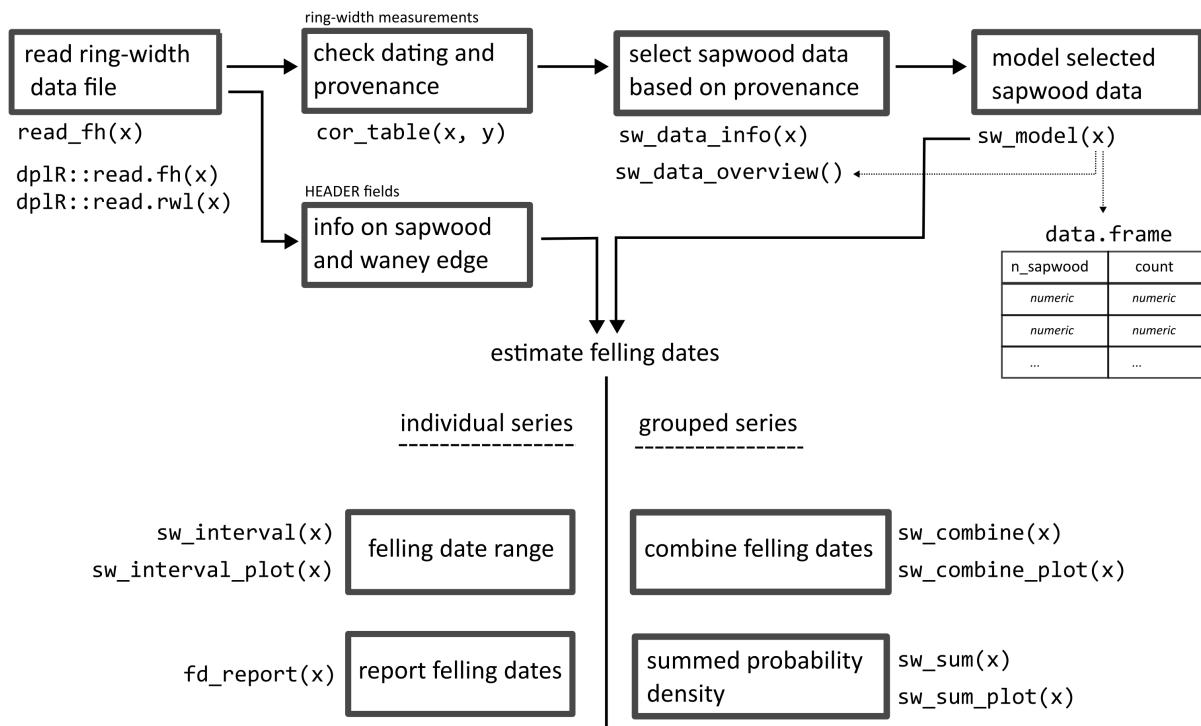


Figure 2: A generalized workflow and related functions, for inferring felling dates from tree-ring dated historical timbers.

Data within the package

The package comes with published datasets of sapwood counts. The original data was in most cases retrieved from the original publication by digitizing scatter plots or frequency histograms (Haneca and Debonne 2012). This was only possible for a limited number of publications as many of those datasets have been published as histograms with wide bins (>1), what does not allow to retrieve the underlying data points. An overview of all currently available sapwood datasets included in the package is generated by `sw_data_overview()`.

More information on the datasets, such as the bibliographic reference to the original publication, the wood species and some basic descriptive statistics (sample size, mean, median, min-max, ...) can be retrieved, for instance, by `sw_data_info("Hollstein_1980")`.

