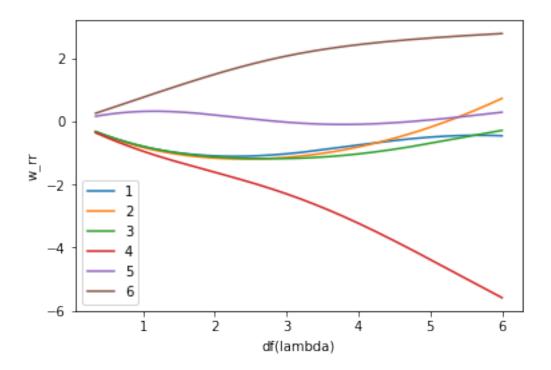
## Coding part

### February 25, 2018

```
In [552]: import pandas as pd
          import numpy as np
          from subprocess import check_output
          print(check_output(["ls", "./hw1-data"]).decode("utf8"))
X_test.csv
X_train.csv
y_test.csv
y_train.csv
In [553]: X_train_full = pd.read_csv("./hw1-data/X_train.csv", header=None)
          X_train = X_train_full.drop([6], axis=1)
          print(X_train.shape)
          X_train.head()
(350, 6)
Out [553]:
                            1
                                     2
                                               3
          0 0.30957 -0.36707 0.45545 -0.200830 -0.73992 -0.80885
          1 0.30957 0.35920 -0.11611 -0.038361 0.16625 -0.80885
          2 -0.86291 -0.99778 -0.89551 -1.225100 -0.55868 -0.26592
          3 -0.86291 -0.69198 -0.42787 -0.562260 -0.15997 1.09140
          4 -0.86291 -0.92133 -0.63571 -1.251000 -0.41369 0.81993
In [554]: y_train = pd.read_csv("./hw1-data/y_train.csv", header=None)
          y_train.head()
Out [554]:
          0 -3.4459
          1 - 5.4459
            5.5541
          2
          3 11.5540
          4 12.2540
```

```
In [555]: u, s, vh = np.linalg.svd(X_train, full_matrices=False)
          u.shape, s.shape, vh.shape
Out[555]: ((350, 6), (6,), (6, 6))
In [556]: np.allclose(X_train, np.dot(u * s, vh))
Out [556]: True
In [557]: s_mat = np.diag(s)
In [558]: WRR = []
          w_ls = np.dot(np.linalg.inv(np.dot(np.transpose(X_train), X_train)), np.dot(np.transpose(X_train))
          v = vh.T
          for lmda in range(5001):
              w_rr = np.append(np.dot(np.linalg.inv(np.dot(X_train.T,X_train) + lmda * np.identi
              WRR.append(w_rr)
          WRR = np.array(WRR)
          WRR.shape
Out [558]: (5001, 7)
In [559]: # df lambda
          df_1 = []
          for i in range(5001):
              df_1.append(np.sum(s**2/(i + s**2)))
          s
Out[559]: array([ 37.96221572, 16.91947966, 15.42100981, 6.70644826,
                   4.68955116, 3.56635938])
In [560]: import matplotlib.pyplot as plt
          plt.figure()
          for i in range(6):
              pp, = plt.plot(df_l, WRR[:, i])
              pp.set_label(str(i+1))
          plt.legend()
          plt.xlabel('df(lambda)')
          plt.ylabel('w_rr')
          plt.show()
```



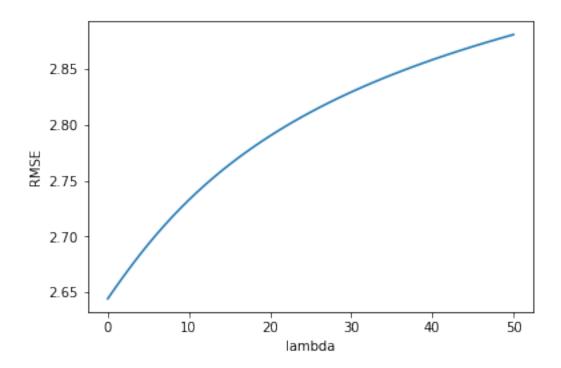
# 0.0.1 (b) The 4th dimension (car weight) and 6th dimension (car year) clearly stand out over the other dimensions. What information can we get from this?

All the other dimensions did not change very much as lambda approached 5000 except the 4th and 6th dimensions. They had considerably higher magnitudes when lambda was close to 0 (maximum likelihood) and decreased the more we penalized them for their magnitudes.

