


Algorithmics	Student information	Date	Number of session
	UO: 277921	2/3/2021	3.1
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## Activity 1. Basic recursive models

### Substraction1

On this class the number of subproblems ‘ $a$ ’ is 1, the value we subtract by, ‘ $b$ ’, is 1 as well and the overall complexity excluding the recursive calls is  $O(n^k) = O(1)$ ; therefore,  $k = 0$ . Now, we know all the parameters and, because  $a = 1$  we apply the formula  $O(n^{k+1})$  to calculate the complexity; that is,  $O(n)$ .

### Substraction2

On this class the number of subproblems ‘ $a$ ’ is 1, the value we subtract by, ‘ $b$ ’, is 1 as well and the overall complexity excluding the recursive calls is  $O(n^k) = O(n)$ ; therefore,  $k = 1$ . Now, we know all the parameters and, because  $a = 1$  we apply the formula  $O(n^{k+1})$  to calculate the complexity; that is,  $O(n^2)$ .

### Substraction3

On this class the number of subproblems ‘ $a$ ’ is 2, the value we subtract by, ‘ $b$ ’, is 1 and the overall complexity excluding the recursive calls is  $O(n^k) = O(1)$ ; therefore,  $k = 0$ . Now, we know all the parameters and, because  $a > 1$  we apply the formula  $O(a^{n/b})$  to calculate the complexity; that is,  $O(2^n)$ .

### Division1

On this class the number of subproblems ‘ $a$ ’ is 1, the value we divide by, ‘ $b$ ’, is 3 and the overall complexity excluding the recursive calls is  $O(n^k) = O(n)$ ; therefore,  $k = 1$ . Now, we know all the parameters and, because  $a < b^k$  we apply the formula  $O(n^k)$  to calculate the complexity; that is,  $O(n)$ .

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## Division2

On this class the number of subproblems 'a' is 2, the value we divide by, 'b', is 2 as well and the overall complexity excluding the recursive calls is  $O(n^k) = O(n)$ ; therefore,  $k = 1$ . Now, we know all the parameters and, because  $a = b^k$  we apply the formula  $O(n^k * \log n)$  to calculate the complexity; that is,  $O(n \log n)$ .

## Division3

On this class the number of subproblems 'a' is 2, the value we divide by, 'b', is 2 as well and the overall complexity excluding the recursive calls is  $O(n^k) = O(1)$ ; therefore,  $k = 0$ . Now, we know all the parameters and, because  $a > b^k$  we apply the formula  $O(n^{\log_b a})$  to calculate the complexity; that is,  $O(n)$ .

## Substraction4

On this case the complexity is known,  $O(3^{n/2})$  and it is divide and conquer by subtraction so we have two possibilities; the number of subproblems 'a' is equal to one or it is greater than one.

If we have a look at the complexity we can notice that the value of  $a$  is 3 and the value of  $b$  is 2; because we can only have that type of complexity applying the formula  $O(a^{n/b})$ . The value of  $k$  is not relevant here, but in my case it is 0.

## Division4

On this case the complexity is known,  $O(n^2)$ . If we have a look at the complexity we can notice that the value of  $a$  is either greater than  $b^k$  or less than  $b^k$ ; because the complexity is not of the form  $O(n^k * \log n)$ .

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I have chosen the case on which  $a > b^k$ , so the formula to calculate the complexity we apply is  $O(n^{\log_b a})$ . Having in mind the previous premises, we can conclude that the value of  $a$  is 4 and the value of  $b$  is 2 to obtain the said complexity. Again, the value of  $k$  is not relevant, but in this case it is 0.