`sw_model()` fits a density distribution (lognormal, normal, weibull or gamma) to the original data, and returns the output of the modelling process. With `sw_model_plot()` the model is visualized as a ggplot-style graph (Wickham 2016) (Fig. 3).

```
library(fellingdateR)

# The function `sw_data_overview()` returns an overview of all available sapwood datasets
# distributed with the package:
sw_data_overview()
#> [1] "Brathen_1982"      "Hollstein_1980"    "Miles_1997_NM"    "Miles_1997_SC"
#> [5] "Miles_1997_WBC"    "Pilcher_1987"     "Sohar_2012_ELL_c" "Sohar_2012_ELL_t"
#> [9] "Sohar_2012_FWE_c"  "Sohar_2012_FWE_t" "Wazny_1990"       "vanDaalen_NLBE"
#> [13] "vanDaalen_Norway"

# Use one of the names given by 'sw_data_overview()' as an argument inside
#`sw_data_info()` to obtain information on the dataset (citation, area covered,
# n_observations, and summary_raw_data)

sw_data_info("Pilcher_1987")
#> $data
#> [1] "Pilcher_1987"
#>
#> $citation
#> [1] "Pilcher J.R. 1987. A 700 year dating chronology for northern France.
#> Applications of tree-ring studies. Current research in dendrochronology and
#> related subjects. BAR International Series 333, 127-139."
#>
#> $area
#> [1] "Northern France"
#>
#> $n_observations
#> [1] 116
#>
#> $summary_raw_data
#>   Min. 1st Qu. Median   Mean 3rd Qu.   Max.
#> 12.00 22.00 26.00 26.72 31.00 49.00

# Pick the dataset most suited for your case-study and fit a (log-)normal, weibul,
# or gamma distribution to the data.
model <- sw_model("Hollstein_1980", plot = FALSE)
sw_model_plot(model)
```

Example of use

The following examples will walk you through the workflow of reading and crossdating ring-width series (Fig. 2), selecting the appropriate sapwood data and modelling options, and finally computing estimates of felling dates and reporting the outcome of this procedure, both for single series as for a group of related tree-ring series .

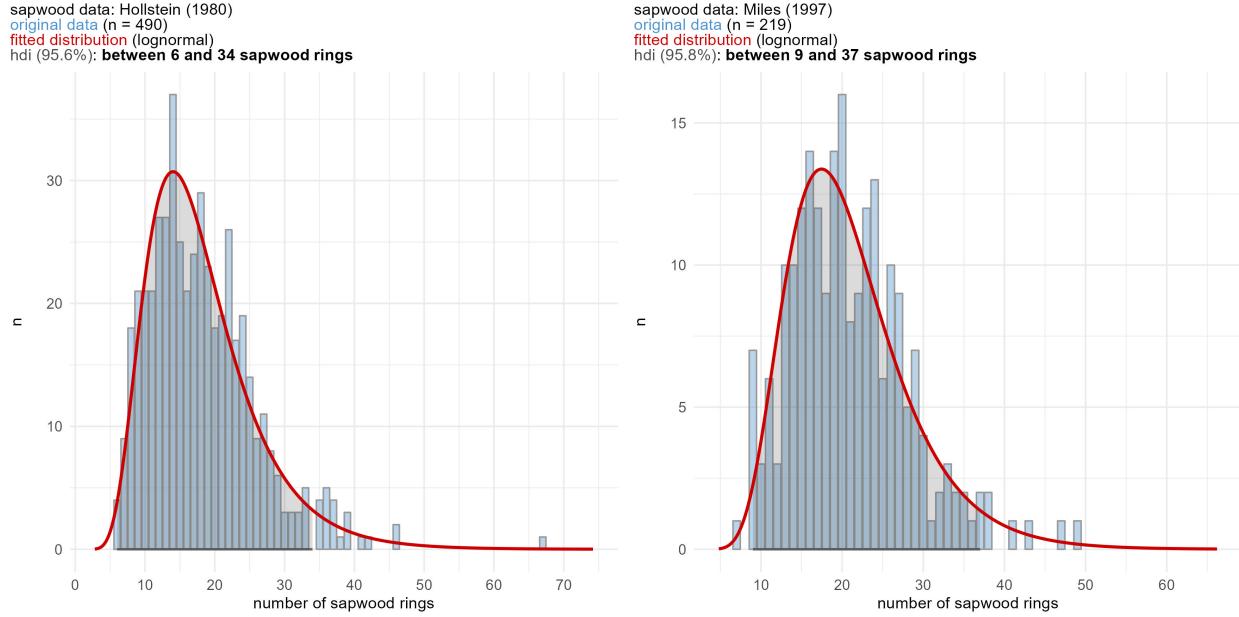


Figure 3: Two sapwood datasets with a density function modeled to the raw data.