This tells us that without any bias and depending strictly on the model's maximum likelihood, those two dimensions are seen as very influencial. I.E. the bigger the car weight and/or the smaller the car year, the lower the miles per gallon of the car. Obviously our RR assumption (prior) is that no single feature should have so much influence therefore lambda's increase brings those features' magnitudes down.

```
In [561]: X_test = pd.read_csv("./hw1-data/X_test.csv", header=None)
          print(X_test.shape)
          X_test.head()
(42, 7)
Out [561]:
                                               3
                            1
             0.30957
                      0.34964
                               0.013785
                                        0.52674
                                                  0.49248
             1.48210
                      1.48680
                               1.572600
                                        0.84226 -1.46490 -1.62320
          2 -0.86291 -0.71110 -0.661690 -0.41510
                                                  1.10870
             0.30957
                      0.53121 -0.116110 0.94586
                                                  0.52872 -0.53739
             1.48210
                     1.02810 0.897110 0.26774 -1.57360 0.54847
```

```
In [562]: y_test = pd.read_csv("./hw1-data/y_test.csv", header=None)
          y_test.head()
Out [562]:
                  0
          0 -2.9459
          1 -8.4459
          2 4.5541
          3 -7.4459
          4 -5.3459
In [563]: def RMSE(y_test, y_pred):
              np.sqrt(np.sum((y_test-y_pred)**2)/42)
          y_pred = []
          for i in range(51):
              w_rr_i = WRR[i]
              y_pred.append(np.dot(X_test , w_rr_i))
          y_pred = np.array(y_pred)
          y_pred.shape
          RMSE_ar = []
          for i in range(51):
              RMSE_ar.append(np.sqrt(np.sum((np.squeeze(y_test) - y_pred[i])**2)/42))
In [564]: plt.figure()
          pp, = plt.plot(range(51), RMSE_ar )
          plt.xlabel('lambda')
          plt.ylabel('RMSE')
          plt.show()
```



#### 0.0.2 (c)

The increase of lambda is only increasing the error so using ridge regression in this example is not helping generalize our model on the test data. We are better off using least square (lambda = 0).

```
Out [566]: (501, 12, 1)
In [567]: WRR_3 = []
          for lmda in range(501):
              w_rr = np.dot(np.linalg.inv(np.dot(X_train_3_norm.T,X_train_3_norm) + lmda * np.id
              WRR_3.append(w_rr)
          WRR_3 = np.array(WRR_3)
          WRR_3.shape
Out [567]: (501, 18, 1)
In [568]: y_pred_1 = []
          for i in range(501):
              w_rr_i = WRR[i]
              y_pred_1.append(np.dot(X_test , w_rr_i))
         y_pred_1 = np.array(y_pred_1)
         y_pred.shape
          RMSE_ar_1 = []
          for i in range(501):
              RMSE_ar_1.append(np.sqrt(np.sum((np.squeeze(y_test) - y_pred_1[i])**2)/42))
          len(RMSE_ar_1)
Out[568]: 501
In [569]: y_pred_2 = []
          for i in range(501):
              w_rr_i_2 = WRR_2[i]
              y_pred_2.append(np.dot(X_test_2_norm , w_rr_i_2))
          y_pred_2 = np.array(y_pred_2).reshape(501, 42)
         RMSE_ar_2 = []
          for i in range(501):
              RMSE_ar_2.append(np.sqrt(np.sum((np.squeeze(y_test) - y_pred_2[i])**2)/42))
          len(RMSE_ar_2)
Out[569]: 501
In [570]: y_pred_3 = []
          for i in range(501):
              w_r_{i_3} = WRR_3[i]
              y_pred_3.append(np.dot(X_test_3_norm , w_rr_i_3))
```

```
y_pred_3 = np.array(y_pred_3).reshape(501, 42)
          RMSE_ar_3 = []
          for i in range(501):
              RMSE_ar_3.append(np.sqrt(np.sum((np.squeeze(y_test) - y_pred_3[i])**2)/42))
          len(RMSE_ar_3)
Out[570]: 501
In [571]: plt.figure()
          pp, = plt.plot(range(501), RMSE_ar_1 )
          pp.set_label("1th")
          pp, = plt.plot(range(501), RMSE_ar_2 )
          pp.set_label("2nd")
          pp, = plt.plot(range(501), RMSE_ar_3 )
          pp.set_label("3rd")
          plt.legend()
          plt.xlabel('lambda')
          plt.ylabel('RMSE')
          plt.show()
           3.4
                      1th
                      2nd
           3.2
                      3rd
           3.0
           2.8
           2.6
           2.4
           2.2
```

200

lambda

300

400

500

100

Ò

### 0.0.3 Part 2 (d)

p=2 is clearly better than the others. Compared to p=1, here ridge regression does make sense as there is an optimal lambda in which the RMSE is at its lowest.