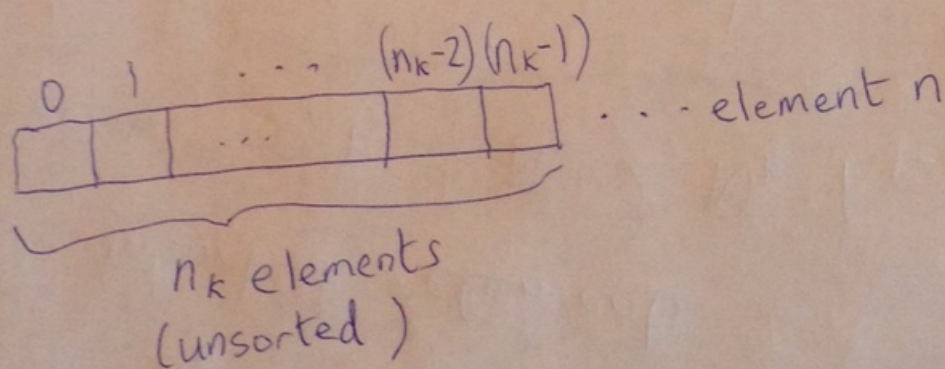


On pass  $k$  of a bubblesort algorithm, the top  $k-1$  elements are already sorted.

If there are  $n$  elements in total, the number of unsorted elements is  $n - (k-1)$   
 $= n - k + 1$

Let  $n_k = n - k + 1 = \# \text{ of unsorted}$

So, on pass  $k$  over the array, only need to pass over (and attempt to sort) the first  $n_k$  elements. In C++ these are indexed starting from zero



### Algorithm at pass $k$

Start at element  $i = 0$

Loop { compare (element  $i$ ) with (element  $i+1$ )  
If (element  $i$ ) > (element  $i+1$ )  
swap values of elements  $i$  and  $i+1$   
Increment  $i$  by 1 ( $i++$ )

When do we stop?



If we continue until  $i = (n_k - 1)$ , there is no element stored in position  $i+1$  to compare with.  $\therefore$  stop before reaching element  $i = n_k - 1$

Or, since  $n_k = n - k + 1$ , stop before reaching  $i = (n - k + 1) - 1 = \underline{n - k}$

Modify for loop (the inner for loop) to:

```
for(int i=0; i < n-k; i++)
```