Installation

Since xxxx-xx-xx, `fellingdater` is available on CRAN, meaning that it can be easily installed using the following commands in R:

```
install.packages("fellingdater")
```

The latest developing version is hosted on GitHub and can be installed locally:

```
#install.packages("pak")
pak::pak("hanecakr/fellingdater")
```

or

```
#install.packages("devtools")
devtools::install_github("hanecakr/fellingdater")
```

Reading tree-ring files

The function `read_fh()` is an extension to the `dplyR::read.fh()` function from the `dplyR` package (Bunn 2008, 2010; Bunn et al. 2022). The function equally allows to read .fh (format Heidelberg) files of ring widths (both in decadal, half-chrono and chrono format) (Brewer and Murphy 2011), but is more focused on retrieving additional information found in the HEADER fields of the .fh files. These HEADER fields often harbour essential information that is necessary to obtain a well informed estimate of the felling date, such as the measured number of sapwood rings, the number of observed but unmeasured rings, the presence of the HW/SW boundary, the presence of the cambial zone, etc. The `read_fh()` function retrieves the information from the HEADER fields and lists the items as attributes to the ring-width measurements. The `fh_header()` function facilitates easy conversion to a `data.frame`.

In the example below, an .fh file with ring-width measurements on timbers from a medieval ship DOEL1 (Haneca and Daly 2014) is read with `read_fh()`.

```
Doel1 <- system.file("extdata", "DOEL1.fh", package = "fellingdateR")

# When header = TRUE, the get_header() function is triggered and HEADER fields
# in the .fh file are returned as a data.frame, instead of the ring-width
# measurements.

Doel1_header <- read_fh(Doel1, verbose = FALSE, header = TRUE)
dplyr::glimpse(Doel1_header)

# Columns: 29
# $ series           <chr> "K1_091", "S38-BB", "GD3-1BB", "GR1mBB", "S13mSB", "S13A-BB"
# $ data_type         <chr> "Single", "Single", "Single", "Quadro", "Quadro", "Single"
# $ chrono_members    <chr> NA, NA, NA, "K1_001,K1_004x,GR1-3BB", "S1-3SB,K1_076", NA
# $ species          <chr> "QUSP", "QUSP", "QUSP", "QUSP", "QUSP", "QUSP"
# $ first            <dbl> 1158, 1193, 1222, 1220, 1164, 1232
# $ last             <dbl> 1292, 1306, 1310, 1310, 1322, 1324
# $ length           <dbl> 135, 114, 89, 91, 159, 93
# $ n_sapwood        <dbl> 15, 0, 5, 3, 20, 19
# $ n_sapwood_chr    <chr> NA, NA, NA, NA, NA, NA
# $ unmeasured_rings <dbl> NA, NA, NA, NA, NA, NA
# $ invalid_rings    <dbl> NA, NA, NA, NA, NA, 1
# $ status            <chr> "Dated", "Dated", "Dated", "Dated", "Dated", "Dated"
# $ waneyedge         <chr> NA, NA, NA, NA, NA, "WKE"
# $ bark              <chr> NA, NA, NA, NA, NA, NA
# $ pith              <chr> "-", "-", "-", "-", "-", "-"
# $ pith_offset       <dbl> NA, NA, NA, NA, NA, NA
# $ pith_offset_delta <dbl> NA, NA, NA, NA, NA, NA
# $ comments          <chr> "keelplank", "framing timber", "hull plank", ...
# $ project           <chr> "Ship timbers DOEL 1", "Ship timbers DOEL 1", ...
# $ location          <chr> "Doel_Deurganckdok", "Doel_Deurganckdok", ...
# $ town              <chr> NA, NA, NA, "Doel", NA, NA
# $ zip               <chr> NA, NA, NA, NA, NA, NA
# $ street            <chr> NA, NA, NA, "Deurganckdok", NA, NA
# $ sampling_date     <chr> NA, NA, NA, NA, NA, NA
# $ measuring_date    <chr> NA, NA, NA, NA, NA, NA
# $ personal_id       <chr> "KH", "KH", "KH", "KH", "KH", NA
# $ client_id         <chr> NA, NA, NA, NA, NA, NA
# $ longitude         <chr> "4.269711", "4.269711", "4.269711", ...
# $ latitude          <chr> "51.298236", "51.298236", "51.298236", ...
```

