

Ejercicio: Para $P(B=r) = 0.4$ y $P(B=b) = 0.6$

$$P(B=r) + P(B=b) = 1$$

Segun la figura encontrar

a = apple - verdes

O = Orange

B = Box

F = Fruit

$$N = 12$$

$$P(F=a) = 55\%$$

$$P(F=a) = P(F=a|B=r)P(B=r) + P(F=a|B=b)P(B=b)$$

$$\frac{2}{8} \cdot \frac{4}{10} + \frac{3}{4} \cdot \frac{6}{10} \Rightarrow \frac{2}{8} \cdot \frac{4}{10} + \frac{3}{4} \cdot \frac{6}{10} \Rightarrow \frac{2}{20} + \frac{9}{20} = \frac{11}{20} = 0.55$$

$$P(F=O) = 45\%$$

$$= P(F=O, B=r) + P(F=O, B=b)$$

$$= P(F=O|B=r)P(B=r) + P(F=O|B=b)P(B=b)$$

$$\frac{6}{8} \cdot \frac{4}{10} \Rightarrow \frac{24}{80} = \frac{3}{10} + \frac{1}{4} \cdot \frac{6}{10} \Rightarrow \frac{6}{40} = \frac{3}{20} \Rightarrow \frac{3}{10} + \frac{6}{40} \Rightarrow 0.45 \Rightarrow \frac{9}{20}$$

$$P(B=r|F=O) = 66.6\%$$

$$\text{Bayes: } P(B=r|F=O) = \frac{P(F=O|B=r)P(B=r)}{P(F=O)}$$

$$= \frac{(6/8) \cdot (4/10)}{(4.5/10)} = \frac{240}{360} \Rightarrow \frac{2}{3} = 0.666$$

$$P(B=b|F=O) = 33.3\%$$

$$= \frac{P(F=O|B=b)P(B=b)}{P(F=O)} = \left(\frac{1}{4} \cdot \frac{6}{10} = \frac{600}{1800} = 0.333 \right)$$

$$P(B=r|F=a) = 18\%$$

$$= \frac{P(F=a|B=r)P(B=r)}{P(F=a)} = \left(\frac{2}{8} \cdot \frac{4}{10} = \frac{800}{4400} = 0.181 \right)$$

$$P(B=b|F=a) = 82\%$$

$$1 - 0.181 = 0.819$$