Crossdating

The function `cor_table()` computes commonly used correlation values between dated tree-ring series and reference chronologies. This function helps to check the assigned end date of the series by comparing the measurements against absolutely dated reference chronologies. This might also provide more information on timber provenance, as some reference chronologies represent a geographically confined region. Such information allows to select the most appropriate sapwood model for your tree-ring data according to the provenance of the wood.

The correlation values computed are:

- glk: ‘Gleichläufigkeit’ or ‘percentage of parallel variation’ (Buras and Wilmking 2015; Eckstein and Bauch 1969; Huber 1943; Visser 2021).
- glk_p: significance level associated with the glk-value (Jansma 1995).
- r_pearson: the Pearson’s correlation coefficient
- t_St: Student’s t-value based on r_pearson
- t_BP: t-values according to the Baillie and Pilcher (1973) algorithm
- t_Ho: t-values according to the Hollstein (1980) algorithm

```
Doel1_trs <- read_fh(Doel1, header = FALSE)
Hollstein_crn <- read_fh("Hollstein80.fh", header = FALSE)

cor_table(x = Doel1_trs,
          y = Hollstein_crn,
          min_overlap = 80, # sets the minimum overlap between series and reference
          output = "table",
          sort_by = "t_BP")
```

Felling date interval

After selecting the appropriate sapwood model (e.g. , one of Fig. 2) one can use the model to estimate the upper and lower limits of the number of missing sapwood rings. The function `sw_interval()` calcualtes the probability density function (PDF) and highest probability density interval (HDI) of the felling date range based on the observed number of sapwood rings (`n_sapwood = ...`), their chronological dating (`last = ...`) and the selected sapwood data (`sw_data = ...`) and model (`densfun = ...`).

In the example below, 10 sapwood rings were observed on a historical timber (last ring dated to 1234 CE) that is supposed to have a provenance in the Southern Baltic region (sapwood model published by (Wazny 1990)). The HDI delineates an interval in which the actual felling date is most likely situated. It is the shortest interval within a probability distribution for a given probability mass or credible interval (`cred_mass = ...`). The HDI summarizes the distribution by specifying an interval that spans most of the distribution (in the example below the credible interval is set to 95%), as such that every point inside the interval has higher credibility than any point outside the interval (Fig. 4).

Note that the more sapwood rings that have been measured, the more probability mass is assigned to the tails of the sapwood model.

```
# 10 sapwood rings observed and the Wazny 1990 sapwood model:

interval <- sw_interval(
  n_sapwood = 10,
  last = 1234,
  hdi = TRUE,
  cred_mass = .95,
  sw_data = "Wazny_1990",
  densfun = "lognormal",
  plot = TRUE)
```

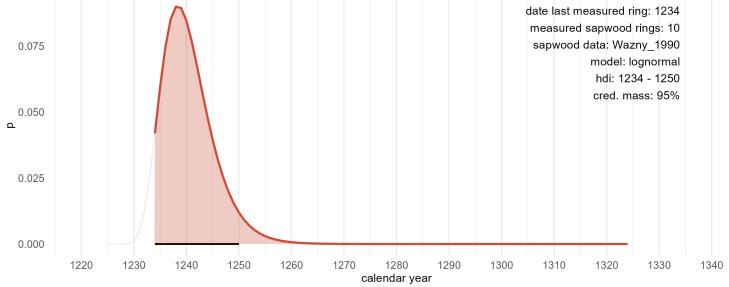


Figure 4: A truncated lognormal distribution, representing the sapwood model for a tree-ring series with 10 sapwood rings. The black line delineates the 95% credible interval for the felling date.

Reporting individual series

Reporting estimates of the felling date range for multiple individual series, is conveniently provided by the function `fd_report()`. The column `felling_date` in the `data.frame` that is returned, reports the felling date in verbatim.

```
df <- data.frame(id = c("trs1", "trs2", "trs3"),
                  swr = c(10, 11, 12),
                  waneyedge = c(FALSE, FALSE, TRUE),
                  end = c(123, 456, 1789)
                 )

fd_report(df,
           series = "id",
           n_sapwood = "swr",
           last = "end",
           sw_data = "Wazny_1990")

#>   series last n_sapwood waneyedge lower upper      felling_date sapwood_model
#> 1     aaa 123      10    FALSE    123    139 between 123 and 139  Wazny_1990
#> 2     bbb 456      11    FALSE    456    471 between 456 and 471  Wazny_1990
#> 3     ccc 1789     12    TRUE     NA    1789      in 1789  Wazny_1990
```

Combine felling dates

`sw_combine`

The procedure to combine felling dates of a group of related tree-ring series with (partially) preserved sapwood, in order to narrow down the range of a common felling date is provided by the function `sw_combine()`. This function returns a `list` with:

- the probability density function (PDF) for the felling date of the individual series and the PDF of the model that combines these individual series (`$data_raw`),
- the HDI for the combined estimate of the common felling date (`$hdi_model`),
- the *Agreement index* (`$A_model`) of the model, expressing how well the individual series fit into the model ,

- an overview of the felling date range for the individual series (`$individual_series`), and their *Agreement index* (A_i) to the combined model.

The function `sw_combine_plot()` allows to visualize the output (or set `plot = TRUE` in `sw_combine(...)` to call the plot function directly).

The rationale and mathematical background of the *Agreement index* (A_i) was introduced and developed by Bronk Ramsey (1995, 2017). Both the A_i of the individual series as for the whole model (A_{model}) should ideally be around 100%, and not lower than the critical threshold $A_c = 60\%$.

The procedure of testing whether a group of timbers might share a common felling date based on their tree-ring patterns is demonstrated in the next section, with an example dataset consisting of 5 dated tree-ring series of which one has an exact felling date (Fig. 5, left). The proposed felling date (dark grey distribution) equals the felling date of the series with an exact felling date (`trs_15`), but now it can be assessed that this falls within the felling date ranges for three other individual series (`trs_11`, `trs_12` and `trs_14`). One other series (`trs_13`) has no remaining sapwood and therefore only a *terminus post quem* (earliest possible felling date) can be given (arrow pointing away from last measured ring). The agreement indexes of all individual series and the overall model are high and above the critical threshold of 60%.

```
trs_example2
#>   series last n_sapwood waneyedge
#> 1 trs_11 1000      5    FALSE
#> 2 trs_12 1005     10    FALSE
#> 3 trs_13 1008     NA    FALSE
#> 4 trs_14 1000      1    FALSE
#> 5 trs_15 1010      3    TRUE

p1 <- sw_combine(trs_example2, plot = TRUE)
```

In the next example, an attempt to compute a common felling date for a group of 5 tree-ring series fails. All but one of the series include partially preserved sapwood, but these tree-ring series do not share a common timing for their estimated felling date (Fig. 5, right). The agreement index of the model is far below 60%, as is the case for most of the individual series. In this particular example, probably two or three separate felling events are present.

```
trs_example4
#>   series last n_sapwood waneyedge
#> 1 trs_21 1000      5    FALSE
#> 2 trs_22 1005     10    FALSE
#> 3 trs_23 1005     NA    FALSE
#> 4 trs_24 1020      1    FALSE
#> 5 trs_25 1040      0    FALSE

p2 <- sw_combine(trs_example4, plot = TRUE)
```

Sum felling dates

For large datasets of dated tree-ring series, it is not always straightforward to assess temporal trends in the frequency of felling dates. Exact felling dates can be stacked by calendar year, but for series with partially preserved sapwood, their felling date is situated in an interval. The individual series each have their own probability density function based on a chosen sapwood model and the number of observed sapwood rings. To make another reference to radiocarbon dating, it is common practice in the analysis of large volumes of calibrated radiocarbon dates to compute the *summed probability densities* (SPD) of the calibrated

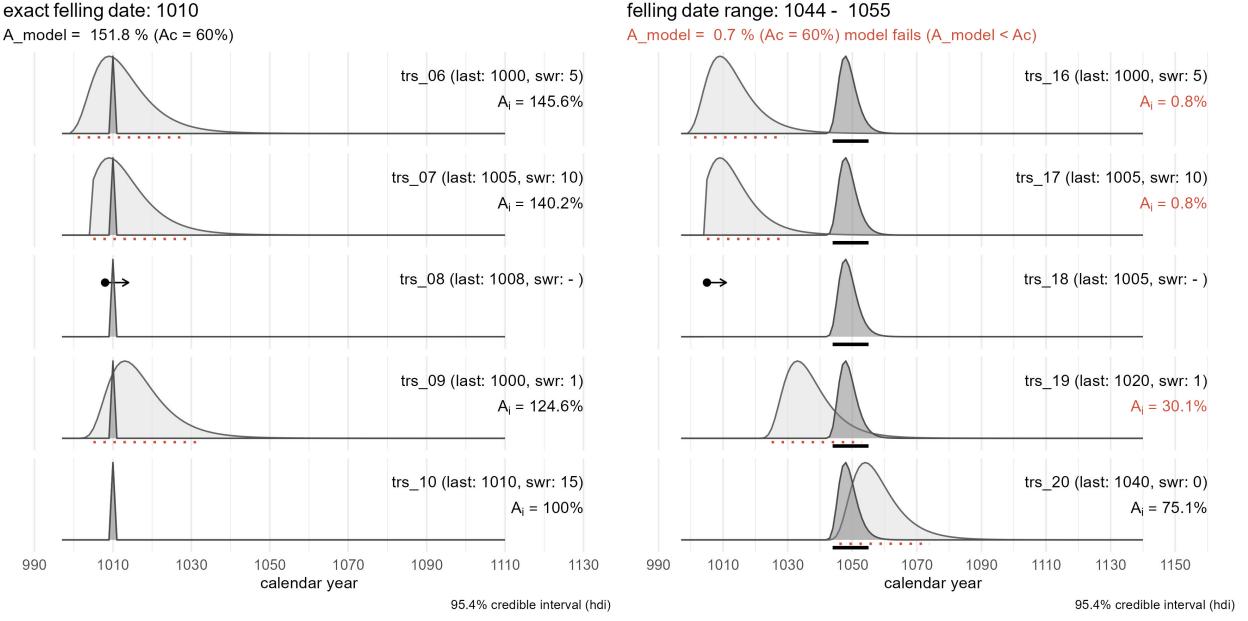


Figure 5: Graphical output of `sw_combine()`. The sapwood model for the individual series in light grey, the probability density function of the combined felling in dark grey tone. The credible interval for the felling date of individual series is shown as a dashed red line and a black line for the combined estimate. The dataset in the left graph includes an exact felling date that matches with the estimates for the other series. The graph on the right shows a model that fails to group all series around a common felling date.

radiocarbon dates. Summed probabilities are used to determine the temporal density of ages (events), where there is no clear prior information on their distribution (Bronk Ramsey 2017). This procedure is implemented in OxCal and the R-package `rcarbon` (Crema and Bevan 2020). The function `sw_sum()` makes his procedure commonly applied in radiocarbon dating available for tree-ring analyses. The summed probability distribution (SPD) of the individual probability densities of felling dates of single tree-ring series with incomplete sapwood allows to visualize fluctuations in the incidence of potential felling dates through time. The resulting p -values should however not be interpreted in a probabilistic way but must be regarded as relative measures that unveil temporal trends in the dataset. Exact felling dates derived from tree-ring series with waney edge are not included in the computational process of the SPD as they would result in anomalous spikes in the SPD, as their associated probability ($p = 1$) would be assigned to a single calendar year, whereas for series with incomplete sapwood the total probability ($p = 1$) is dispersed over a wider time range. Therefore exact felling dates are plotted separately on top of the SPD (Fig. 6).

```
sum <- sw_sum(trs_example7)
sw_sum_plot(sum, dot_size = 2, dot_shape = 25)
```

Future work

In its current version the package `fellingdater` is tailored to the general workflow for analyzing tree-ring datasets from wooden cultural heritage objects and constructions, made of European oak (*Quercus* sp.). The sapwood data included in the current version reflect this focus on oak. But all functions can also work with a custom sapwood dataset, provided as a `data.frame` with columns named `n_sapwood` and `count`. The latter reporting the number of occurrences a certain number of sapwood rings (`n_sapwood`) was observed on

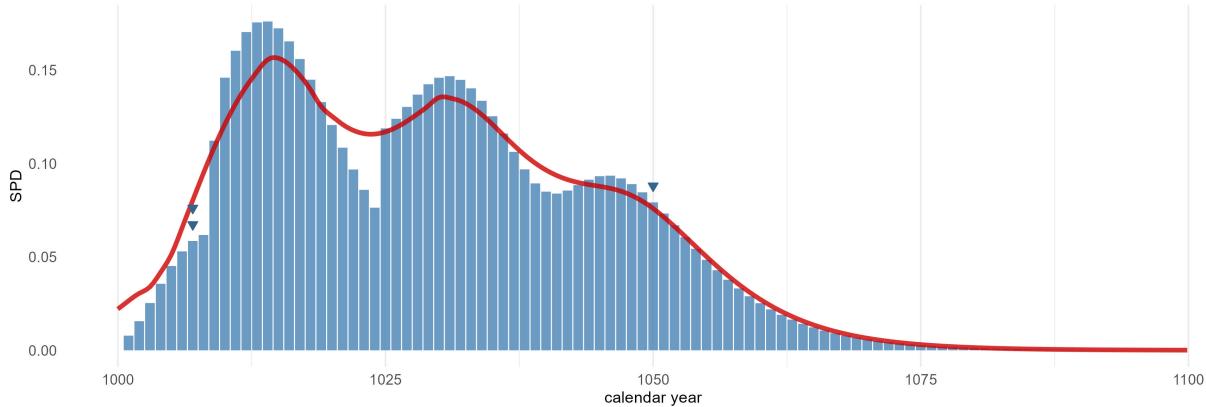


Figure 6: Graphical representation of the output of `sw_sum()`. The blue bars represent the summed probability density (SPD) of the individual series with partial sapwood. The red line is a window filter applied to the SPD to highlight the general trend. Series with exact felling dates (presence of waney edge) are plotted as triangles above the blue bars of the SPD.

a timber or core sample from the reference dataset. As such, sapwood data from other regions and species can also be explored, modeled and used to report felling dates by the users of `fellingdateR`.

When new datasets of sapwood counts become available, these can be incorporated in future versions of the package.

Acknowledgements

Koen Van Daele and Ronald Visser fueled me with valuable feedback on earlier versions of the package. Koen VD also introduced me to the concept of unit tests and wrote the first examples.

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